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Micellization of dodecyltrimethylammonium bromide in water-dimethylsulfoxide mixtures: a multi-length scale approach in a model system

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ABSTRACT:

The micellization in mixed solvent was studied using conductimetry, density measurements (molar volumes) and small angle neutron scattering (SANS) to explore dodecyltrimethylammonium bromide (DTABr) micelle formation throughout the entire composition range of water-dimethylsulfoxide (DMSO) mixtures. As the concentration of DMSO was increased in the mixture, the critical micelle concentration (CMC) increased, the aggregation number decreased and the ionization degree increased, until no aggregates could be detected any more for DMSO molar fraction higher than 0.51. The results were consistent with the presence of globular micelles interacting via a coulombic potential. The experimental CMC values and aggregation numbers were successfully reconciled with a molecular thermodynamic model describing the micellization process in solvent mixtures (Nagarajan et al., Langmuir, 16;5242, 2000). The structural and thermodynamic characterization of the micelles agreed with the prediction of a dissymmetric solvation of the surfactant entity: the hydrocarbon chain was surrounded only by DMSO while the polar head was surrounded only by water. The decrease of the ionization degree was due to the condensation of the counterions and was definitely linked to the geometrical characteristics of the aggregates and by no means to the CMC or salinity. This multi-technique study provides new insight into the role of solvation in micellization and the reason for the decrease in ionization degree, emphasizing the dissymmetric solvation of the chain by DMSO and the head by water. This is the first time that, for a given surfactant in solvent mixtures, micellization is described using combined analysis from molecular to macroscopic scale.

KEYWORDS: dodecyltrimethylammonium bromide, water-DMSO mixtures, micellization, SANS, conductimetry, molar volume, solvation
INTRODUCTION

The existence of micelles in organic or hydro-organic solvents has drawn considerable attention over the past decades [1-26] for their fundamental and industrial applications, and there is still much interest in the nature of the micellization mechanism in polar organic solvent and their aqueous mixtures. In the delicate balance of forces that rules micellization, a solvent’s capability to enable micellization is said to relies on its cohesive energy density, which encompasses all of the solvent’s intermolecular forces (comprising H-bonds) [25]. It is remarkable that this parameter be sufficient and does not request any information on the surfactants specificity. For instance, in the case of ionic surfactants, the electrostatic interactions between surfactants heads indeed plays a particularly important role in the formation of the aggregates. We address the question of the solvent key parameter for micellization by studying a cationic surfactant in water-DMSO mixtures. Continuously changing the solvent’s quality by mixing two solvents with different properties provides an opportunity to finely explore the dependence of the micellization mechanism upon the surrounding medium. Moreover, many properties of water-DMSO mixtures present an extremum at the molar fraction $x_{\text{DMSO}} = 0.33$, but the existence of an extremum of micellization for the same solvent composition is not obvious.

Among the aprotic solvents able to promote micellization, DMSO is indeed controversial. DMSO is a polar solvent completely miscible with water and water-DMSO mixtures have been studied extensively, from experimental points of view (e.g., dielectric constants, viscosity, surface tension, partial molar volumes, densities, heat capacities, etc.) and theoretically [27-34]. The molar fraction of DMSO, $x_{\text{DMSO}} = 0.33$ was found to be a threshold for many properties such as viscosity, excess enthalpy of mixing, and the chemical shift of protons[31], due to the formation of the complex containing 1 DMSO : 2 H$_2$O[30]. By varying the composition of water-DMSO mixtures, the solutions range between a highly structured solvent with many H-bonds (water), to a solvent with no H-bonds (DMSO). Micellization has been studied in such mixtures and the composition $x_{\text{DMSO}} = 0.33$ was also found to be a limit after which no micelles form, but these results are somewhat contradictory depending on the techniques and surfactants explored [13-22]. The main reason for this situation is that monotechnique approaches, which are the
most common, cannot report of the various aspects of micellization and can only render a partial view of
the phenomenon. The question is thus still open whether micellization also presents an extremum or a
threshold at this DMSO composition. For this purpose, we established a set of data about the
micellization of dodecyltrimethylammonium bromide (DTABr), using several complementary
techniques to provide a description of the micelles from several points of views.

Although DTABr has been well characterized in water by various techniques including surface
tension, X-rays, conductivity[35,36], small angle neutron scattering (SANS) [37-39], light scattering
[40] or combinations of several techniques[35,41], little is known about its behavior in a mixed solvent,
since homologues of DTABr with longer chains are studied more frequently. The scope of this study was
first to link the main parameters of the micelles (i.e., critical micelle concentration [CMC], aggregation
number and ionization degree) to the relevant solvent characteristics (i.e., cohesive energy density,
surface tension and dielectric constant) and secondly, to determine some of the details of the
micellization process at the molecular level and describe the solvation phenomenon in water-DMSO
mixtures having compositions below and above $x_{\text{DMSO}} = 0.33$. The onset of micelle formation was
determined by conductimetry and volumetry, whereas the size and effective charge of the micelles were
obtained from SANS. Molecular thermodynamics according to the model proposed by Nagarajan et
al.[23] was used to calculate the CMC and clarify the forces driving micellization. This model is widely
cited but seldom tested and, to our knowledge, it has not been validated on solvents other than alcohols
mixed with water (e.g., ethyleneglycol[23] and ethanol[24]). In parallel, the changes of the DTABr
environment were explored through density measurements, which allowed us to determine partial molar
volume values and provided insight to the molecular organization of the DTABr environment. This
multi-view approach at different length scales rendered valuable information that ultimately improved
our understanding of the solvent effects on the self-assembly of amphiphilic compounds.

MATERIALS AND METHODS

Products
DTABr obtained from Acros Organics was recrystallized twice from acetone-ether before use. DMSO obtained from SDS-Carlo Erba was distilled under vacuum and used rapidly afterward. Tetraethylammonium bromide was obtained from Janssen Chimica and used as received. Water was ultrapure quality (18 MΩ-cm).

Solvents (i.e., mixtures of water and DMSO) were prepared by first adding the desired amount of DMSO to a volumetric flask. Almost all the necessary amount of water was added immediately and the flask was left at room temperature for 24 hours before adjusting the final volume with water. Since the mixture of DMSO and water is exothermic, this procedure allowed spontaneous degassing, cooling down and changes in the volume of the solution to take place before the final solution was obtained. The solvents named \( y \) \% DMSO thus contained a volume \( y \) of pure DMSO mixed with water in a total volume of 100. The notation \( x_{\text{DMSO}} \) stands for the final DMSO molar fraction. All DTABr solutions in the solvents were formulated by weight and, if needed, the concentrations were calculated by their densities.

