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# Wave Analysis in the Atmosphere of Venus Below 100-km Altitude, Simulated by the LMD Venus GCM

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## Abstract

A new simulation of Venus atmospheric circulation obtained with the LMD Venus GCM is described and the simulated wave activity is analysed. Agreement with observed features of the temperature structure, static stability and zonal wind field is good, such as the presence of a cold polar collar, diurnal and semi-diurnal tides. At the resolution used (96 longitudes  $\times$  96 latitudes), a fully developed superrotation is obtained both when the simulation is initialised from rest and from an atmosphere already in superrotation, though winds are still weak below the clouds (roughly half the observed values). The atmospheric waves play a crucial role in the angular momentum budget of the Venus's atmospheric circulation. In the upper cloud, the vertical angular momentum is transported by the diurnal and semi-diurnal tides. Above the cloud base (approximately 1 bar), equatorward transport of angular momentum is done by polar barotropic and mid- to high-latitude baroclinic waves present in the cloud region, with frequencies between 5 and 20 cycles per

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Venus day (periods between 6 and 23 Earth days). In the middle cloud, just above the convective layer, a Kelvin type wave (period around 7.3 Ed) is present at the equator, as well as a low-latitude Rossby-gravity type wave (period around 16 Ed). Below the clouds, large-scale mid- to high-latitude gravity waves develop and play a significant role in the angular momentum balance.

*Keywords:* Venus, atmosphere ; Atmospheres, dynamics ; Superrotation ; Numerical modeling

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## 1 **1. Introduction**

2 The general circulation in Venus's atmosphere is dominated by the phe-  
3 nomenon called superrotation, with most of the atmosphere rotating in the  
4 same direction but about sixty times faster than the solid surface. The  
5 mechanism that controls this phenomenon combines transport of angular  
6 momentum by the mean meridional circulation with compensation done by  
7 planetary-scale waves. This idea was originally proposed by Gierasch (1975)  
8 and Rossow and Williams (1979), and has been demonstrated in recent years  
9 with the study of numerical simulations conducted by General Circulation  
10 Models (GCMs) of the Venus's atmosphere (e.g. Yamamoto and Takahashi,  
11 2003; Lee et al., 2007). These tools are very useful to study the wave ac-  
12 tivity and its role in the angular momentum budget. In addition to the  
13 balance between transport by the mean meridional circulation and transport  
14 by the horizontal planetary waves, the role of thermal tides that transport  
15 angular momentum vertically in the low latitudes was confirmed by recent  
16 works (Takagi and Matsuda, 2007; Lebonnois et al., 2010). The most recent

17 and realistic GCMs either use a full radiative transfer module to compute  
18 temperature self-consistently (Lebonnois et al., 2010; Ikeda, 2011; Lee and  
19 Richardson, 2011; Mendonca et al., 2015), or force the temperature structure  
20 with carefully prepared heating rate profile and Newtonian cooling (Sugimoto  
21 et al., 2014a,b).

22 A variety of waves in Venus's atmosphere has been observed in the cloud  
23 region, in the middle cloud from infrared observations or at the cloud-top  
24 from reflected visible and ultraviolet sunlight (e.g. Belton et al., 1976; Rossow  
25 et al., 1980; Del Genio and Rossow, 1990; Peralta et al., 2008; Piccialli et al.,  
26 2014). These observed waves range from planetary-scale waves to small-scale  
27 gravity waves. Variability observed in the wind reveals periods from 4-5  
28 Earth days to 1 Venus day, or even longer (Rossow et al., 1990; Kouyama  
29 et al., 2013; Khatuntsev et al., 2013). Small-scale gravity waves are observed  
30 in Venus-Express datasets, with VIRTIS images (Peralta et al., 2008), VMC  
31 images (Piccialli et al., 2014), or VeRa radio-occultations (Tellmann et al.,  
32 2012). The theoretical analysis of waves present in Venus's atmosphere is  
33 different from the Earth case, because of the cyclostrophic regime and the  
34 crucial role played by the mean zonal wind field. Most analytical works  
35 studying Venus's atmospheric waves use a realistic vertical wind profile, but  
36 with a solid-body rotation approximation for the latitudinal wind profile  
37 (e.g. Covey and Schubert, 1982; Schinder et al., 1990; Smith et al., 1993).  
38 A detailed theoretical analysis of waves in the context of a realistic zonal  
39 wind field for Venus has been recently undertaken by Peralta et al. (2014a,b,  
40 2015), exploring wave solutions and their classification.

41 Kouyama et al. (2015) explores the possibility of retroactive interactions



42 between a low-latitude Kelvin type wave and mid-latitude Rossby type waves  
43 at the cloud top: the variations of the zonal wind induced by each wave  
44 favor the vertical propagation of the other one, that process yields long-term  
45 variability of the wind over periods of several Venus days.

46 Using a high-resolution Venus GCM starting from superrotation and  
47 forced by observed heating rate profile and Newtonian cooling, Sugimoto  
48 et al. (2014a,b) analysed the wave activity produced in the cloud region. The  
49 large vertical zonal wind shear and latitudinal temperature gradient generate  
50 the basic state of baroclinic instability in the cloud region. Baroclinic waves  
51 develop, and at cloud-top, Rossby type waves are produced by this baro-  
52 clinic activity. However, further studies of Venus waves using various GCMs  
53 are required to get a comprehensive understanding of Venus's atmospheric  
54 dynamics.

55 In this work, we present the recent evolutions of the LMD Venus GCM  
56 (Lebonnois et al., 2010), that simulates realistic temperature and zonal wind  
57 fields (Section 2), with a detailed analysis of the waves produced in this  
58 simulation (Section 3).

## 59 **2. Simulations and Validation against Observations**

### 60 *2.1. The LMD Venus GCM*

61 The model developed at LMD for the study of Venus's atmosphere has  
62 been described in details in Lebonnois et al. (2010). It is based on the LMDZ  
63 latitude-longitude grid finite-difference dynamical core (e.g. Hourdin et al.,  
64 2006), including a longitudinal polar filter.

65 Most of the features of this GCM are similar to those presented in Lebon-  
66 nois et al. (2010). Among the physical parameterisations, the main difference  
67 is the use of a boundary layer scheme taken from Mellor and Yamada (1982)  
68 to compute the eddy diffusion coefficient and the time evolution of the mixed  
69 variables. The equations used are described in the Appendix B of Hourdin  
70 et al. (2002). This boundary layer scheme is based on a more physical repre-  
71 sentation of the unstable regions. It was successfully used for other planetary  
72 applications of the LMD GCM (e.g. Lebonnois et al., 2012a, for Titan). At  
73 surface, the drag coefficient is similar to the one used in the previous param-  
74 eterisation:  $C_d = (0.4/\ln(1 + z_1/z_0))^2$ , where  $z_1$  is the altitude of the center  
75 of the first layer of the model (roughly 10 m in our case) and  $z_0$  is the rough-  
76 ness coefficient, taken equal to 1 cm. Otherwise, compared to Lebonnois  
77 et al. (2010) we use the same hybrid vertical coordinates with topography  
78 (50 vertical levels), the soil model is unchanged, the temperature dependence  
79 of the specific heat is taken into account, the radiative transfer includes solar  
80 heating rate profiles as a function of solar zenith angle taken from a look-  
81 up table based on Crisp (1986), and the infrared net-exchange rate (NER)  
82 matrix formulation discussed in Eymet et al. (2009). For the computation  
83 of the IR NER matrix, opacity sources (gas, clouds) are taken horizontally  
84 uniform and properties are the same as in Lebonnois et al. (2010).

85 The second main difference is the horizontal resolution. For the study  
86 that is presented here, the resolution was increased to 96 longitudes by 96  
87 latitudes ( $3.75^\circ \times 1.875^\circ$ ). A few years ago, a simulation was performed with  
88 this model with a horizontal resolution of 48 longitudes by 32 latitudes and  
89 run for up to 190 Venus days (1 Venus day (Vd) = 117 Earth days (Ed))

90 starting from an atmosphere already in superrotation. Modeled temperature  
91 field was compared with VIRTIS/Venus-Express temperature retrievals to  
92 discuss thermal tides above the clouds (Migliorini et al., 2012). It must be  
93 noted that when starting from rest, the superrotation was not fully evolved  
94 in this version of the GCM, with weaker zonal wind in the deep atmosphere  
95 and a peak around 80 m/s at the cloud-top, after more than 1000 Vd. In the  
96 present work, the simulations were started either from rest (for 300 Venus  
97 days) or from a zonal wind field already in superrotation (for 190 Venus  
98 days). Both simulations converged toward very similar wind fields, meaning  
99 that the superrotation is fully evolved by the LMD VGCM from motionless  
100 state for the first time. The present work will focus on the analysis of the  
101 simulation started from superrotation.

#### 102 **TABLE 1**

103 Increasing the resolution had a drawback: it has induced a larger residual  
104 term in the angular momentum budget as indicated in Table 1 (that can be  
105 compared to simulations presented in Lebonnois et al., 2012b). As mentioned  
106 in Lebonnois et al. (2012b), the lack of angular momentum conservation is  
107 a problem for simulations of Venus's atmosphere, and Table 1 shows that in  
108 this configuration, our GCM has a bias in the angular momentum budget.  
109 This is currently investigated and needs to be improved in future simula-  
110 tions. This numerical inaccuracy alters the balance of angular momentum  
111 transport, the non-zero term due to dynamics in the angular momentum  
112 budget being compensated by a non-zero balance of the surface momentum  
113 exchanges. However, the convergence between simulations started from rest  
114 and started from superrotation gives confidence in the achieved wind dis-

115 tributions, except near the surface where the winds must be biased. This  
116 bias should be taken into account when comparing the resulting simulated  
117 circulation to the observations near the surface.

## 118 *2.2. Temperature and Winds Fields*

### 119 **FIG 1**

120 The temperature structure obtained both in the simulation started from  
121 superrotation (after 190 Vd) and in the simulation started from rest (after  
122 300 Vd) are displayed in Fig. 1. Though the vertical profile is close to the  
123 VIRA reference atmosphere (Seiff et al., 1985), the modeled surface tempera-  
124 ture is colder than observed, and the temperature in the cloud slightly higher  
125 (e.g. Tellmann et al., 2009; Migliorini et al., 2012; Grassi et al., 2014).

### 126 **FIG 2**

127 The temporal variation of the temperature at a fixed longitude, at cloud  
128 top, is shown in Fig. 2. It is dominated by the thermal tides, but high-  
129 frequency variations are also clearly present. As in previous simulations  
130 (Lebonnois et al., 2010; Migliorini et al., 2012), the semi-diurnal tide is dom-  
131 inant at low latitudes, while the diurnal tide is dominant at high latitudes.  
132 The quasi-bidiurnal oscillation that was present in L10 is not present in these  
133 simulations. This mode of oscillation, which is not understood yet and which  
134 is clearly not present in the observations, appeared in previous simulations  
135 only when starting from rest, and in simulations when the zonal wind speed  
136 in the cloud region remained weaker than observed.

### 137 **FIG 3**

138 The horizontal structure of the temperature at  $3 \times 10^3$  Pa (roughly 67 km,  
139 just below the cloud-top) is shown in Fig. 3, with four panels separated by

140  $1/100 V_d$  (1.17 Ed). Though the zonally and temporally averaged latitudinal  
141 profiles show a small cold-collar signature at cloud-top, an equator-to-pole  
142 contrast around 30 K is obtained near 60 km altitude (Fig. 1b). The struc-  
143 ture of the cold polar collar is much more visible in the maps shown in Fig. 3  
144 (without zonal and temporal averaging). This structure is very similar to the  
145 cold polar collar structure discussed in Ando et al. (2016), which is obtained  
146 with the GCM named AFES (Sugimoto et al., 2014a,b). A similar feature  
147 was also obtained previously in the works of Lee et al. (2005) and Yamamoto  
148 and Takahashi (2012). The model of Lee et al. (2005) obtained quite a differ-  
149 ent circulation compared to the present results and to the AFES model, so  
150 comparison is difficult. Yamamoto and Takahashi (2012) showed a partially  
151 formed cold collar with a warm core, but did not investigate the mecha-  
152 nism producing this feature. In a detailed investigation, Ando et al. (2016)  
153 demonstrated the role of the thermal tide in this temperature distribution.

