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► **To cite this version:**

David Aubin. ” I’m Just a Mathematician ”: Why and How Mathematicians Collaborated with Military Ballisticians at Gâvre. 2010. hal-00639895v2

**HAL Id: hal-00639895**

**<https://hal.sorbonne-universite.fr/hal-00639895v2>**

Preprint submitted on 23 Sep 2014

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## ‘I’m Just a Mathematician’: Why and How Mathematicians Collaborated with Military Ballisticians at Gâvre

David Aubin

ABSTRACT. This chapter examines the way in which mathematicians were led to contribute to ballistic studies in France during World War I. It pays special attention to the French Navy’s Gâvre Experiments Commission first established in 1829, where University Professor Jules Haag, Navy Engineer Maurice Garnier and high school teacher Osée Marcus jointly developed a new method for computing ballistic trajectories (the so-called GHM method). It highlights the difficulties and successes encountered by mathematicians when they approached a military culture that was already mathematically sophisticated. It reviews briefly the history of ballistics at Gâvre before the First World War to understand the bitter feeling among artillerymen serving on the front about the inadequacies of their ballistic tables. In a final part, the technical contributions made by mathematicians, their experimental practices, and their efforts to disseminate their results are examined. A focus on various tensions: between civilians and those in the military, between theory and experiment, between frontlines and rearlines, serves as a means to understand the value of the contributions of mathematicians to the war effort.

On September 18, 1915, Jules Haag (figure 1), a young professor of rational mechanics from the University of Clermont-Ferrand, wrote to his old mentor, Professor Paul Appell, in Paris. Mobilized in a non-fighting unit of the Army, Haag was in charge of overseeing a workshop of the Michelin Tyre Company that produced ammunition for the celebrated 75-mm cannon. Asked to compute ballistic trajectories for a new airplane bomb design called “*bombe Michelin*,” he first tried, as he wrote, to apply “the artillerymen’s classical methods.”<sup>1</sup> Having computed logarithms for three half-days in order to construct the required curves, Haag spent the little time he could spare to try to improve the methods. Rather surprisingly—since ballistics was, after all, a sensitive matter that the Academy had expressly indicated it wanted to study further for the benefit of the French Army—but luckily, as we will see, the short paper Haag wrote up and sent to Appell was published a week

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In the writing of this chapter, I used documents provided to me by Cécile Aguilhaume, June Barrow-Green, Alain Carrière, Claudine Fontanon, Sébastien Gauthier, Hélène Gispert, Catherine Goldstein, and Anne-Sandrine Paumier, whom I wish to thank here for their kind help. I would also like to thank the members of the WWI study group at the Institut de mathématiques de Jussieu, as well as Patrice Bret and Pierre Mounier-Kuhn. This work was supported in part by the French Agence Nationale de la Recherche.

<sup>1</sup>“Les méthodes classiques des artilleurs” [Academy of Sciences, Haag to Appell, September 18, 1915; pochette de séance, September 27, 1915]. All translations are mine.



FIGURE 1. Jules Haag as correspondent to the Academy of Sciences. With permission of the Académie des sciences–Institut de France.

later in the *Comptes rendus hebdomadaires des séances de l'Académie des sciences* [hereafter *CRAS*] [Haag 1915a].<sup>2</sup>

Characteristically for a scientist in the first months of World War I, Haag felt that his skills were not used to their fullest extent. His superiors apparently showed no interest in the results he was sending Appell: “In their eyes,” Haag complained, “*I am just a mathematician*, without practical use other than serving as a computing machine when the occasion arises.” A mere sergeant [maréchal des logis], Haag had been barred from the local branch of the Commission of Inventions, since only

<sup>2</sup>Two more papers on ballistics would then be published by Haag in the same year [Haag 1915b, Haag 1915c]. Some context about the work of the Michelin Company in WWI can be found in [Chapeaux 2006], pp. 145–146. The first planes produced by Michelin (in collaboration with the Breguet Company) were delivered in July 1915. On Jules Haag (1882–1953), see [Broglie 1953, Mesnage 1953, Châtelet & Chazy 1955, Meyer 1989].

officers (or civilians) could sit on it.<sup>3</sup> His only recourse, he explained, was to study a bit of ballistics in his spare time and wish that one would let him devote more time to it. He admitted that this might have no immediate effect in helping to “drive out the Germans,” but “the questions I am asked, without being told more about the mysterious studies that give rise to them” made him suspect that his contribution might indeed be directly pertinent to the war effort.<sup>4</sup>

Less than a month later, on October 12, 1915, the professional ballistician, General Prosper-Jules Charbonnier (1882–1936) (fig. 2), sent a memo to his superiors calling attention to the tremendous ballistic effort that war operations now demanded. A Navy officer trained at the *École polytechnique* who had served in Africa and in the Far East, Charbonnier was at the time President of the so-called *Commission d'expériences d'artillerie navale de Gâvre*, which was both a proving ground and the main military body in charge of ballistic computations for the French Navy and Army. In his memo, President Charbonnier explained that his overworked personnel were now unable to face the huge quantity of experiments and computations the War Ministry asked them to carry out. Acknowledging that most artillerymen were, of course, otherwise busy on the battlefields, he noted that university professors possessed an “intellectual and professional training that would quickly make them useable by the Commission for computations and even experiments.” A regular reader of the *Comptes rendus*, Charbonnier put forward Haag’s name as a likely candidate.<sup>5</sup> A fortnight later, on October 29, 1915, the mathematician left Clermont-Ferrand to reach his new assignment post at Gâvre, near the seaport of Lorient in Brittany [SHD–Terre, 6–Ye-17966, Haag’s military file].

As a result of Charbonnier’s memo, a dozen mathematicians, physicists, and astronomers would join the Gâvre Commission over the course of the war, including Albert Châtelet (1883–1960), Georges Valiron (1884–1955), Joseph Kampé de Fériet (1893–1982), and Arnaud Denjoy (1884–1974). The work they did at Gâvre was part of the establishment of new theoretical foundations for computing in exterior ballistics. New experimental methods for studying ballistics were also pursued, while the astronomer and future director of the Paris Observatory, Ernest Esclangon (1876–1954), carried out much praised work on sound-ranging, that is, the localization of enemy batteries by an analysis of the sound waves they emitted.<sup>6</sup> Other prominent mathematicians such as Henri Lebesgue (1875–1941), Émile

<sup>3</sup>A promotion to the rank of Second Lieutenant [*sous-lieutenant*] in the artillery had indeed been considered in favor of Haag and rejected. On the Commission, see [Roussel 1989] as well as the contribution by David Aubin, Hélène Gispert, and Catherine Goldstein to this volume.

<sup>4</sup>“*Je ne suis, à leurs yeux, qu'un mathématicien, sans utilité pratique autre que celle de servir, quand l'occasion se présente, de machine à calculer*”; “*Cela ne serait peut-être d'aucune utilité pratique pour chasser les Allemands. Cependant, les questions qu'on me pose, sans m'initier davantage aux mystérieuses recherches qui les font naître, pourraient bien laisser supposer le contraire.*” All quotes come from [Academy of Sciences, Haag to Appell, September 18, 1915; pochette de séance, September 27, 1915; my emphasis]. The misuse of scientific personnel at the start of World War I is a common theme among contemporary scientists and historians. For reviews, see [Kevles 1978, Hartcup 1988, Aubin & Bret 2003], and references therein.

<sup>5</sup>Charbonnier to the Minister (October 12, 1915), quoted in [Patard 1930, p. 274]. It is not known whether Charbonnier was in contact with Appell.

<sup>6</sup>Although it properly belonged to the field of ballistics at the time, sound ranging will not be examined in detail here. On this topic, see esp. [Schiavon 2003a, Schiavon 2003b]. See also [Jones 1921–1922, Kevles 1969, Palazzo 1999], as well as other chapters in this volume by June Barrow-Green and by the present author.



FIGURE 2. Colonel, later General Prosper-Jules Charbonnier pondering a ballistic problem on the beach of Gâvre, undated. From [Patard 1930, p. 253].

Borel (1871–1956) and Paul Montel (1876–1975) took part in ballistic research and enrolled several mathematics teachers in their effort.

Exterior ballistics was one of the few areas where French mathematicians truly were able, as mathematicians, to play a prominent part in World War I. This chapter examines the way in which young mathematicians such as Haag were drawn into military work at a time when the general belief was that there was no better way for them to contribute to the war effort than by fighting on the front. As the 22-year old Pierre Abeille wrote in his last letter to his parents:

Shame on intellectuals who fail to understand that they have . . . the sacred duty of putting their arms and chests in the same location as the arms and chests of their brothers. . . . To us, the privileged, the guardians of tradition, the transmitters of the Ideal, [the duty] of risking our lives and happily sacrificing ourselves for the preservation, the extension, the exaltation of all this beauty, of all this pride that we are the first to feel and to take advantage of.<sup>7</sup>

Historians have shown that in all belligerent countries the exact contours of research scientists' participation in the defense effort were far from being clearly delineated in 1914 and that many of them did not survive the first years of the war.<sup>8</sup> Most historians' accounts of the war work of mathematicians and scientists often, if not always, focus on the stories told by surviving scientists themselves. Most, therefore, view scientists' contributions on their own terms. But I would like to argue that to understand correctly the value of such contributions, it is necessary to widen the scope of our investigations. One needs to have a clear view of the military demands from the points of view both of general staffs and of men in the field. One also needs to pay special attention to the military technical structures that existed before the outbreak of the war to see why officers serving in these structures felt the need to enlist civilian expertise.

I want to argue that the incorporation of university mathematicians into military research structures was neither preordained nor straightforward. One may well argue that some mathematical knowledge has always been mustered in warfare.<sup>9</sup> But before 1914 there also seems to have been a widespread feeling that professional mathematicians—that is, the university professors teaching and carrying out research in mathematics—had little to do with it.<sup>10</sup>

In the United States, Princeton University mathematician Oswald Veblen, despite his enthusiasm for war service, had difficulties finding a place where he could apply his mathematical skills. But he quickly found a befitting assignment at the

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<sup>7</sup>A public servant, Sergeant Abeille had volunteered for active duty and was killed on November 12, 1914 in Vingré, Aisne. His letter, dated September 26, 1914, is repr. in [Foch 1922, p. 13].

<sup>8</sup>For France, see [Roussel 1989], [Aubin & Bret 2003], & [Galvez-Behar 2008].

<sup>9</sup>On the history of mathematics and war, see among others [Mehrtens 1996, Booß-Bavnbek & Høyrup 2003, Steele & Dorland 2005]. On the WWI period especially, see [Siegmond-Schultze 2003].

<sup>10</sup>Even after the war, this feeling remained entrenched. A reviewer of a book on the history of ballistics [Charbonnier 1928a]—"the value of whose results I was able to appreciate for more than four years and the perfection of which I have known without joy"—expressed his surprise at encountering the names of the "greatest perhaps of the history of science: Galileo, Huygens, Newton, Euler, among others" [L.G. 1931, pp. 376–377].

Aberdeen Proving Ground, which was the U.S. counterpart of the Gâvre Commission. According to the internal history of this institution, “Exterior ballistics—that part of the science dealing with the behaviour of projectiles in flight—underwent a major revolution during World War I.”<sup>11</sup> Military historians in the U.S. easily acknowledged that scientists were major players in this revolution: Forest Ray Moulton, an astronomer from the University of Chicago, was the first head of the Ballistic Branch, and even though the computation of firing tables followed standard European procedures, their implementation and improvement were the work of three mathematicians linked to Princeton (Oswald Veblen, Gilbert Ames Bliss, and Thomas Hakon Gronwall). Although historians assessed that World War I had little effect on the postwar development of mathematics in the U.S., which remained characterized by the high value placed on abstractness, the field of ballistics appeared as a paradigmatic example of a research problem hitherto unsolvable by military structures and that only university scientists’ special skills could solve.<sup>12</sup> Likewise, the history of British ballistics has been centered on the scientist, the team assembled by the Cambridge biophysicist Archibald Vivian Hill and involving the mathematicians John E. Littlewood, Edward Arthur Milne, and Ralph Howard Fowler, the last two being definitively turned away from prior involvement in pure mathematics.<sup>13</sup>

In France, by contrast, the situation seemed rather more complex and perhaps also more interesting. It was more complex because for a least a century most military officers had received their first academic training at the *École polytechnique*, before going on with their career as military officers. As a result, they often had the mathematical sophistication required for efficiently tackling the main problems of ballistics. Indeed French military ballisticians had a long acquaintance with the use of advanced mathematical techniques, but also physical and chemical theories and experimental procedures, to tackle every aspect of the problem of artillery firing.<sup>14</sup> The French situation was also more complex because many more mathematicians were involved almost from the start in ballistic research, joining various military institutions that already possessed a high degree of expertise that civilians—no matter how *savant*—did not necessarily have. The circumstances under which civilian, or formerly civilian, mathematicians were drawn to the problem and the specific contributions they were able to bring to it therefore need to be assessed from the point of view of the encounter of people coming from various perspectives. This encounter was forced upon them by the special circumstances of war and the specific demands that emerged from frontline fighting experience.