Conductimetry

Conductimetry measurements were made at 298.0 ± 0.1 K, with a Philips PM6303 conductimeter operating at 1000 Hz and calibrated with KCl. Aliquots of DTABr stock solutions (between 0.4 and 0.6 mol kg\(^{-1}\)) in the solvent were added to a sample volume of the same solvent, and the conductance was recorded after the signal stabilized (2–5 min). In the solvent of composition \( x_{\text{DMSO}} = 0.50 \), the stock solution was 0.21 mol kg\(^{-1}\) to avoid crystallization of DTABr at higher concentrations. The curves were drawn in two runs: one in which the stock solution samples were diluted by adding solvent and the other in which the stock solution samples were added to samples of solvent.

Densities and molecular volume determination

Densities were measured at 298.15 K on an Anton Paar DMA 5000 electronic densitometer. Temperature accuracy was ± 0.01 K. All solutions were prepared by weighing. The precision of the
density values was $\pm (5 \times 10^{-6})$ kg dm$^{-3}$. For calibration, the density of pure water at 298.15 K was taken as 0.997043 kg dm$^{-3}$.

The apparent molar volumes $V^{\text{app}}$ for DTABr in different solvents were calculated from the experimental density values of solutions using the following equation[42]:

$$V^{\text{app}} = \frac{1}{m} \left( \frac{1}{\rho} - \frac{1}{\rho^o} \right) + \frac{M}{\rho}$$  \hspace{1cm} (1)

where $m$ is the molality of a solution of DTABr in the solvent, $M$ the molecular weight of DTABr, and $\rho$ and $\rho^o$ are the densities of the solution and the solvent, respectively.

**Phase diagram**

The transitions between a clear solution and a precipitate were determined by visual inspection of the DTABr solutions in water-DMSO mixtures. To avoid supersaturation effects, all samples were first placed at 277 K until crystals formed. They were then left at ambient temperature (~295 K) for one week before being analyzed. The whole procedure was repeated twice on the same samples.

**Small angle neutron scattering (SANS)**

We used D$_2$O and deuterated DMSO to enhance the scattering contrast of the micelles/solvent and to minimize the incoherent hydrogen background. Experiments were performed at the Laboratoire Léon Brillouin (LLB), Saclay (France) using the PAXE spectrometer of the Orphée reactor. Quartz optical cells with a 1 mm path length were mounted on a thermostated brass block at a temperature of 298 ± 0.5 K. The overall angular range ($0.011 < q$ (Å$^{-1}$) $< 0.46$) was accessed with three configurations: $\lambda = 4.5$ Å, $D = 105$ cm; $\lambda = 6$ Å, $D = 254.7$ cm; and $\lambda = 10$ Å, $D = 505$ cm. The acquisition time was between 30 and 60 minutes for each sample, depending on the configuration used. Neutron detection and counting was achieved with a built-in two-dimensional sensitive detector composed of $64 \times 64$ cells. Standard LLB data treatments were used for radial averaging and correction for the empty cells and electronic background.
The samples were prepared by weight and the concentrations are listed in Table 1. For the solvents containing the higher DMSO concentrations, the DTABr concentrations were chosen to avoid precipitation (see phase diagram section).

<table>
<thead>
<tr>
<th>solvent composition (x_{\text{DMSO\textsubscript{d6}}} )</th>
<th>0</th>
<th>0.14</th>
<th>0.26</th>
<th>0.37</th>
<th>0.51</th>
<th>0.67</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\rho_{\text{N}} ; \text{(cm}^{-2}\text{)} )</td>
<td>(6.34 \times 10^{10})</td>
<td>(5.92 \times 10^{10})</td>
<td>(5.72 \times 10^{10})</td>
<td>(5.60 \times 10^{10})</td>
<td>(5.50 \times 10^{10})</td>
<td>(5.40 \times 10^{10})</td>
</tr>
<tr>
<td>(\varepsilon )</td>
<td>78</td>
<td>76</td>
<td>72</td>
<td>69</td>
<td>63</td>
<td>57</td>
</tr>
<tr>
<td>([\text{DTABr}]_{\text{tot}} ; \text{(mol L}^{-1}\text{)} )</td>
<td>0.46</td>
<td>0.50</td>
<td>0.51</td>
<td>0.28</td>
<td>0.20</td>
<td>0.22</td>
</tr>
</tbody>
</table>

Table 1: Scattering length densities \(\rho_{\text{N}}\) (see text) and dielectric constants \(\varepsilon\) (from [32]) of the solvents used for SANS. \([\text{DTABr}]_{\text{tot}}\) is the total concentration of DTABr used for SANS in the corresponding solvent.

**Model for the adjustment of SANS spectra.**

For the micelle model, we used anisotropic particles with an ellipsoid shape, interacting with a spherical potential. Using the decoupling approximation, the absolute intensity scattered by a solution of such interacting objects can be written as [43,44]:

\[
I(q) = C_{\text{micelles}} (\Delta \rho_v)^2 V f^2(q) \overline{f^2(q) + f(q)^2 (S(q) - 1)}
\]

(2)

where \(q\) is the scattering vector, \(C_{\text{micelles}}\) is the concentration of micelles, \(\Delta \rho_v\) is the contrast between the objects and the solvent, \(V\) is the volume of one micelle, \(f(q)\) is the amplitude of the form factor and \(S(q)\) is the structure factor. Assuming monodispersed ellipsoidal particles, the bars represent the average on the solid angle between the anisotropic particle and the \(q\) vector. For the particles concerned in this study (i.e., only with a small anisotropy), it was assumed that the interactions were independent of
particle orientation and dependent only on the average size of the particles. The interactions are described using a hard sphere potential of radius \( R \) and a classical DLVO repulsive part (equation (3)).

\[
v(r) = \begin{cases} 
+\infty & r < 2R \\
\kappa \left( \frac{Z_{\text{eff}}^2 L_B}{r} \frac{\exp[-\kappa(r - 2R)]}{(1 + \kappa R)^2} \right) & r > 2R
\end{cases}
\]

where \( Z_{\text{eff}} \) is the effective charge of the micelle, \( L_B \) is the Bjerrum length, \( \kappa = (8 \pi L_B I) \) is the screening constant, which is related to the ionic strength \( I = N_A (\text{CMC} + 1/2 C_{\text{micelles}} Z_{\text{eff}}) \), in the absence of added salt, and \( N_A \) is the Avogadro number.

Using the above potential, the pair correlation function \( g(r) \) and then the structure factor are calculated by iterative resolution, using the Ornstein-Zernike (OZ) equation with the hypernetted chains (HNC) equation[45]. For the systems interacting via long-range electrostatic potentials, the HNC closure relation is valid and requires no further refinements. We used a program kindly provided by Luc Belloni to calculate the scattered intensities; details are reported as Supplementary Material.

