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Characterization of Zeolitic Intraframework Molybdenum Sites

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ABSTRACT

An integrated experimental and computational study was carried out on molybdenum loaded BEA zeolite in order to scrutinize the most stable state of the molybdenum site at various oxidation and hydration states. After a two-step post-synthetic process, the incorporation of Mo ions into the vacant T-atom sites of the SiBEA framework zeolite as mononuclear Mo^{VI} centers has been evidenced by combined use of XRD, FTIR and diffuse reflectance UV-vis spectroscopy. The consumption of OH groups upon Mo loading has been monitored by FTIR and adsorbed pyridine is used as probe molecules for characterization of Brønsted and Lewis acidity in SiBEA and $\text{Mo}_{3.0}\text{SiBEA}$. Periodic DFT calculations in sodalite (SOD) framework indicate a trigonal-bipyramidal conformer at the Mo^{VI} site with molybdenum being incorporated into the zeolite framework by four $\text{SiO}-$ bonds and a $\text{Mo}=\text{O}$ functionality under anhydrous conditions. Water splitting formally to O^{2-} and 2H^+ is computed to be feasible in SOD cage, whereas it is strongly favored in MoBEA framework at the T1 position. Depending on the hydration state, it is shown that the Mo sites formed can exhibit two $\text{Mo}=\text{O}$ functionalities in a trigonal-bipyramidal and a pseudo-octahedral arrangement.

Introduction

Transition metal modified or substituted oxide materials have found many applications in catalysis. Zeolites, a typical group of materials used as support for heterogeneous catalysts are used for decades in industrial applications. The continuous search to improve or discover new catalyst has led to the chemical modification of the oxide support or zeolite in particular at atomic level^{1,2}

In earlier work Dzwigaj et al.³⁻⁵ have applied a two-step post-synthesis method to favor the incorporation of group VI metal, chromium, into the framework of the BEA zeolite and to obtain mononuclear chromium species. The transition metal intra framework site was characterized using a series of experimental techniques, followed by quantum chemical calculations by the Tielens group⁶. A logic continuation of this study is the introduction of the other group VI elements, Mo, and W into the zeolite structure, in the same spirit as for the group V transition metals performed earlier: V⁷⁻¹¹, Nb¹², Ta¹³, and Cr¹⁴.

Molybdenum species grafted on silica have attracted considerable attention because of their relevance to a variety of catalytic reactions, including the selective oxidations of alkanes^{15, 16}, alkenes¹⁷, and alcohols^{18, 19}. Many research groups have reported methods of characterization and synthesis, which is supposed to generate specific surface molybdenum oxide species. It is well known that framework transition metal ions are considered to be active in selective oxidation reactions²⁰⁻²³. Nevertheless, the structure, stability and reactivity of Mo oxide functionalities encapsulated in zeolites are much less studied, especially as isolated mononuclear species.

To our knowledge no combined theoretical/experimental characterization studies are available on molybdenum oxide species inserted into zeolite frameworks. The most related material known to pure silica molybdenum zeolites is molybdenum oxide supported on silica surface. This material

characterized by SiO–Mo linkages and has been thoroughly investigated, and molecular models have been studied theoretically²⁴.

The still growing computational power enables us to study models with increasing complexity and reliability. Until now, *ab initio* quantum chemical calculations have been performed on cluster models involving only dozen of atoms²⁵⁻²⁷. The present work follows the same spirit as those performed on the group V elements²⁸⁻³⁰, and in particular Si substituted by Cr, characterized experimentally on BEA zeolite and theoretically using periodic DFT⁶.

Different framework site models are proposed after a systematic theoretical study. The sites are characterized by structural parameters, vibrational frequencies, and (de)protonation energies. The results are in good agreement with the experimental findings.

Experimental Details

Material preparation

A tetraethylammonium BEA (TEABEA) zeolite with a Si/Al atomic ratio of 17 provided by RIPP (China) was dealuminated by a treatment with nitric acid solution ($c = 13 \text{ mol L}^{-1}$) at 353 K for 4h, to obtain SiBEA with atomic Si/Al ratio > 1300 and then washed several times with distilled water and dried at 368 K overnight.

SiBEA zeolite and molybdenum(II) acetate with a desired amount of Mo (3 Mo wt. % in Mo-containing SiBEA sample) were ground and mixed in agate mortar for 15 minutes. The obtained mixture was transferred to glass reactor and heated in flowing argon of 150 mL min^{-1} up to 773 K with heating rate of 2 K min^{-1} and left in this temperature for 12 h. After that, the gas flow was changed from argon to oxygen and the solid was calcined at 773 K for 3 h. As obtained, Mo-containing SiBEA was labeled $\text{Mo}_{3.0}\text{SiBEA}$.

Material characterization

Power X-ray diffractograms (XRD) of the prepared samples were recorded at room temperature on a Bruker D8 Advance diffractometer using the CuK_α radiation ($\lambda = 154.05$ pm).

Analysis of the acidic properties of samples was performed by adsorption of pyridine (Py) followed by transmission FT infrared spectroscopy. Before analysis, the samples were pressed at ~ 1 ton cm⁻² into thin wafers of ca. 10 mg cm⁻² and placed inside the IR cell.