154 The shape of the polar temperature distribution (cold collar and warm  
155 pole) obtained in our results is affected both by the thermal tide and by high-  
156 frequency wave activity, though the variations illustrated in Fig. 3 are weak.  
157 The contrasts inside the polar regions are also weaker than in the AFES  
158 simulations of Ando et al. (2016). Note that AFES is a spectral model used  
159 at higher resolution. These two significant differences, spectral model and  
160 high resolution should improve the description of the polar region. It must  
161 be noted that the latitudinal variation of the cloud structure is not taken  
162 into account in any of these works. This could play a role in the shape  
163 and strength of the cold collar, since the radiative impact of the clouds in  
164 the polar region is significant, but the results discussed here show that this

165 interaction is of second order for the presence of the cold collar.

166 **FIG 4**

167 The static stability profile is shown in Figure 4. It may be compared to  
168 the stability profiles deduced from the Pioneer Venus data (Schubert, 1983),  
169 from the Vega 2 entry probe (also reproduced on Fig. 4, Zasova et al.,  
170 2007), and from the VeRa/Venus Express data (Tellmann et al., 2009). The  
171 dominant features are the convective region located in the lower and middle  
172 clouds (the region with very small stability around 50 km altitude), the stable  
173 layer below the clouds, and the low-stability deep atmosphere (below 30 km  
174 altitude). Compared to the simulations done in Lebonnois et al. (2010), the  
175 change of boundary layer scheme has clearly improved the agreement with  
176 observations close to the surface. The thickness of the modeled convective  
177 region is smaller than in the observations. As mentioned in Lebonnois et al.  
178 (2015), the cloud model used to compute the radiative transfer plays a  
179 role in this feature. Simulations based on a new cloud model (Haus et al.,  
180 2014) in which the thickness of the convective layer is improved compared to  
181 observations will be studied in future work.

182 **FIG 5**

183 **FIG 6**

184 The zonally and temporally averaged zonal wind field obtained in the  
185 simulation is presented in Fig. 5, together with the mean meridional circula-  
186 tion. As in Lebonnois et al. (2010), the meridional circulation is divided in  
187 three regions along the vertical: a dominant pair of equator-to-pole Hadley-  
188 like cells in the lower and middle cloud (roughly  $10^5$  to  $10^4$  Pa), a similar  
189 pair above  $10^4$  Pa (up to the model top), and another below the clouds,

190 though in the deep atmosphere the cell structure is affected by perturba-  
191 tions from topography. The comparison between the modeled zonal wind  
192 field and observations has improved compared to Lebonnois et al. (2010)  
193 as shown in Fig. 6, where the vertical and latitudinal profiles of the zonal  
194 wind are compared to in-situ vertical profiles (adapted from Schubert, 1983)  
195 and cloud-tracking latitudinal profiles (taken from Hueso et al., 2015). The  
196 improved treatment of the boundary layer yields more efficient pumping of  
197 angular momentum in the deep atmosphere, and thus the zonal wind below  
198 the clouds can reach more than 20 m/s. Although it is approximately half  
199 of the observed values (Fig. 6), this is a significant step forward compared to  
200 Lebonnois et al. (2010) where the deepest atmosphere was moving with only  
201 very weak zonal winds. However, the increased horizontal resolution plays  
202 also a role. The simulations previously mentioned, done with the improved  
203 boundary layer but at lower horizontal resolution, led to weaker zonal wind  
204 (especially in the deep atmosphere) when started from rest. One possible ex-  
205 planation is that the increase in the model grid resolution have improved the  
206 representation of the planetary-scale waves at the smallest resolved scales,  
207 with therefore an effect on the global angular momentum balance (see in  
208 particular Section 3.5 below). This will be investigated in order to confirm  
209 the present results.

210 In the upper region of the clouds, the modeled zonal wind is close to the  
211 observations. However, several discrepancies must be mentioned: (1) above  
212 the clouds, the zonal wind does not decrease as fast with altitude as the  
213 thermal wind computations suggest (e.g. Piccialli et al., 2012) and values  
214 around 100 m/s extends up to 90 km altitude; (2) the equatorial jet is too

215 strong compared to mid-latitudes – it must be noted that this region is ex-  
216 tremely sensitive to radiative forcings, and to details in the model (such as  
217 cloud structure), which affect the balance in angular momentum and the  
218 zonal wind distribution; (3) the vertical gradient between the lower and up-  
219 per cloud is higher than observed; (4) the latitudinal gradient in the polar  
220 region is too steep compared to the cloud-tracking zonal wind profiles. This  
221 is related to the temperature field in the polar vortex (position and amplitude  
222 of the cold collar). Several investigations are on-going in order to improve on  
223 these discrepancies, mainly regarding the potential role of small-scale pro-  
224 cesses (gravity waves, convective mixing) and improvements in the radiative  
225 transfer. Despite these discrepancies, the overall structure of the zonal wind  
226 field is close to the observed structure, and we focus now on the analysis of  
227 the waves produced in the GCM simulation.

### 228 **3. Wave analysis**

#### 229 *3.1. Analysis technique*

230 To study the waves developing in the modeled atmospheric circulation,  
231 we use Fast Fourier Transform (FFT) to analyse frequency spectrum of tem-  
232 perature, zonal and meridional wind fields. Modeled atmospheric fields are  
233 output with a frequency of 100 points per Venus day. For each grid point  
234 in the GCM (given latitude, longitude and pressure level), the FFT is ap-  
235 plied to this time series over the last four Venus days of the simulation. The  
236 amplitude of the FFT signal at a given frequency is averaged over the lon-  
237 gitudes before study. To minimize the impact of the 4-Vd time window, the  
238 time series is multiplied by a triangular window (0 at  $t=0$  and  $t=4$  Vd, 2 at



239  $t=2 Vd$ ) (Harris, 1978). Resolution of the FFT spectra is  $0.25/Vd$ , over the  
 240 range  $0.25-50/Vd$ .

241 **FIG 7**

242 The amplitude of the FFT of temperature, zonal and meridional wind  
 243 fields as a function of pressure and frequency are displayed in Fig. 7, for the  
 244 equator and  $70^\circ N$ . Several groups of waves appear in these plots:

- 245 • The diurnal and semi-diurnal tides are the strongest waves visible above  
 246 roughly  $10^5$  Pa (see Section 3.3 and Fig. 11 below).
- 247 • In the cloud region, between  $10^5$  Pa and  $10^3$  Pa, a large group of waves  
 248 is visible at high latitudes, with frequencies between 5 and  $20/Vd$ .
- 249 • At  $2 \times 10^4$  Pa, in the equatorial region, a wave is visible around  $16/Vd$ ,  
 250 mostly on the zonal wind. Its harmonics are visible too.
- 251 • In the deep atmosphere, below the clouds, waves are mostly visible at  
 252 high latitudes, with frequencies up to  $30/Vd$ , and a peak near  $8/Vd$ .  
 253 Additional waves are also visible in the equatorial region, at very low  
 254 frequencies.

255 **FIG 8**

256 Latitudinal dependence of the spectra are displayed in Fig. 8 for the  
 257 cloud region (pressure of  $2 \times 10^4$  Pa) and for the deep atmosphere (pressure  
 258 of  $1 \times 10^6$  Pa). At  $2 \times 10^4$  Pa, the diurnal and semi-diurnal tides are visible,  
 259 as well as the high- to mid-latitude group of waves, with maxima between 10  
 260 and  $16/Vd$ . This broad activity from mid- to high-latitudes, without a typical  
 261 frequency, is certainly resulting from instability (barotropic or baroclinic)

262 in this region (see Section 3.4). Near  $16/Vd$ , the equatorial wave mentioned  
 263 previously is also visible in the zonal wind (with its harmonics) and tempera-  
 264 ture. In the meridional wind, this wave is seen at low latitudes but not on the  
 265 Equator. These are characteristics of a Kelvin type wave (as confirmed by  
 266 its horizontal structure, see Section 3.4 below). Another low-latitude wave is  
 267 seen at a frequency around  $8/Vd$ , with the opposite characteristics: visible  
 268 only in the meridional wind at the equator, and in the zonal wind at low  
 269 latitudes. This could indicate a Rossby-gravity type wave. At  $1 \times 10^6$  Pa, the  
 270 distribution of the waves in the mid- to high-latitudes is displayed.

271 It is also possible to apply the FFT bi-dimensionally (longitude-time) for  
 272 a given latitude and pressure level. In this case, the direction of the wave  
 273 propagation and the longitudinal wavenumber are obtained. Note that the  
 274 mean zonal flow is westward, as Venus's surface is in retrograde rotation  
 275 compared to the Earth's rotation. Apart from the thermal tides that are  
 276 eastward (along with the Sun), all the previously mentioned waves are west-  
 277 ward, with wavenumber 1 for the group in the clouds and wavenumber 2 or 3  
 278 for the group in the deep atmosphere. In the cloud, the Kelvin type wave is  
 279 moving almost at the same speed as the mean zonal flow, while its harmonics  
 280 are faster. The other group is slower, thus propagating eastward relatively to  
 281 the mean flow. In the deep atmosphere, waves both faster and slower than  
 282 the zonal wind are present.

### 283 **FIG 9**

284 To separate the different waves, we apply filters on the FFT spectra,  
 285 before applying a reverse FFT. At a given frequency  $f_0$ , the shape of the  
 286 lowpass filter is: 1 for  $f < f_0 - \delta f$ , 0 for  $f > f_0 + \delta f$  and  $0.5 + \sin(\pi/2 \times$

287  $(f_0 - f)/\delta f)/2$  in between, where  $\delta f$  is  $1/Vd$ . A similar shape is applied for  
 288 a highpass filter, and a bandpass filter is obtained between two frequencies  
 289  $f_1$  and  $f_2$  by combining a highpass filter at  $f_1$  and a lowpass filter at  $f_2$ .  
 290 Filtering is done at these cutting frequencies: 4, 10 and  $22/Vd$ , as illustrated  
 291 in Fig. 9.

### 292 3.2. Angular momentum transport

293 The specific angular momentum  $M$  is computed as  $M = u \times a \cos \phi$ , where  
 294  $a$  is Venus's radius,  $\phi$  is the latitude, and  $u$  is the zonal wind. The total  
 295 meridional transport  $[\overline{vM}]$  of the angular momentum can be decomposed as:

$$[\overline{vM}] = [\overline{v}][\overline{M}] + [\overline{v^*}][\overline{M^*}] + [\overline{v'M'}], \quad (1)$$

296 where  $[M]$  is the zonal mean,  $\overline{M}$  the temporal average,  $M^* = M - [M]$ ,  
 297 and  $M' = M - \overline{M}$ .  $[\overline{v}][\overline{M}]$  is the contribution from the mean meridional  
 298 circulation (MMC),  $[\overline{v^*}][\overline{M^*}]$  is the contribution from stationary waves, and  
 299  $[\overline{v'M'}]$  is the contribution from transient waves. The same equation applies  
 300 for vertical transport of  $M$ , using the vertical wind  $w$  (in Pa/s) instead of the  
 301 meridional wind  $v$ . The stationary waves component appears to be negligible.

302 The transient term can be computed either with the complete perturbation  
 303 field  $M'$ , or with the perturbations obtained after wave filtering. This  
 304 allows to separate the contribution of each group of waves in the horizontal  
 305 or vertical transport.

### 306 FIG 10

307 The total horizontal transport is obtained with a vertical integration of  
 308 each term, weighted by the mass of each cell. The total vertical transport is

309 done with a horizontal integration, weighted only by  $\cos \phi$ . Figure 10 shows  
 310 these total horizontal and vertical transports of angular momentum. In the  
 311 horizontal, the poleward MMC transport is compensated by the equatorward  
 312 transport by the waves. Note that this plot is similar if the vertical integra-  
 313 tion is done only down to the cloud bottom, which means that this balance  
 314 is obtained both in the cloud region and in the deep atmosphere. In the  
 315 vertical, the upward MMC transport is compensated by downward transport  
 316 by the waves. In the cloud region and above, this transport is mostly done  
 317 by the thermal tides. This is consistent with our previous analysis done  
 318 in Lebonnois et al. (2010). Therefore, in our simulations, superrotation is  
 319 obtained and maintained through the Gierasch-Rossow-Williams mechanism  
 320 (mean meridional circulation and horizontal waves), with a significant ad-  
 321 ditional contribution of the thermal tides in the global angular momentum  
 322 balance. It must be noted that the residual poleward transport is a combi-  
 323 nation of the latitudinal distribution of the numerical inaccuracies discussed  
 324 at the end of Section 2.1, and of latitudinal redistribution of angular momen-  
 325 tum at the surface. In the vertical, the net transport should be zero and the  
 326 residual is also an indication of these numerical inaccuracies.