**Fitting procedure**

The adjustable parameters of the model are: \( R \) (the radius of the interacting spheres); \( Z_{\text{eff}} \) (the effective charge of the micelle); \( C_{\text{micelles}} \) (the concentration of micelles); and \( R_1 \) (the semi-biaxis of the ellipsoid). The ionic strength \( I \) is calculated as described for equation 3, and the semi-monoaxis \( R_2 \) of the ellipsoid is imposed so that the volumes of the ellipsoid \( (4\pi/3 R_1^2 R_2) \) and of the interacting spheres \( (4\pi/3 R^3) \) are equal. HNC calculations are the results of an iterative convergence that makes difficult the use of the weighed nonlinear least-squares fit of the spectra[41].

**Scattering length densities**

We chose a simple model with two scattering length densities, one for the micelle and one for the solvent. This model is valid in the case of DTABr in water[37]. Assuming the condensation fraction of
Br\(^-\) onto the micelles (1-\(\beta\)) is known by the conductivity experiments, one can calculate the mean scattering density \(\rho_N\) of a micelle as:

\[
\rho_N = \frac{b_{\text{DTA}} + (1-\beta)b_{\text{Br}}}{V_{\text{DTA}} + (1-\beta)V_{\text{Br}}}
\]  

(4)

with \(b_{\text{DTA}}\) and \(b_{\text{Br}}\) the scattering lengths of the DTA\(^+\) cations and the Br\(^-\) anions, respectively, and \(V_{\text{DTA}}\) and \(V_{\text{Br}}\) their respective volumes. The mean value\([46]\) of 31 \(\text{cm}^3\ \text{mol}^{-1}\) was used as the volume for Br\(^-\) throughout the entire solvent composition range. The volume of DTA\(^+\) was deduced by subtracting this value from that of the DTABr salt\([47]\) \((V_{\text{mic}} = 295 \ \text{cm}^3 \ \text{mol}^{-1})\). The scattering lengths for each atom were obtained from ref. \([48]\). The scattering length density of the micelles was virtually constant over the DMSO range studied and was \(-0.28 \times 10^{10} \ \text{cm}^{-2}\). The scattering length densities \(\rho_N\) for the water-DMSO solvents are reported in Table 1.

**Determination of the aggregation number \(N_{\text{ag}}\) and micellar ionization degree \(\beta\)**

The aggregation numbers can be determined in two ways:

\[
N_{\text{ag}} = V / V_{\text{mono}}
\]  

(5a)

or

\[
N_{\text{ag}} = (C_{\text{tot}} - \text{CMC}) / C_{\text{micelle}}
\]  

(5b)

with the volume of the micelle \(V = 4\pi/3 \ R^3\) and \(C_{\text{tot}}\) the total concentration of surfactant monomers. The first equation relies on a correct value for the volume of the monomer in the scattering micelle, \(V_{\text{mono}}\). We took the volume of DTA\(^+\), with the condensed counter-ion:

\[
V_{\text{mono}} = V_{\text{DTA}} + (1-\beta)V_{\text{Br}}
\]  

(6)

The second equation is largely dependent on the determination of \(C_{\text{tot}} - \text{CMC}\) (the concentration of monomers involved in micelles). In the same manner, the micellar ionization degree \(\beta = Z_{\text{eff}} / N_{\text{ag}}\) can be calculated using (5a) or (5b) for \(N_{\text{ag}}\).
RESULTS

Conductimetry

The conductivity curves for DMSO molar fractions of 0, 0.06, 0.14, 0.26, 0.35, and 0.50 are shown in Figure 1. Except for the compositions $x_{\text{DMSO}} = 0.35$ and 0.50, the conductivity curves consisted of three domains: two straight parts joined by a curved transition. As the concentration of DMSO increased, the curved junction became larger. This result indicated micellization occurred over a range of DTABr concentrations rather than at an abrupt threshold. The CMC is classically taken as the intersection of the two straight portions of the curve. However, the treatment for conductivity data of surfactants proposed by Carpena et al.[49] allows the CMC to be determined more precisely. The conductivity $K$ vs concentration $C$ is modeled with:

$$K(C) = K(0) + A_1 C + d(A_2 - A_1) \ln \left( \frac{1 + e^{(C - C^o)/d}}{1 + e^{-C^o/d}} \right)$$ (7)

$K(0)$ is the conductivity of the pure solvent, $A_1$ and $A_2$ are the slopes of the limiting straight lines linked by a transition whose position is controlled by $C^o$ and whose width is $d$. The CMC is taken as $C^o$. The values for $A_1$ and $A_2$, $C^o$ and $d$ are reported in Table 2. The conductivities in $x_{\text{DMSO}} = 0.35$ and 0.50 could not be fitted to this model and we only report the initial slope $A_1$ of the curve. The conductivity of DTABr was compared to the conductivity of a classical electrolyte with similar structure and no micellization properties (tetraethyl ammonium bromide, Et₄NBr) (Supplementary Material). Since DTABr and Et₄NBr exhibited similar non-linear conductivity responses, we concluded that no CMC existed for DTABr at $x_{\text{DMSO}} = 0.35$ and 0.50.

The decrease of the initial slope $A_1$ with the increase of DMSO content in the solvent might be due to enhanced ion pairing of DTABr in the mixed solvent or to an increase in the viscosity of the solvent. We verified that the plot of $A_1$ vs the reciprocal of the solvent viscosity $1/\eta$ [34] describes a linear curve defined by the following equation, with $\eta$ in cP:
\[ A_1 \, (\text{S cm}^2 \cdot \text{mol}^{-1}) = 88 \times 1/\eta - 5.6 \] with \( R^2 = 0.9944 \) \hspace{1cm} (8)

where \( R^2 \) is the determination coefficient (figure SM-3 in Supplementary Material). The linearity confirms that the decrease in molar conductivity due to the addition of DMSO is indeed attributable to viscosity only and that the addition of DMSO in the solvent does not favor ion pairing. In this case, though the exact thermodynamic treatment of these conductivity data is not obvious [50], the ionization degree \( \beta \) remaining on the micelle after counterion condensation can be approximated as \( A_2/A_1 \) (Table 2).

![Figure 1](image.png)

Figure 1: Conductivity data at 298 K (a) \( \Delta \): water; \( \square \): \( x_{\text{DMSO}} = 0.06 \) (20\%); \( \circ \): \( x_{\text{DMSO}} = 0.14 \) (40\%); (b) \( \mathcal{O} \): \( x_{\text{DMSO}} = 0.26 \) (60\%); \( \bullet \): \( x_{\text{DMSO}} = 0.35 \) (70\%); \( * \): \( x_{\text{DMSO}} = 0.50 \) (80\%). The straight lines correspond to the fit with equation (7) and the parameters listed in Table 2.