Before Py adsorption/desorption experiments, the wafers were activated by calcination in static conditions at 723 K for 3 h in O₂ ($1.6 \cdot 10^4$ Pa) and then outgassed under secondary vacuum at 573 K (10^{-3} Pa) for 1 h. These wafers were contacted at room temperature with gaseous Py (133 Pa) via a separate cell containing liquid Py. The spectra were then recorded following desorption from 423 and 573 K with a Bruker Vector 22 spectrometer (resolution 2 cm⁻¹, 128 scans). The reported difference spectra were obtained after subtraction of the spectrum recorded before Py adsorption.

Diffuse reflectance (DR) UV-vis spectra of Mo_{3.0}SiBEA were recorded at ambient atmosphere on a Cary 5000 Varian spectrometer equipped with a double integrator with polytetrafluoroethylene.

Computational Details

Periodic density functional theory (DFT) calculations were performed using *ab initio* plane-wave pseudopotentials implemented in the Vienna Ab Initio Simulation Package^{31, 32}. The gradient-corrected revised Perdew-Burke-Ernzerhof (PBE) exchange-correlation functional^{33, 34} was chosen to carry out all calculations. The valence electrons and their interactions with the ionic cores were described with the projector augmented-wave (PAW) method^{35, 36} and for valence electrons a plane wave basis set was applied.

A $(3 \times 3 \times 3)$ k-point grid is used in the Brillouin-zone sums, and the partial occupancies are set for each wave function using the tetrahedron method with Blöchl corrections³⁷. The convergence was reached when the total energy difference between the self-consistent field loops was less than 10^{-4} eV. To calculate the Hessian matrix each ion was displaced in all three Cartesian directions.

Figure 1. Structure of model sodalite (SOD) cage in a supercell. (Mo substituted position is in purple)

The sodalite structure (SOD, Figure 1), commonly referred as the β -cage was used to perform a systematic study using periodic calculations. The use of the SOD cage as a model for a zeolite and in particular for BEA zeolite has been compared and justified in our previous study¹¹. The unit cell has a regular network of tetrahedral sites (equal T-sites) and contains 36 atoms ($\text{Si}_{12}\text{O}_{24}$). The use of such a small periodically repeated model makes the computationally very demanding calculations attainable. We also calculated, however, the most stable structures in BEA zeolite, to investigate the effect of the unit cell flexibility on the Mo insertion. The BEA unit cell contains 192 atoms ($\text{Si}_{64}\text{O}_{128}$), and has 9 different T-sites. We verified our calculations in the β -cage in

BEA zeolites to exhibit very different affinity to host metal ions¹¹.

Figure 2. Investigated Mo model sites in sodalite framework as the function of the Mo oxidation state and degree of hydration. Relative energies are given in eV for each corresponding series, and reaction energies (ΔE_r) in eV on the arrows.

Several configurations were systematically investigated to study the environment of the Mo site as the function of its oxidation state and its degree of hydration (Figure 2). This study is a complementary work to our previous work on chromium-substituted zeolite⁶. We started from a hypothetical structure in which one silicon atom of the pure SiO₂ framework is isomorphously substituted by one molybdenum atom, where the oxidation state of the transition metal is +4 (MoSOD). As a next step the metal center was reduced and oxidized by molecular hydrogen (H₂, right in Figure 2) and oxygen (O₂, left in Figure 2), respectively to form the parent Mo^{III} (**B3**) and Mo^{VI} (**Mo6**) sites. For both species, we added up to two water molecules (dissociated or not) and considered Mo=O and Mo–OH groups in the structures as summarized in Figure 2. In order to distinguish the different functional groups formed in the site and to be consistent with earlier studies, we use our previously introduced nomenclature¹⁰⁻¹² system being the following: B (Bridging hydroxyl), T (Terminal OH group), Mo (Mo=O, molybdenyl group), and nW (n physisorbed or chemisorbed water molecules). The Arabic number next to letter code indicates the oxidation state of the metal. The schematic representations of the different models and their relationship with each other are shown in Figure 2.

Results and discussion

Experimental investigation

Incorporation of molybdenum into the framework of SiBEA evidenced by XRD and FTIR

As Figure 3 indicates, the X-ray diffractograms of SiBEA and Mo_{3.0}SiBEA are similar, suggesting that the incorporation of molybdenum into framework of SiBEA zeolite does not significantly affect the structure of the zeolite. While the determination of the unit cell parameters in BEA zeolite is made difficult because of the coexistence of several polytypes, it is, however,

possible to obtain information on the contraction/expansion of the framework from the position of the diffraction peak (302) at $2\theta = 22.5\text{-}22.7^\circ$.

Figure 3. X-ray diffractograms of SiBEA and $\text{Mo}_{3.0}\text{SiBEA}$ recorded at room temperature and ambient atmosphere.

Upon introduction of Mo into SiBEA the d_{302} spacing, related to the narrow main diffraction peak near 22.7° , increases from $3.920 \text{ \AA}$ (SiBEA) (with 2θ of 22.69°) to $3.950 \text{ \AA}$ ($\text{Mo}_{3.0}\text{SiBEA}$) (with 2θ of 22.48°) (Figure 3). This increase can be taken as an evidence of framework expansion of the BEA structure and suggests incorporation of molybdenum atoms into the vacant-T-atom sites of the framework of SiBEA zeolite, in line with earlier reports for Cr_xSiBEA ⁶, VSiBEA zeolites³⁸.