### 327 *3.3. Thermal Tides*

#### 328 **FIG 11**

329 Latitude vs pressure maps of the FFT spectrum of the temperature, for  
 330 the frequencies  $1/V_d$  and  $2/V_d$  are plotted in Fig. 11. They show that the  
 331 tides are mostly visible above  $10^4$  Pa. The semi-diurnal tide is dominating in  
 332 the low to mid latitudes between  $10^4$  Pa and  $10^2$  Pa, while the diurnal tide  
 333 dominates above  $10^2$  Pa, and at high latitudes. This is consistent with the

334 analysis of our previous simulations at lower resolution that was discussed in  
 335 Migliorini et al. (2012), in comparison with VIRTIS/Venus-Express dataset  
 336 analysis. The amplitude of the diurnal and semi-diurnal tides (5 to 10 K  
 337 in the pressure range  $10^4$  to  $10^2$  Pa) is consistent with the observed values  
 338 (Migliorini et al., 2012; Grassi et al., 2014).

### 339 *3.4. Waves in the Cloud Layer and Above*

#### 340 **FIG 12**

341 To illustrate the distribution of the waves present in the cloud region and  
 342 above, Fig. 12 shows the latitude vs pressure maps of the FFT spectra of the  
 343 zonal and meridional winds for two frequencies,  $7.25/V_d$  and  $16/V_d$ . One  
 344 group is located on the poles, where the latitudinal gradient of the zonal  
 345 wind speed is large, so the waves would be caused by barotropic instability.  
 346 Another group is at mid latitudes ( $40$  to  $70^\circ$ ), in a region dominated by  
 347 a large vertical gradient of the zonal wind. The level at which the phase  
 348 speed of these disturbances is equal to the background speed (steering level)  
 349 is deeper for the lower frequency waves, which explains that this mid- to  
 350 high-latitude wave group is located deeper ( $5 \times 10^4$  to  $1 \times 10^5$  Pa) than the  
 351 higher frequency wave group (around  $2 \times 10^4$  Pa). On the equatorial region,  
 352 the Kelvin type and mixed Rossby-gravity type waves are also visible.

353 As seen in Fig. 1, the latitudinal gradient between the equator and the  
 354 poles at  $1 \times 10^4$  Pa (roughly 60 km altitude) is around 30 K. This latitudinal  
 355 gradient of temperature and the strong vertical zonal wind shear in the  $10^5$ -  
 356  $10^4$  Pa region may be the source of baroclinic instabilities. A necessary  
 357 condition for baroclinic instability has been used by Sugimoto et al. (2014a),  
 358 following Young et al. (1984), though the validity of this criterion for Venus

359 may be taken with caution. The following latitudinal gradient must change  
 360 sign for instabilities to occur:

$$\frac{\partial \bar{q}}{\partial \phi} = 2a\Omega_u \cos \phi - \frac{\partial}{\partial \phi} \left( \frac{1}{\cos \phi} \frac{\partial}{\partial \phi} (\cos \phi \tilde{u}) \right) - \frac{4a^2 \Omega_u^2 \sin^2 \phi}{p} \frac{\partial}{\partial z} \left( \frac{p}{N^2} \frac{\partial \tilde{u}}{\partial z} \right) \quad (2)$$

361 where  $\Omega_u$  includes the rotation of the atmosphere at a reference level of  
 362  $3 \times 10^4$  Pa, and  $\tilde{u}$  is the mean zonal field relative to this reference level.  $N^2$   
 363 is the Brunt-Väisälä frequency, computed from the temperature lapse rate:

$$N^2 = \frac{g}{T} \left( \frac{\partial T}{\partial z} + \frac{g}{c_p} \right). \quad (3)$$

364 Such a criterion appears to be fulfilled in the mid to high latitudes, be-  
 365 tween  $10^5$ - $10^4$  Pa, as seen in Fig. 12c,d. Note also that criteria are also  
 366 satisfied in the polar region because of the second term in Eq.2, suggesting  
 367 that barotropic instability would happen.

### 368 **FIG 13**

369 Figure 13a shows the vertical and longitudinal structure of the waves at  
 370  $45^\circ\text{N}$ , for temperature and meridional wind fields filtered in the [10-22]/Vd  
 371 frequency range. Both present a tilt from up-east to down-west. They are  
 372 phase-shifted by approximately a quarter period. This structure is similar  
 373 to the one obtained in the GCM simulations of Sugimoto et al. (2014b)  
 374 (their Fig. 2; note that in their simulations, the zonal wind is flowing from  
 375 west to east while it is flowing from east to west in our plots) and it is  
 376 characteristic of a baroclinic mode. At  $80^\circ\text{N}$  (Fig. 13b), the structure is  
 377 different and the wave activity is barotropic, rather than baroclinic. These  
 378 mid-latitude baroclinic activity may be related to the Rossby waves obtained

379 at mid-latitude in the analysis of cloud-tracking observations by Del Genio  
 380 and Rossow (1990) (Pioneer Venus UV images) and by Kouyama et al. (2013)  
 381 (VMC/Venus Express images). However, due to the model-dependence of the  
 382 wave and mean-flow interactions, further investigations are needed to assess  
 383 the robustness of possible correlations with observed waves.

#### 384 **FIG 14**

385 The latitudinal transport of heat  $\overline{(C_p T)'v'}$  in the cloud region is plotted  
 386 in Fig. 14a for filtered fields in the frequency range [4-10]/Vd, and Fig. 14b  
 387 for filtered fields in the frequency range [10-22]/Vd. In the region where they  
 388 develop (30 to 70° of latitude, pressures around  $2 \times 10^4$  Pa for frequency range  
 389 [10-22]/Vd and deeper, around  $5 \times 10^4$  to  $1 \times 10^5$  Pa for frequency range [4-  
 390 10]/Vd), the baroclinic waves transport heat poleward. Below, equatorward  
 391 transport is visible, so that these waves tend to transport heat as in a direct  
 392 meridional cell, a behavior that was already mentioned in Sugimoto et al.  
 393 (2014b).

394 The latitudinal transport of angular momentum by these waves is shown  
 395 in Fig. 14c,d. Equatorward transport is dominant in the frequency range [10-  
 396 22]/Vd around  $3 \times 10^4$  Pa, but is also noted near  $1 \times 10^5$  Pa for frequency range  
 397 [4-10]/Vd. In the region around 60° and  $5 \times 10^4$  Pa, poleward transport of  
 398 angular momentum by the waves is visible, which can be related to the local  
 399 jet in this region (as seen in Fig. 5). In the equatorial region around  $2 \times 10^4$  Pa,  
 400 the Kelvin like wave transfers both heat and momentum equatorward.

#### 401 **FIG 15**

402 In the equatorial region, at  $2 \times 10^4$  Pa, the horizontal structure of the two  
 403 low-latitude waves previously mentioned, with frequencies around 7.25 and

404  $16/Vd$ , are shown in Fig. 15. Both waves are westward, with a wavenumber 1.  
405 The typical structure of a Kelvin type wave is visible in Fig. 15b (frequency  
406  $\sim 16/Vd$ ). This Kelvin type wave is propagating faster than the zonal wind,  
407 as seen on Fig. 8(c,e), except at the equator where it accelerates the flow.  
408 The structure of the other wave (Fig. 15a) has similar characteristics as a  
409 Rossby-gravity type wave of order  $n = 0$  as in Fig. 6a of Matsuno (1966). It  
410 is propagating slower than the zonal wind. The pressure at which these two  
411 waves develop ( $2 \times 10^4$  Pa) corresponds to a layer where the stability becomes  
412 large, just above the convective region in the cloud.

413 Both type of waves are suggested in the analysis of cloud-top observations  
414 by Del Genio and Rossow (1990) from Pioneer Venus UV images and by  
415 Kouyama et al. (2013) from VMC/Venus Express images. In Del Genio and  
416 Rossow (1990), the Kelvin wave is present when the zonal flow is faster.  
417 Kouyama et al. (2013) have a different conclusion with their analysis: the  
418 Kelvin wave appears when the zonal wind is slower, while Rossby waves  
419 prevail when the zonal wind is faster. However, it must be noted that in our  
420 work, these waves appear in the middle cloud and do not propagate upward  
421 to the cloud-top region. The vertical shape of the equatorial zonal wind field  
422 and its time variations are crucial to the development and propagation of  
423 these waves, and they are therefore very model-dependent. In the simulation  
424 started from rest, the Kelvin type wave was not present after  $200 Vd$ , but has  
425 developed after  $300 Vd$  when the equatorial jet is stronger. This suggests that  
426 wave and mean-flow interaction may be significant in the equatorial region,  
427 a conclusion consistent with the works of Del Genio and Rossow (1990) and  
428 Kouyama et al. (2013). Time-variation and interaction of this wave with the



429 mean flow will be the focus of a future more detailed study.

### 430 *3.5. Waves Below the Clouds*

#### 431 **FIG 16**

432 In the deep atmosphere, the dominant waves are seen at mid- to high-  
 433 latitudes, with frequencies up to  $30/Vd$ , as seen in Fig. 8. The dominant  
 434 frequency in the spectra is around  $7-8/Vd$ . Fig. 16 shows the contributions of  
 435 these waves in the angular momentum transport. They transport momentum  
 436 downward and equatorward in the mid- to high-latitude regions of the deep  
 437 atmosphere. This is the dominant contribution for transients, that balances  
 438 the horizontal and vertical transport of angular momentum by the mean  
 439 meridional circulation below the clouds.

#### 440 **FIG 17**

#### 441 **FIG 18**

442 Figure 17 illustrates the meridional distribution of these waves. Merid-  
 443 ional wind perturbations are associated to temperature perturbations: when  
 444 the meridional wind converges, the temperature increases, and reversely, neg-  
 445 ative temperature perturbations are associated to region where the merid-  
 446 ional wind diverges. This is characteristic of gravity waves (e.g. Holton,  
 447 2004). Wave trains are visible in Fig. 18, with wavenumbers 2 to 3. The  
 448 wind field presents strong convergence and divergence, but rather low vortic-  
 449 ity, which is again in favor of gravity waves. These waves are therefore iden-  
 450 tified as gravity waves. The source region is the stable zone below the clouds  
 451 (around  $2-3 \times 10^5$  Pa), where these waves may be excited through the pertur-  
 452 bations in temperature induced in this layer by the cloud-region baroclinic  
 453 waves. Note that these waves are completely different from the small-scale

454 gravity waves that are observed at and above the cloud-top region in the  
455 images and radio-occultation data from Venus-Express, which are supposed  
456 to be generated in the convective region located in the middle cloud and  
457 propagate upwards. Small-scale gravity waves generated by this convection  
458 and propagating downwards may also be present in the deep atmosphere,  
459 but they can not be resolved by the GCM and need to be parameterized,  
460 which is not done in this work.

#### 461 **FIG 19**

462 Figure 19 shows the temporal evolution of these waves both vertically  
463 and horizontally. Propagation is downward and equatorward, inducing mo-  
464 mentum transport where the mean zonal wind is smaller than in their source  
465 region. These large-scale downward-propagating gravity waves have never  
466 been suggested before. They were not present in the LMD Venus GCM  
467 simulations done at lower resolution. The increase in horizontal resolution  
468 may have improved the representation of wave activity at the lowest resolved  
469 scale, and favored the development of these gravity waves. Since their role in  
470 the angular momentum budget is significant in the deep atmosphere in the  
471 present simulations, their presence needs to be confirmed in future works, as  
472 well as their role in the superrotation of the atmosphere below the clouds.

#### 473 **4. Conclusion**

474 The LMD Venus GCM was used in this work to produce an updated  
475 simulation of Venus atmospheric circulation. At the resolution used here (96  
476 longitudes  $\times$  96 latitudes), convergence is obtained when started from rest  
477 or from an atmosphere already in superrotation, though numerical inaccu-

478 racies in the dynamical core have increased with resolution and affect the  
479 angular momentum budget. The temperature structure features a vertical  
480 profile close to observations, yet slightly colder in the deep atmosphere, a  
481 vertical profile of static stability in agreement with observations, dominating  
482 thermal tides above the cloud-base, and a cold polar collar structure in the  
483 upper cloud. To improve the fit of temperatures to observations, future work  
484 will include improvement in the radiative transfer properties (based on our  
485 recent work Lebonnois et al., 2015), and taking into account the latitudi-  
486 nal variations of the cloud. The modeled zonal wind distribution presents a  
487 fully developed superrotation, though winds are still weak below the clouds  
488 (roughly half the observed values).

