

Supplementary Material for “Excitation energies along a range-separated adiabatic connection”

Elisa Rebolini^{1,2,*}, Julien Toulouse^{1,2,†}, Andrew M. Teale^{3,4}, Trygve Helgaker⁴, and Andreas Savin^{1,2,‡}

¹*Sorbonne Universités, UPMC Univ Paris 06, UMR 7616, Laboratoire de Chimie Théorique, F-75005 Paris, France*

²*CNRS, UMR 7616, Laboratoire de Chimie Théorique, F-75005 Paris, France*

³*School of Chemistry, University of Nottingham, University Park, Nottingham NG7 2RD, United Kingdom*

⁴*Centre for Theoretical and Computational Chemistry, Department of Chemistry, University of Oslo, P.O. Box 1033 Blindern, N-0315 Oslo, Norway*

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The total energies \mathcal{E}_k^μ and excitation energies $\Delta\mathcal{E}_k^\mu = \mathcal{E}_k^\mu - \mathcal{E}_0^\mu$ of the partially interacting Hamiltonian given in Eq. (5) of the main article have been calculated with the DALTON program as a function of the range-separation parameter μ for the helium and beryllium atoms and for the dihydrogen molecule. The computational details can be found in Section IV. The total ground-state energies were then fitted to the following analytical expression which satisfies the form of the expansions at small μ and large μ given in Eqs. (27) and (39)

$$\mathcal{E}_0^\mu = E_0 + \frac{\mathcal{E}_0^{\text{KS}} - E_0 + c_1\mu + c_2\mu^2 + c_3\mu^3}{1 + d_1\mu + d_2\mu^2 + d_3\mu^3 + d_4\mu^4 + d_5\mu^5},$$

where $c_1 = -N(N-1)/\sqrt{\pi} + (\mathcal{E}_0^{\text{KS}} - E_0)d_1$ and $c_2 = -N(N-1)d_1/\sqrt{\pi} + (\mathcal{E}_0^{\text{KS}} - E_0)d_2$ are fixed by the small- μ expansion, E_0 and $\mathcal{E}_0^{\text{KS}}$ give the ground-state total energies of the physical system and of the Kohn-Sham (KS) system, and N is the number of electrons. The excitation energies were fitted to the expression

$$\Delta\mathcal{E}_k^\mu = \Delta E_k + \frac{\Delta\mathcal{E}_k^{\text{KS}} - \Delta E_k + c_1\mu + c_2\mu^2 + c_3\mu^3}{1 + d_1\mu + d_2\mu^2 + d_3\mu^3 + d_4\mu^4 + d_5\mu^5},$$

where $c_1 = d_1(\Delta\mathcal{E}_k^{\text{KS}} - \Delta E_k)$ and $c_2 = d_2(\Delta\mathcal{E}_k^{\text{KS}} - \Delta E_k)$ to ensure the correct behavior at small μ , and ΔE_k and $\Delta\mathcal{E}_k^{\text{KS}}$ give the excitation energies of the physical system and of the KS system.

The fits were performed on about 30 points for a range of μ going from 0 to 10 bohr⁻¹ (with about half the points between 0 and 1 where the energies vary the most). The parameters of the fit can be found in Tables I, II, III and IV, and reproduce the calculated curves shown in the article with a maximum error of about 0.1 mhartree. All the energies are in hartree and μ is in bohr⁻¹.

Table I: Fitted parameters of the ground-state and excitation energies along the range-separated adiabatic connection for the helium atom using an uncontracted triple-augmented quintuple zeta basis set and a truncated singular-value decomposition cutoff of 10⁻⁷.