Using the conductivity data (CMC and \( \beta \)), and supposing large aggregation numbers, the molar free enthalpy of micellization, \( \Delta G_{\text{mic}} \), was calculated according to the following equation [51]:

\[ \Delta G_{\text{mic}} = (2-\beta) \, RT \ln \text{CMC} \] \hspace{1cm} (9)

where the CMC is expressed as a molar fraction (Table 2). The CMC slightly increases as the fraction of DMSO increases (\( \Delta G_{\text{mic}} \) increases), while aggregation occurs more gradually: the width of the transition, \( d \), increases to a greater extent than the CMC increase (Table 2). The ionization degree \( \beta \) also increases as the fraction of DMSO increases.
Table 2: A1, A2, C°, d: fitting values for conductivity (equation (7)). A1 values in xDMSO = 0.35 and 0.50 are the initial slopes. ΔGmic: free enthalpy of micellization. CΦ: CMC from the molar volumes. The compositions of the solvents are given as molar fractions and in v%.

Phase diagram

Figure 2: CMC and precipitation vs composition of the solvent. □: CMC by conductimetry. Δ: CMC from density measurements (molar volumes) ●: solid samples. *: clear, liquid samples. The solid lines are guides that indicate trends. Micelles are assigned on the basis of SANS data.
The Krafft temperature of DTABr in water-DMSO mixed solvent is above the ambient temperature (~295 K) for the highest concentrations of DMSO ($x_{\text{DMSO}} > 0.366$ [14]). We determined the physical state of a series of samples, as observed by eye at ambient temperature (Figure 2).

**Molar volumes**

We next explored the solvation during the micellization process through molar volumes (Figure 3). Two different behaviors were observed that depended on the solvent composition. For solvents with compositions lower than $x_{\text{DMSO}} = 0.35$ (70v%), two volumes ($V_{\text{CMC}}$ and $V_{\text{mic}}$) and a CMC can be determined. The plot of the apparent molar volume of DTABr vs. molality displays a classical shape for ionic surfactants[42] as exemplified by the solvent $x_{\text{DMSO}} = 0.06$ (20v%) (Figure 3a). At concentrations below the CMC, DTABr behaved like a 1:1 electrolyte and $V^{\text{app}}$ (the apparent molar volume of the monomeric form) remained virtually constant. The departure from this plateau indicates the CMC ($\text{CMC} = 0.025 \text{ mol kg}^{-1}$ for $x_{\text{DMSO}} = 0.06$ in Figure 3a). At concentrations above the CMC, $V^{\text{app}}$ is a combination of the volumes of the monomeric and micellar forms of the surfactant in solution. If we consider that the concentration of the monomeric form is equal to the CMC, $V^{\text{app}}$ is given by:

$$V^{\text{app}} = \text{CMC}_{(m)} \times \left(V_{\text{CMC}} - V_{\text{mic}}\right) \frac{1}{m} + V_{\text{mic}}$$

where $\text{CMC}_{(m)}$ is the critical micelle concentration expressed in molality, $V_{\text{CMC}}$ is the apparent molar volume of free surfactant (monomer) at the CMC and $V_{\text{mic}}$ is the apparent molar volume of micellized monomers.

The plot of $V^{\text{app}}$ vs. $1/m$ is shown in Figure 3b for $x_{\text{DMSO}} = 0.06$ and in the Supplementary Material for the other solvent compositions (figures SM-4 and SM-5). At high $1/m$ values, only monomers are present in the solution and, within experimental error (around ± 0.5 cm$^3$ mol$^{-1}$), $V^{\text{app}}$ is independent of $1/m$. We can thus take $V_{\text{CMC}}$ to be the mean value of $V^{\text{app}}$ at DTABr concentrations below the CMC ($V_{\text{CMC}} = 286 \pm 0.5 \text{ cm}^3 \text{ mol}^{-1}$ for the solvent $x_{\text{DMSO}} = 0.06$). At low $1/m$ values, the curve is a straight line described by equation 10. The linearity of this plot is a validation of the hypotheses that the free surfactant concentration remains equal to the CMC and that $V_{\text{mic}}$ is independent
of the total concentration in the studied range of concentration. The CMC may be determined from Figure 3b by the intercept between the two lines. These CMC values are shown in Figure 2 and listed in Table 2 ($C_\Phi$, after conversion of molalities in molarities). They are in good agreement with the values obtained by conductimetry.

![Figure 3: Apparent molar volumes $V^{app}$ vs. molality of DTABr in water-DMSO mixtures. T =298.0 K.](image)

(a) ♦: $x_{\text{DMSO}} = 0.06$ (20v%); *: $x_{\text{DMSO}} = 0.50$ (80v%); △: $x_{\text{DMSO}} = 0.67$ (90v%); ×: $x_{\text{DMSO}} = 1$. (b) Apparent molar volume of solutions $V^{app}$ vs. reciprocal of molality in water-DMSO mixtures ($x_{\text{DMSO}} = 0.06$ (20v%).

At higher DMSO contents ($x_{\text{DMSO}} > 0.35$), the $V^{app} = f(m)$ plot is a constant for DTABr concentrations between 0 and 0.20 mol kg$^{-1}$ (Figure 3a). The volumes of the monomeric form $V_{\text{CMC}}$ and the micellar form $V_{\text{mic}}$ are shown in Figure 4 for conditions in which they can be determined separately ($x_{\text{DMSO}} < 0.35$). The unique volume $V$ determined afterwards (for $x_{\text{DMSO}} > 0.35$) is shown on the same figure. The numerical values of $V_{\text{CMC}}$ and $V_{\text{mic}}$, are provided in the Supplementary Material. The surfactant volume in the micelle $V_{\text{mic}}$ is independent of the DMSO content (295.0 cm$^3$ mol$^{-1}$). As the DMSO content increases in the solvent, the monomeric volume first decreases from 288.5 to 285.5 cm$^3$ mol$^{-1}$ and then increases to the micellar volume at $x_{\text{DMSO}} \approx 0.35$. It then remains constant up to $x_{\text{DMSO}} \approx 0.6$ and slightly decreases to 292.5 cm$^3$ mol$^{-1}$ in pure DMSO.
Figure 4: (Δ) Apparent molar volumes in the monomeric form at the CMC $V_{CMC}$ and (◊) in the micellar phase $V_{mic}$ for conditions in which they can be determined separately. (*) indicate an equal value of $V$ for monomeric or micellar species throughout the molality range of DTABr. $T = 298.0$ K.

SANS:

Micelles in D$_2$O and H$_2$O may have slightly different properties depending on the number of carbon atoms in the chain. However, DTABr behaves nearly the same in either fluid[38]. We assumed that this would also be true if hydrogenated DMSO was replaced by deuterated DMSO, and that the micelles characterized by SANS would be very similar to those characterized by other techniques in hydrogenated solvents. The SANS spectra are displayed in Figure 5 along with the fits. The spectrum in the solvent $x_{DMSO} = 0.67$ (90v%) with a DTABr molality 0.20 mol kg$^{-1}$ is not shown as it was a constant at $I = 0.13$ cm$^{-1}$ above the solvent intensity. The parameters used for the fits of the other spectra are detailed in Table 3. The sample in $x_{DMSO} = 0.51$ contained a very small amount of scattering objects. The surfactant concentration in this solvent could not be increased due to precipitation. For this reason, the overall signal was weak and a very precise fit could not be achieved. However, the presence of small charged objects was clearly evident.
The main parameters we derived from the SANS spectra were the aggregation numbers and the ionization degrees, which were calculated from the volume of the interacting objects and the interacting potential and were not sensitive to the shape. The exact shape of the object is thus of little relevance as long as they remain globular and we used oblate ellipsoids for all spectra. Polydispersity was not tested in order to limit the number of fitting parameters.
Figure 5: SANS spectra fitted with the parameters listed in Table 3 for DTABr in DMSO-water mixtures. The DTABr concentrations are listed in Table 1 (the spectra were multiplied by powers of 10 for the sake of clarity). The solvent compositions $x_{\text{DMSO}}$ are shown in the insert.