489 We have analysed the waves present in this simulation, and their role in  
490 the balance of angular momentum budget in the atmosphere of Venus. The  
491 role of diurnal and semi-diurnal tides in vertical angular momentum transport  
492 is confirmed in the upper cloud. Polar barotropic and mid- to high-latitude  
493 baroclinic waves are present in the cloud region, with frequencies between 5  
494 and 20 cycles per Venus day (periods between 6 and 23 Earth days), that  
495 redistribute angular momentum significantly. In the middle cloud, just above  
496 the convective layer, a Kelvin type wave (period around 7.3 Ed) is present  
497 at the equator, as well as a low-latitude Rossby-gravity type wave (period  
498 around 16 Ed), but the characteristics of these wave activities and their  
499 interaction with the background zonal wind may be very sensitive to the  
500 modeled circulation and comparison with cloud-top observations should be  
501 done with caution. Below the clouds, wave activity that transport angular  
502 momentum both downward and equatorward is dominated by large-scale

503 mid- to high-latitude gravity waves. The presence and role of these waves  
504 was never mentioned in previous works. However, their sensitivity to details  
505 of the model needs to be assessed more completely, so that their role in the  
506 superrotation mechanism on Venus may be robustly established.

507 To assess the robustness of the wave activity in the different atmospheric  
508 region of Venus's atmosphere and their role in the mechanisms of superrota-  
509 tion, further investigations should always explore how sensitive these different  
510 waves are to the background circulation and temperature structure, and to  
511 the model and configuration used. In particular, the numerical bias in the  
512 angular momentum budget seen in the present simulations might affect the  
513 wave activity, and this analysis will need to be confirmed by using a more  
514 conservative dynamical core. However, the waves analysed in the present  
515 work present many similarities with the ones developing in the AFES Venus  
516 GCM (Sugimoto et al., 2014a,b; Ando et al., 2016), though forcing conditions  
517 are very different between these two GCMs. This brings confidence in the  
518 robustness of these features and of their role in the mechanism of superrota-  
519 tion. Temporal variability over long timescales (several Earth years, tens of  
520 Venus days) needs to be investigated too, since hints of such variability are  
521 present in the analysis of observational datasets.

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Table 1: Values of the terms in the total angular momentum budget, averaged over the last 2 Vd (units are  $10^{18}$  kg m<sup>2</sup> s<sup>-2</sup>).

	$\overline{dM_r/dt}$	$\overline{T}$ ( $\overline{T^+}$ )	$\overline{F}$ ( $\overline{F^+}$ )	$\overline{D}$	$\overline{S}$	$\overline{\epsilon}$	$\overline{\epsilon^*}$	$\xi$
300 Vd (from rest)	1.5	-28.3 (42.5)	-7.6 (3.0)	1.6	-3.2	39.0	37.4	0.46
190 Vd (from superrotation)	6.8	-28.1 (41.6)	-7.0 (1.8)	1.9	-3.5	43.5	41.9	0.53

$M_r$  = Relative part of the total atmospheric angular momentum, due to zonal wind  $u$

$T$  = Mountain torque on the atmosphere due to topography ( $T^+$  is its positive (source) component)

$F$  = Surface torque on the atmosphere due to friction ( $F^+$  is its positive (source) component)

$D$  = Residual torque due to conservation errors in the horizontal dissipation parameterization

$S$  = Torque on the atmosphere due to upper boundary conditions (sponge layer)

$\epsilon$  = Residual numerical rate of total angular momentum variation due to conservation errors in the dynamical core

$\epsilon^* = S + D + \epsilon$ , should theoretically be zero

$\xi$  = Ratio between  $|\overline{\epsilon^*}|$  and  $Max(\overline{T^+} + \overline{F^+}, |\overline{T^-} + \overline{F^-}|)$  (Lebonnois et al., 2012b)

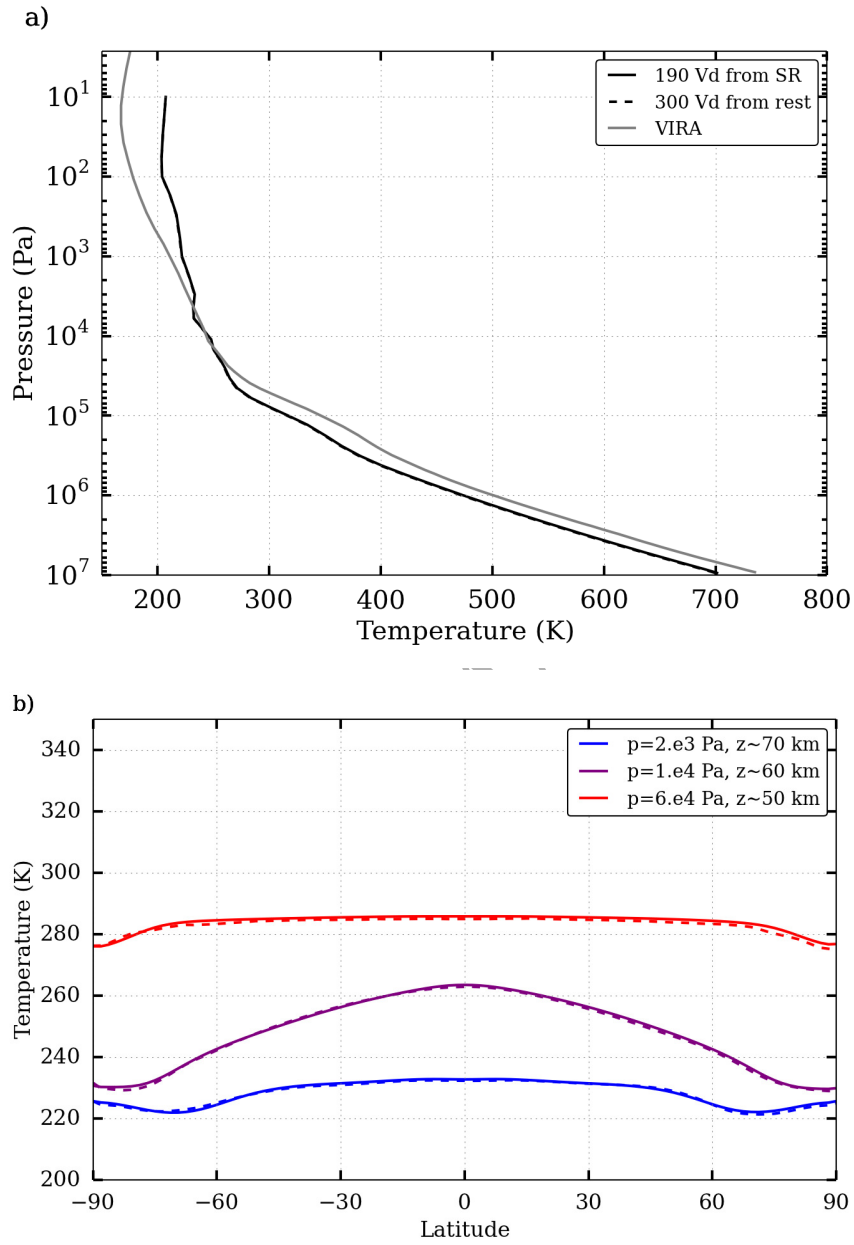


Figure 1: Temperature structure obtained in the simulation started from superrotation, after 190 Vdays: (a) vertical profile of globally averaged temperature; (b) latitudinal profiles of temperature (zonal and temporal average) at roughly 50, 60 and 70 km altitude. The dashed lines are from the simulation started from rest, after 300 Vd.

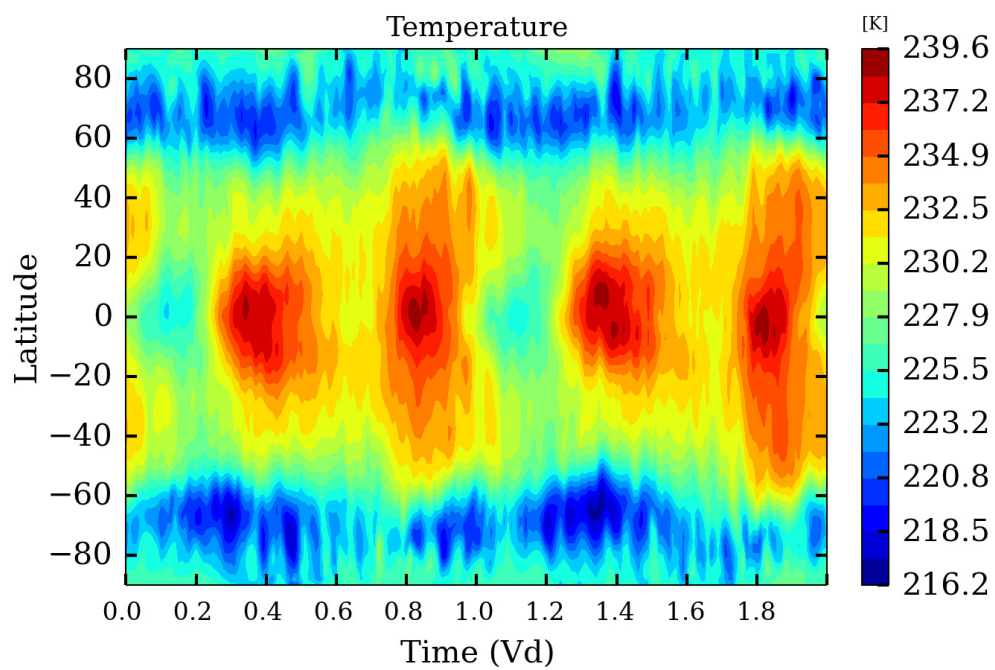


Figure 2: Temporal variations of the temperature field at pressure  $p=2\times 10^3$  Pa (near 70 km altitude, cloud top), and longitude 0, for the last 2 Venus days of the simulation.

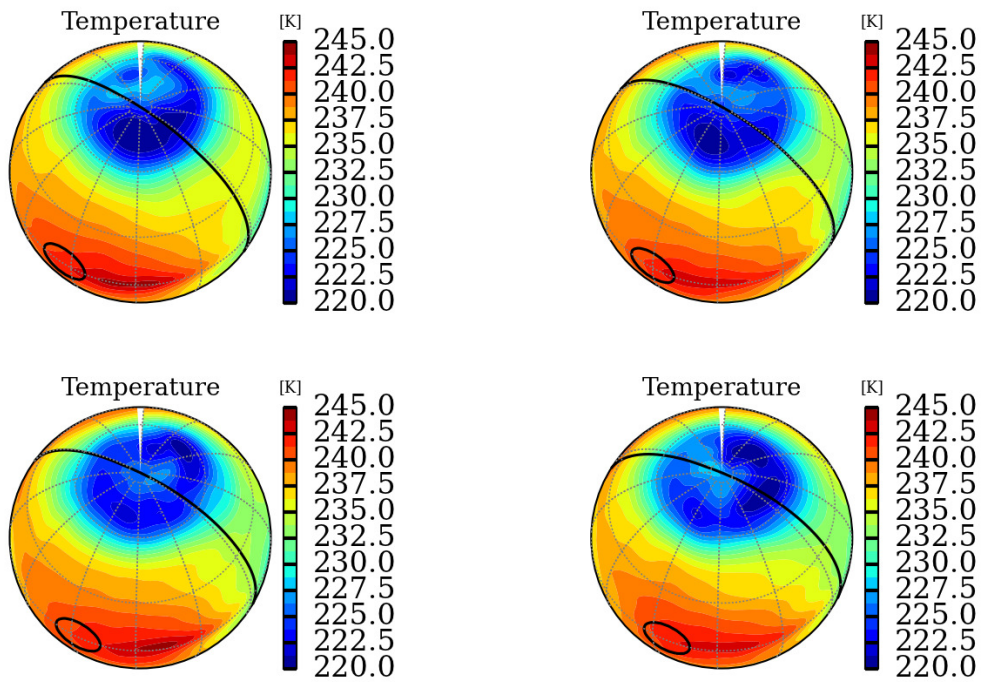


Figure 3: Temperature fields at pressure  $p=3 \times 10^3$  Pa ( $\sim 67$  km altitude) in the northern polar region. In each panel, the temperature field is averaged over  $1/100 Vd$  ( $1.17 E_d$ ), and the panels are separated by this time interval. The black contours show the sub-solar area and the terminator. The latitude and longitude divisions are  $30^\circ$ .