In the rearlines, mathematicians and ballisticians engaged in the production of range tables and computing procedures, which were hybrid entities straddling the various worlds of the fighting artilleryman, the military specialist, and the academic

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<sup>11</sup>[U.S. n.d., p. 3]. The military work of American mathematicians is considered in the contribution by Deborah Kent, Della Fenster, and Thomas Archibald in this volume. On Veblen, see also the introduction to this volume. For contemporary assessments of American methods by the French, see [Schwartz 1927, Dodier & Valiron 1927].

<sup>12</sup>For an assessment of the lack of effect of World War I on mathematics in the U.S., see [Parshall & Rowe 1994, p. 444]. This view was nuanced in [Parshall 2000].

<sup>13</sup>See [Smith 1990, Hill n.d.]. The war work of the Cambridge mathematicians is discussed in June Barrow-Green’s contribution to this volume.

<sup>14</sup>On the *École polytechnique*, see the contribution of Jean-Luc Chabert and Christian Gilain to this volume.

mathematician. In so far as it was a hybrid product hastily put together in a time of emergency, the new ballistics that came out of the First World War only found its place with difficulty within institutional and epistemological frameworks after the Armistice. While military strategists insisted on the renewed importance of the artillery in modern warfare, resistances persisted to the complete transformation of ballistics into a branch of applied mathematics. From the early 1920s onward, civilian scientists were, however, associated to the Gâvre Commission on a permanent basis. Almost nonexistent before the war, the relationship between university mathematicians and military research bodies was made permanent.

Seeing in the research bodies hastily put in place during the war by military as well as by civil authorities a prefiguration of the state-controlled system of science funding that was fully developed during the Cold War, historians of science have mostly focused on the scientists' place in new organizations such as boards of inventions and research councils and turned a blind eye to older military research traditions.<sup>15</sup> Our look at French ballistic research shows that scientists' involvement in these institutions in 1914–1918 resulted in their lasting association with military research structures that preexisted the start of the First World War and endure to this day.<sup>16</sup>

### 1. Tradition, the Scientific Method and the “Gâvrais Virtues”

Early in the 20th century, Gâvre was a small fishing village sitting at the tip of a long and thin peninsula that separates the harbor of Lorient from the Atlantic Ocean on the south shore of Brittany.<sup>17</sup> On the isthmus connecting it to the mainland, a proving ground was established in 1829, when the Gâvre Commission was created by the Navy Minister. The Commission was composed of military officers and engineers, coming in proportions that varied over the years from the naval, colonial, and sometimes land, artilleries. Its main objective was to carry out all types of research connected to gunnery, including experimentation with cannons, rockets and guns, with powder and with projectiles. Their effect on various types of steel plates was also investigated. But most of all, the Gâvre Commission was famous for its expertise in ballistics, both interior and exterior, both theoretical and experimental. Since its foundation, its principal task was the compilation of numerical tables giving the range as a function of the initial shooting angle (or line of departure) for each new cannon model introduced in the Navy.

When he reached the Gâvre proving ground, Haag was hardly stepping into virgin territory. There, he and other civilian scientists found cannons of all sizes, cranes, railways, telegraphic and telephonic lines, chronographs and photographic cameras, all types of ballistic instruments needed to measure the initial velocity of projectiles, their power of penetration in steel plates, etc. (figure 3). But above

<sup>15</sup>On Britain, see [MacLeod & Andrews 1971, Pattison 1983, Hull 1999]. On the U.S., see [Kevles 1968]. On France, see [Roussel 1989]. On Germany and Italy, see [Mehrtens 1996, Eppele et al. 2005]. A more detailed study of the Italian case is given in Pietro Nastasi and Rossanna Tazzioli's contribution to this volume.

<sup>16</sup>Let us note here that the successor institution of the Gâvre Commission, called GERBAM (*Groupement d'études et de recherches balistiques, armes et munitions*), was closed down on January 1, 2010. Only a naval training center for shooting now remains at the Gâvre polygon.

<sup>17</sup>After much debate, the standard usage today is to write Gâvres (with an *s* at the end). At the time of the First World War, however, military officials had decided to use Gâvre which is much more common in contemporary documents. I will thus follow the latter usage.

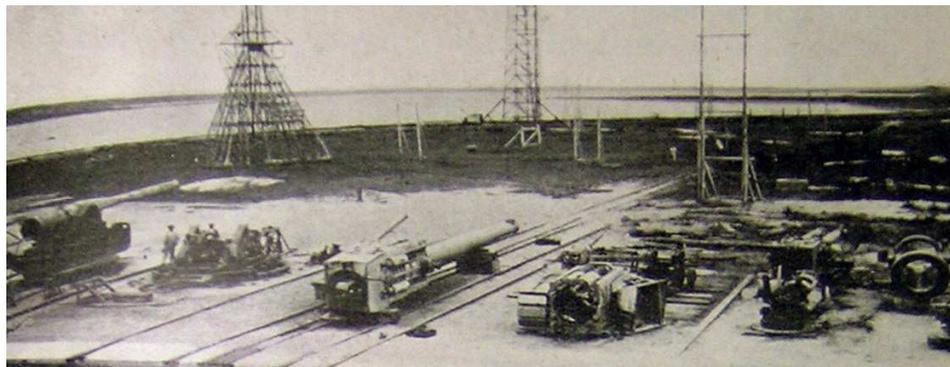


FIGURE 3. A View of the Gâvre Polygon in the Early 1930s. From *Le centenaire de la Commission de Gâvre*, *Revue maritime et coloniale* (2nd semester 1930), pp. 233–237; on p. 235.

all, they came into contact with a handful of Navy officers who shared a strong scientific “ethos” attached to its own tradition and characterized by its own distinctive values. For mathematicians who were suddenly confronted with them, the “Gâvrais virtues [*les vertus gâvraises*],” as Charbonnier called them, might at first have been discomfiting [Charbonnier 1906, p. 425].<sup>18</sup> This is what Léon Patard, the official historian of the Gâvre Commission at the time he was its President, alluded to in the following passage written in 1930:

A success of the Naval Artillery during this war, and not the least, was the use of the good will of all these men, some of whom [were] eminent savants but little prepared for their new role. Their trust had to be won; they had to be shown that, while they were not their equals in the domain of pure science, naval artillery engineers were able to understand their ideas, discuss their theories, and answer their objections. One can only infer the tact needed to subject them to long training courses in routine computing, to stem their professional attempts at perfecting computing methods as soon as they got there, to make them comply with the strict rules of experimentation and observation, and finally to lead them progressively from the role of auxiliaries to that of collaborators [Patard 1930, p. 279].<sup>19</sup>

Charbonnier also insisted on the “scientific-technical” organization put in place at Gâvre, whereby collaborative work was done by “savants and officers.” At Gâvre, “theoreticians remained in close and permanent contact with users” of cannons [Charbonnier 1929, pp. 27–28]. Léon Lecornu (1854–1940), a Professor of Mechanics at the *École polytechnique*, hinted at something similar when he praised the

<sup>18</sup>The idea that the Gâvre “virtues” may be understood in relation to the scientific ethos was first popularized by [Merton 1942]. More recently, John Ziman suggested that the Mertonian ethos (which he calls *cudos*, for Communalism, Universality, Disinterested, Originality, Skepticism) might have coexisted with an industrial research ethos he called *place* (for Proprietary, Local, Authoritarian, Commission, Expertise), which might be closer to the Gâvre ethos [Ziman 2000].

<sup>19</sup>Patard (1872–1963) was President of the Gâvre Commission from January 26, 1925 to February 20, 1931.

fact that “several science professors transformed by mobilization into improvised artillerymen, brought a precious collaboration to the professionals: together they contributed in a large part to the final victory” [Lecornu 1924, p. 38].

Compare this emphasis on collaboration to scientists’ accounts with which historians of science are much more familiar. The general tone used in the latter makes them fall in one of two categories: while many are self-congratulatory and emphasize the unique contributions civilian scientists were able to bring to the war effort, many others are overfull with bitterness, resentment, and acrimony towards the military authorities’ incompetence and their criminal misuse of the mathematicians’ or of the scientists’ special abilities. An instructive example of the second attitude can be found in the pamphlet privately published by the physicist and industrialist, Georges Claude: “Our savants? Ah! if only you knew what was done of them [*ce que l’on a fait d’eux*]! If only you knew their hopes, their efforts, their struggles, and in the end their powerlessness” [Claude 1919, p. 33].<sup>20</sup> By contrast, Patard underscored the difficulty faced by the military members of the Gâvre Commission when they endeavored to integrate civilian scientists into their working procedures. Although Haag was asked to work on the solution of a new problem (anti-aircraft gunnery) and, in the process, introduced new mathematical methods at Gâvre (error analysis), the main problem, as Patard saw it, lay in containing scientists’ impatience, acquainting them with the Gâvre tradition and making them comply with entrenched working procedures.

Some scientists seemed to have been quite aware of the fact that they were stepping on other experts’ turf when they offered their help to military engineers. Aimé Cotton (1869–1951) was an established physicist and already recognized by military officials for having developed, in collaboration with Pierre Weiss (1865–1940), one of the most successful instruments used in sound-ranging. In 1916, Cotton wrote General Hubert Gossot (1853–1935), a former President of the Gâvre Commission, to offer his help on the problem of determining the effect of weather conditions on artillery fire. It is interesting to note the very cautious wording used by Cotton in his letter: “if you judge that the reflections of a physicist who is perforce incompetent on many points may be of some interest to you, I put myself at your disposal to extract from them results that would seem useable and to give them [the results] a form more easily applicable in practice (relying on the advice of men of the trade).”<sup>21</sup> Clearly, rather than assuming that he knew better, the physicist placed himself at the disposal of the military and not merely of his country.

Tradition at Gâvre was no empty rhetoric. It was the bedrock of its scientific credibility. One is struck not only by the palimpsest-like manner in which the history of the Gâvre Commission has been written and rewritten on several occasions by some of the major ballisticians who worked there, but also by the insistence put on tradition, despite important breaks in the methods and despite rapid changes in the gunpowder and materials used by artilleries.<sup>22</sup> As Charbonnier wrote in

<sup>20</sup>On Claude, see [Aubin 2003] and [Baillot 2010].

<sup>21</sup>“*Si vous estimez que les réflexions d’un physicien, nécessairement incompetent sur bien des points, présentent quand même quelque intérêt, je me mets à votre disposition pour en extraire les résultats qui paraîtraient pouvoir être utilisés et leur donner une forme plus facile à appliquer pratiquement (en m’aidant des conseils des gens du métier)*” [SHD–Terre, 2W292; Cotton to Gossot, February 8, 1916].

<sup>22</sup>Besides [Charbonnier 1906] and [Patard 1930] already cited, other insider’s histories of Gâvre are: [Poyen-Bellisle 1889–1893] and [Crémieux 1930]. Secondary literature about the Gâvre

1906, Gâvre was characterized by its special virtues: “respect for the continuity of doctrines, freedom of thought, faith in experimentation, [and] patience for long computations and for careful verifications” [Charbonnier 1906, pp. 425–426]. Another ballistic engineer, Maxime Crémieux, would concur in 1930: “beyond all experimental and theoretical investigations, one senses a working method that presided over the whole: . . . submission to experimental facts, scientific probity, respect of tradition, minute consideration of details, clarity of deductions, freedom in technical opinions” [Crémieux 1930, p. 145]. Let us be more specific: although it has remained in the shadows of more public institutions, like observatories and laboratories, or institutions recently studied in more details, like factory workshops, Gâvre was one of the main theaters for the development of strict experimental procedures in the nineteenth century. Indeed, it is probably no exaggeration to say that it was one of the places where modern procedures for the mathematical and quantitative testing of theories against experiments were designed and tested on a large scale.<sup>23</sup> In ballistics, the comparative merits of empiricism and theory were often discussed explicitly. Like the observatory, it played a leading role in the slow convergence between empirical procedures and theoretical approaches derived from Newton’s first principles.<sup>24</sup> “While mathematicians subsequent to Cauchy were usually more interested in proofs of existence and in functional relations among solutions obtained, than in numerical results, there were already cultivated two fields which especially called for numerical methods, namely astronomy and ballistics” [Bennett et al. 1956, p. 61]. While one may contest Bennett’s view of mathematicians on the ground that the latter did manifest some interest in computation, one cannot deny the importance of astronomy and ballistics for the history of computing.

After the establishment of the Gâvre Commission, it was the Professor of Hydrology at the Lorient Naval School, Félix Hélie (1795–1885), who soon assumed the scientific leadership.<sup>25</sup> Starting in 1834, after summers devoted to experimentation and cannon testings, Hélie alone would carry out all the computations needed to interpret the experimental results and draft all the reports sent to the Navy Ministry. A staunch empiricist, he distrusted theories developed from first principles, which gave poor results when tested on the proving ground. Charbonnier thought that, in his work, Hélie showed more patience than originality [Charbonnier 1906, p. 413]. In Hélie’s mind, every new range table had to be established through extensive experimental work, and the laws and formulas derived from this massive work could hope for no more than an ephemeral existence. In his *Traité de balistique expérimentale*, Hélie developed his method: summarize experimental results by as simple a mathematical formula as possible that should not be applied outside of the experimental limits used to derive it. He opened this treatise with the following words:

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Commission is however much rarer, but see [Bru 1996], [Seddik-Ameur 2003], and [Mounier-Kuhn 2010, pp.194–195]. On ballistics in France more generally, see also [Belhoste & Lemaitre 1990] and [Fontanon 2005].