Formation of Isolated Mo^{VI} Species in SiBEA evidenced by DR UV-vis

Figure 4. DR UV-vis spectra of SiBEA and Mo_{3.0}SiBEA recorded at ambient atmosphere.

Figure 4 shows the diffuse reflectance UV-vis spectra of SiBEA and Mo_{3.0}SiBEA. For Mo_{3.0}SiBEA only two absorption bands at 265 and 310 nm appear. These new absorption bands observed can be assigned to ligand to metal low-energy charge transfer (LMCT) transitions^{39, 40} involving oxygens in bridging (Mo–O–Si) and terminal (Mo=O) positions, which is in line with Mo-containing materials and earlier works on V^V- and Cr^{VI}-containing zeolites^{3, 41-44}. Conventionally, absorption bands between 250 and 280 nm are assigned to a tetrahedral, whereas bands from 300 to 330 nm to an octahedral geometry of isolated molybdenum oxide centers^{45, 46}. The absence of d-d transition within the range of 600-800 nm indicates that practically all molybdenum centers are oxidized to Mo^{VI} and no reduced Mo^{III} or Mo^{IV} forms are present.

Figure 5. FTIR spectra recorded at room temperature of SiBEA and Mo_{3.0}SiBEA calcined at 773 K for 2 h in flowing 2.5 % O₂/Ar (50 mL min⁻¹) and then outgassed at 573 K (10⁻³ Pa) for 1 h.

FTIR spectroscopy.

The IR bands at 3735 and 3705 (Figure 5) are attributed to isolated internal SiO–H groups of SiBEA and the broad band of 3520 cm⁻¹ shows the presence of vacant T-atom sites associated with SiO–H groups, as previously shown^{4, 41, 47}. The incorporation of molybdenum into SiBEA leads to the decreasing of the intensity of the IR bands at 3735, 3705 and 3520 cm⁻¹ of terminal internal

and hydrogen bonded SiO-H groups (Figure 5), respectively, and suggest that those silanol groups react with the Mo precursor.

Figure 6. FTIR difference spectra recorded at room temperature of SiBEA and Mo_{3.0}SiBEA (calcined at 673 K for 1 h in O₂ ($2 \cdot 10^4$ Pa) and then outgassed at 673 K (10^{-3} Pa) for 1 h) after adsorption of pyridine for 1 h at 423 K and then desorption at 423 K for 1 h.

Figure 6 shows the FTIR difference spectra recorded at ambient temperature of SiBEA and Mo_{3.0}SiBEA, after calcination at 673 K for 1 h under O₂ and then outgassed at 673K (10^{-3} Pa) for

1 h after adsorption of pyridine recorded at 423 K temperature and followed desorption at 423 K.

For SiBEA very small bands at 1638, 1546 and 1491 cm^{-1} are observed indicating the presence of only very low amounts of Brønsted and Lewis acidic sites (Figure 6, Table 1 in line with earlier reports on SiBEA and VSiBEA^{42, 48}. The bands typical of pyridinium cations^{3, 49-51} are observed at 1638 and 1546 cm^{-1} indicating the presence of Brønsted acidic sites and suggesting that $=\text{Mo}-\text{O}(\text{H})-\text{Si}=$ acidic sites (see also section acid base properties) are formed upon outgassing of $\text{Mo}_{3.0}\text{SiBEA}$, as were suggested earlier also for Cr_xSiBEA ⁶ and VSiBEA^{8, 10}. The other bands observed at 1611 and 1451 cm^{-1} correspond to pyridine interacting with strong Lewis acidic sites related to Mo^{VI} species (See Table 1), confirming the formation of bridging $\text{Mo}^{\text{VI}}-\text{O}(\text{H})-\text{Si}$ groups in $\text{Mo}_{3.0}\text{SiBEA}$, which is in line with earlier data for CrSiBEA ³ and VSiBEA^{42, 48}.

Table 1. Evolution of Brønsted and Lewis acidic centers concentration in SiBEA and $\text{Mo}_{3.0}\text{SiBEA}$ samples. (Values in $\mu\text{mol g}^{-1}$)

Samples	Brønsted acidic centers	Lewis acidic centers
SiBEA	8	3
$\text{Mo}_{3.0}\text{SiBEA}$	13	53

4.2. Theoretical investigation

Geometry and energetics of the Mo-zeolite framework sites

The geometrical parameters of the substituted framework sites are obtained after full optimization; ion positions, cell volume and cell shape were allowed to relax. The spin state of the different Mo^{III} , Mo^{IV} , Mo^{VI} models has been investigated and respected. For Mo^{III} structures,

quartet state was always found to be lower in energy, than the doublet state, whereas for Mo^{VI}, being d⁰, only the singlet state was considered. The Mo^{IV} state, d², was calculated as triplet. The bond distances and angles of the most stable optimized structures are tabulated in Table 2 and are used to determine the type of the Mo–O bonds in the zeolites.