DISCUSSION

Aggregation in DMSO-water mixtures

The calculated SANS intensities matched the experiments for solvents with DMSO compositions between 0 and 80 v%, validating the use of the OZ and HNC equations for DMSO-water mixtures, even those with high DMSO content.

a) Aggregation numbers $N_{\text{ag}}$

We analyzed a large DMSO composition range ($0 < x_{\text{DMSO}} < 0.67$) by SANS. The aggregation numbers decreased as the DMSO content increased. For very high DMSO contents ($x_{\text{DMSO}} > 0.51$) no micelles were observed. From Table 3, the changes in the shape and the aggregation numbers are
continuous, indicating that solvent composition has a predominant role in micelle formation. The solvent overwhelms the influence of slight sample-to-sample variations in the surfactant concentration (between 0.2 and 0.5 M) in the definition of the aggregates.

b) Micellar ionization degree

The SANS values for the ionization degree $\beta$ are in good agreement with the conductivity results obtained at the CMC (Table 1 and Table 3). The value obtained in pure water ($\beta \sim 0.25$) is also in agreement with previously reported scattered values between 0.23 [52,53] and 0.34 [41,35], which depend on the technique used and on the DTABr concentration. As the DMSO content increased, the ionization degree $\beta$ also increased. If it is assumed that aggregate structure remains constant, their ionization degree $\beta$ is related to the solvent’s capacity to dissociate ions pairs (evaluated through the reciprocal dielectric constant $1/\varepsilon$ (Figure 6)). Using this criterion only, we predict that as the amount of DMSO present increases, the solvent becomes less dissociating. Thus, the ionization degree would be expected to decrease, the inverse effect of the experimental observation. As a consequence, the increase of $\beta$ can only be attributed to a change in the structure of the micelles (aggregation numbers and shape) that counterbalances this dielectric effect. To explain the variation in $\beta$, the micelle may be described by a spherical colloid of radius $R$, with a structural charge $Z_{str}$ and an effective charge $Z_{eff}$. The structural charge $Z_{str}$, which is equal to the aggregation number of the micelle, decreases by a factor of 10 in solvent mixtures having $x_{\text{DMSO}}$ between 0 and 0.51 (Table 3). In contrast, the effective charge $Z_{eff}$, (i.e., that obtained after the condensation of counterions) varies little as it decreased by only a factor of 2 in the same $x_{\text{DMSO}}$ range. This effect is expected from charged renormalization considerations[54], which demonstrate that the ratio of the effective charge $Z_{eff}$ to the radius “$R$” of the colloid, $Z_{eff}/R$, is independent of the corresponding structural quantity $Z_{str}/R$ (for the same solvent and ionic strength). Counterions are more strongly attracted to charged micelles (i.e., those with high $Z_{str}/R$ ratios) in solvents having equivalent dielectric constants. This leads to a greater condensation and an equivalent effective charge (i.e., a constant $Z_{eff}/R$ ratio). Structural charge $Z_{str}$ and radius $R$ are related in an
equation derived from equation (5a): \( Z_{str}/R = N_{ag}/R = (4\pi/3) R^2/V_{mono} \). A decrease in the aggregation number results in a decrease in the aggregate’s size \( R \) and also in \( Z_{str}/R \). As a consequence, because \( Z_{eff}/R \) remains constant regardless of the value of \( Z_{str}/R \), the ionization degree \( \beta = Z_{eff} / Z_{str} \) increases.

The increase in the ionization degree \( \beta \) is thus a direct consequence of the decrease in the aggregation number and is only slightly influenced by the variation of the dielectric constant of the DMSO-water mixture as \( x_{DMSO} \) increases. This interpretation, taking into account the size of the aggregate and the related change in counterion condensation as the cause for the increase in \( \beta \), is seldom used to explain the increase in \( \beta \) despite the decrease of \( \varepsilon \). The same increase in \( \beta \) was observed for other surfactant micelles in different water-organic solvent mixtures, along with a decrease in the aggregation numbers [25,26]. However, these authors did not link the thermodynamic and the geometric properties of the micelles and proposed that the variation in the ionic strength in the bulk phase was due to an increase in the CMC.

**Figure 6.** The reciprocal dielectric constant \( 1/\varepsilon \) (◊; values taken from [32]) vs solvent composition \( x_{DMSO} \) and the Gordon parameter \( G = \gamma/V^{1/3} \) (*; where \( \gamma = \) solvent/air surface tension and \( V = \) molar volume of the solvent; values taken from [32]) vs solvent composition \( x_{DMSO} \)

c) **Onset of micellization: CMC**
A classical increase in the CMC of DTABr occurred with increasing DMSO content. This effect has been reported for cetyltrimethylammonium bromide (CTAB), DTAB, sodium dodecylsulfate (SDS) and other surfactants[14-18,21,22,55] but generally for more narrow DMSO composition ranges. Using the Rico and Lattes’ criteria[56], the increase in CMC that coincides with increasing DMSO content can be linked to a decrease in the dielectric constant of the solvent, a decrease in solvent structure and also to a decrease in solvating properties. However, these effects are difficult to evaluate and quantify. Other attempts have been made to link the capacities of solvents to solubilize hydrocarbon and to promote micellization[55]. One widely used approach[11,57] is the Gordon parameter G defined by $G = \gamma / V^{1/3}$ (where $\gamma$ is the solvent/air surface tension and $V$ is the molar volume of the solvent). G is related to the cohesion of the solvent, which is the driving force for aggregation. This force decreases with a decrease in cohesive energy density, which, in turn, increases the CMC. The effect of $x_{\text{DMSO}}$ on G is shown in Figure 6. The change in G is of a larger magnitude than that of $1/\varepsilon$, confirming that the cohesion of the solvent has a greater bearing on micellization in this system than the dielectric properties of the solvent.