<sup>23</sup>On the role of the military in scientific research in France in the period preceding the establishment of the Gâvre Commission, see [Bret 2002]. For studies on the history of observatory techniques in the 19th century, see [Aubin et al. 2010].

<sup>24</sup>On the history of the observatory in the nineteenth-century, see [Aubin et al. 2010]. On the importance of computing between theory and practice, see [Warwick 1995].

<sup>25</sup>On Hélie, see [Delauney 1892] and compare with the history of ballistics at Metz in [Bru 1996].

The principles of rational mechanics are not sufficient to solve [all the questions relative to artillery shooting and its effects]; the forces and resistances at play can only be appreciated through observation. A treatise on ballistics must therefore be in large part composed of descriptions and discussions of experiments whose results are often the only possible demonstration for the propositions which one may consider as having been established [Hélie 1865, p. 1].

Hélie's attitude may in part be explained by the fact that, compared to the academic setting, the Gâvre Commission was never allowed to lose sight of its practical mission: to produce the knowledge necessary for aiming guns accurately. So, even when later ballisticians expressed the wish to revalue the role of theory in their field (see below), they came up with stringent criteria.<sup>26</sup> According to the Gâvre ballisticians, a theory was judged satisfactory only in so far as it could be checked numerically, even if this entailed a considerable amount of work [Charbonnier 1906, p. 432]. According to Crémieux, the Gâvrais character was shaped in this period and entailed an "absolute respect" for carefully documented experimental results and repugnance toward erasing disagreement between theory and experiment. On the contrary, all discordances had to be underscored in written reports so that one knew exactly where methods were in need of improvement [Crémieux 1930, p. 149]. This was, Charbonnier insisted, the application of Francis Bacon's method, which led to practical prescriptions: (1) never to fire a useless shot; (2) never to fire a necessary shot without having first computed all experimental results expected from it; and (3) "perform all experiments necessary in the toughest circumstances, that is such that disagreement between theory and experiment has the greatest chance of manifesting itself."<sup>27</sup>

For theoretical considerations to be put in practice, he added, three precautions were required:

- (1) compute all necessary tables in full, without disdainfully leaving this vulgar care to technicians [*praticiens*];
- (2) provide full and detailed numerical examples;
- (3) prepare with great care computation skeletons, which can be lithographed and whose columns are merely left so to speak to be filled out numerically.<sup>28</sup>

In short, Charbonnier wrote, the Gâvrais character could be summarized as "a very practical outlook . . . which holds a theory as satisfactory only in so far as it has been numerically checked, compared to all the known experiments, and when necessary numerical tables have been computed often at the price of considerable and off-putting labor an idea of which only those who have themselves executed a similar task can have" [Charbonnier 1906, p. 432].

In 1915, procedures followed by the Gâvre Commission therefore were particularly stringent. They were solutions adopted over the course of almost a hundred

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<sup>26</sup>Note that this was not only felt at Gâvre. See the way in which an engineer in the artillery branch of the Creusot Factories argues in favor of theory and for the insufficiency of experiments alone in [Morel 1904, p. 7].

<sup>27</sup>[Charbonnier 1906, p. 417]. One should here be reminded that in the course of the 19th century it became increasingly expensive to fire a cannon shot.

<sup>28</sup>[Charbonnier 1906, p. 432n].

years of confrontation with intricate problems and practical demands from fighting artillerymen on ships around the world. If these procedures insured the international high regard in which results coming out of the Gâvre were held, “doctrinal” thinking, the requirements of efficiency, and respect for hierarchy also rigidified procedures. Once adopted after extensive series of tests, computing procedures were rarely changed and then only after much debate. To understand what was at stake in theoretical and practical ballistics at the time when Haag and his colleagues reached the Gâvre peninsula, let us now briefly review the status of exterior ballistics at that time.

## 2. Exterior ballistics before 1915

Ballistics is a complex science in which theoretical, experimental, and computational uncertainties always clash with one another. Moreover, technological innovation in cannon and projectile design sometimes increased the complexity of the problem. The first complication to consider came from the fact that the motion of a projectile actually involves two very different sets of problems: interior ballistics, which deals with what happens inside the cannon muzzle, can be tackled mostly by mobilizing the tools of thermodynamics and chemistry, and exterior ballistics which is mainly a mechanical and mathematical problem. Both problems, moreover, require some input from fluid mechanics. It is a remarkable fact that up to WWI, and beyond, military ballisticians would address both interior and exterior ballistics, often with an equal degree of competency.

Restricting our attention to exterior ballistics, while the laws of dynamics easily allowed the determination of the differential equations governing the trajectory of a projectile through the air, various effects combined to make its general solution very hard to find. At the beginning of the 20th century, Charbonnier drew inspiration from astronomical methods to introduce a useful distinction that considerably simplified the presentation of exterior ballistics [Charbonnier 1907].<sup>29</sup> “Secondary” problems, as he called them, were considered perturbations to the “principal” problem. They were supposed to take into account the effects of the wind, of variations in atmospheric temperature and pressure, of the wear of the piece, of the projectile’s spin around its axis, of the earth’s rotation, etc. The principal ballistic problem therefore amounted to solving an ordinary differential equation, called the “hodograph,” whose simplest form was:

$$(2.1) \quad dv_x = \frac{cv}{g} F(v) d\tau,$$

where  $v$  is the magnitude, and  $v_x = v \cos \tau$  the horizontal component, of the velocity  $v$  of the projectile in the  $(x, y)$ -plane, expressed as a function of the uniformly decreasing angle  $\tau$  with respect to the horizontal at each point of the trajectory (figure 4);  $g$  is the acceleration due to gravity at the surface of the earth (taken in first approximation to be constant);  $c$ , the so-called “ballistic coefficient” (varying according to the size and shape of the projectile); and  $F(v) = f(v)/v^2$ , the

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<sup>29</sup>Many publications give the state of the art in the first decade of the 20th century; see, e.g.: [Gilman 1905] and [Cranz & Vallier 1913].

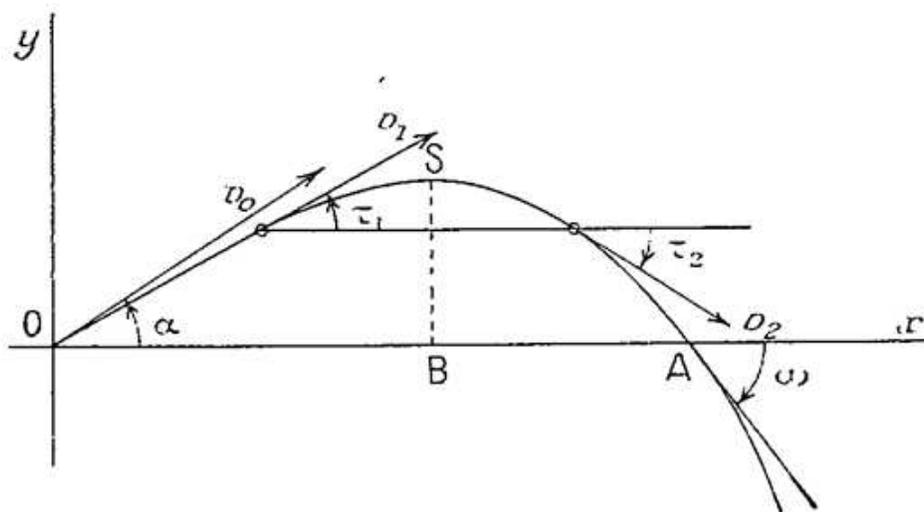


FIGURE 4. Schematic representation of a projectile's trajectory, displaying variables relevant to the hodograph. On this view, taken from [Adhémar 1934, p. 7], two steps in the piecewise integration method, at angle  $\tau_1$  and  $\tau_2$ , have been pictured. At a generic point on the trajectory, the magnitude of the velocity was simply noted  $v$  and the angle with the horizon  $\tau$ . Courtesy of MIR Library, Paris.

law of resistance of the air to the motion of the projectile supposed in first-order approximation to be a function of  $v$  only.<sup>30</sup>

The principal ballistic problem is therefore mathematically equivalent to finding the solution (or at least a fairly accurate approximation of certain quantities derivable from the solution) of an ordinary differential equation involving some unknown functions. Issues connected to the resolution of the principal ballistic problem were of three sorts: (1) how to compute the ballistic coefficient  $c$ ; (2) what was the exact form of the air resistance function  $F(v)$ ; and (3) in case these quantities gave rise to differential equations that were insoluble by formal means, what was the best method for finding a good approximation of the solution? Although at first sight the former two questions would seem to be soluble by the tools of fluid mechanics and the latter to be a purely mathematical problem, all questions were intertwined, a fact that can be illustrated by recalling that in the first experiments carried out by the Gâvre Commission, before the ballistic pendulum was introduced there, initial bullet velocities were essentially determined by measuring the range of their trajectories!<sup>31</sup>

<sup>30</sup>Because of its great simplicity, I adapt here Charbonnier's own presentation in [Charbonnier 1929]. Note however that he also included as another factor the air density  $H(y)$  that prior to WWI was generally taken to be a constant in the principal ballistic problem (corresponding to low altitude trajectories). When vertical differences in air density were taken into account (as a secondary problem), an exponential law  $H(y) = e^{-hy}$  was usually assumed. A very similar, equivalent expression is found in [Charbonnier 1906, p. 449].

<sup>31</sup>Invented by Benjamin Robins in the 18th century, the ballistic pendulum was greatly improved by the ballisticians of the Metz Artillery School, Guillaume Piobert, Arthur Morin, and

**2.1. Ballistic Coefficient and Air Resistance.** At the beginning of WWI, the Gâvre Commission had, under Charbonnier’s leadership, adopted a theoretical framework and strict computational procedures for dealing with exterior ballistics. If the practical needs of the artillery were thereby met by the Gâvre savants, any unforeseen innovation modifying shooting parameters would immediately throw ballisticians into uncharted territory. For most purposes, reliable results seemed to be obtained using the following formula for the ballistic coefficient:

$$c = \frac{i\Delta_0 a^2}{p}$$

where  $\Delta_0$  was the air density on the ground;  $a$  and  $p$ , respectively, the calibre and the weight of the projectile and  $i$  its “form factor” often considered proportional to  $\sin \gamma$ , with  $\gamma$  the penetrating angle at the tip of the projectile. But all attempts at securing a theoretical foundation for this formula remained elusive.

As far as the resistance law was concerned, ballisticians first used the Newton resistance law proportional to the square of the velocity ( $v^2$ ). When rifled barrels were introduced, initial speeds greatly increased and the Alexandre-Hippolyte Piton-Bressant (1820–1847) resistance law (proportional to  $v^4$ ) was adopted for a while.<sup>32</sup> In the second half of the century, smokeless powder again increased initial projectile speed. New extensive series of experiments were carried out in the 1860s by Nikolai Maievski near Saint-Petersbourg in Russia and by Francis Bashforth with the help of his electric chronographs in Woolwich England. In the next decades, new evidence from experiments performed from 1879 onward by the Krupp Company on the Meppen shooting range in Germany and by Colonel Hojel in Holland in 1884 showed that the resistance law decreased at higher velocity. As a result the functional form of the law became tremendously complicated. In Italy, Francesco Siacchi (1839–1907) suggested the following expression [Cranz & Vallier 1913, p. 16]:

$$F(v) = 0.2002v - 48.05 + \sqrt{(0.1648v - 47.95)^2 + 9.6} + \frac{0.442v(v - 300)}{371 + \left(\frac{v}{200}\right)^{10}}.$$

In 1896, an empirical resistance law was adopted at Gâvre: the famous “*fonction de Gâvre*.” Thousands of numerical results, derived from firing tests with initial speeds from 400 to 1200 m/s with all calibres and all types of projectiles were used to determine this function which was presented as a table, as a graph, and, finally, as an analytic expression introduced by *chef d’escadron* Demogue [Crémieux 1930,

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Isidore Didion in the 1840s [Didion 1860, pp. 321–326], [Morin & Tresca 1860, vol. 1, pp. 228–233]. It was adopted by the Gâvre Commission in the same decade. On the Metz artillery school, see [Belhoste & Picon 1996].