Table 2. Unit cell volume (Å³), reaction energies (eV), coordination number and bond distances D (Å) of the different reactive sites.

	MoSOD	Mo6	Mo6W	TT6	MoTB6	MoMo6	Mo6-2W ^{1p,1c}	Mo6-2W ^{2p}	MoTT6	MoMo6W	MoTTB6
Cell volume of Mo	720.2	722.0	731.9	731.8	733.7	728.5	732.1	747.5	730.4	727.2	695.1
Cell volume of Cr	709.7	716.9	716.9	716.9	716.9	716.9	714.5	714.5	709.7	707.3	697.9
ΔE _r	-	-2.68	-4.08	-3.36	-3.51	-3.69	-5.34	-5.13	-3.66	-5.37	-2.64
Coordination#	4	5	5	6	6	5	5(6)	5	6	5	6
Distance	1.912 ^a	2.022 ^a	1.988 ^a	1.963 ^c	2.023 ^a	1.874 ^a	1.859 ^a	2.003 ^a	1.728 ^b	1.999 ^a	1.967 ^a
	1.912 ^a	1.881 ^a	1.883 ^a	1.969 ^c	1.922 ^a	1.965 ^a	2.007 ^a	1.858 ^a	1.956 ^a	1.861 ^a	1.970 ^a
	1.912 ^a	1.882 ^a	1.868 ^a	1.877 ^a	1.849 ^a	2.252 ^f	1.922 ^a	1.894 ^a	1.879 ^a	2.215 ^c	2.240 ^d
	1.912 ^a	1.879 ^a	1.882 ^a	1.863 ^a	2.247 ^d	2.762 ^f	1.880 ^a	1.843 ^a	1.977 ^c	1.728 ^b	1.956 ^c
		1.730 ^b	1.738 ^b	1.942 ^a	1.966 ^c	1.719 ^b	1.734 ^b	1.739 ^b	2.028 ^c	2.312 ^c	1.879 ^c
			2.011 ^e	1.923 ^a	1.725 ^b	1.738 ^b	1.970 ^c	2.048 ^c	2.180 ^d	1.735 ^b	1.720 ^b
2.421 ^g											
a. Mo–O–Si b. Mo=O; c. Mo–OH; d. Mo–OH–Si; e. Mo=O···HOH; f. Mo···OHSi; g. Mo···OH ₂											
	B3	B3W	TB3	TBB3	MoBB3	B3-2W	TTB3				
Cell volume of Mo		723.2	701.0	698.7	708.8	689.7	722.3	740.5			
Cell volume of Cr		663.1	693.2	683.8	709.7	690.8	714.5	726.6			
ΔE _r		0.77	-0.58	-0.37	-0.06	0.04	-2.11	-1.28			
Coordination#		4	5	3(4)	5	4	6	4(6)			
Distance		1.924 ^a	1.955 ^a	1.967 ^a	2.177 ^a	2.089 ^a	2.042 ^a	2.033 ^a			
		1.918 ^a	1.981 ^a	1.913 ^a	1.979 ^a	2.525 ^d	2.075 ^a	2.011 ^c			

1.926 ^a	2.011 ^a	1.920 ^c	2.147 ^d	2.363 ^d	2.051 ^a	2.083 ^c
2.627 ^f	2.341 ^g	2.649 ^f	2.277 ^d	1.723 ^b	2.189 ^d	2.185 ^d
	2.233 ^d		1.987 ^c		2.309 ^g	2.303 ^f
					2.236 ^g	2.144 ^f

a. Mo–O–Si b. Mo=O; c. Mo–OH; d. Mo–OH–Si; e. Mo=O···HOH; f. Mo···OHSi; g. Mo···OH₂

The Mo=O double bonds adopt interatomic distances from 1.72 to 1.74 Å, which agrees well with bond lengths observed in tetrahedral MoO₄²⁻, pentacoordinated Mo₃O₁₂⁶⁻ and octahedral MoO₆⁶⁻ type molybdenum oxides^{24, 52}. The Mo–OSi bonds are characterized by typical lengths of 1.85 – 2.09 Å, while terminal Mo–OH bonds are slightly longer in general varying between 1.86 and 2.08 Å. Significantly weaker Mo···O attractions are predicted for the interaction of the molybdenum center with neutral ligands, such as O(H)Si– and H₂O. It is in line with the decreasing electron donating ability and decreasing electrostatic attraction of oxygen when going from the formal -2 charge to neutral form. Interactions characterized by distances between 2.0 and 2.2 Å can be viewed as unconstrained dative bonds in the coordination sphere.

Compared to the Cr–O bond lengths, the Mo–O bonds further elongate by about 0.10 Å in general in the sodalite cage, which is in line with the increased ion size as going down in the periodic table. The expansion of the coordination sphere results in the increase of the unit cell volume by about +2.5% on average compared to the chromium-substituted models. This finding is again in full agreement with the experimentally determined structure expansions, which is indeed slightly more characteristic for Mo incorporation than for Cr incorporation⁶. Note that there are also systems, for example **TB3** (698.7 Å³), with smaller unit cell than the parent MoSOD structure. As discussed for the CrSOD to B3(Cr) case⁶, this behavior can be linked to the shrinkage caused by the evolution of plausible hydrogen networks between well oriented OH donor and O acceptor functionalities.