The Gordon parameter is controversial since it cannot predict all situations[58], but as its simplicity can provide a first approximation of the capacity of a solvent to promote micellization, we tested G against the free enthalpies of micellization $\Delta G_{\text{mic}}$ and the aggregation number $N_{\text{ag}}$ (Figure 7). Nearly all the experimental data fit on a straight line, both for $\Delta G_{\text{mic}}$ and $N_{\text{ag}}$. This trend for the aggregation number versus G has been reported previously [25,57]. The decrease in the aggregation number is continuous, and by no means shows an abrupt change at $x_{\text{DMSO}} = 0.33$ (which corresponds to $G = 1.6 \text{ N m}^{-2}$). A threshold of $G = 1.3 \text{ N m}^{-2}$ is generally thought to be necessary for micellisation to be possible. Our results for $N_{\text{ag}}$ agree with this assertion. However, in our case, the value of $1.3 \text{ N m}^{-2}$ for G coincides with the onset of oligomerization rather than micellization, if we define micellisation as the cooperative aggregation of a large number of monomers, as explained in the following.
Role of solvation in the micellization process

a) Solvation of the free monomer

To further explore how micellization properties are affected by changing DMSO content, we examined the molar volume of the monomers in the presence of different DMSO contents in the solvent. This relationship provides new insight about the solvation of the monomers and the role of solvophobicity. Since the concentrations of DTABr are very low, we assume that apparent and partial molar volumes are identical.

Experimentally, the molar volumes of the monomeric and of the micellized surfactant are different for DMSO compositions less than $x_{\text{DMSO}} = 0.35$ whereas they are equal for higher DMSO contents (Figure 4). The partial molar volume of a solubilized species can be artificially split into an intrinsic volume, which is independent of the surrounding environment, and a volume that depends on its alteration of the solvent structure. This latter quantity can be positive or negative, depending on the reorganization of the solvent around the dissolved compound[59]. Amphiphiles make two contributions to the total perturbed volume: one from the chain, and one from the polar head.

Figure 7: Plots of the molar free enthalpy of micellization $\Delta G_{\text{mic}} (\text{O})$ and the aggregation number $N_{\text{ag}} (\bullet)$ vs the Gordon parameter $G$ of solvents having various DMSO contents (obtained from Figure 6). The lines are visual guides.
Figure 8: Experimental (this study; ♦️) and calculated (from equation (11)) partial molar volumes of monomeric DTABr at different DMSO contents relative to the volume in pure DMSO.

\[ V_{\text{chain}}^\infty (\text{---}) \quad V_{\text{head}}^\infty (\cdots\cdots) \quad V_{\text{DTABr}}^\infty (\text{-----}). \]

For DTABr, these two contributions can be evaluated from volume data for tetraalkylammonium bromides (R₄NBr, with R = methyl [Me], n-butyl [Bu], n-pentyl [Pen]) in DMSO-water solvents[46,60]. The partial molar volumes of DTABr can be calculated, assuming the additivity of the volumes of each chemical group, using the following equations:

\[ V_{\text{chain}}^\infty = \frac{1}{4} V_{\text{Pen}}^\infty + 7 \times \frac{1}{4} \left( V_{\text{Pen}}^\infty - V_{\text{Bu}}^\infty \right) - \frac{1}{4} V_{\text{Br}}^\infty \quad (11a) \]

\[ V_{\text{head}}^\infty = \frac{3}{4} V_{\text{Me}}^\infty + \frac{1}{4} V_{\text{Br}}^\infty \quad (11b) \]

\[ V_{\text{DTABr}}^\infty = V_{\text{chain}}^\infty + V_{\text{head}}^\infty \quad (11c) \]

where \( V_{\text{R}}^\infty \) is the partial molar volume at infinite dilution of R₄NBr; \( \frac{3}{4} V_{\text{Me}}^\infty \) is the volume of the polar head; \( \frac{1}{4} \left( V_{\text{Pen}}^\infty - V_{\text{Bu}}^\infty \right) \) is the volume of one CH₂ group in the chain; \( \left[ \frac{1}{4} V_{\text{Pen}}^\infty + 7 \times \frac{1}{4} \left( V_{\text{Pen}}^\infty - V_{\text{Bu}}^\infty \right) \right] \) is the volume of the dodecyl chain; \( V_{\text{Br}}^\infty \) is the volume of the bromide ion (31 cm³).

The difference between the partial molar volume of DTABr in the solvent \( x_{\text{DMSO}} \) and its partial molar volume in pure DMSO is plotted in Figure 8; pure DMSO was used as the reference behavior. This plot shows the extra perturbation of the water on the surfactant in the mixed solvent. For the experimental as well as the calculated values, minima are observed at low \( x_{\text{DMSO}} \) values and maxima.
appear near \( x_{\text{DMSO}} = 0.4 \). The assumptions made for the calculation (additive rule to calculate the different group contributions of the volume and equality of partial and apparent volumes) lead to slight differences between the experimental values and the calculated values, but the trend was accurately reproduced.

The first part of the curve \((x_{\text{DMSO}} < 0.4)\) is due to the contribution of the polar head and the aliphatic chain, with the chain being responsible for the initial U-shape of the curve. In the second part of the curve, the small volume changes are due to reorganization around the polar head, with the chain environment remaining unchanged.

The determination of the partial molar volumes of tetraalkylammonium \( R_4 \text{N}^+ \) in several organic solvents\[59\] showed that, for a given large alkyl group \( R \), this volume is constant, independent of the nature of the organic solvent and much higher than it is in water. In water, these large ions undergo hydrophobic hydration, resulting in a lower volume (destruction of the water network), whereas they are not affected in this way by an organic solvent. This suggests that for organic solvents, the solvent structure is unaffected by these solutes. For DMSO-water mixtures, the final volume of the chain of the surfactant is reached at \( x_{\text{DMSO}} \approx 0.4−0.5 \). Therefore, for the highest DMSO contents, the introduction of the chain in the mixed solvent produces no volume change (no extra perturbation of the solvent, compared to pure DMSO). This suggests that the chain is only surrounded by DMSO. This better solvation leads to an increase in the solubility of the chain in the presence of high DMSO contents. The partial molar volume of the chain remains constant with \( x_{\text{DMSO}} \) and the changes of the overall partial molar volume are solely attributable to perturbation of the solvent around the head.

\( b) \) Solvation of surfactant in micelles

As can be seen on Figure 4, up to \( x_{\text{DMSO}} \approx 0.6 \), the micellized volume \( V_{\text{mic}} \) remained constant. This means that the perturbation of the solvent around the micelle is independent of the DMSO content and is identical to that in pure water: the micellized surfactant encounters the same environment whether in water or in mixed solvents. It is unlikely that the two contributions to the volume detailed in equation (11c) (the core and the head) change in exactly opposite directions. To achieve this constancy in molar...
volume, each contribution must be invariant with the DMSO content in this composition range, and equal to the corresponding value in water. This implies that: 1) the micellar core is composed of aliphatic chains that are either free of solvent, as it has been established for water [61] or, if DMSO can penetrate the core, it does not affect the volume (vide supra); and 2) the solvation of the head is independent of the presence of DMSO and thus must be composed of water molecules only. This latter point is confirmed in Figure 8, which indicates that the main contribution to the molar volume of free DTABr is due to the solvation of the chain. Once this contribution is suppressed by aggregation, the only remaining contribution is that of the heads, which have a much lower impact. The highly charged surface of the micelle could promote the approach of the more polarizable water molecules and enhance the phenomenon by repelling DMSO from the vicinity of the surface.