<sup>32</sup>Many other laws  $f(v)$  were suggested and used in the 19th century:  $bv^3$  by Bashforth;  $av^2(1 + bv)$  by Saint-Robert;  $av^2(1 + bv^2)$  by Didion;  $a + bv$  by Chapel, etc. See [Charbonnier 1906, p. 444]. A short and simple mathematically-oriented introduction to the question of air resistance is to be found in [Long & Weiss 1999].

p. 152].<sup>33</sup> According to Haag,<sup>34</sup> the function used during WWI had the following form where the exponential term was introduced by the naval engineer, Maurice Garnier:

$$F(v) = v^2 \left[ 0.255 + \frac{\sqrt[4]{1 + 0.0392 \left(\frac{v-300}{50}\right)^8}}{27,226 + 494 \left(\frac{v-330}{50}\right)^2} \arctan \frac{v-330}{50} \right] \exp\left(\frac{v-600}{10^6}\right).$$

**2.2. Siacci's Direct-Fire Approximation.** Eschewing simple power laws for the air resistance often meant that resulting differential equations became intractable by formal methods.<sup>35</sup> Two types of approximation methods were used by the Gâvre Commission: (1) step-by-step integration methods [in French, *calcul des trajectoires par arc*], and (2) approximations derived using the “direct-fire” assumption [in French “*tir de plein fouet*”]. Let us review how they were successively adopted by the Gâvre Commission for the computation of firing tables.

Step-by-step integration methods, which French ballisticians called the “arc method,” dated back to Leonhard Euler (1753).<sup>36</sup> In this approach, the equation was solved on a small interval only assuming that the air resistance was quadratic over the interval. Interest in these methods was given a boost when the second edition of Hélié's treatise was published in 1884.<sup>37</sup> After the Franco-Prussian War and the death of Hélié in 1887, the “struggle engaged between traditionalism and progress was vigorously undertaken” [Charbonnier 1906, p. 416] and ballisticians at Gâvre adopted a more theoretical approach. The second edition of the treatise received significant contributions from the polytechnician mathematical physicist, Pierre-Henry Hugoniot (1851–1887), whose inclination for mathematical theories was much greater than Hélié's.<sup>38</sup> While the work of Bashforth and George Greenhill in Britain, of Francesco Siacci (1839–1907) in Italy, and of Carl Cranz (1858–1945) in Germany was renewing the field of ballistics, Hélié and Hugoniot showed that

<sup>33</sup>The resistance law was first expressed as a numerical table and presented in reports nos. 1414 and 1429 of the Gâvre Commission (March 14 and July 21, 1896), giving  $\log f(v)$  or  $\log[f(v)/v^2]$  for values of  $v$  from 0 to 1200 m/s; see Table I1 in [Gâvre 1916, pp. 3–6]; “Tableaux nécessaires au calcul des trajectoires par arcs successifs” [SHD–Terre, 2W292], and [Bingen 1928, pp. 20–22]. One finds a graphic representation of the laws and the various experimental trials that led to it in [Cranz & Vallier 1913, p. 17].

<sup>34</sup>[Haag 1921, p. 3]. Note that there is a mistake in this function. To reproduce the numerical data in published tables, the coefficient of the arctangent, and this one alone, should be multiplied roughly by a factor of 3500.

<sup>35</sup>During the war, several mathematicians studied conditions to be imposed on  $F(v)$  in order for the hodograph to remain integrable. This is point 2 in the report on ballistics drafted after the war [Hadamard 1920]. Jules Drach suggested a method using Galois theory in 1914. Denjoy wrote a report about this method while he was at the Gâvre Commission in July 1917. For more on this, see [Drach 1914], [Drach 1920]. See also the note written by Paul Montel in [Charbonnier 1927, vol. 1, pp. 498–515]. Several notes and letters concerning Denjoy's role are to be found in [Academy of Sciences, “Ballistics” file of the “*Commission nommée pour l'étude des questions la défense nationale*,”].

<sup>36</sup>On the early history of exterior ballistics, see [Charbonnier 1929], [Hall 1952], and [Steele 1994].

<sup>37</sup>Note that while the second edition of the treatise was published by two authors [Hélié & Hugoniot 1884], the first one had only one [Hélié 1865].

<sup>38</sup>On the life and work of Hugoniot, see [Chéret 1990]. A clear offshoot of his ballistic studies, Hugoniot's seminal paper on shock compression was published in two parts in the *Journal de l'École polytechnique* in 1887 and 1889.

old step-by-step methods could be as accurate as desired, provided the intervals chosen were numerous and small enough [Hélie & Hugoniot 1884, vol. 2, p. 289].

After Hugoniot's untimely death in 1887, Hubert Gossot, also a graduate of the *École polytechnique* (1874) who had joined the Naval Artillery Corps, took over the Gâvre Commission.<sup>39</sup> In 1887 and 1888 he used the method to compute firing tables for new 34-cm and 90-mm caliber cannons. At long last, the Gâvre Commission had mastered a method for computing firing tables that was safe, accurate, and dependable. But it was also time-consuming and, many felt, inelegant: it was “a computing process, not a theory” [Patard 1930, p. 243].

The Commission thus consented to submit itself deliberately and for many long years to the boredom of very long, very fastidious and very inelegant computations using the step-by-step method . . . because it understood what were the consequences of its liberation from empirical methods and of the return of ballistics back to its natural source: possibility a priori of computing any trajectory from any cannon; extreme reduction of ballistic shots needed to establish a firing table; . . . exact determination of non observed elements of the trajectory ([Charbonnier 1906, p. 423]; quoted in [Patard 1930, p. 243]).

A second group of methods was concurrently developed for approximately solving the hodograph. The most successful was introduced in 1880 by Siacci whose treatise was quickly translated into French. The principle of the method was to replace the velocity  $v$  by a pseudo-velocity  $u$  defined as [Siacci 1892, p. 47]:

$$v \cos \tau = u \cos \alpha,$$

where  $\alpha$ , called the angle of projection (or line of departure), corresponded to the actual initial shooting angle.<sup>40</sup> The pseudo-velocity was equal to the velocity only at the origin and in the descending branch of the trajectory when  $\tau = -\alpha$ , but in the case of direct fire when the angle  $\tau$  was close to zero over the whole trajectory, the difference between velocity and pseudo-velocity also remained small. Writing the hodograph equation in terms of the pseudo-velocity  $u$ , Siacci found a general equation for the trajectory [Siacci 1892, p. 49]:

$$(2.2) \quad y = x \tan \alpha - \frac{gx^2}{2v_0^2 \cos^2 \alpha} G\left(\frac{x}{c}\right),$$

where  $G$  was a function that depended on the air resistance law  $F(u)$  that was adopted, but that could be computed, provided four secondary functions  $J(u)$ ,  $S(u)$ ,  $D(u)$  and  $A(u)$  defined as follows were computed and tabulated for every value of  $u$ :

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<sup>39</sup>On Gossot, see [Challéat 1933–1935, vol. 2, p. 314] and [SHD–Terre, 11–Yd–47]. Gossot was later Central Director of Naval Artillery (1905–1909) and *Inspecteur des études et expériences techniques de l'artillerie* from July 1915 to 1917.

<sup>40</sup>Note that Siacci used  $\theta$  instead of  $\tau$  and  $\varphi$  instead of  $\alpha$ .

$$\begin{aligned}
 J(u) &= -g \int \frac{du}{uF(u)}, & D(u) &= - \int \frac{udu}{F(u)}, \\
 S(u) &= - \int \frac{du}{F(u)}, & A(u) &= - \int \frac{uJ(u)du}{F(u)}.
 \end{aligned}$$

Using the tabulated values of these functions, most elements of a trajectory could be computed rather quickly, typically in less than twenty to thirty simple operations. For example, given the value of the pseudo-velocity  $u$  at a point on the trajectory and the initial velocity  $v_0$ , the  $x$ -coordinate of the projectile was simply given by the formula  $x = C[D(v_0) - D(u)]$ , for a certain constant  $C$ . Siacci also relied on the assumption that a certain variable  $\beta$  was constant and equal to 1. Under this assumption, the results computed using Siacci’s method remained relatively reliable in the case of direct fire, that is, provided  $\alpha < 20^\circ$  [Charbonnier 1907].

To compute deviations due to secondary problems such as the rotation of the projectile or wind, a few other secondary functions were required, all of which were computed and tabulated. Written by the ballistician Anne, Gâvre reports from December 23, 1912, and July 28, 1913, contained the required tables. Having joined the Gâvre Commission in 1907, Anne died in October 1921, “worn-out by the exhausting labor he was submitted to during the war” [Patard 1930, p. 293]. This extensive computing effort was completed and printed in January 1916 [Gâvre 1916]. By that time, however, war had made them obsolete!

### 3. The Mathematical War Viewed from the Front

“One of the surprises of the present war,” the ballistician Emmanuel Vallier (1849–1921) from the Academy of Sciences wrote in May 1915, “certainly is the great development of indirect fire” [Vallier 1915, p. 297]. Few indeed had foreseen the tremendous change of fortune artillery—and as a result ballistics—would undergo during WWI. To understand the evolution of problems and solutions considered worthwhile at Gâvre, one needs to take into account fighting men’s reactions to what the Commission had to offer. While it struck the “everyman at war” that mathematics played a crucial part in his predicament, the way this was translated in practice is straightforward.<sup>41</sup> Indeed, the very usefulness of the mathematical apparatus for ballistics was drastically questioned. Due to the rapid evolution in the tactical and strategic use of artillery, commanding officers immediately found that mathematical support for directing fire was imprecise, confusing, or simply lacking. At the hostilities’ outbreak, there even seemed to have been a widespread sentiment among artillerymen that, as a practical science, mathematical ballistics had failed them and a “conflict arose between artillerymen and their [firing table] suppliers” [Boissonnet 1920, p. 36].

At a strategic level, it was quickly realized that artillery was to play a major role in this war. Less than a week after the declaration of war, Captain Lombal observed that the standard 75-mm cannon adopted by the French Army in 1897 (fig. 5) was unexpectedly deadly. With just 16 shots fired on August 7, 1914, he estimated he had taken down 600 to 700 German cavalrymen. Some computed

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<sup>41</sup>This alludes to British Private Edgar Norman Gladden’s feeling that this was a “war of guns and mathematics” [Gladden 1930, p. 121]. See the introduction to this volume by David Aubin and Catherine Goldstein.

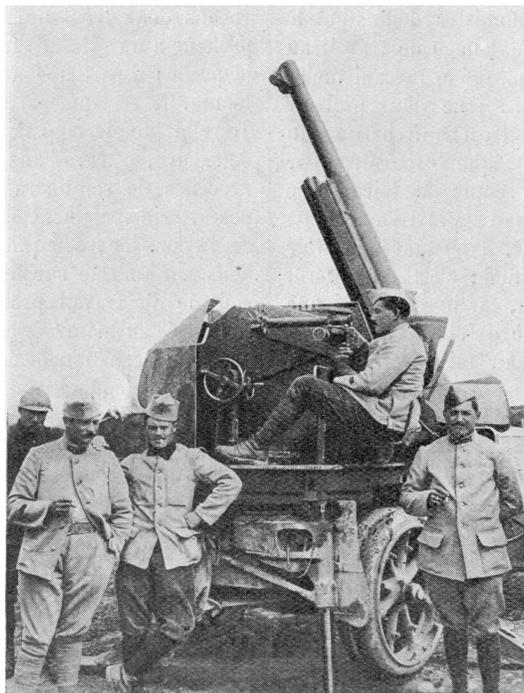


FIGURE 5. The celebrated 75-mm cannon of the French field artillery, here adapted for anti-aircraft shooting. Note the high-angle of shooting. From *La Nature* 44–2 (1916), p. 135. Courtesy of the MPIWG, Berlin.

that this amounted to one dead per kilo of explosive—and marveled at such a high return!<sup>42</sup>

Among the first “lessons” drawn from the emergence of scientific warfare was the conviction that heavy artillery now played a much bigger role than expected (see, e.g., [Bos 1923] and [Rouquerol 1920]). Following General Hippolyte Langlois’s doctrine, the French Army had hitherto emphasized the auxiliary role of artillery with respect to infantry in open warfare. A regulation of 1913 that is often quoted stated: “artillery does not prepare the attacks, it supports them.”<sup>43</sup> Despite the success of “the little Frenchman” as the light rapid-firing 75-mm cannon was sometimes called [Sainean 1916, p. 145], in 1914 the French troops’ morale greatly suffered from the German domination in terms of heavy artillery. Shell shock was made worse by the evidence that the long range of German guns kept them out

<sup>42</sup>[Gascouin 1920, pp. 78–81]. On the 75-mm cannon, literature is abundant; see especially an early praise [Houllevigue 1914], and more informed studies in [Challéat 1933–1935, vol. 2, pp. 338–364] and [Rouquerol 1919, pp. 58–77].

<sup>43</sup>“*L’artillerie ne prépare pas les attaques, elle les appuie*” (quoted in [Gascouin 1920, p. 56]). For the French combat doctrine before WWI, see [Percin 1914, p. 165], and [Foch 1903, p. 314]. This doctrine was by and large based on [Langlois 1892] and [Langlois 1906]. On Langlois, see [P.N. 1907], [Glück 1919], and [Ripperger 1995]. For contrary opinions expressed just before the outbreak of WWI, see [Herr 1913] and [Rouquerol 1914].

of reach of their French counterparts, which were overwhelmed, too few in numbers, and generally outdated. The President of the Republic, Raymond Poincaré, lamented the lack of cannons and ammunition. Marshall Ferdinand Foch himself underscored the inefficiency of the 75s for indirect fire. In this domain as well as in many others, unpreparedness seemed appalling not only to military officers but also to some astute civilian observers.<sup>44</sup> What made this realization even more painful was the fact that it had been discussed at length in artillery circles just before the war.<sup>45</sup> In haste, naval artillery and siege cannons were brought to the frontline and positioned on terrain they had not been designed to occupy. As is well known, new material was ordered en masse. In May, the Socialist Member of Parliament, Albert Thomas, was put in charge of armament production at the ministerial level, and the former Director of Artillery, General Louis Baquet, was sent back to the front: in his eyes, a politician was “better armed than a general to sustain political assaults.”<sup>46</sup> In the summer of 1915, the French Army started to receive new pieces of large caliber.