Concerning the relative energy of the various states, the MoSOD with Mo^{IV} oxidation states has been taken as the reference configuration and the relative energies were defined as the reaction energy (ΔE_r) of the following reaction:

, where $n=0$, or $\frac{1}{2}$, $m=0$, or $\frac{1}{2}$, and $k=0$, 1, or 2, X (oxidation state)= +3 or +6

For products **Mo6** ($n=\frac{1}{2}$, $m,k=0$) and **B3** ($m=\frac{1}{2}$, $n,k=0$), the reaction energy can give, as first approximation, an idea about the feasibility of oxidation and reduction processes, respectively, starting from Mo^{IV} loaded zeolites. The oxidation (-2.68 eV) is highly exothermic revealing a spontaneous process, whereas the reduction is endothermic and needs 0.81 eV to take place. These results might be linked to the exclusively observed Mo^{VI} state, unlike Mo^{III}, in the various experiments. Also, for example, going from **Mo6** to **Mo6W** and **Mo6-2W**, the relative ΔE_r values indicate the energy associated with water adsorption in Mo^{VI} containing SOD cage. These values are extracted from the ΔE_r values and given in Figure 2 (vertical). The computed values of -1.39 and -1.05 eV for water adsorption are consistent with previously reported values of 1.66 – 1.13 eV in high-silica zeolites⁵³, indicating energetically favored adsorption processes.

Most importantly, the relative stabilities of isomeric sites, i.e. structures with the same oxidation state and hydration, can be determined by comparing their ΔE_r values. Accordingly, four groups of species can be distinguished (Group 1-4). Group 1 with Mo^{VI} center and with one equivalent of water contains **Mo6W**, **TT6**, **MoTB6** and **MoMo6**, whereas formal addition of a water molecule to the systems (Group 2) results in structures **Mo6-2W^{1p,1c}**, **Mo6-2W^{2p}**, **MoTT6**, **MoTTB6** and **MoMo6W**, all depicted schematically in Figure 2. Similarly, two sets of Mo^{III} systems can be identified: Group 3 (**B3W**, **TB3**, **TBB3** and **MoBB3**) and Group 4 (**B3-2W** and **TTB3**) contains one and two added water molecules in the system, respectively.

The most stable Mo^{VI} state after hydration (Group 1) is the simple physisorbed structure, **Mo6W**, in which the adsorbed water molecule forms a strong hydrogen bond ($d = 2.01 \text{ \AA}$) with the molybdenyl ($\text{Mo}=\text{O}$) group (Figure 2). **MoMo6** represents the second most stable species lying 0.39 eV higher in energy than **Mo6W**. In the latter structure the water molecule is formally split into O^{2-} and 2H^+ to form the second $\text{Mo}=\text{O}$ functionality and two Si-OH termini (Figure 2 and Figure 7). The two other Mo^{VI} structures (**TT6** and **MoTB6**) having only one molybdenyl ($\text{Mo}=\text{O}$) group and adopting hexacoordinated octahedral geometry lie significantly higher in energy than the former two structures. Further hydration causes notable change in the relative energies: **Mo6-2W^{1p,1c}** with one metal coordinated water and one physisorbed water molecules and **MoMo6W** (Figure 7), which represents the above described $[(\text{SiO})_2\text{MoO}_2]$ core with one physisorbed water, become the two most stable, practically isoenergetic (within 0.05 eV) structures. **Mo6-2W^{2p}** with two physisorbed water molecules has a relative energy of 0.141 eV respect to **Mo6-2W^{1p,1c}**.

Figure 7. Adopted geometries and relevant structural metrics for the most important Mo^{VI} and Mo^{III} sites.

Compared to Mo^{VI} systems, water molecules entering the zeolite cage behave differently when approaching a Mo^{III} substituted site. Due to the ease with which the zeolite framework distorts around the metal, the excess water coordinates to the Mo^{III} center with one of its lone pairs to adopt a pentacoordinated, trigonal bipyramidal structure, **B3W** (Figure 2 and 7). The latter structure is the most stable one at this hydration state, however it is worth noting that splitting of water to OH⁻ and H⁺ (**TB3**) is again a feasible process (0.21 eV). Similarly to the first step, in the next hydration the water molecule prefers to build in into the coordination sphere of the metal as a ligand (**B3-2W**) to form an octahedral arrangement with two H₂O ligands *cis* to each other. Mo–O distances of 2.05 Å indicate a typical dative bond and relatively strong interaction between the metal and the chemisorbed water molecules.

Until the latter behavior of Mo^{III} with water is very similar to that of Cr^{III} substituted zeolite sites⁶, the reactivity difference between Cr^{VI} and Mo^{VI} is remarkable. In contrast to the physisorbed most stable state for **Mo6W**, chromium(VI) tends to prefer hard Cr···O interactions and, thus, it splits water to develop two Cr=O interactions. Accordingly, the [(SiO)₂CrO₂] chromyl functionality is about 0.9 eV more stable than the physisorbed state.