Ground-state	$\mathcal{E}_0^{\text{KS}}$	E_0	c_3	d_1	d_2	d_3	d_4	d_5
1 ¹ S	-1.813977	-2.902589	0.2886122	-0.5256672	1.267965	0.7302989	1.729618	0.6215862
Transition	$\Delta\mathcal{E}_k^{\text{KS}}$	ΔE_k	c_3	d_1	d_2	d_3	d_4	d_5
1 ¹ S → 2 ³ S	0.7476677	0.7281453	0.06186663	-1.148460	0.7875350	3.601280	-0.8453350	3.279870
1 ¹ S → 2 ¹ S	0.7476670	0.7576321	-0.09598863	-1.799520	3.139774	9.153716	6.331953	8.164700
1 ¹ S → 1 ³ P	0.7787323	0.7701976	0.2572886	-4.517757	11.06152	37.53672	-27.73374	90.37671
1 ¹ S → 1 ¹ P	0.7787322	0.7795772	0.05426567	11.97447	-47.11893	114.6076	-82.48554	51.72106

*Electronic address: rebolini@lct.jussieu.fr

†Electronic address: julien.toulouse@upmc.fr

‡Electronic address: savin@lct.jussieu.fr

Table II: Fitted parameters of the ground-state and excitation energies along the range-separated adiabatic connection for the beryllium atom using an uncontracted double-augmented double zeta basis set and a truncated singular-value decomposition cutoff of 10^{-6} .

Ground-state	$\mathcal{E}_0^{\text{KS}}$	E_0	c_3	d_1	d_2	d_3	d_4	d_5
1^1S	-9.124165	-14.65438	46.83671	-0.2090221	-1.923411	3.658671	10.96260	5.215731
Transition	$\Delta\mathcal{E}_k^{\text{KS}}$	ΔE_k	c_3	d_1	d_2	d_3	d_4	d_5
$1^1S \rightarrow 1^3P$	0.1336714	0.1009080	-0.02498641	2.675899	-1.103249	66.59735	-39.94845	24.42414
$1^1S \rightarrow 1^1P$	0.1336461	0.1974410	-0.3142418	2.670149	-5.243878	40.77140	-44.04497	36.69480

Table III: Fitted parameters of the excitation energies along the range-separated adiabatic connection for the dihydrogen molecule at the equilibrium distance using an uncontracted double-augmented triple zeta basis set and a truncated singular-value decomposition cutoff of 10^{-6} .

Transition	$\Delta\mathcal{E}_k^{\text{KS}}$	ΔE_k	c_3	d_1	d_2	d_3	d_4	d_5
$1^1\Sigma_g^+ \rightarrow 1^3\Sigma_u^+$	0.4359619	0.3890173	0.2799389	1.767023	13.40149	19.23359	24.79910	19.29466
$1^1\Sigma_g^+ \rightarrow 1^1\Sigma_u^+$	0.4359571	0.4677408	-0.01241781	1.264479	-0.4431237	21.85013	-16.49858	12.33904
$1^1\Sigma_g^+ \rightarrow 2^3\Sigma_g^+$	0.4740336	0.4598110	0.2481387	0.9229492	-10.10530	21.52073	-16.87971	25.28795
$1^1\Sigma_g^+ \rightarrow 2^1\Sigma_g^+$	0.4740150	0.4814739	0.04156341	-5.018161	10.11410	-3.755105	-2.033443	8.145262
$1^1\Sigma_g^+ \rightarrow 1^3\Pi_u$	0.480003	0.4670848	0.1376852	30.80894	-13.52176	121.4909	-67.14926	32.50543
$1^1\Sigma_g^+ \rightarrow 1^1\Pi_u$	0.4799835	0.4852236	0.01995048	0.5766261	-5.036269	37.87564	-20.46073	10.75388

Table IV: Fitted parameters of the excitation energies along the range-separated adiabatic connection for the dihydrogen molecule at three times the equilibrium distance using an uncontracted double-augmented triple zeta basis set and a truncated singular-value decomposition cutoff of 10^{-6} .

Transition	$\Delta\mathcal{E}_k^{\text{KS}}$	ΔE_k	c_3	d_1	d_2	d_3	d_4	d_5
$1^1\Sigma_g^+ \rightarrow 1^3\Sigma_u^+$	0.05176212	0.01700837	0.6515038	-1.415220	4.923966	118.7312	-176.1438	667.7109
$1^1\Sigma_g^+ \rightarrow 1^1\Sigma_u^+$	0.05174852	0.2813186	-9.042050	-9.080417	27.82670	57.35565	-188.3668	718.6815
$1^1\Sigma_g^+ \rightarrow 2^3\Sigma_g^+(\sigma_u^+)^2$	0.1034820	0.2988327	-8.364428	-6.876502	37.68192	51.86662	-151.0807	783.8883