While the strategic importance of artillery, and especially heavy artillery increased significantly, the tactical use of cannons underwent important changes as well. Anti-aircraft and anti-zeppelin firing, mountain engagements, and the general need for shooting from entrenched positions behind a protective monticule—which was called indirect fire—required new procedures. In August 1915, General Frédéric-Georges Herr was put in charge of the defense of Verdun and suffered the full blow of the German offensive in February 1916. In 1912, Herr had observed the Balkan wars and predicted many of the features of the war he was now fighting [Herr 1913]. By 1915 it had become clear to him that the main problem facing artillery was no longer a simple question of supply and materials: “a gigantic intellectual effort was required.” In particular, shooting had become the focus of attention. “It had become necessary to [be able to] shoot on invisible objectives, during the night, and, in all circumstances, shots had to be of the utmost accuracy . . . so as not to hit friendly troops” [Herr 1923, p. 39]. Now, to shoot accurately had become a complex technoscientific problem, which involved the identification of targets using sound-ranging or aerial reconnaissance, their localization on large-scale maps that needed to be produced in large quantities, the development of reliable telephonic communication between observers and gunners, better knowledge of meteorological data at various altitudes (wind, pressure, and temperature), and precise firing tables. “Meteorology, acoustics, optics, cartography, what branch of science was not drafted in artillery’s service?” [Bédier 1919, p. 180]. As a testimony of the importance of artillery in the war, it is worth noting that, in all these areas, significant technological and scientific advances were made from 1914 to 1918.<sup>47</sup>

The new guns required new firing tables. The new uses demanded that existing tables be extended to higher shooting angles. It had made sense to compute direct

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<sup>44</sup>For example [Lebon 1915, p. 220] and [Reinach 1916, pp. 253–260]. See also the testimonies of the commanders, such as [Poincaré 1928, vol. 5, pp. 333–334] or [Foch 1931, vol. 1, p. 19]. On the insufficiencies of the 75, see [Percin 1914, p. 264].

<sup>45</sup>See [Ripperger 1995], as well as [Bédier 1919, pp. 147–157].

<sup>46</sup>[Baquet 1921, p. 15]. For an overview of the evolution of the materials in the artillery during the war, see [D’Aubigny 1921].

<sup>47</sup>On observation, see [Morgan 1959–1960]. On map-making, see [Laves 1919, Winterbotham 1919, Heffernan 1996]. On sound-ranging, see note 6 above. On meteorology, see [Launay 1919, Launay 1922].

fire tables for guns to be used at sea, just as there was no harm in relying on time-consuming procedures to adjust the fire of siege cannons. This was no longer the case. Information was needed about the whole trajectory of projectiles, and not just their range. Hence the change in terminology, whereby what used to be called “range tables” was now known as “firing tables.” But ballistic military structures were totally unprepared to supply them. When war broke out in August 1914, Gâvre was no exception to this general trend. All but five officers deserted the proving ground and joined fighting units. For lack of personnel, most technical activities were abruptly interrupted, and the five military engineers who remained desperately idled at Gâvre while their repeated requests to be reassigned to the front were denied one after the other.<sup>48</sup>

To make matters worse, while the Navy had paid small attention to ballistics, the Army had paid almost no attention to it. Before 1914, low regard, and indeed disdain, for ballistics was entrenched among artillerymen.<sup>49</sup> Despite a rich tradition of ballistic studies, in the first decades of the century the Officers’ Training School for Artillery and Engineering in Fontainebleau (the *École d’application d’artillerie et du génie* formerly located in Metz, mentioned earlier) allowed time for barely four lessons in the officers’ training curriculum devoted to ballistics and the principles of firing tables.<sup>50</sup> A conscript once complained that during instruction, “ballistics [was] nothing other than a soporific lesson in terminology” [Malloué 1911, p. 136]. As a result, the philosopher Alain [Émile Chartier] who served in the artillery during WWI was hardly impressed by the mathematical skills of the polytechnicians he met on the front: “Our artillerymen seemed poor mathematicians to me.”<sup>51</sup> More shockingly perhaps, among the staggering number of casualties there were not only young mathematicians who might later have turned out to be precious resources for ballistic work, but also fully-trained ballisticians whose expertise was acutely missed at Gâvre. Born in 1871, Commandant Henri Batailler had been in charge of the ballistics course at the Fontainebleau school, and he had already published several articles on the topic in the *Revue d’artillerie*. But on June 9, 1915, Commandant Batailler was killed on the Marne front.<sup>52</sup>

“Up until 1916, the artilleryman and the ballistician lived on knowledge acquired in peace time” [Boissonnet 1920, p. 41]. In fact, artillerymen in fighting units more often than not were forced to resort to their own means for improving the accuracy of their fire. On September 9, 1914, Jules-Émile Henches wrote from the Marne front that “each day” he became more and more convinced that in the fighting “science is necessary, but its application must be [made] the simplest possible” [Henches 1918, p. 8].<sup>53</sup> “War,” wrote the physicist and astronomer Charles Nordmann, who actively served both in the artillery and on the Commission of Inventions, “had ceased to be an art to become an experimental science like physics”

<sup>48</sup>[Patard 1930, p. 270n] and [Crémieux 1930, p. 158].

<sup>49</sup>See, e.g., [Baquet 1921, p. 28n] and [Anonymous 1921].

<sup>50</sup>[Challéat 1933–1935], vol. 2, p. 64, n. 1; see also p. 259; Challéat’s course at Fontainebleau most probably condensed the lessons of his predecessor *chef d’escadron* Pierre-Émile Henry, who was among those who introduced Siacci’s methods in France [Henry 1894]. On ballistics at Metz and Fontainebleau, see [Bru 1996].

<sup>51</sup>“*Nos artilleurs m’ont paru assez peu géomètres*” [Alain 1937, p. 115].

<sup>52</sup>[Sebert 1915]; see also [Garnier 1920, p. 8].

<sup>53</sup>Also interesting in regard to the scientific work of artillerymen on the front are the following testimonies [Pastre 1918, Lintier 1916, Cardot 1987].

[Nordmann 1917, p. 9].<sup>54</sup> The front itself was likened to a gigantic experiment in ballistics that should be exploited to increase shooting accuracy: “Because of the rich harvest in experimental shooting that everyone is able daily to reap on the front, firing tables produced before the war were found to hold insufficient, and even erroneous, information” [Herr 1923, p. 40].

In fact, badly equipped experimental polygons sometimes lagged behind the front, notably in the study of atmospheric densities [Boissonnet 1920]. Using accurate ballistic coefficients (provided by ballisticians) and atmospheric studies made by the meteorologists enrolled by the Army, fighting artillerymen were able to find inaccuracies in the Gâvre air resistance function, which had hitherto remained within the margin of error. Frontline expertise was developed, with which ballisticians from the rearlines were hard pressed to compete. Reports had been written by officers on the front questioning either the accuracy of the air resistance function  $F(v)$  or the firing tables themselves. Some officers were worried “not only about the firing tables at their disposal, but also about those that can still be delivered to them, if they are computed on the basis of the present inaccuracies.”<sup>55</sup> A specialist in anti-aircraft shooting since September 1914, Henches wrote from his command post he called “Aviatik-City” on June 18, 1915:

There have been, concerning those airplane shootings, papers over-filled with mathematics done by people who could never see that the instinct of a “hunting animal” is necessary here. They reach, for that matter, by very complicated, inapplicable processes, results that are close to, but not as valuable as, those I have been using for the last six months [Henches 1918, p. 59 & p. 85].<sup>56</sup>

On the front, artillery material was put to much more extensive testing than it ever was on proving grounds, and, in the process, firing tables computed in the rearlines appeared defective. In a letter from General Curières de Castelnau written weeks before he was replaced by Philippe Pétain as the head of 2nd Army, it was stated that regulatory tables for the 75-mm cannon differed from nomograms (or abacs) given to motorized artillery sections. “These discordances not only concern trajectories corresponding to high angles but even trajectories that are regularly used” on the field [SHD–Terre, 2W309; Général commandant la II<sup>e</sup> armée à M.le colonel Leleu, chef de la section technique de l’artillerie, place Saint-Thomas d’Aquin, May 19, 1915]. As a result, commanding officers had their own tables of corrections, or networks of trajectories computed [Boissonnet 1920, p. 39]. Others designed special slide rulers or mechanical aiming devices [Garnier 1922, p. 111]. Some artillery units lost confidence in the tables computed by theoretical means and corrected them on their own by experimental means. “Thus instead of having a single range table carefully established in the rearlines, there were many built with the help of a very large number of shots carried out in lousy experimental conditions.”<sup>57</sup>

<sup>54</sup>On Nordmann, see David Aubin’s contribution in [Goldstein & Aubin forthcoming].

<sup>55</sup>“*Quelques officiers . . . manifestent quelque inquiétude, non seulement sur les tables de tir dont ils disposent, mais sur celles qu’on peut encore leur délivrer, si elles sont calculés par les errements actuels*” [Garnier 1918a, p. 1]. This book which gathers various secret notes written during the war by Garnier can be found in various slightly different versions. I quote from one of the differing copies kept at the Bibliothèque nationale de France, in Paris, call number 8-V-42188.

<sup>56</sup>On the lack of practical knowledge of heavy artillery officers, see also *ibid.*, pp. 149–150.

<sup>57</sup>“*On l’a bien vu au cours de la guerre : il est arrivé souvent, en effet, qu’une batterie, avertie par des insuccès de l’inexactitude de sa table de tir établie par des procédés théoriques,*

The electrical engineer Hippolyte Parodi, who would come to play an important part in computing new ballistic tables for the French Army using graphical methods, underscored that he had first become aware of the initial insufficiency of firing tables while he was fighting on the front:

When I was called to head the *Service de balistique et de préparation des tables de tir*, I had long been aware, according to the shots I had taken or controlled on the front, that the near totality of firing tables in use in the Army were clearly false and that they had been established ... through “archaic,” *inexact* and *simplified* methods.<sup>58</sup>

The tables, Parodi went on, were not only wrong; they were also inconsistent and self-contradictory. Some projectile might, for example, have, for the same line of departure, a greater range for a smaller initial velocity.

These errors and these incoherencies, which thankfully were uncovered only by a handful of artillery officers, were susceptible of arousing doubts in the mind of the combattants and to withdraw all confidence in the technical documents that were distributed to them... Yet, who knows whether by making some battery commanders excessively prudent this distrust would not have allowed, at the beginning of the war, for the saving of precious human lives?<sup>59</sup>

Parodi’s hopes notwithstanding, officers did notice deficiencies in firing tables. “Artillerymen demanded experimental firing tables, established by cannon fire [*à coups de canon*],” not by theory which they distrusted [Boissonnet 1920, p. 40]. In the face of such criticism, professional ballisticians repeated that “exterior ballistics was, before the war, brought by the Gâvre Commission to a degree of perfection which fully satisfied all practical requirements” [Garnier 1918b, p. i].<sup>60</sup> This meant that there existed accurate firing tables corresponding to initial speed up to 850 m/s and initial angle up to 20°. But fighting officers sometimes not only questioned the accuracy of the firing tables they had at their disposal but also the very possibility of computing them with enough precision [Garnier 1918a]. At the *Section technique de l’artillerie*, Parodi concluded that many cannon shots were necessary to establish a firing table: “One should not forget that firing tables are only worth what the

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*l’a rectifiée expérimentalement sur le front. Ainsi, au lieu d’une seule table de tir bien établie à l’arrière, il y en avait plusieurs construites à l’aide de très nombreux tirs, faits dans de mauvaises conditions expérimentales et présentant souvent de gros inconvénients militaires.*” [Academy of Sciences, Lebesgue to Hadamard, October 23, 1919; Commission de la défense nationale, dossier “Balistique”].

<sup>58</sup>“Quand j’ai été appelé à la direction du *Service de balistique et de préparation des tables de tir*, il y avait longtemps que je savais, d’après les tirs que j’avais dirigés ou contrôlés au front, que la presque totalité des tables de tir en usage aux Armées étaient nettement fausses et qu’elles avaient été établies ... par des méthodes ‘archaïques,’ *inexactes* ou *simplifiées*” [Academy of Sciences, Parodi to Hadamard, October 30, 1919; Commission de la défense nationale, dossier “Balistique;” emphasized by Parodi]. On Parodi, see [Darrieus 1968] and [Merger 1994].