It is also worth discussing the overall geometries around the metal centers in the most stable structures (Figure 7), because the zeolite frame causes some deviations from the ideal structures in spite of its flexibility. Until the coordination sphere can adopt an almost perfect trigonal bipyramidal structure in **Mo6W** with very short Mo=O bond in axial position (*d* = 1.738 Å), the structure of **Mo6-2W** deviates slightly from the ideal octahedral structure mostly due to the weak donor ability of the coordinated water molecule (*d*(Mo–O7) = 2.421 Å), which allows the shift of the “ligands” towards this position. Similar distortions occur in **MoMo6** and **MoMo6W**, in which the Si–OH group *trans* to the very strong oxo group elongates to 2.76 Å and 2.60 Å, respectively,

resulting in the bending of the equatorial plane. As mentioned above, with the entering of the water molecules to the coordination sphere of Mo^{III}, the structure is changing from tetrahedral to trigonal-bipyramidal (tbp) and to octahedral as going from **B3** to **B3W** and to **B3-2W** (Figure 7), respectively. The structure of **B3W**, however, is not a perfect tbp, one of the angles between Si–OH and Si–O– ligands in the equatorial plane distorts to 160°, from the ideal 120°. This metrical change actually opens a ‘position’ at the metal exactly in the direction of the sodalite cage, and this is where the next water molecule coordinates to form a slightly distorted octahedral structure (Figure 7).

Table 3. OH and Mo=O vibrational frequencies in cm⁻¹, calculated for different Mo model sites.

Vibration	Frequency	Vibration	Frequency
SiO–H		MoO–H	
B3 (SiO-H)	3811	MoTT6	3773
TB3(SiO-H)	3814	MoTT6	3787
		TT6	3772
SiO(H)Mo		TT6	3816
MoMo6	3754	MoTB6	3742
MoMo6	3808	TBB3	3740
MoTT6	3761	TTB3	3752
MoTB6	3770	TTB3	3793
B3	3811	TB3	3700
TBB3	3678		
TTB3	3765	Mo=O	
TTB3	3777	Mo6	1032
TB3	3769	MoMo6	1070
B32W	3540	MoMo6	1036
		MoTT6	1032

MoTB6	1038
Mo6W	1033
MoMo6W	1033

Vibrational frequency calculations were carried out to verify that the structures reached a real minimum with only real frequencies and also to obtain spectroscopic properties. The computed frequencies (Table 3) are compared with experimental data for Mo loaded BEA using FTIR *in situ* measurement.

The calculations predict that the bridging Mo–O(H)–Si groups vibrate between (3540 – 3777 cm⁻¹), terminal molybdenum-hydroxyl between 3700 – 3816 cm⁻¹, while molybdenyl groups around 1030 cm⁻¹ (probably visible with RAMAN) and silanol groups up to 3814 cm⁻¹. From the experimental spectra showing a band around 3605 cm⁻¹ a bridging hydroxyl Si–O(H)–Mo is expected.

Acid-base properties

To characterize the Brønsted acidity of the investigated structures, the protonation and deprotonation energy were calculated for the different energetically plausible sites^{54, 55}. The deprotonation energy is evaluated to be a positive value as the energy of the conjugate base, E(SOD⁻) minus the energy of the acid (eq. 2). ΔE_{deprot} indicates how acidic the proton is at a given site of the zeolite; the larger the ΔE_{deprot} value the less acidic the proton is.

$$\Delta E_{\text{deprot}} = E(\text{SOD}^-) - E(\text{SOD-H}) \quad (2)$$

The protonation energy is defined analogously in eq. 3 to measure the basicity of sites; however note that in this case a higher value of ΔE_{prot} defines a more basic zeolite site.

$$\Delta E_{\text{prot}} = E(\text{SOD}) - E(\text{SOD-H}^+) \quad (3)$$

One has to realize that a periodically repeated charged unit cell is modeled when computing energies $E(\text{SOD}^-)$ and $E(\text{SOD-H}^+)$ resulting in an unphysical state of infinite overall charge for the macroscopic systems. The deprotonation and protonation energies should, thus, be corrected accordingly in order to obtain realistic absolute values. For example, the divergence of the Coulomb energy in the charged system is eliminated by adding a uniform positive/negative background charge to the deprotonated/protonated unit cell. Nevertheless, our experience is that the values computed via eq. 2 and 3 using this method reveal the correct acidity and basicity trends for the various sites, which is the primary aim of these simulations.

In practice, one can determine the acidity of the distinct silanol (SiO-H) groups, bridging hydroxyl (SiO(H)-Mo) groups and metal coordinated hydroxide (MoO-H) groups in the various oxidation and hydration states. Similarly, one can add a proton (H^+) to the terminal molybdenum-oxo group (Mo=O) or protonate the bridging oxygen (Mo-O-Si) forming Mo=OH^+ and $\text{Mo-O(H}^+)-\text{Si}$ functionalities, respectively. The computed protonation and deprotonation energies are tabulated in Table 4 for the most relevant structures in electron volts.