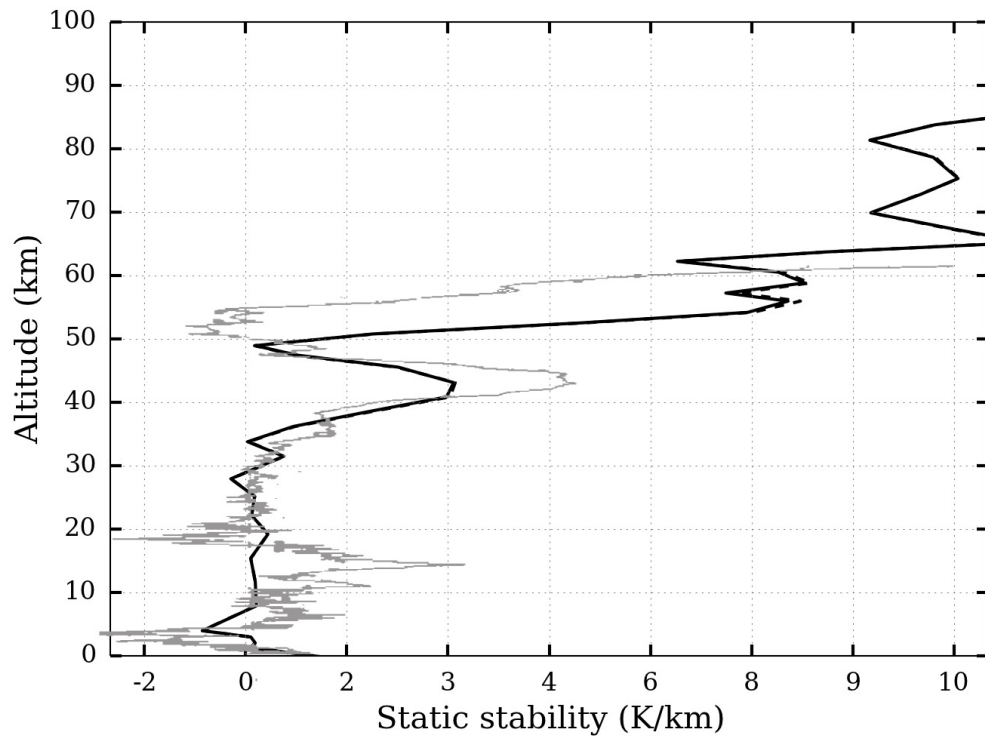


Figure 4: Vertical profile of globally averaged static stability obtained in the simulation started from superrotation, after 190 Vd, compared to profile retrieved from the Vega 2 entry probe dataset (adapted from Zasova et al., 2007), shown in gray. The dashed line is from the simulation started from rest, after 300 Vd.



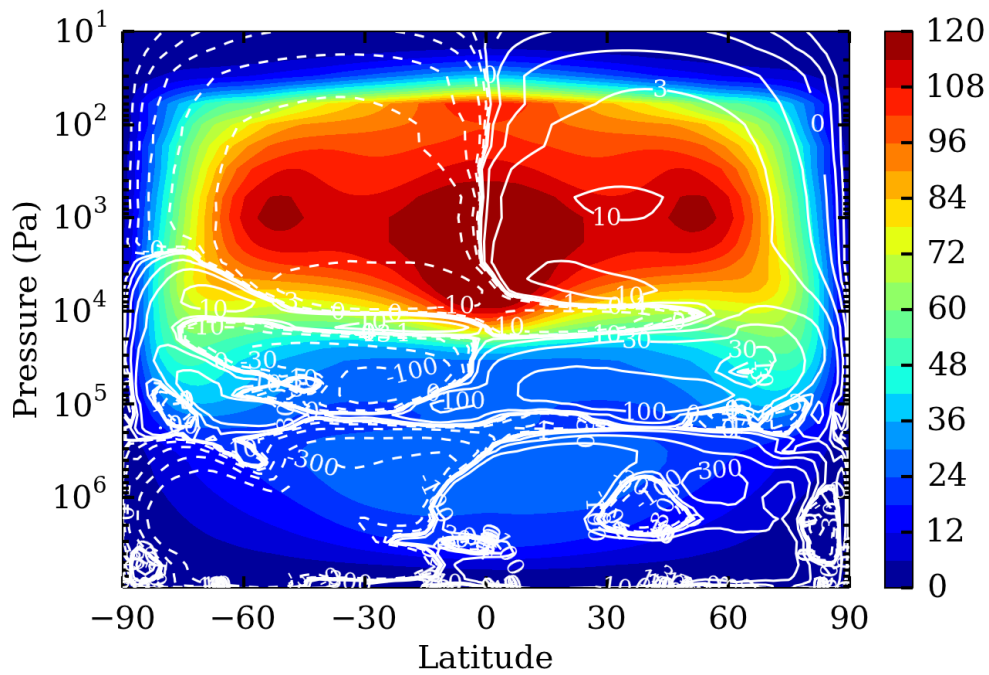


Figure 5: Distribution of the mean zonal wind field (white contours show the mean meridional stream function, in units of  $10^9$  kg/s) obtained in the simulation started from super-rotation, after 190 Vdays.

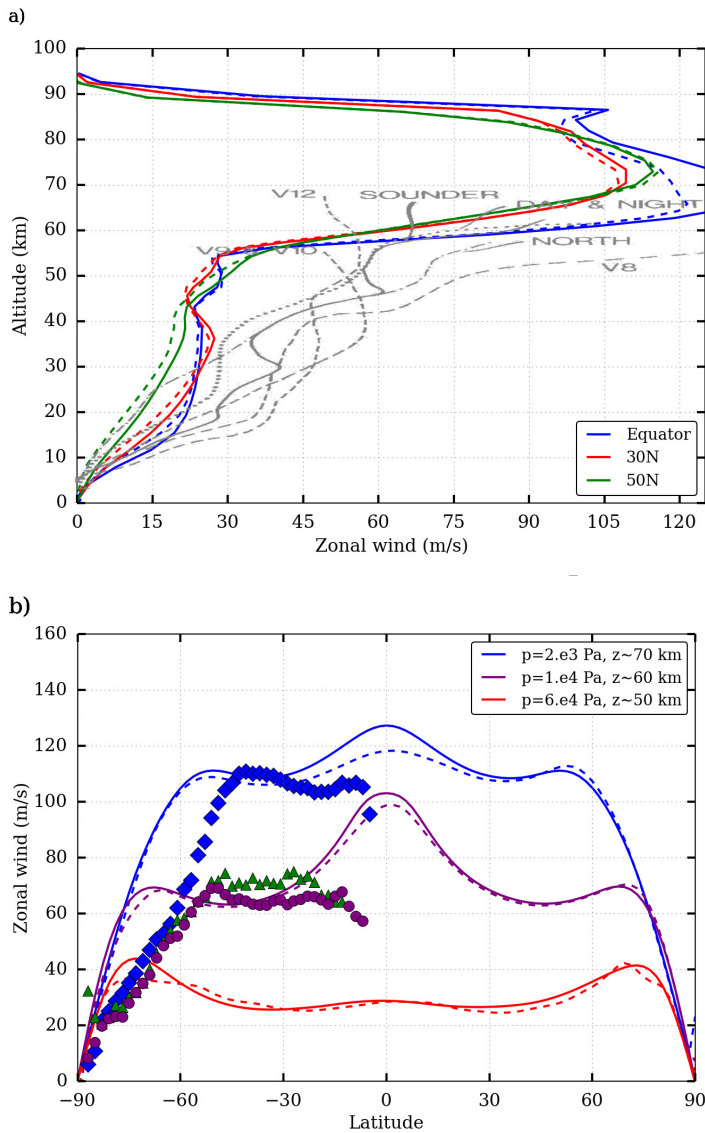


Figure 6: Zonal and temporal averaged profiles of the zonal wind: (a) vertical profiles at three different latitudes, compared to observed profiles from Venera and Pioneer Venus probes (gray, adapted from Schubert, 1983); (b) latitudinal profiles at roughly 50, 60 and 70 km altitude, compared to averaged cloud-tracking zonal wind profiles obtained with VIRTIS-M images at UV (blue diamonds), visible (green triangles) and near-IR (magenta circles) wavelengths. They correspond to altitudes 66-72 km for UV spectral range, and a few kilometers below that level for visible/near-IR wavelengths (adapted from Hueso et al., 2015). The dashed lines are from the simulation started from rest, after 300 Vd.

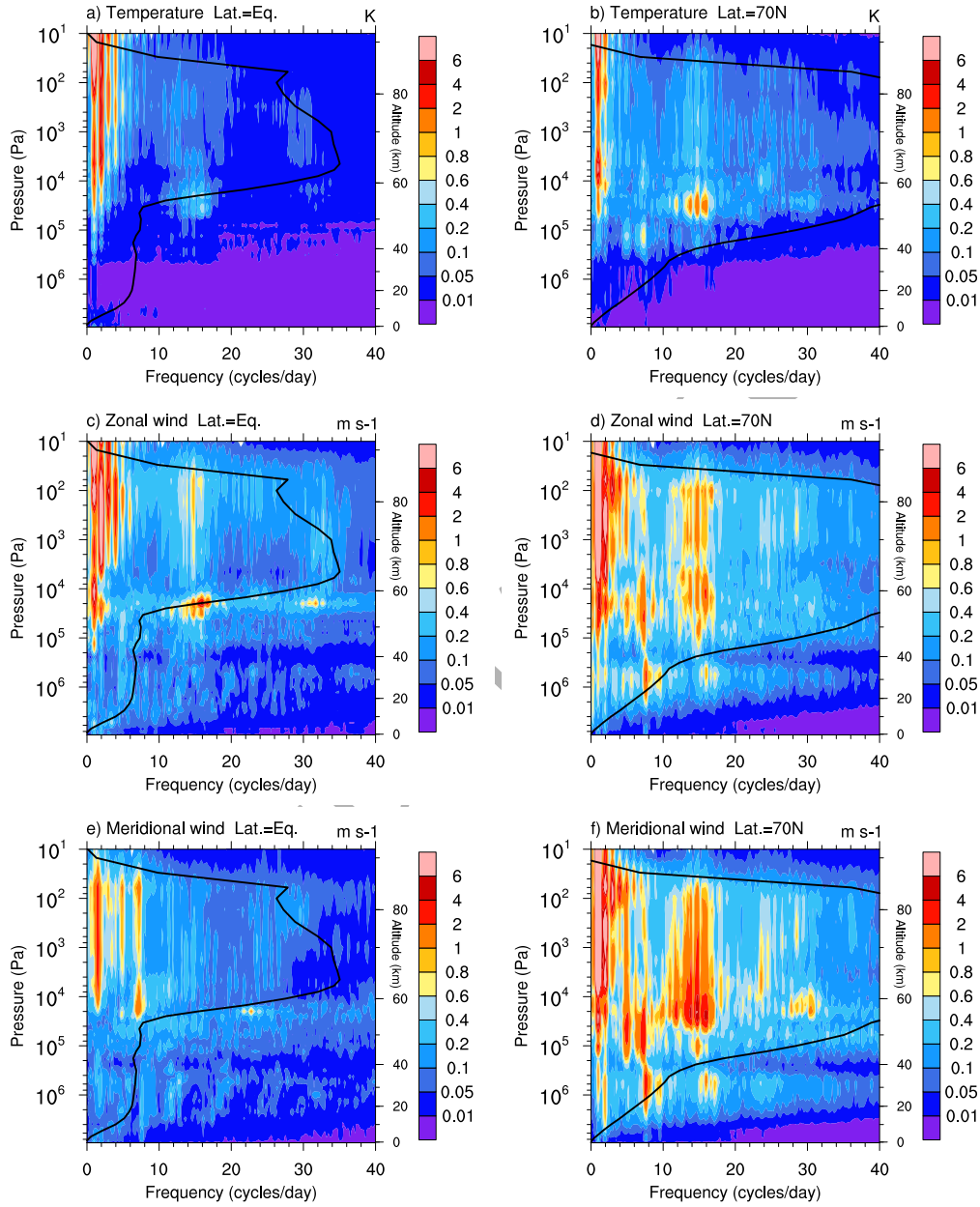


Figure 7: Frequency analysis of the temperature, zonal and meridional wind time series as a function of pressure, at the equator and 70°N. The solid black line indicates the frequency corresponding to the zonal and temporal average of the zonal wind speed.