<sup>59</sup>“*Ces erreurs et ces incohérences qui, heureusement n’ont été décelées que par un très petit nombre d’officiers d’artillerie, étaient de nature à porter le doute dans l’esprit du combattant et à lui enlever toute confiance dans les documents techniques qui lui ont été remis... Qui sait pourtant si cette défiance, en rendant systématiquement prudents certains commandants de batteries, n’aurait pas permis, au début de la guerre, d’économiser de précieuses vies humaines ?*” Ibid.

<sup>60</sup>See also [Peira 1955–1957, vol. 1, p. 36].

experiments used as a basis for computations are worth, and that the mathematical apparatus [*appareil mathématique*] in which they have been enclosed is incapable in itself of increasing their precision. Many cannon shots must be fired [*Il faut consentir à tirer beaucoup de coups de canon*] [Academy of Sciences, Parodi to Hadamard, October 30, 1919]. Even the mathematician, Henri Lebesgue (1875–1941), who had collaborated with Parodi in the Mathematics Section placed under the under-secretary of inventions concurred: “What is this computing sickness, when experiments are (apparently), and in all cases can be, carried out. There are certainly places in France where real shooting by 75s is done . . . and there is the front.”<sup>61</sup>

The ballisticians at Gâvre therefore felt the need to emphasize that the “mathematical toolbox [*outillage mathématique*]” they used was no “smokescreen [*trompe-l’œil*]” [Garnier 1918a, p. 8]. On the contrary, ballisticians emphasized, mathematics was indispensable for correctly evaluating perturbations depending on the particular circumstances of shooting. As the war unfolded, hopes indeed increased as to the possibility of firing without preparation. Was it possible to open fire on a target, having allowed for all modifications due to the special circumstances by means of computations, without any prior warning? This question had a solution, and all belligerents were looking for it from the moment the war had started.

#### 4. Scientific Work at Gâvre

How the requirements of fighting artillerymen impacted the Gâvre Commission, and the specific role played by mathematicians over there remains to be examined. As was hinted at above, Gâvre was not the only institution involved in the French ballistic effort of 1915–1918. Under Parodi’s energetic leadership, the Calais Commission played a major part in the computing effort together with the Board of Inventions (the *Direction des inventions intéressant la défense nationale*, in which the Paris mathematicians Lebesgue and Montel were also involved). To fulfill his tasks, Parodi suggested that high school teachers and university professors be mobilized for the task. More than 400 answered positively and about 300 effectively worked on the project. The team computed trajectories for every initial angle  $\alpha$  multiple of  $5^\circ$  from  $0^\circ$  to  $90^\circ$ ; for initial velocities varying from 0 to 1000 m/s and for various values of ballistic coefficients.<sup>62</sup> Intense computational work was moreover carried out by the so-called “Commission ALVF” [*artillerie lourde sur voie ferrée*, that is, heavy artillery on rail], the committee in charge of organizing railway artillery headed by Lieutenant-Colonel Girardville, which produced extensive tables giving range as a function of initial angle, initial velocity, and ballistic coefficient.

<sup>61</sup>[Lebesgue 1991], letter CCXIII, p. 319; this letter is tentatively dated early 1915 by Pierre Dugac. On the Lebesgue–Borel correspondence during WWI, see Hélène Gispert’s contribution to [Goldstein & Aubin forthcoming].

<sup>62</sup>Details above come from [Ottenheimer 1924, pp. 51–52]. One should however take these numbers with care. According to a secret report from December 1916, the computing board put together by Lebesgue and Montel had only recruited between 30 and 40 voluntary collaborators including actuaries and astronomers [Fonds Painlevé, 313/AP/62]. Numbers cited by Ottenheimer are considerable considering the available pool of mathematics professors and teachers at the time. Before the war, there were only 65 university professors in mathematics in the whole of France. To approximate the number of high school teachers, one may consider that the professional union [*Association des professeurs de l’enseignement secondaire public*] counted 501 members in 1913, of which 102 were in Paris [Barbazo & Pombourcq 2010].

Contrary to all previous practices, these tables, called the “ $(\alpha, V_0, c)$  tables” (here with a capital “V”) were abstract constructs corresponding to no specific cannon or projectile.<sup>63</sup> At Gâvre, the naval engineer, Georges Sugot, also introduced a new method for speeding up computations, called the fictitious speed method [*méthode des vitesses fictives*] [Sugot 1918].

As was pointed out, all this work, whose immediate usefulness was questioned, was only as good as the physical assumptions on which it was based. Knowledge of air resistance laws and the atmospheric density variation with respect to altitude might be improved with unknown effects on the computed tables. From both a mathematical and a practical point of view, it was the step-by-step method developed collaboratively by the mathematician Haag and the military ballistics Maurice Garnier that was the most innovative as well as the most lasting effort in ballistics during WWI.

On June 16, 1917, Haag was assigned to the testing center of Vitry-le-François where he instructed training officers. On November 29, he was promoted to the rank of Lieutenant. In his commendation, Charbonnier wrote:

Ever since he arrived at Gâvre, M. Haag has studied the improvement and practical application of the new ballistic methods required by present shooting conditions, and especially by the problems of aerial shooting. . . . Monsieur Haag significantly contributed to this work and, among the important questions to whose solution he contributed I must name the following:

- (1) the improvement of step-by-step computing processes;
- (2) the invention and development of a computation method for differential coefficients;
- (3) new and original applications of probability theory to the determination of the detonation ellipses of projectiles with fuses.<sup>64</sup>

Charbonnier’s commendation clearly distinguished between principal and secondary problems in ballistics, as well as problems linked with probability theory. After the war, Haag summarized some of his work on probability theory in the fourth volume of Borel’s *Treatise on Probability* [Haag 1926]. As we shall see below, Haag’s contribution to secondary ballistics problems played a crucial part in increasing the accuracy of scientific shooting procedures. But from a mathematical point of view, it was his contribution to the principal problem of ballistics—to solve

<sup>63</sup>Established in 1916 by the War Ministry, the Commission ALVF had computed several general tables for angles of 22°, 28°, 33° and 44°, with initial velocities between 300 to 900 m/s and various ballistic coefficients. In 1919, the tables used the Gâvre air resistance law and a better estimate of the variation of atmospheric density with altitude [ALVF 1921].

<sup>64</sup>Jules Haag’s military file [SHD–Terre, 6–Ye–17966]: “*Depuis son arrivée à Gâvre, M. Haag a été employé à l’étude du perfectionnement et à la mise en application pratique des méthodes balistiques nouvelles qu’exigeaient les conditions de tir actuelles et en particulier les problèmes de tirs aériens, qui ont pris une importance si grande, aussi bien pour le Département de la Guerre que celui de la Marine.*”

*Monsieur Haag a contribué dans une large mesure à ces travaux et, parmi les questions importantes à la solution desquelles il a collaboré, je dois citer les suivantes :*

- a) *Amélioration des procédés de calculs des trajectoires par arcs successifs.*
- b) *Élaboration et mise au point d’une méthode de calcul des coefficients différentiels.*
- c) *Applications nouvelles et originales du calcul des probabilités à la détermination des ellipses d’éclatement des projectiles fusants.”*



FIGURE 6. Preparing for aerial shooting at the training center for practical anti-aircraft shooting in Arnouville, 1917. From left to right in the foreground, Jules Haag (taking a photo), Garnier, Pagézy (the head of the training center), Rouch (head of the Army Meteorological Service) and an unidentified officer from the training center. From [Patard 1930, p. 288].

the hodograph—that is the most significant. In the following, we shall examine the mathematicians’ work at Gâvre from two perspectives: (1) we will look in more detail at the specific ways in which Haag was able to work on and improve the step-by-step method that, as we have seen, can be dated back to Euler; and (2) we will review collaborative experimental and computing procedures followed at Gâvre and the role played by mathematicians in them.

**4.1. The Theory of Errors.** Already in the note he sent to the *CRAS* in 1915, Haag made an interesting innovation in exterior ballistics. Since, in practice, initial conditions were never known exactly, every gunner was perfectly aware of the need for determining the effects of small variations in the main three parameters: initial velocity, line of departure, and ballistic coefficient. This was usually done by simple interpolation in the tables. Alternatively, Siacci had analyzed, in the case of direct fire, the effect of substituting  $v_0 + \Delta v_0$ ,  $\alpha + \delta\alpha$ , and  $c + \Delta c$  in the equation of the trajectory (equation 2.2). No method existed, however, for providing such estimates in the Eulerian step-by-step method to which one was forced to resort in the case of general trajectories, in particular those involved in airplane bombings with which Haag was at first concerned [Haag 1915a]. With his formal training in mathematical analysis, Haag was easily able to evaluate the size of the error without

having to integrate the equation.<sup>65</sup> In a formal analogy with celestial mechanics, he simply tracked down, at any given order of approximation, the errors thus produced. This is the work that had caught Charbonnier's eye.

When he reached Gâvre at the end of 1915, Haag undertook the systematic study of errors in ballistic theory. The first to work on this problem, he published his results after the war [Haag 1921]. In this account, Eulerian integration methods produced two kinds of error. The *ballistic* error came from the assumption that air resistance was quadratic over the small integration step. The *geometric* error was due to approximations in the method of integration. Assuming that the arc was infinitely small, Haag therefore produced a complete analysis of both types of error. Hopefully, this method would provide an estimate of the maximal arc lengths that gave the precision needed with minimal computation time, allowing the considerable acceleration of the laborious process of computation. At Gâvre, piecewise integration procedures used the angle  $\tau$  of the projectile velocity with respect to the horizontal as the independent variable, whereas American and British ballisticians instead chose time. Following an *ad hoc* rule, arcs were selected so that the angle decreased by less than  $5^\circ$  and the velocity loss did not exceed 50 m/s over the length of the arc. Using his method, Haag could show that this rule was no guarantee against imprecision or inefficiency: "parts of the trajectory are computed with a precision that is much too high, while others are insufficiently precise" [Haag 1921, p. 21]. A new, more complicated rule was derived for determining the arcs for which the relative error remained smaller than 1/500.

Together with the naval engineer, Maurice Garnier, Haag applied this rule and designed a new computing procedure. Computing skeletons can be found in Haag's article [Haag 1921, pp. 18–19, 27 & 30]. Convergence radii of the expansion series were studied carefully to achieve the given precision. This at last provided a basis for making the "rational choice of the amplitude" of integration steps [Garnier 1922, p. 126]. This computing method was called the GH method (for Garnier–Haag) and was presented in a special report in January 1917.

But this scientific method was not as efficient as one might have wanted. Later that year, the mathematics teacher [*agrégé de mathématiques*] Osée Marcus (figure 7), who was employed as a computer, pointed out that computing procedures could be quickened by dispensing with the consideration of radii of convergence and by relying instead on simple Taylor approximations.<sup>66</sup> Incorporating other minor

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<sup>65</sup>Note that Haag's work in ballistics is *not* directly related to his previous research in differential geometry. Supervised by Gaston Darboux, his doctoral thesis dealt with Lamé surfaces [Haag 1910].

<sup>66</sup>A Jewish immigrant from the Baltics, Marcus appears not to have been drafted in a fighting unit. For the rest of his life, he remained on the French Navy's payroll, carrying out computations for them in his home in Neuilly-sur-Seine. I wish to thank Marcus' niece, Simone Marcus, for these informations.



FIGURE 7. Osée Marcus in the 1920s. Courtesy of Simone Marcus.

points made by Captain Lévy (from the Mining Corps)<sup>67</sup> and from Georges Valiron,<sup>68</sup> the GHM (Garnier–Haag–Marcus) method was adopted in September 1917 and remained in use until after World War II in France.<sup>69</sup>

Discussions about the approximation introduced by Marcus highlight a divergence of viewpoints between theory and practice:

In the case of practical computations involving numerical integration, it is more often harmful than useful, more complicated than it is advantageous, to perform the rigorous quadratures provided by analysis. Thus are we sometimes led to reject certain analytical formulae—no matter how elegant and seductive they may seem to a mathematician’s eyes—to perform quadratures by simple approximation methods, apparently coarser, but in truth quicker and more precise [Garnier 1918b, p. vi].

As one can see, these debates lay at the root of the later development of applied mathematics and numerical analysis.

**4.2. Practical Work and Collaborative Procedures.** At Gâvre, Haag’s work took place in a special unit devoted to anti-aircraft gunnery. As discussed above, anti-aircraft gunnery posed a difficult challenge to older ballistic methods.

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<sup>67</sup>This is probably an allusion to the probabilist, Paul Lévy, who was in the Mining Corps and an anti-aircraft officer during WWI. Although he served as an instructor at Arnouville-lès-Gonesses (figure 6) in 1916, Lévy was mobilized in a fighting unit for most of the war and did not mention his work at Gâvre in his autobiography [Lévy 1970, pp. 54–55]. He is, however, mentioned in [Charbonnier 1928b, p. 580].

<sup>68</sup>Later a Professor of Analysis at the Sorbonne, Valiron was then a mathematics teacher at the *lycée* of Lyons (in the *classes préparatoires*). On the French system of higher education, see the contribution by Jean-Luc Chabert and Christian Gilain to this volume.