Table 4. Deprotonation and protonation energies calculated for the Mo^{VI} model sites for Mo6 and MoMo6. (Values in eV)

	ΔE_{deprot}		ΔE_{prot}
MoMo6(SiO-H)	4.57	Mo6	4.03
MoMo6(SiO(H)-Mo)	5.23	MoMo6	4.56
		MoMo6	3.98
		Bridging oxygen	
		Mo6	4.25
		MoMo6	4.62

Two conclusions can be drawn from the computed deprotonation energies in general; the values span a range of 1.75 eV indicating that the acidity can vary drastically in the zeolite amongst sites and there is no unambiguous tendency in the acid strengths of Mo–OH, SiO(H)–Mo and SiO–H sites. The latter finding might sound discouraging at first, however it clearly emphasizes the importance of H-bond networks and auxiliary electrostatic interactions in the zeolite frame. By allowing the relaxation of the deprotonated structure we can witness the reorganization of these hydrogen-networks, which has a non-systematic contribution to the stabilization in the structures with different arrangement around the metal, oxidation state and hydration state. Still, if one looks only at the distribution, one finds more Mo^{III} sites in the very acidic as well as in the most basic regimes indicating high affinity to react and, accordingly, one should expect the absence of these sites in the zeolite, as it is indeed the case for molybdenum.

Concerning the most relevant Mo^{VI} sites, the Si–OH functionality appears to be more acidic than the SiO(H)–Mo functionality in **MoMo6**. Finally, side-by-side comparison of the ΔE_{deprot} values for Cr and Mo substituted analogues reveals more acidic Mo-based sites (by about 0.3 - 0.5 eV) as a result of the larger effective charge, which stabilizes the negative charge generated upon dehydrogenation.

ΔE_{prot} varies in a wide range of about 2.7 eV indicating very different basicity for some sites, however the Mo^{VI} sites appear exclusively in the low basicity regime ($\Delta E_{\text{prot}} = \sim 4$ eV). Bridging oxygens act slightly basic than terminal hydroxyls and molybdenyl groups. Comparing to Cr substituted zeolites we see a systematic negative shift (-0.5 – -1.5 eV) in the bridging oxygen (M–O–Si) basicity showing that these bridging oxygens become less basic when Cr is replaced to Mo.

BEA Results

We have repeatedly demonstrated in integrated experimental and computational studies that the simple sodalite (SOD) model provides a sufficiently realistic structural description for the metal containing site of the zeolite. Nevertheless, in cases when structurally significantly differing but energetically similar sites are present, e.g. **Mo6W** vs. **MoMo6**, the sodalite framework might be too rigid to account for subtle differences in the stability-structure relationship. To get a more realistic insight into the structures and energetics of the most stable forms, we remodeled the **Mo6**, **Mo6W**, **MoMo6**, **Mo6-2W^{1c,1p}**, **Mo6-2W^{2p}** and **MoMo6W** sites in BEA zeolite. Due to the size of the BEA unit cell (192 atoms), and the number of different T sites (9), a complete BEA study would have been computationally very resource demanding. For this reason, our investigation is limited to three T-sites, T1, T2, and T9, which were selected on the bases of our previous work ¹¹, showing that these T-sites exhibit very different affinity to accommodate M=O, M–OH groups, respectively.

Table 5. Relative stabilities of the most stable structures at T1, T2 and T9 sites in BEA zeolite in eV.

	T1	T2	T9
Mo	0.09	0.03	0.00
Mo6	0.18	0.10	0.00
Mo6W	0.19	0.12	0.00
MoMo6	0.08	0.08	0.89
Mo6-2W ^{2p}	2.08	0.23	n.a.
Mo6-2W ^{1p,1c}	0.53	2.34	n.a.
MoMo6W	0.00	0.35	1.02

Table 5 shows how the relative stabilities of the selected structures depend on three T sites of the BEA zeolite. There are only subtle differences (0.089 and 0.034 eV) between T sites for the isoelectronic substitution of a silicon atom to a Mo^{IV}. More pronounced differences can be seen for the Mo^{VI} state (**Mo6**); the (–SiO)₄Mo=O functionality is 0.100 and 0.179 eV more stable at the T9 position than in T2 and T1, respectively. As expected, the same pattern in T sites with similar magnitudes appears for the **Mo6W**, which has the same electronic structure around the molybdenum as in **Mo6** but with an extra physisorbed water molecule. For **Mo6-2W^{2p}** with two physisorbed water molecules, one would expect the same behavior, however, spatial requirements and hydrogen networks completely hinder this original trend amongst T sites, resulting in a most stable T2 site.

Very different behavior is revealed for the **MoMo6** and **MoMo6W** forms. Then again, in these structures the water molecule is split into an ‘O²⁻’ and two ‘H⁺’s to form a new Mo=O bond and two H–OSi functionalities. Significant structural distortions of the zeolite framework are accompanied with this process and our simulations clearly demonstrated that the different T sites adopt these structural changes very differently. Namely, T1 and T2 sites profit more from this structural relaxation/distortion than T9 site and accordingly the water splitting process, i.e. going from **Mo6W** to **MoMo6**, becomes preferred at T1 and T2 sites by 0.1 and 0.04 eV, respectively. The appealing consistency of our calculations is clearly reflected in the stability order of **MoMo6W** amongst the T sites being similar to that of **MoMo6**, as expected on the electronic structure similarity; T1 site is the most stable whereas T9 is the least stable when hosting Mo^{VI} with two Mo=O functionalities. At this hydration state water spitting is strongly preferred at T1 (-0.53 eV), it is an equilibrium process at T2 (0.12 eV), whereas most probably is an uphill process at T9. Thus, our calculations unambiguously revealed different structural relaxation or distortion

ability at different T sites which is manifested in the reactivity of the molybdenum center at these positions.