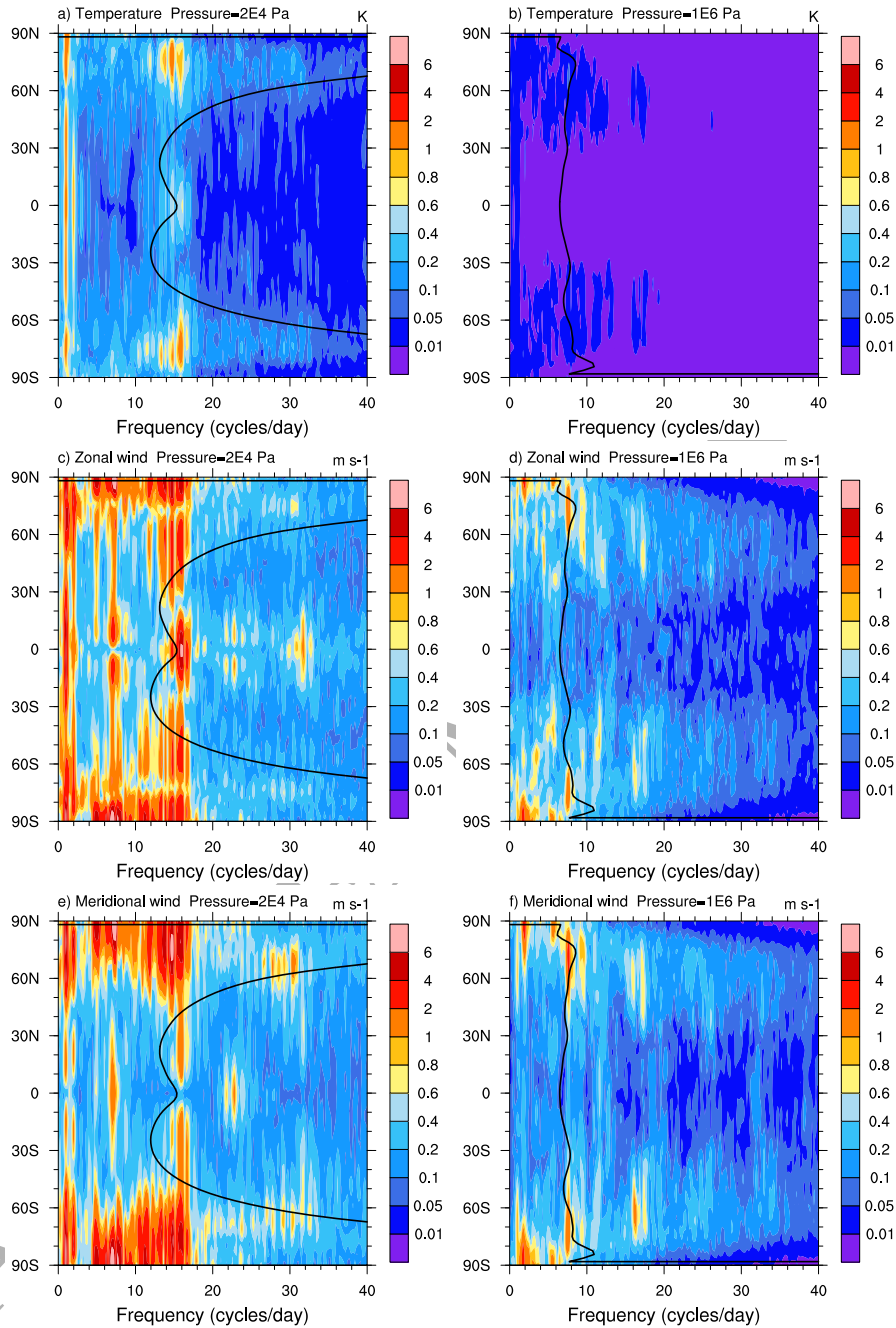


Figure 8: Frequency analysis of the temperature, zonal and meridional wind time series as a function of latitude, at pressure levels  $2 \times 10^4$  Pa and  $1 \times 10^6$  Pa. The solid black line indicates the frequency corresponding to the zonal and temporal average of the zonal wind speed.

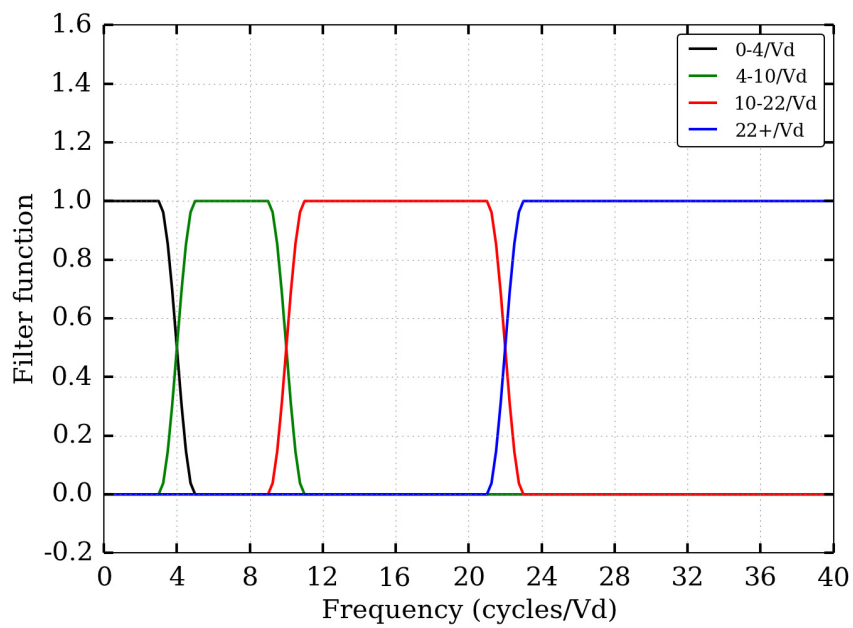


Figure 9: Filter functions applied to the FFT spectra to separate the different waves present in the temperature and wind fields.

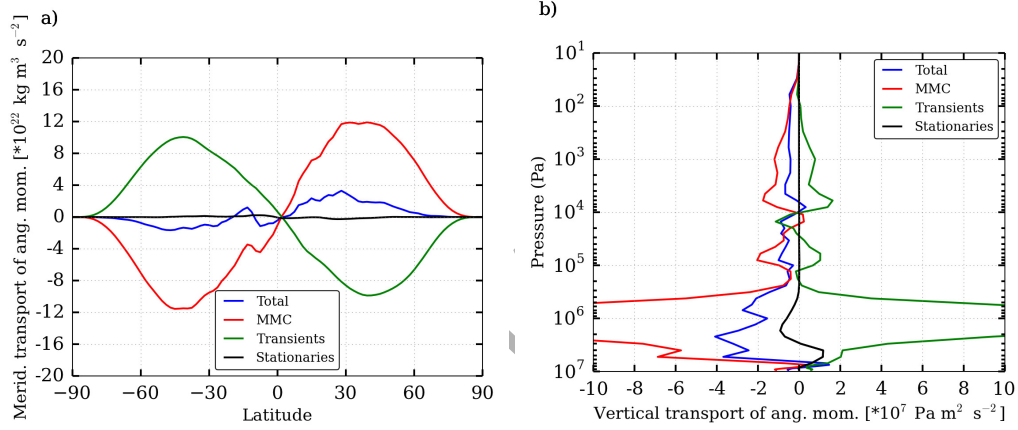


Figure 10: Meridional (a) and vertical (b) transport of angular momentum, separating MMC contribution from transients and stationaries. The net horizontal transport is compensated by exchanges with the solid surface. However, the net vertical transport should be zero and the residual is indicative of the numerical inaccuracies discussed at the end of Section 2.1.

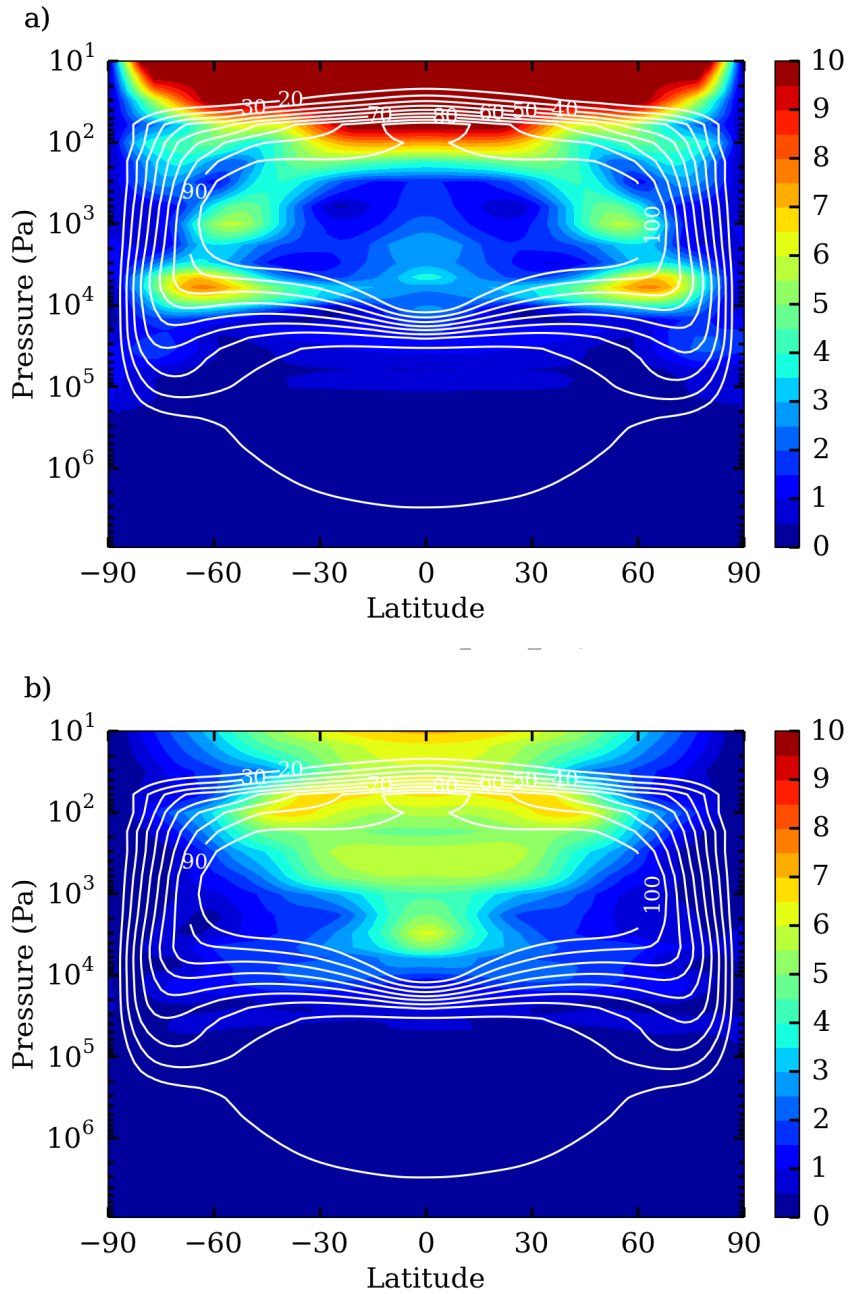


Figure 11: Amplitude of the FFT spectrum of the temperature at the frequency (a)  $1/V_d$ , i.e. diurnal tide and (b)  $2/V_d$ , i.e. semi-diurnal tide. The white contours show the mean zonal wind field (in m/s).

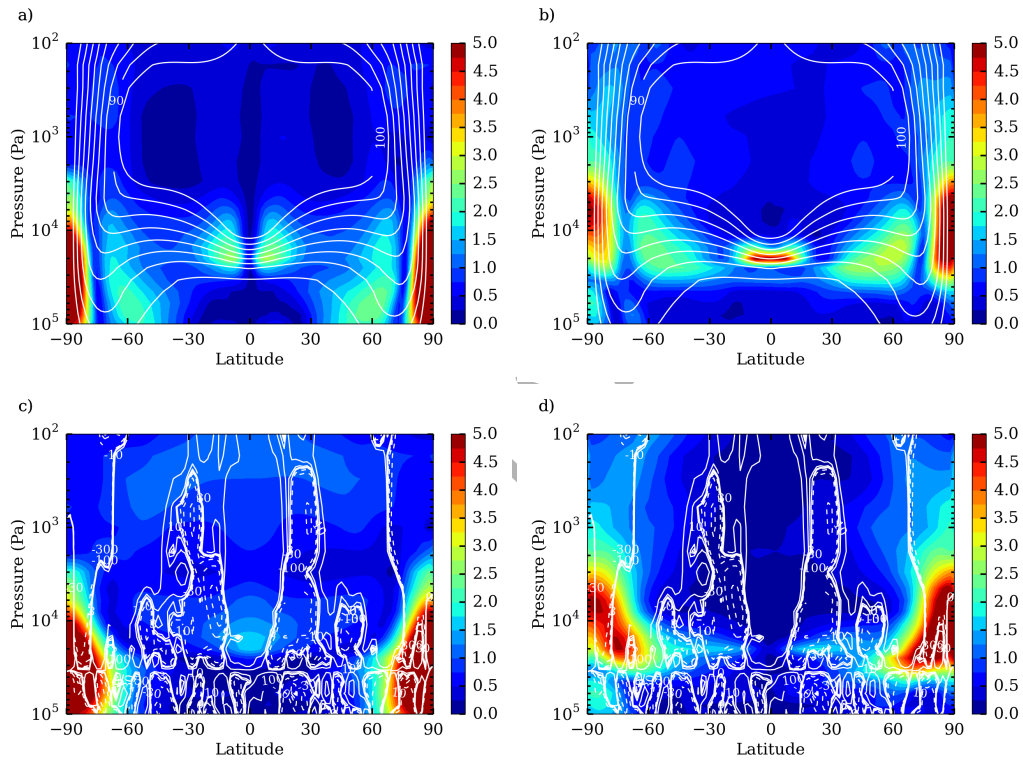


Figure 12: Amplitude of the FFT spectrum of (a,b) the zonal and (c,d) meridional winds, at the frequency  $7.25/Vd$  (left) and  $16/Vd$  (right). The white contours show (a,b) the mean zonal wind field (in m/s), (c,d)  $d\bar{q}/d\phi$  (in  $\text{m s}^{-1}$ ).