<sup>69</sup>In the GH method, the final velocity of the arc was first computed by approximating the arc as a parabola. The variations of the elements of motion  $Ds$  and  $D\sigma$  were first computed by exact quadratures.  $Dx$  and  $Dy$  were approximately computed with  $Ds$  and  $Dt$  with  $D\sigma$ . In the GHM method, variations were computed directly using Taylor series and averages [Garnier 1918b].



FIGURE 8. From left to right, Maurice Garnier, Louis Fort, and Gustave Lyon with measuring instruments, undated. From [Patard 1930, p. 275].

It was the engineer, Gustave Lyon (figure 8, on the right), who pushed for its creation. A polytechnician (X 1877) working as an acoustical engineer, Lyon had volunteered in 1914 and was soon in charge of the protection of the port of Cherbourg against airborne assaults. The *Mission du tir aérien de Gâvre* (MTAG) was set up under Lyon and Garnier's authority in April 1916. Soon, this "scientifico-technical organization" [Charbonnier 1928b, p. 580] counted a dozen mathematicians and physicists working under military guidance (table 1). Charbonnier described the procedure followed by the MTAG in a memo written in December 1917. This led to its formal establishment by the Navy Ministry, on January 30, 1918, under the name of *Mission balistique du tir aérien* (MBTA), with a section based in Paris for

Name	Rank and title	Functions
Châtelet	2nd-class officer in health services; Assistant Professor at University of Lille; Doctor of Sciences	First assigned to the MTAG until Sept. 1917, then assistant to Naval Engineer Anne: helps with the preparation and execution of shootings; drafts reports and computations
Denjoy	Soldier in infantry; Doctor of Sciences; Professor at University of Montpellier	General service
Ferdinand Dreyfus	Soldier in infantry; Bachelor in Science actuary at Ministry of Work	Assistant to Naval Artillery Engineer Sugot: same functions as Châtelet
Fort	Warrant officer in the infantry; mathematics teacher at naval school and <i>lycée</i> of Neuilly	Preparation, execution, and interpretation of aerial shootings
Goullins	Lieutenant in reserve metropolitan artillery; Naval Artillery Engineer	Helps with, then directs, shots; main drafter of reports (flares and incendiary shells) after he becomes member of the Commission in Sept. 1917. Assist. to Sugot on gunpowders
Haag	Second lieutenant in artillery; Professor at University of Clermont-Ferrand	Improvement and application of new methods for computing trajectories
Kampé de Fériet	Auxiliary in infantry; Doctor of Sciences; Assistant Astronomer at Paris Observatory	Assistant to Sugot: helps with shooting; drafts reports and computations
Marcus	Ordnance soldier; mathematics teacher	Assistant to Garnier for experiments and computing
Pélicier	Auxiliary in infantry, then second lieutenant in artillery student at <i>École normale supérieure</i>	Assistant to Anne; same functions as Châtelet
Sauvigny	Temporary Second Lieutenant in artillery; mathematics teacher at <i>lycée</i> of Nancy	Assistant to Anne; same functions as Châtelet
Valiron	Soldier in the infantry; special mathematics teacher at <i>lycée</i> of Lyons	Assistant to Garnier for experiments and computing

TABLE 1. Mobilized Scientific Personal at the Gâvre Commission during WWI. From [Patard 1930, pp. 277–278]. In addition, Ernest Esclangon, from the Bordeaux Observatory, and Gabriel Foëx, from Zürich, were present as non-mobilized scientific personal.

theoretical investigations and another in Lorient in charge of experimental studies.<sup>70</sup> It is interesting to examine the procedure outlined by Charbonnier to get a precise understanding of the type of work mathematicians were doing at Gâvre.

First, for all types of guns and projectiles, the ballistic coefficient was evaluated with one or two shots. A network of 19 trajectories was completely computed

<sup>70</sup>Charbonnier, Rapport No. 7, Note adressée à l'Ingénieur général, directeur central de l'Artillerie navale, December 17, 1917 [SHD–Terre, 10W73].

using the labor-intensive step-by-step method, and computed twice to insure that no mistake was made. The second step of the procedure was new with respect to previous customs. Extensive series of experiments were performed to measure the trajectory and duration of flight using a simplified theodolite designed by Lyon and a chronophotographic instrument. This led to an immense amount of work. For 60 to 80 shots, 1,000 to 1,200 observations were taken that had to be analyzed. Atmospheric conditions were measured using weather balloons. Using all this material, the third step in the procedure consisted of preparing a corrected table using the computing method developed by Haag and Garnier. For each series of 9 shots, the piecewise integration had to be performed on about ten arcs. Finally, the MTAG produced networks of curves with shell trajectories and isochrone lines. “Refraining from imposing a method or an apparatus, the MTAG strictly limited itself to its ballistic role: to give combattants (Army and Navy) the networks they wanted.”<sup>71</sup> This led them however to produce extensive networks: for the 75-mm cannon, for example, it contained more than 40 sheets for each type of projectile.

Notes written for a series of experiments undertaken in the spring of 1916 can help to convey an even clearer sense of the mathematicians’ activities at Gâvre. In one set, Garnier wrote down very specific instructions: “In view of coordinating efforts in the best possible way and to achieve [our objectives] as fast as possible . . . I indicate in the following the detailed division of labor.”<sup>72</sup> The workload was divided into field and office work. In the field, Garnier, another officer, and a soldier operated the battery; mathematicians (Haag and Châtelet), officers, workers, and apprentices manned three observation stations, while others tended the registering instrument (figure 8). In order to communicate between observation stations, mathematicians were asked to study Morse code [SHD–Terre, 10W73; Comptes rendus de la Commission de Gâvre. Note no. 6, May 29, 1916 & note no. 9, June 2, 1916].

The office work was also strictly divided among participants. Haag, for example, assisted by an apprentice named Guillaouic, was supposed to compute the fundamental trajectories and the differential coefficients that allowed for correct trajectories for given experimental conditions and, on this basis, draw the networks. Together with a military officer, Louis Fort, a mathematics teacher at the *lycée* of Neuilly, was assigned the task of preparing the shots and analyzing shooting conditions. On the chronophotographic plates, Fort was in charge of measuring the Cartesian coordinates of every explosion of the fuses that were recorded. Assisted by an apprentice, Albert Châtelet, a *maître de conférences* at the University of Lille, was supposed to perform all the operations needed to draw isochrone lines on the networks.<sup>73</sup>

On June 12, 1916, experiments had been performed and computational assignments were ready to be carried out. In a very explicit report, Garnier listed all

<sup>71</sup>Charbonnier, Rapport No. 7, p. 6 [SHD–Terre, 10W73].

<sup>72</sup>“*En vue de coordonner le mieux possible les efforts, pour aboutir dans les délais les plus rapides, . . . j’indique ci-après la répartition détaillée du travail.*” Comptes rendus de la Commission de Gâvre. Note no. 6, May 29, 1916 [SHD–Terre, 10W73]. This series of 13 numbered notes from May and June 1916 follow from the establishment of the MTAG in April 1916. All are signed by Garnier and can be found in [SHD–Terre, 10W73].

<sup>73</sup>In fact, Châtelet had been called to Lille on August 5, 1914 and only took up his position there in 1919. See [Condette 2009] and Sébastien Gauthier’s contribution to [Goldstein & Aubin forthcoming].

the operations that everyone had to do in sequence [SHD–Terre, 10W73; Comptes rendus de la Commission de Gâvre, Note no. 12, June 12, 1916]. But two weeks later, orders were modified due to changes in personnel and in priorities. All personnel not otherwise busy were to contribute to the computation of the networks under Haag’s supervision. A 16-step procedure explained the work in an even more detailed manner. All apprentices received precise assignments; sample tables were drawn for computers to fill in; the number of copies to be made and the destination of each copy was specified; every computation and drawing to be done was described in detail [SHD–Terre, 10W73; Comptes rendus de la Commission de Gâvre, Note no. 16, June 26, 1916].

While military work at Gâvre may have seemed enviable compared to the lot of soldiers on the front, it was not without danger. In a talk delivered in Lille in 1924, Châtelet recalled an accident that occurred to him. In one of the shootings, observers behind the cannon was huge red flares and abundant black smoke coming out of the mouthpiece that was expelling shades of shell for about one minute. The shell had exploded in the barrel and the cannoneers had nowhere to hide: “I can insure you, even if this is not in the written report, that observers . . . felt that one minute can be very long.”<sup>74</sup>

From the minute description of the work done at Gâvre, one gets a rich impression of what it meant to use the mathematicians’ skills in the First World War. That impression is far from the Romantic vision of genius solving a problem that had frustrated ignorant militarymen for ages. On the contrary, ballisticians at Gâvre had enough mathematical sophistication to be able to see the added value mathematicians were susceptible of bringing to their trade. It also seems clear that mathematicians were not “well prepared for their new role” [Patard 1930, p. 279] and that, at first, their experience at Gâvre may have been rather humbling. But in time, all could see how tight collaboration and division of labor was necessary for producing important results such as firing tables. Only then, could collaborative procedures drafted by ballisticians make room for mathematicians’ special abilities and sometimes assign them to positions of leadership.

**4.3. Application to the Battlefield.** Firing tables were not the end of the story. Artillerymen needed to be trained in order to make good use of them. In this, mathematicians had, once again, a crucial part to play. Officers testified that a “*carnet de Haag*” [Boissonnet 1920, p. 39] circulated underground, one year before it was printed and distributed officially (see figure 9). In this course designed for trainee officers, Haag wrote that the exact solution of the ballistic problem was a “chimera.” But, he added, “one can, as in all experimental problems, look for an approximate solution. I will try to show you what this solution is and *what degree of confidence we may grant to it.*”<sup>75</sup>

In this course, Haag argued for the usefulness of the mathematical approach to firing, which was presented as a mathematical problem. “Given a target, a cannon,

<sup>74</sup>“*je puis vous assurer, quoique ce ne soit pas sans le procès verbal, que les observateurs . . . trouverent qu’une minute, ça peut être très long.*” The typed text of Châtelet’s speech with handwritten annotations can be found among his papers [Fonds Châtelet, 81 J 117]. I wish to thank Sébastien Gauthier for making this document available to me.

<sup>75</sup>“*Le problème est ardu. La solution exacte est une chimère. Mais on peut, comme pour tous les problèmes d’ordre expérimental, en chercher une solution approchée. Je vais essayer de vous montrer en quoi consiste cette solution et quel est le degré de confiance qu’on peut lui accorder*” [Haag 1917, p. 3].

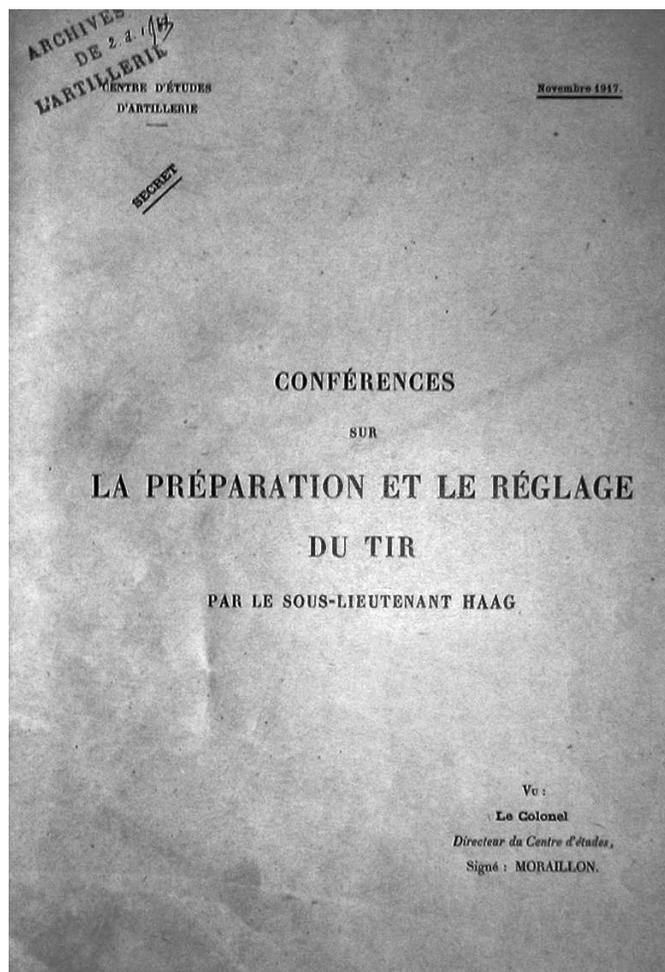


FIGURE 9. *Le carnet de Haag*: Haag's Course to Artillery Officers in Training [Haag 1917]. Coll. Ministère de la défense, service historique.

[and] ammunition, it is asked to send one or several shells to the target, or at least to its immediate neighborhood."<sup>76</sup> The problem had two solutions: the first was to fire several shots and observe the effect; the second was to prepare the shooting in such a way that the first shot fell, if not on the target, then at least in its vicinity. If the first method was simpler and applicable without special training, if it did the trick for the daily operations of 75-mm cannons, it was too expensive, too time-consuming as far as heavy artillery was concerned.

The various mathematical operations required in the artillery and the different procedures developed on the field were evaluated in terms of efficiency: computing

<sup>76</sup>“Étant donné un objectif, un canon, des munitions, il s'agit d'envoyer un ou plusieurs obus sur l'objectif, ou au moins dans un voisinage immédiat” [Haag 1917, p. 3].