It is also worth noting that in cases when the reactive site undergoes so drastic structural change upon a reaction as in the case of going from **Mo6W** to **MoMo6**, i.e. water splitting, the sodalite cage might not provide a realistic picture about the energetics due to its inability to distort its frame properly. For example, simulations in SOD predict a thermodynamically not preferred water spitting for the **Mo6W** to **MoMo6** transition, whereas it is clearly a feasible process at the T1 position in the BEA frame. In these instances, modeling the processes in BEA zeolite is crucial after prescreening the various structures with the simple SOD model. Similar conclusion can be drawn for the computed equilibrium geometries: simulations in SOD and BEA reveal conceptually similar arrangements around the molybdenum center, however, fluctuations in the structural metrics, up to 0.2 Å for weak bonds, might be expected when going from one zeolite frame to another.

Conclusions

We effectively prepared Mo-containing BEA zeolites by using a two-steps post-synthesis method starting from SiBEA and Mo^{II} acetate. The incorporation of molybdenum ions into the zeolite framework was evidenced and characterized by several experimental techniques; most importantly X-ray diffractograms indicate a characteristic framework expansion upon Mo loading, whereas FTIR measurements strongly support that the isolated Mo containing sites have been formed upon reaction of Mo ions with silanol groups of vacant T-atom sites. Moreover, DR-UV-vis measurements provide unambiguous evidence for LMCT charge transfer for O²⁻ to Mo^{VI} transitions; the peaks at 265 and 310 nm resemble to documented O → Mo^{VI} transitions in tetrahedral and octahedral environments, respectively, however other geometries, e.g. five

coordinated trigonal-bipyramidal or square-pyramidal structures also cannot be definitely excluded due to the overlap of the characteristic peaks of $O^{2-} \rightarrow Mo^{VI}$ in these arrangements. The formation of Brønsted and Lewis acidic sites, i.e. $-OH$ and Mo^{VI} functionalities, in $Mo_{3.0}SiBEA$ were further evidenced by FTIR investigations; using pyridine as adsorption probe molecule, the appearance of pyridinium ion and Mo^{VI} coordinated pyridine was observed.

Systematic periodic plane-wave simulations using a model sodalite cage have been carried out to get insight into the relative stability and structure of plausible isomeric molybdenum sites in +6 and +3 oxidation states and different hydration states. The low protonation and deprotonation values as well as the ease with which Mo^{III} centers bind water molecules indicate that Mo^{III} loaded sites are very reactive and most probably undergo oxidation to Mo^{VI} with suitable reactants, e.g. under O_2 , in line with the lack of d-d transitions in the DR UV-vis spectra indicating only Mo^{VI} cores. The most plausible Mo^{VI} site under anhydrous conditions has a trigonal-bipyramidal structure with four $Mo-OSi-$ bonds integrated into the zeolite frame and with a molybdenyl ($Mo=O$) functionality in an axial position (**Mo6**). Upon hydration, we see the coordination of the entering water molecule to this $Mo=O$ functionality via an $O \cdots H$ hydrogen bond (**Mo6W**). The second water molecule rather coordinates to the molybdenum center with its oxygen to form a pseudo-octahedral species (**Mo6-2W^{1p,1c}**). Water splitting might be feasible in the former case at higher temperatures, whereas this process is energetically favorable (-0.031 eV) in the latter hydration state according to the calculations in the SOD model cage. The reaction with water results in two $Mo=O$ functionalities at the metal and $SiOH$ termini for the zeolite frame.

Remodeling the most stable Mo^{VI} sites in three T positions (T1, T2 and T9) of BEA framework, using a unit cell of 192 atoms periodically, indicates that reactivity of molybdenum based sites is significantly influenced by the rigidity/flexibility of the zeolite frame to adopt a certain structure

characteristic the product. A slight preference for the penta-coordinated $(\text{SiO})_4\text{Mo}=\text{O}$ species is revealed at the T9 position over T1 and T2. T1 is, however, superior in adopting pseudo-octahedral $(\text{SiO})_2(\text{Si}(\text{H})\text{O})_2\text{Mo}(=\text{O})_2$ structures resulting in significantly favoured water splitting processes. The latter process is also feasible at molybdenum in T2 position, but it is an energetically uphill process for Mo sites at T9 due to the rigidity of the zeolite frame in this position. From these results it is also clear that the sodalite model cage might serve to pre-estimate the stability of the numerous plausible isomers, however, more realistic zeolite models, such as BEA, is needed to adequately assess the stability-structure relationship for close energy states, such as for water splitting reaction in this study.

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Author Contributions

The manuscript was written through contributions of all authors. All authors have given approval to the final version of the manuscript.

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