If the volume of micellization (i.e., the difference between the volume of a monomer in solution and its volume in an aggregate) decreases as the solvent DMSO content increases, the tendency toward micellization (the release of solvent perturbation upon micellization) is weaker. As a consequence, the $\Delta G_{\text{mic}}$ is less favorable and the CMC increases.

**Thermodynamics of micellization**

Experimentally, DTABr aggregates were characterized throughout the entire DMSO-water composition range. We determined the variation in the partial molar volume of the surfactant and related these changes to the differences in solvation of the head and chain in the solvent. The first conclusion is that the insolubility of one part of the surfactant drives the process of aggregation [51] in DMSO-water mixtures like for pure water solvent.

The free enthalpy of micellization experimentally obtained from the CMC value (Table 2 and Figure 2) can be decomposed into different contributions [51]:

$$\Delta G^0_{\text{mic}} = (\Delta \mu_g^0)_{\text{tr}} + (\Delta \mu_g^0)_{\text{int}} + (\Delta \mu_g^0)_{\text{def}} + (\Delta \mu_g^0)(\text{HG})$$

where $(\Delta \mu^0)_{\text{tr}}$ is the hydrophobic free enthalpy contribution, related to the transfer of a hydrocarbon chain from the surrounding medium to the interior of micelles. It is the driving force for aggregation.
The other contributions counteract aggregation: \((\Delta \mu^°)_{\text{int}}\) is the cost of creating the interface; \((\Delta \mu^°)_{\text{def}}\) (deformation or packing) is the term related to the restriction of the different conformations of the chain in the micelles; \((\Delta \mu^°)_{(HG)}\) is the most positive contribution, and is related to the interactions between head groups. This final term can be divided into a contribution from steric repulsion \((\Delta \mu^°)_{\text{iste}}\) and another one from electrostatic interactions \((\Delta \mu^°)_{\text{ionic}}\). In a first approximation, for ionic surfactants, it is related to the Debye screening length, which at constant ionic strength is proportional to the reciprocal of the dielectric constant \(1/\varepsilon\) of the solvent.

We used the formalism developed by Nagarajan et al[23] to calculate the various contributions to the free enthalpy of micellization in the DMSO-water mixtures. For an aggregate of aggregation number \(g\), the expressions and details of calculations are summarized in supplementary materials, only the results of the calculation are discussed in the article.

An interesting result from this formalism is the volume fraction \(\varphi^S_{\text{DMSO}}\) in the vicinity of the micellar surface which can be calculated from equation (15):

\[
\ln \left[ \frac{(\varphi^S_{\text{DMSO}} / \varphi^S_{\text{DMSO}})^{1/N_{\text{DMSO}}}}{(1-\varphi^S_{\text{DMSO}})(1-\varphi^S_{\text{DMSO}})} \right] = \frac{\sigma^S_{\text{W}} - \sigma^S_{\text{DMSO}}}{kT} v^2_w/3 + \frac{3}{4} \chi_{\text{W-DMSO}} (1 - 2\varphi^S_{\text{DMSO}}) - \frac{1}{2} \chi_{\text{W-DMSO}} (1 - 2\varphi^S_{\text{DMSO}})
\]

\((12)\)

\(N_{\text{DMSO}}\) is the ratio of the molecular volume of DMSO to the molecular volume of water and is equal to 3.96 at 298 K. \(v^2_w\) is the molecular volume of water. \(\sigma^S_{\text{DMSO}}\) and \(\sigma^S_{\text{W}}\) are the hydrocarbon-DMSO and hydrocarbon-water) interfacial tensions, respectively. Their estimated values are \(\sigma^S_{\text{W}} = 50\) mN m\(^{-1}\) ([23]) and \(\sigma^S_{\text{DMSO}} = 11\) mN m\(^{-1}\) ([62]).
Figure 9: DMSO volume fraction $\varphi_{\text{DMSO}}^S$ at the interface between a hydrocarbon core and the mixed solvent (water-DMSO) vs DMSO bulk volume fraction $\varphi_{\text{DMSO}}$ in the mixed solvent. Calculated from equation (12).

The resulting surface composition $\varphi_{\text{DMSO}}^S$ is plotted vs. the bulk volume fraction $\varphi_{\text{DMSO}}$ in Figure 9, which shows that the hydrocarbon-solvent interface is clearly enriched in DMSO. The very steep slope at the beginning reflects the high affinity of DMSO for the aliphatic chain. It is comparable to the steep decrease in the partial molar volume of the chain shown in Figure 8, which is caused by the same phenomenon.

<table>
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<th>Depends on</th>
<th>Transfer $(\Delta \mu^\circ g)_{\text{tr}}$</th>
<th>Deformation $(\Delta \mu^\circ g)_{\text{def}}$</th>
<th>Interface $(\Delta \mu^\circ g)_{\text{int}}$</th>
<th>Steric $(\Delta \mu^\circ g)_{\text{ste}}$</th>
<th>Ionic $(\Delta \mu^\circ g)_{\text{ionic}}$</th>
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<tr>
<td>Monomer molar fraction $X_1$</td>
<td>N</td>
<td>N</td>
<td>N</td>
<td>N</td>
<td>Y</td>
</tr>
</tbody>
</table>

Table 4: Dependency of the various contributions to the free enthalpy $\Delta G^\circ_{\text{mic}}$ on micelle and solvent parameters. Y = dependency; N = No dependency.
For a given $x_{\text{DMSO}}$, the sum of the five contributions ($\Delta \mu_g^o = \Delta G_{\text{mic}}^o$) is calculated with the monomer molar fraction $X_1$ and the aggregation number $g$ (between 1 and 60) as independent variables. The mole fraction $X_g$ of each $g$-aggregate arises from:

$$X_g = X_1 g \exp \left( -\frac{\Delta \mu_g^o}{kT} \right)$$

The total molar fraction $X_{\text{tot}} = X_1 + \Sigma g X_g$ (or the molar concentration: $C_{\text{tot}} = C_1 + \Sigma g C_g$) is deduced. Table 4 summarizes the dependencies of these five contributions on the various parameters. $(\Delta \mu_g^o)_{\text{tr}}$ can be calculated for each solvent composition, independently of the size of the aggregates $g$. For a given solvent composition, the other contributions to $\Delta G_{\text{mic}}^o$ depend on the aggregation number and must be calculated for each size. The ionic contribution depends on all parameters: $g$, $x_{\text{DMSO}}$, monomer concentration (i.e, CMC).