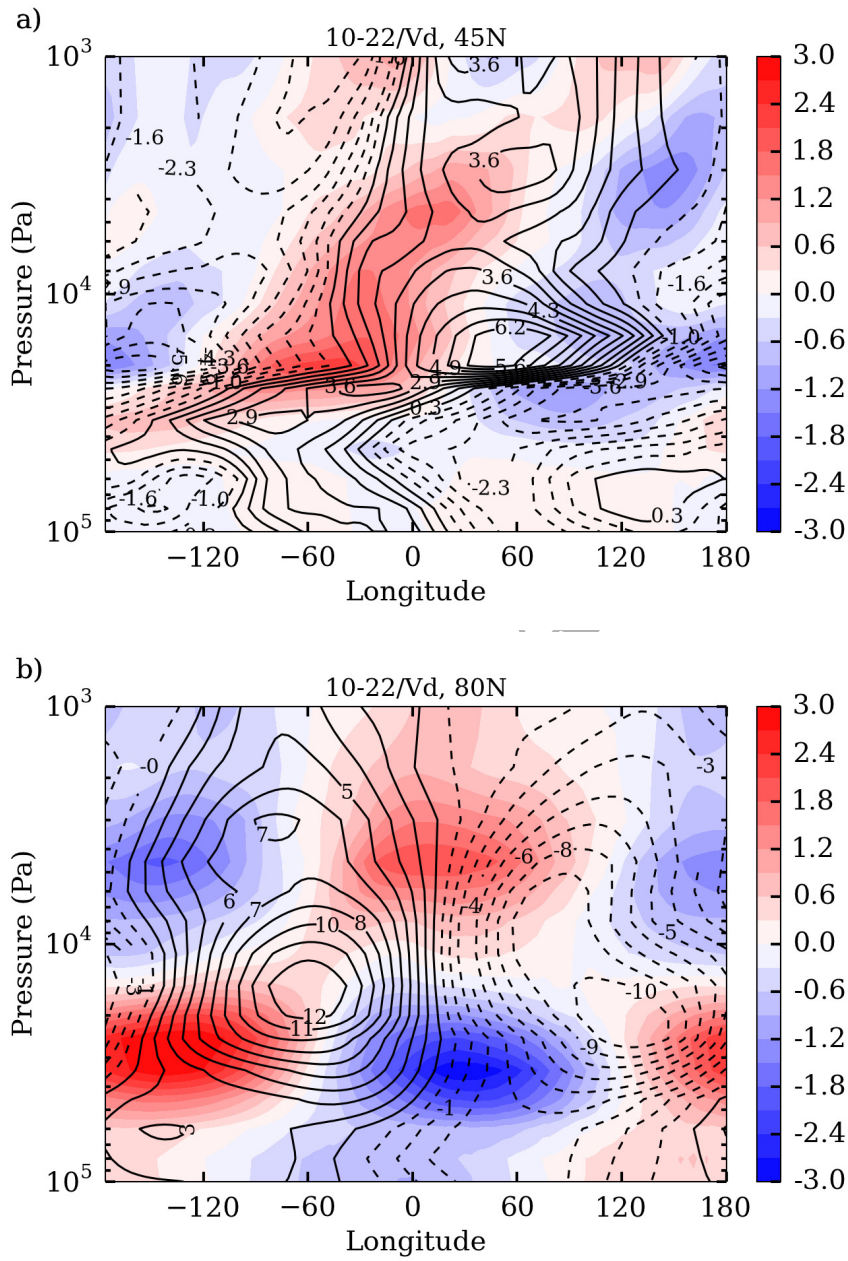


Figure 13: Temperature (colors, in K) and meridional wind (contours, in m/s) perturbations filtered in the frequency band  $[10-22]/Vd$ , at (a)  $45^\circ\text{N}$  (baroclinic structures) and (b)  $80^\circ\text{N}$  (barotropic structures). Note that the zonal wind is moving westward. These perturbations are shown at a fixed point in <sup>45</sup>time (without averaging).

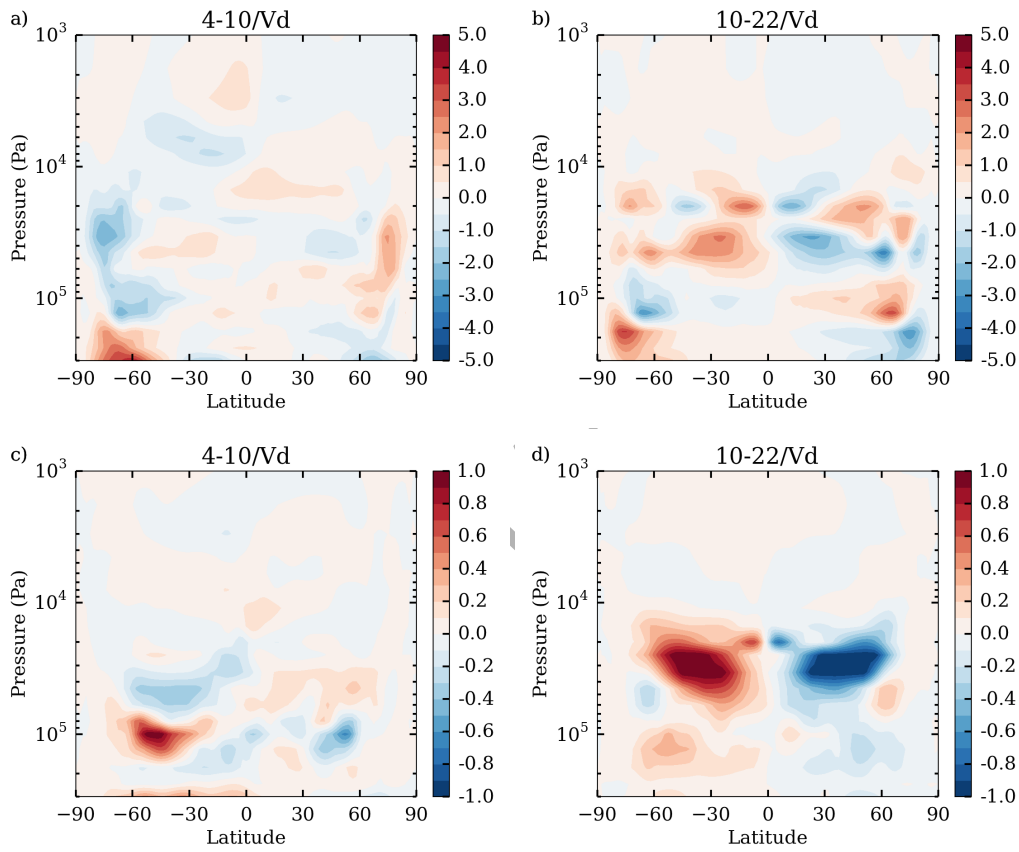


Figure 14: Horizontal transport of heat (upper row) and angular momentum (lower row) computed using zonal and meridional fields filtered in the frequency bands  $[04-10]/Vd$  (left) and  $[10-22]/Vd$  (right). Units are  $1 \times 10^{16} \text{ J m s}^{-1}$  for heat transport and  $1 \times 10^{21} \text{ kg m}^3 \text{ s}^{-2}$  for angular momentum transport.

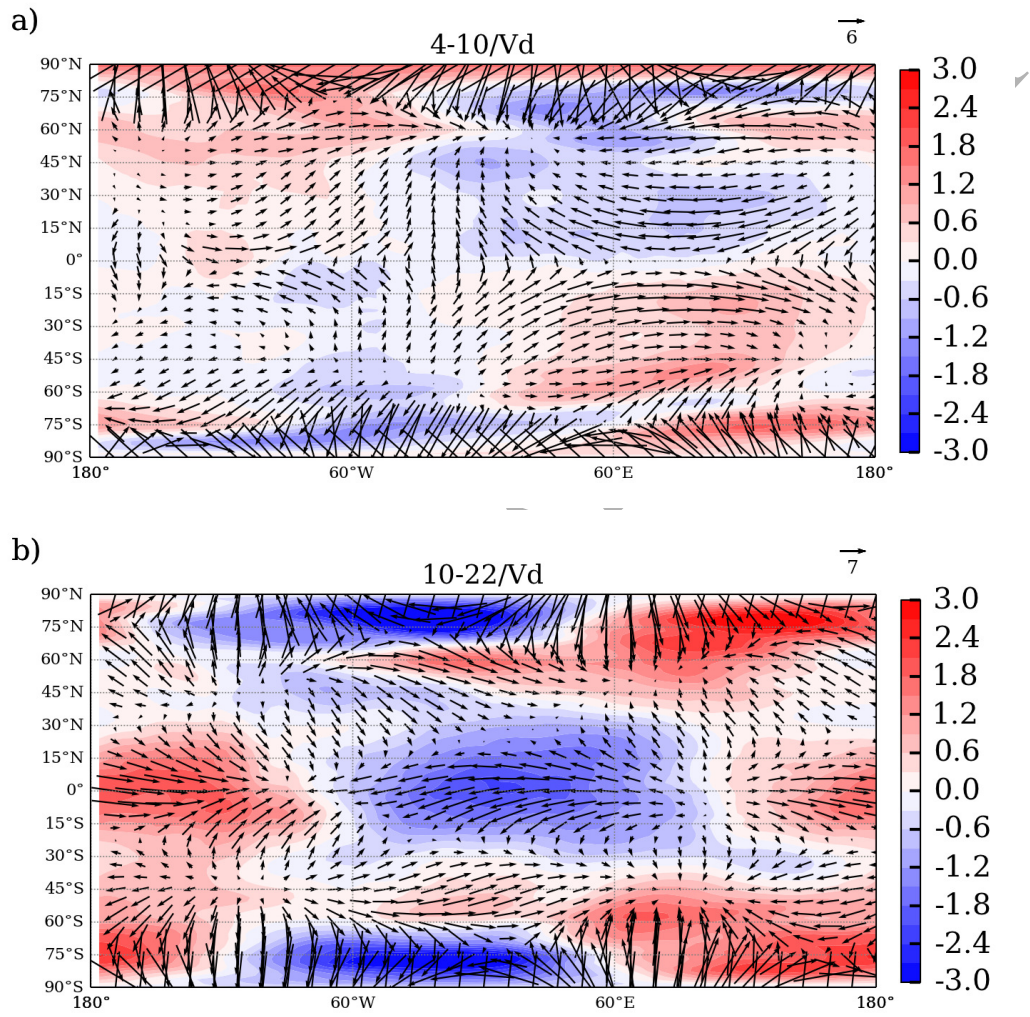


Figure 15: Temperature (colors, in K) and horizontal wind (vectors, in m/s according to rule) perturbations filtered in the frequency bands (a)  $[04-10]/Vd$  and (b)  $[10-22]/Vd$ , at  $2 \times 10^4$  Pa. These perturbations are shown at a fixed point in time (without averaging).