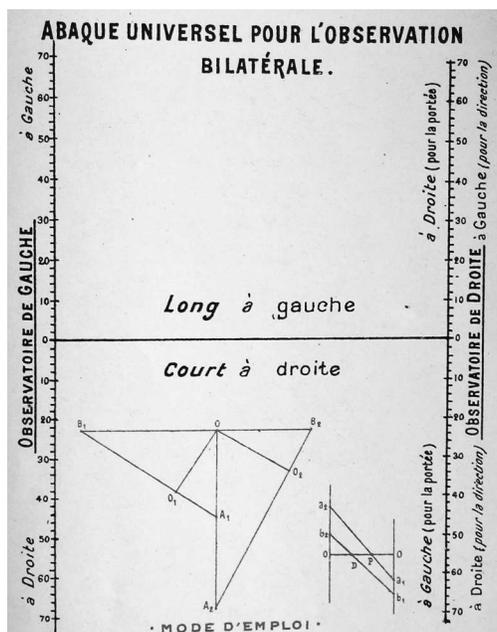


FIGURE 10. Nomogram used to adjust artillery fire developed by Haag during WWI. Repr. from [Haag 1917]. Service historique de la Défense.

in the command post, the use of double-entry tables for deviations, the manipulation of slide rulers, the considerations of graphs, and mechanical instruments. Figure 10 shows a nomogram prepared by the Army in order to adjust the fire given two observers at different spots. 750 copies of this nomogram were produced by November 1917. But were they used? Haag’s course clearly shows that the hierarchy seemed intent on increasing the mathematical level of artillerymen serving on the front.

Testimonies from men in the field show that this intention was not illusory. Take the case of the young Jean-Alexandre Cardot. He was merely 16 when war broke out and pursued his mathematical education in the troubled circumstances of war. In 1917, he may have been among Haag’s audience at the artillery school at Fontainebleau. He gave a vivid account of his first campaign in a battery of 75s in Lorraine in 1918. In Cardot’s description, firing had indeed become a scientific exercise. Every target was located on maps by their coordinates. Weather reports transmitted daily the force and direction of the wind. Communications between observers and cannoneers were insured via the telephone. One day, he went out with his Lieutenant to test new shells that could reach a target at 11 kilometers. Cardot described firing maneuvers in detail. He explained how he was asked to use simple mathematical instruments and computations. The lieutenant told him: “You will direct the fire. . . . Go. Here’s the firing table” [Cardot 1987, p. 65]. Although the lieutenant tried to trick him by handing him the wrong table, Cardot was wiser and the German train in the distance was finally shot down.

At the level of the General Staff, scientific firing was now taken for granted. At the end of 1917, according to General Herr, “the time ha[d] come when the

French artillery at long last found, if not a complete and definitive [answer], at least one that was precise enough to be applicable henceforth.” The solution to the problem of firing by surprise was “the scientific preparation of shooting [*la préparation scientifique du tir*]” [Herr 1923, p. 93]. In October 1917, the French artillery was able to fire at night or in the fog: “a fearful innovation” [Herr 1923, p. 94]. It now possessed:

a scientific shooting method [that allowed] for shooting under any weather condition, at any time, on every terrain, in all circumstances. . . . It [was] able to open fire almost instantaneously on any seen or unseen point merely identified by its coordinates on a map [Herr 1923, p. 95].

By the end of the war, the French artillery was finally using “scientific ballistics” [Challéat 1933–1935, vol. 2, p. 314]. Those were “the French methods of firing” that American artillerymen were taught in 1917 [Grotelueschen 2001, p. 20]. Although less praised than tanks and less bedeviled than poison gas, the new firing methods played no small part in the outcome of the war, and the cannon was called the “artisan of Victory” [Rouquerol 1920]. “It was the massive surprise action of our artillery which, from July 18, 1918 onwards, insured the success of our great offensives until Germany’s capitulation” [Campana 1923, p. 122]. Ballisticians, it would seem, had successfully fulfilled their mission. As we have argued, this success owed much to their ability to enroll the effective collaboration of some mathematicians.

### 5. Mathematicians’ Attitudes towards Ballistics

After the war, ballisticians wished to assert the new scientific status of their trade. Charbonnier praised the progress on ballistics achieved by the “alliance, made by the war, of ballisticians and savants” (Charbonnier’s preface in [Garnier 1918b, p. viii]). While it used to be the exclusive domain of engineers and technicians, ballistics had, he wanted to say, truly become a first-rank science. “Because of its intrinsic interest, as pure science as well as for national interest, ballistics deserves to become, as it once was, a topic of research for pure scientists.”<sup>77</sup> Mathematicians, however, appeared rather more circumspect about the mathematical value of wartime ballistic research. Asked by Jacques Hadamard to report on the ballistic computations in which he had taken part, Lebesgue wrote on October 23, 1919:

such a report would perhaps be more pertinent if it were addressed to a Committee awarding the *prix de vertu* [attributed at that time for the most courageous act on the part of a poor Frenchman], since none of those who worked on the construction of systems of ballistic trajectories claims to have done scientific work by performing numerical computations using well-known procedures; all merely tried to be useful.<sup>78</sup>

<sup>77</sup>See Charbonnier’s preface in [Garnier 1918b, p. viii]. Charbonnier reached out again to mathematicians at the International Congress of Mathematicians in Toronto in 1924 [Charbonnier 1928b].

<sup>78</sup>“*Un tel rapport serait peut-être plus légitime s’il était adressé à la Commission des prix de vertu, car aucun de ceux qui ont travaillé à la construction du réseau ne prétend avoir fait œuvre scientifique en effectuant des calculs numériques par des procédés bien connus ; tous se sont efforcés simplement d’être utiles*” [Academy of Sciences, Lebesgue to Hadamard, October 23, 1919].

Lebesgue went on to explain that the team he headed (together with Montel) computed more than a thousand trajectories, each of them independently computed by two persons. This work, Lebesgue concluded, was useful because it allowed the quick construction of range tables at a time when few shooting tests could be carried out due to the overload of work encountered by proving grounds and military research institutions. “But the extent of the effort should not lead one to think that the tool that was constructed is worth so much that it could be used for a long time to come.”<sup>79</sup> Recalling the two main uncertainties in ballistic theory (the air resistance law  $F(v)$  and the air density law  $\Delta(y)$ ), Lebesgue stated that no computation could compete with pure empiricism. Past experience during the war had shown that the latter method was simpler, cheaper, and more efficient from a military point of view.

Lebesgue’s poor opinion of the value of computational ballistics was formed early on. Asked by Borel to get involved in both ballistics and sound-ranging studies, Lebesgue reluctantly agreed. “If this is useful to you, I am willing to do the computations. But then you have to tell me explicitly and in detail the operations I must carry out. I am willing to be a computing machine, but nothing less.” He went on: “I will do the computations you ask in the manner of a stupid clerk; but nothing more.”<sup>80</sup> As a result of this episode, relations soured between Borel and Lebesgue whose *amour-propre* seemed to have been hurt by Borel’s managerial style. But I think that Lebesgue’s reluctance, which was due to many factors that were deeply personal to him, was also the result of his very high ethical ground which forbade him to take credit he did not believe his war work had earned him. Lebesgue insisted that one should not put too much importance on the war contribution of the “*Sorbonnoids*” at the *Bureau des calculs* of the Board of Invention.<sup>81</sup> His reticence toward computational ballistics was rooted in his lack of satisfaction with the experimental basis of theoretical ballistics. Distancing himself from many mathematicians who had taken part in the war effort, he underscored that “mathematics cannot create the world.” In the absence of a solid experimental basis, Lebesgue thought, the time was not ripe for mathematical ballistics.<sup>82</sup>

During the war and after, Lebesgue’s opinion about the value of the mathematical war effort varied little. He thought that in ballistics as well as in sound-ranging, the physical problems overshadowed the mathematical effort. The only contribution mathematicians could make—and effectively made, according to him—was to

<sup>79</sup>“*Mais il ne faudrait pas que la grandeur de l’effort accompli fasse croire que l’outil construit a une valeur telle qu’on pourra l’employer encore longtemps.*” [Academy of Sciences, Lebesgue to Hadamard, October 23, 1919].

<sup>80</sup>“*Si cela vous est utile, je veux bien faire des calculs. Mais alors dites-moi expressément, et dans le détail, les opérations que je dois faire. Je veux bien être une machine à calcul, mais rien de plus. . . . Je ferai donc les calculs que vous me demandez à la façon d’un bon employé idiot ; rien de plus*” [Lebesgue 1991, letter CCXIII, n.d., pp. 318–319]. In this correspondence with Borel, letters explicitly dealing war work are often undated; editors believe they can date them from early 1915.

<sup>81</sup>Lebesgue to Borel, letter n.d. [April 1917], in [Lebesgue 1991, p. 339]. On the fate of the friendship between Borel and Lebesgue during WWI, see Hélène Gispert’s contribution to [Goldstein & Aubin forthcoming].

<sup>82</sup>“*les mathématiques ne peuvent pas créer le monde ; qu’elles ne peuvent suppléer l’expérience et l’observation mais, tout au plus, les résumer ; que le moment n’est donc pas encore venu de faire de la balistique mathématique et que l’effort à faire actuellement est d’ordre expérimental*” [Academy of Sciences, Lebesgue to Hadamard, October 23, 1919].

organize computing methods and their execution by technical assistants. However ingenious the methods developed during the war (although Lebesgue hardly believed they were), this contribution would only last as long as deficient experimental bases would—not very long, Lebesgue thought.

Hadamard shared Lebesgue’s opinion and was not overly impressed by the mathematics and science coming out of war work. As most commentators, he believed that the great scientific war was mostly one of the application of known results rather than one of striking innovation. The ballistics papers he reviewed, he wrote, “for the most part bring, not scientific improvements concerning the principles, but rather modifications of a purely technical nature aimed at applying these principles more or less easily in specific practical consequences. These are topics with which the Academy wishes to remain involved, but that nonetheless are on the sidelines of its proper function” [Hadamard 1920, p. 437].

### Conclusion

Our study has shown that, although it was not always trivial, the mathematics of ballistics was, for the most part, tedious. Mathematicians at Gâvre did work on topics that had some wider implications, but, for the most part, they were involved in menial tasks of experimentation, computation, and education. Still, their contribution to the war effort was significant, useful, and perhaps crucial to the final victory—and it was recognized as such. Ballisticians could legitimately pride themselves on having been able to use mathematicians’ special abilities to their own ends.

Many prominent mathematicians were involved in ballistics during the war. To Lebesgue, Hadamard, Montel, and Drach already mentioned, we may add Arnaud Denjoy who worked on the solubility of the hodograph at Gâvre in July 1917, Ernest Vessiot, later to succeed Borel as Director of the *École normale supérieure*, and René Garnier who taught at the Sorbonne after the war. But the result was paradoxical. They were happy to close the parenthesis and leave behind the work that had seemed most useful from a ballistics standpoint, as it had seemed to them rather trivial from a mathematical point of view. But of Drach’s and Montel’s work, most admired by Hadamard and which led to further work in the abstract theory of differential equations after the war, Charbonnier bluntly wrote: “this conquest, which honors the mathematicians, does not seem susceptible of providing ballisticians with new resources in view of applications” [Charbonnier 1928b, p. 574].

Yet, one wonders whether the ballistics experience of some French mathematicians and physicists did not have a deeper influence on the work they later did. Most mathematicians who were active at Gâvre indeed kept their connection to the military research institution. In 1921, civilians joined the Commission for the first time since Hélie. Several mathematicians were nominated including Haag, Châtelet, Valiron, and Joseph Kampé de Fériet by then at the University of Lille.

Some pure mathematicians never returned to their earlier concerns. Haag later became the director of the chronometric school in Besançon and produced some of the most important work in France on the theory of dynamical systems. Joining the Lille faculty, Kampé de Fériet became a specialist in fluid mechanics and a world leader in turbulence studies after World War II. Also at Lille, Châtelet was so invested in the institutional rebuilding of his university that his mathematical

research in number theory and algebra begun before the war was relegated to a minor place [Goldstein 2009]. The style of mathematical research this generation of mathematicians perpetuated was characterized by very formal approaches to problems directly inspired by applications.<sup>83</sup> Although they were pushed aside by the turbulent Bourbaki generation, these mathematicians planted the seeds of applied mathematics research in France.

### Abbreviations

- ALVF: *Artillerie lourde sur voie ferrée* (Heavy Artillery on Rail).
- CRAS: *Comptes rendus hebdomadaires des séances de l'Académie des sciences*.
- GHM: Garnier–Haag–Marcus (ballistic computing method).
- MTAG: *Mission du tir aérien de Gâvre* (Gâvre's Mission for Air Firing).
- MBTA: *Mission balistique du tir aérien* (Air Firing Ballistic Mission).

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<sup>83</sup>The work of Henri Villat in fluid mechanics, which rose to high prominence in interwar France, fitted squarely in these approaches. On this, see [Aubin, forthcoming].

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