Figure 10: Free enthalpy contributions calculated according to Nagarajan’s model. Solid lines: $x_{\text{DMSO}} = 0$; $C_{\text{tot}} = 1.12 \times 10^{-2}$ mol L$^{-1}$ and $X_1 = 0.000203$. Dashed lines: $x_{\text{DMSO}} = 0.26$; $C_{\text{tot}} = 1.32 \times 10^{-1}$ mol L$^{-1}$ and $X_1 = 0.0038$
The various free enthalpy contributions calculated for pure water and for \( x_{\text{DMSO}} = 0.26 \) according to Nagarajan’s model are shown in Figure 10. The surfactant concentration \( X_1 \) was chosen at the onset of micellization (\textit{vide infra} for the definition of micellization). The contributions that depend most highly on the solvent composition are: the free enthalpy of transfer (\( \Delta \mu \gtrless^0 \)tr), the creation of the interface between the core and mixed solvent (\( \Delta \mu \gtrless^0 \)int), and the electrostatic repulsion between polar heads (\( \Delta \mu \gtrless^0 \)ionic\textsuperscript{[23]}. For this reason, we considered only these three.

As the DMSO content in the solvent increases, the transfer free enthalpy \( \Delta \mu \gtrless^0 \)tr increases rapidly: the solubilization of the chains becomes more favorable since it induces a limited perturbation of the solvent (Figure SM-6 in Supplementary Material). Under these same conditions, the electrostatic and interfacial contributions change to far lesser extents. The balance between the forces that dominate micellization is modified, which results in altered DTABr micellization when DMSO replaces water in the solvent.

![Figure 11: Comparison of calculated (solid line) CMC values to experimental CMC values determined from density measurements (△) and from conductivity measurements (□).](image)

This model also allows the calculation of the CMC. Evans\textsuperscript{[51]} suggested defining the CMC as the concentration at which the probability that a monomer remains in solution is equal to its probability of aggregation. On a plot \( \frac{dC_1}{dC_{\text{tot}}} \) vs \( C_{\text{tot}} \), this criterion corresponds to the concentration \( C_{\text{tot}} \) for which
dC1/dC_{tot} = 0.5. However, since our experimental determination of CMC using molar volumes is based on the detection of the very beginning of aggregation, we modified this definition and used two conditions to determine the CMC: (i) the onset of aggregation was given as the concentration for which dC1/dC_{tot} = 0.95. (ii) this onset of aggregation was defined as a CMC (i.e., a cooperative aggregation process) only when aggregation was steep enough, with the quantitative criterion that the concentration difference between dC1/dC_{tot} = 0.95 and dC1/dC_{tot} = 0.5 should be smaller than one CMC value. This procedure is illustrated in Figure SM-7 for the limiting case x_{DMSO} = 0.26. We compared the calculated CMC values to the ones determined experimentally (Figure 11).

For x_{DMSO} between 0.26 and 0.30, the calculated CMC vanishes. Indeed, for x_{DMSO} higher than 0.26, aggregation could be predicted but no cooperative CMC could be defined. This is in agreement with the experimental features. For higher DMSO contents, aggregates are characterized (Figure 5 and Table 3) but the micelle formation cannot be described by a cooperative aggregation (Figure 1 and Table 2).

The changes in the weight-average aggregation numbers according to the different water-DMSO compositions can also be obtained from the model according to equation (14):

\[ n_{w,\text{app}} = \frac{X_f + \Sigma g^2 X_g}{X_f + \Sigma g X_g} \]  

(14)

The weight-average aggregation numbers decrease continuously with increasing DMSO content (for example, n_{w,\text{app}} decreases from 30 to 2.5 between pure water and x_{DMSO}=0.51 for C_{tot} = 0.4 mol L^{-1}), as observed experimentally (Table 3). Qualitative agreement is obtained between the experimental data and the model.

The x_{DMSO} = 0.33 composition, which corresponds to the formation of a 1 DMSO: 2 H_{2}O complex, is indeed a threshold for many properties of DMSO-water mixtures (e.g., viscosity, excess volume, excess dielectric constant, excess enthalpy of mixing, etc.). These properties undergo progressive changes between x_{DMSO} = 0.3 and 0.4. Aggregation of DTABr behaves similarly, changing from a clearly defined micellization at low DMSO contents to no aggregation at all at high DMSO contents, as experimentally
observed and theoretically predicted. The transition between these two behaviors occurs at approximately $x_{\text{DMSO}} = 0.3$, where we observed a zone of oligomerization. The process was continuous as micellar properties ($N_{\text{ag}}$ and CMC) increased continuously until the aggregates vanished. These changes in the aggregation properties of the surfactant were a direct consequence of the mixed solvent properties, which were the input parameters of the model.

**CONCLUSION**

Using a combination of different techniques (SANS, conductivity and density measurements) and complementary approaches for the interpretations (statistical physics using the HNC equation, molecular thermodynamics with Nagarajan’s model, and group additivity for partial molar volumes), we studied the aggregation properties of a cationic surfactant, DTABr, in water-DMSO mixtures having compositions between pure water and pure DMSO. This complete study allowed us to follow the aggregation properties of this surfactant in water-DMSO mixtures at different length scales (molecular to supramolecular).

The global methodology we used here is certainly not specific to DTABr and could be extended to other surfactants in solvent mixtures. Several main conclusions emerged from this work. (i) The DMSO composition threshold, $x_{\text{DMSO}} = 0.33$, observed for many properties of the binary DMSO-water mixture remains valid for micellization, although a third component (the surfactant) is involved. For high DMSO composition solvents, no micellization occurred. Micellization is thus more controlled by the properties of the solvent than by the nature of the surfactant in a mixed solvent. (ii) The previously described phenomenon of increasing effective micelle charge with increasing $x_{\text{DMSO}}$ [25,26] is explained here in the framework of SANS and statistical physics and can be solely attributed to the decreasing size of the micelles. (iii) Although controversial, the Gordon parameter was used to interpret the experimental data. In this system, aggregates are observed for Gordon parameter values higher than 1.3, which is a generally accepted threshold value for the presence of aggregates. (iv) The micellization process can be clearly distinguished from the aggregation process as a function of the DMSO
composition using the thermodynamic model described by Nagarajan et al[23] for another solvent mixture (water-ethyleneglycol) containing various surfactants. (v) Finally, analysis of the molar volumes of DTABr as a function of increasing DMSO content revealed information about the organization of the solvent around the surfactant molecules. These results are compatible with a dissymmetric solvation for the amphiphile, in which the hydrocarbon chains would be preferentially surrounded by DMSO and the polar heads surrounded by water molecules. This finding reveals that the motor for micellization (i.e., the unfavorable solvation of the chains) decreases as water is replaced by DMSO around the hydrocarbon chains.

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Supplementary Material available: Additional graphs or fitting parameters, model for SANS spectra fitting, apparent molar volumes values, equations reported from [23] are available free of charge via the internet.

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