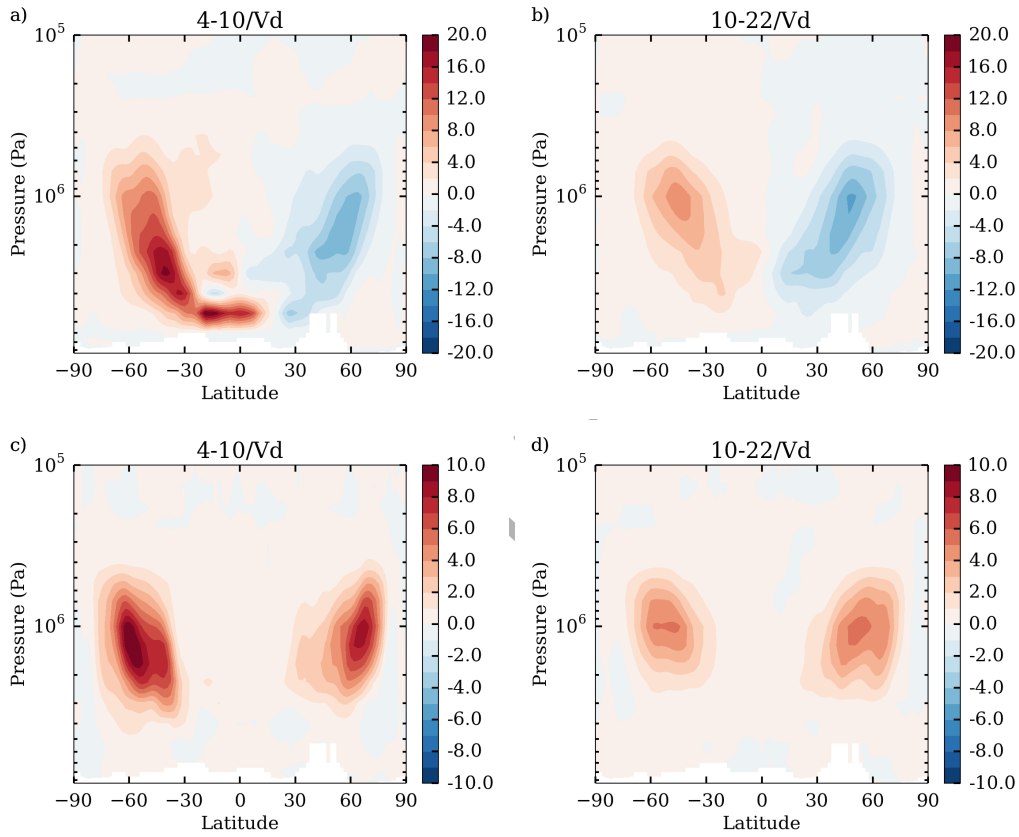


Figure 16: Meridional (top) and vertical (bottom) transport of angular momentum below the clouds computed using zonal and meridional (a,b) or vertical (c,d) wind fields filtered in the frequency bands [04-10]/Vd (left) and [10-22]/Vd (right). Units are  $1 \times 10^{21} \text{ kg m}^3 \text{ s}^{-2}$  for panels a and b and  $1 \times 10^6 \text{ Pa m}^2 \text{ s}^{-2}$  for panels c and d.

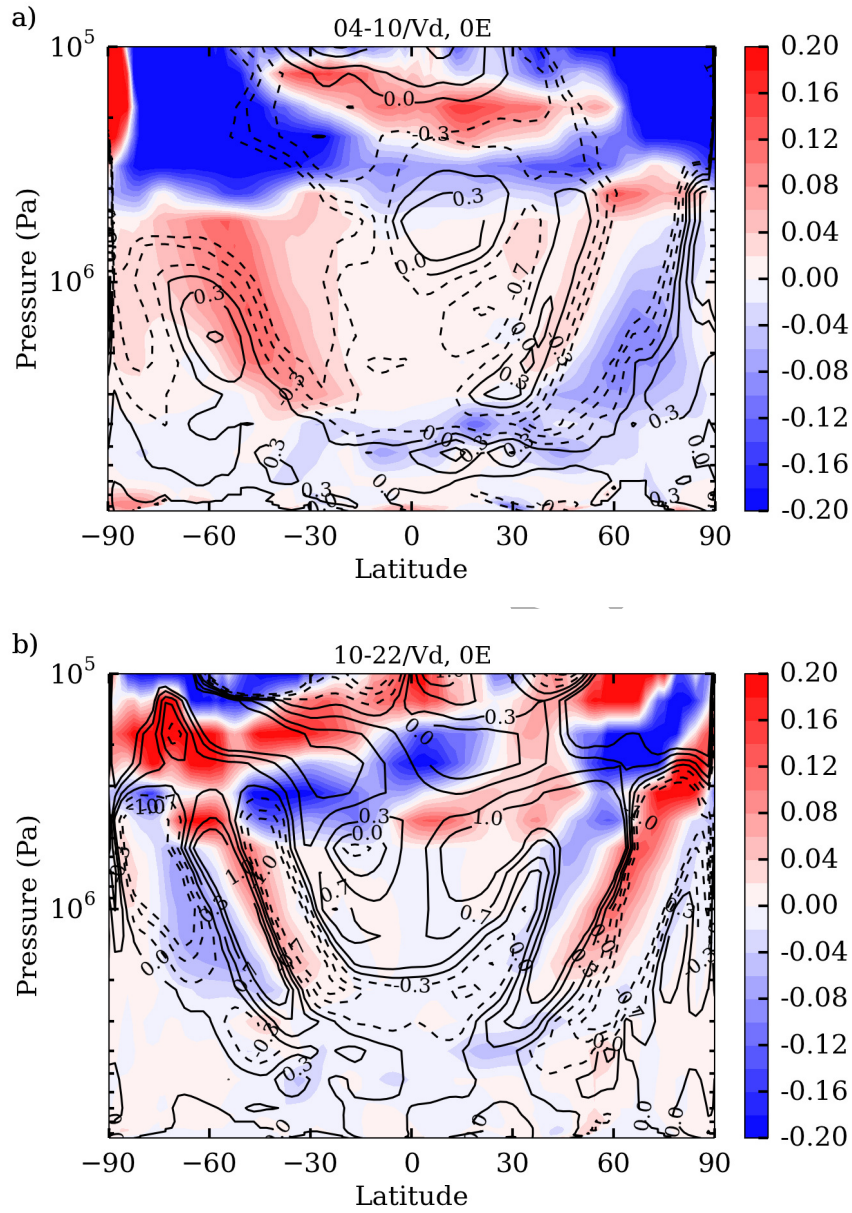


Figure 17: Temperature (colors, in K) and meridional wind (contours, in m/s) perturbations filtered in the frequency bands (a) [04-10]/Vd and (b) [10-22]/Vd, at  $0^\circ$  longitude. These perturbations are shown at a fixed point in time (without averaging).



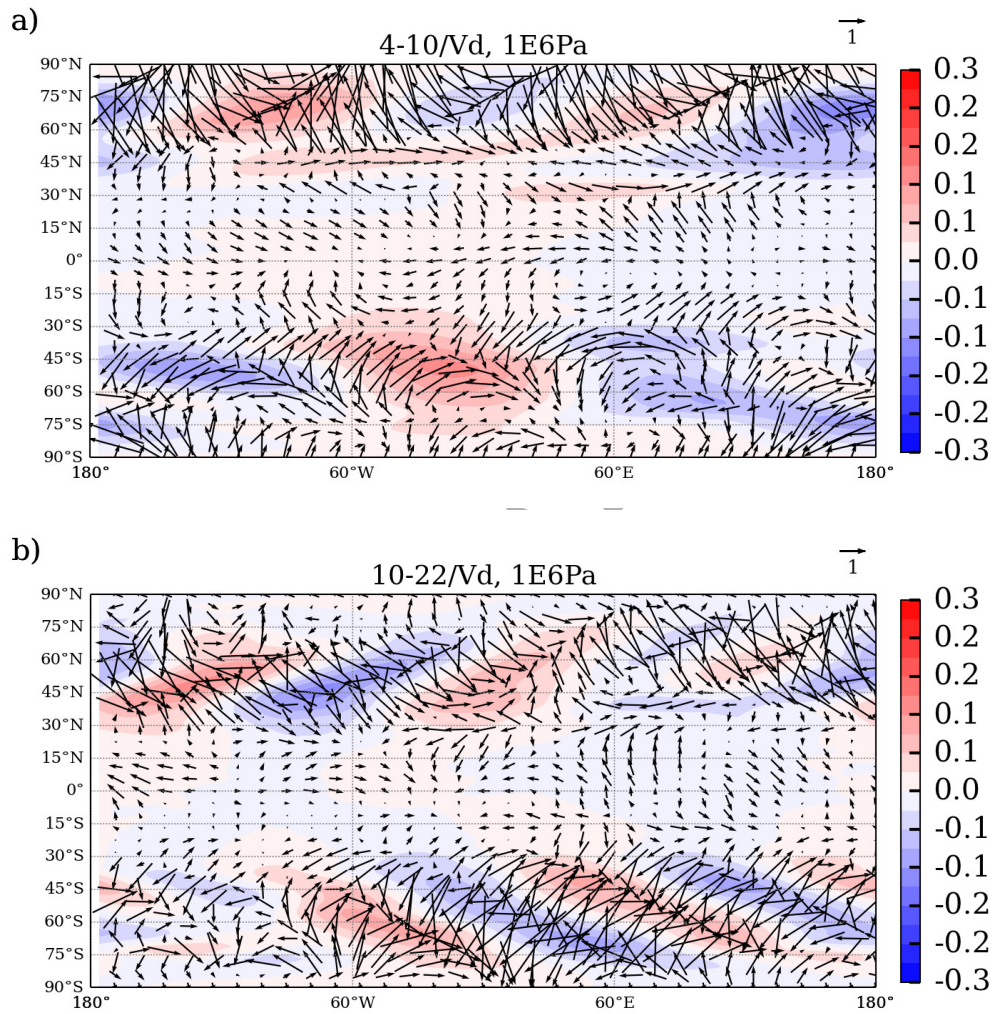


Figure 18: Temperature (colors, in K) and horizontal wind (vectors, in m/s according to rule) perturbations filtered in the frequency bands (a)  $[04-10]/Vd$  and (b)  $[10-22]/Vd$ , at  $1 \times 10^6$  Pa. These perturbations are shown at a fixed point in time (without averaging).

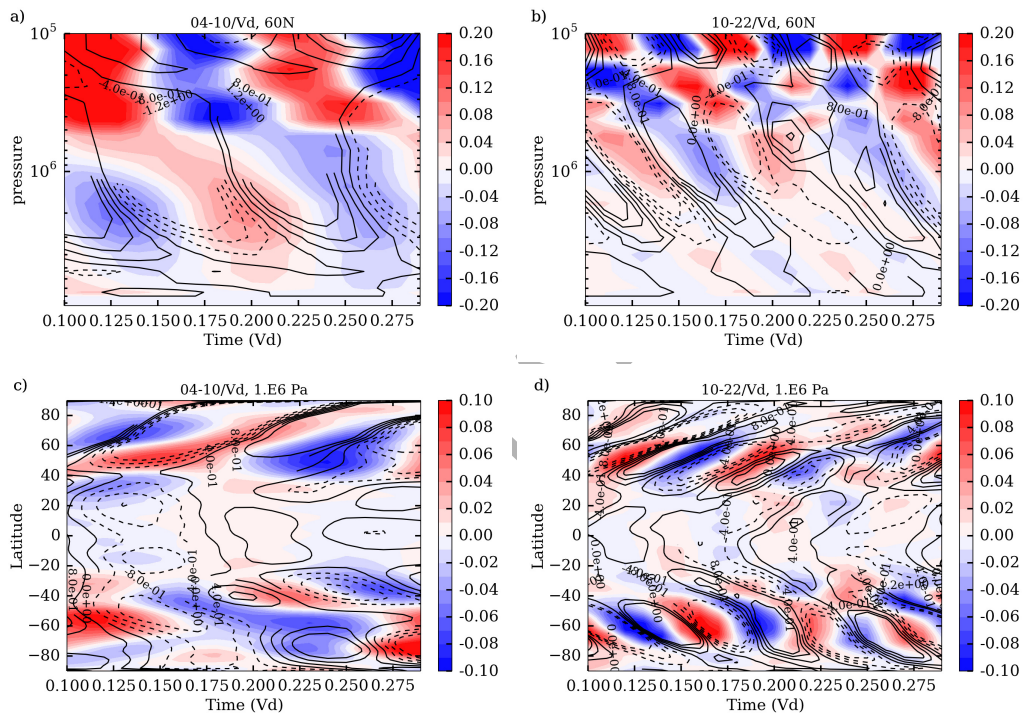


Figure 19: Temporal variations of temperature (colors, in K) and meridional wind (contours, in m/s) perturbations filtered in the frequency bands  $[04-10]/Vd$  (left column) and  $[10-22]/Vd$  (right column), at  $0^\circ$  longitude,  $60^\circ N$  latitude (top) and  $1 \times 10^6$  Pa (bottom).