Quantification of the specific yield in a two-layer hard-rock aquifer model
Véronique Durand, Véronique Léonardi, Ghislain de Marsily, Patrick Lachassagne

To cite this version:

HAL Id: hal-01537837
https://hal.sorbonne-universite.fr/hal-01537837
Submitted on 13 Jun 2017

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L’archive ouverte pluridisciplinaire HAL, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d’enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.
Quantification of the specific yield in a two-layer hard-rock aquifer model

Véronique Durand (1), Véronique Léonardi (2), Ghislain de Marsily (3), Patrick Lachassagne (4)

(1) Laboratoire GEOPS; Univ. Paris-Sud; CNRS, UMR 8148; Bât. 504, 91405 Orsay Cedex, France; veronique.durand@u-psud.fr
(2) Laboratoire Hydrosciences; Université de Montpellier; CNRS, UMR 5569; CC57, 163 rue Auguste Broussonet, 34090 Montpellier, France; veronique.leonardi@umontpellier.fr
(3) Laboratoire Metis; Sorbonne Universités, UPMC Univ. Paris 06; CNRS, UMR 7619; EPHE; 4 place Jussieu, 75005 Paris, France; gdemarsily@aol.com
(4) Water Institute by Evian, Danone Waters, Evian-Volvic World, BP 87, 74500 Evian-les-Bains Cedex, France; patrick.lachassagne@danone.com

Abstract

Hard Rock Aquifers (HRA) have long been considered to be two-layer systems, with a mostly capacitive layer just below the surface, the saprolite layer and a mainly transmissive layer underneath, the fractured layer. Although this hydrogeological conceptual model is widely accepted today within the scientific community, it is difficult to quantify the respective storage properties of each layer with an equivalent porous medium model. Based on an HRA field site, this paper attempts to quantify in a distinct manner the respective values of the specific yield (Sy) in the saprolite and the fractured layer, with the help of a deterministic hydrogeological model. The study site is the Plancoët migmatitic aquifer located in north-western Brittany, France, with piezometric data from 36 observation wells surveyed every two weeks for eight years. Whereas most of the piezometers (26) are located where the water table lies within the saprolite, thus representing the specific yield of the unconfined layer (Sy1), 10 of them are representative of the unconfined fractured layer (Sy2), due to
their position where the saprolite is eroded or unsaturated. The two-layer model, based on field observations of the layer geometry, runs with the MODFLOW code. 81 values of the Sy1/Sy2 parameter sets were tested manually, as an inverse calibration was not able to calibrate these parameters. In order to calibrate the storage properties, a new quality-of-fit criterion called "AdVar" was also developed, equal to the mean squared deviation of the seasonal piezometric amplitude variation. Contrary to the variance, AdVar is able to select the best values for the specific yield in each layer. It is demonstrated that the saprolite layer is about 2.5 times more capacitive than the fractured layer, with Sy1=10% (7%<Sy1<15%) against Sy2=4% (3%<Sy2<5%), in this particular example.

Keywords
Hard-rock aquifer; Specific yield; Two-layer numerical model; Quality-of-fit criterion

Highlights
- Quantitative evidence that the saprolite layer is more capacitive than the fractured one
- New quality-of-fit criterion, AdVar, based on the piezometric amplitude variations

1 Introduction
Hard-Rock aquifers (HRA) have long been considered to be two-layer systems, with (i) a weakly transmissive but rather capacitive layer (with a high specific yield) just below the surface, the unconsolidated weathered layer (also called the saprolite here, or the regolith) and (ii) a more transmissive but less capacitive layer underneath, the fractured layer. This hydrogeological conceptual model is now widely accepted in the scientific community (see for instance Chilton and Foster, 1995; Cho et al., 2003; Dewandel et al., 2006; Dewandel et al., 2011; Lachassagne et al., 2011; McFarlane, 1992; Taylor and Howard, 1999, 2000; Wright, 1992). These two layers belong to the HRA weathering profile and reach, in general, a thickness that may exceed 100 m (Lachassagne et al., 2011). At the watershed scale, the hydrodynamic storage and flow properties of the underlying...
unfractured rocks (basement) are negligible. The capacitive (or storage) properties of this two-layer system, namely its storativity, or specific yield $S_y$ where the aquifer is unconfined, were first studied and characterized to gain a better estimate of the long-term groundwater storage available in HRAs.

It was established early on that the fractures in HRAs are well connected (Lenck, 1977) and later, that this fractured layer could be considered a continuous aquifer (Guihéneuf et al., 2014; Lachassagne et al., 2001). Some studies have focused on the specific yield of the saprolite layer, and consequently on the capacitive role it can play during withdrawals (Detay et al., 1989; Howard and Karundu, 1992; Rushton and Weller, 1985). The processes controlling the development of these two layers are increasingly well understood and the ways to define their respective geometry and thickness are more precise (Dewandel et al., 2006; Lachassagne et al., 2011; Wyns et al., 2004); moreover, pumping test methods to characterize their hydrodynamic properties at the borehole scale have been improved (Maréchal et al., 2004). However, the precise determination of the respective storage properties of each layer remains an issue, particularly at the watershed scale (Dewandel et al., 2012).

A number of authors have modelled these systems as equivalent porous media, but none of them has managed to calibrate the specific yield of both layers simultaneously. Gupta et al. (1985) used a single-layer model, considering that both layers were interconnected. Ahmed et al. (2008) presented a two-layer model calibrated on an Indian site, but unfortunately the saprolite layer was always unsaturated, which made it impossible to calibrate its specific yield. An interesting specific yield calibration for a two-layer model of an HRA is presented in Lubczynski and Gurwin (2005), but the paper did not focus on this parameter, so that the specific yield values were not presented, nor the potential differences between the saprolite and the fractured layer. The authors point out the difficulty in calibrating the specific yield with an automatic inverse method like PEST, and prefer a trial-and-error calibration, in order to "have the best fit of the pattern of rises and recessions of the groundwater table". The same kind of difficulty was also highlighted by Mazi et al. (2004), where to calibrate the specific yield, the authors needed the help of an expert as a complement to the
automatic calibration. In fact, automatic calibration methods are mainly focused on the hydraulic conductivities, adjusted with the help of a quality-of-fit criterion based on the differences between the modelled and observed hydraulic heads (Carrera et al., 2005; de Marsily et al., 2000; Zhou et al., 2014). For aquifer management purposes, a correct quantification of the distinct specific yields of the two layers is important, as a potentially highly capacitive layer represented by the saprolite may sustain the exploited water resources in the fractured layer.

In this context, the main objective here is to calibrate the specific yield in each of the two layers of a finite-difference hydrogeological model, at the watershed scale. This parameter, representative of the storage properties, is crucial in groundwater management purposes. Because of the difficulties mentioned above, this calibration required the development of a new quality-of-fit criterion. This study uses field data from an HRA in Brittany, France, described in the following section. The model is then presented, followed by the calibration (approach and results). The results are discussed, and a conclusion summarizes the main results of the study.

2 Geology and hydrogeology of the study site

2.1 General presentation

The studied site (Durand et al., 2006) is located in north-eastern Brittany, France, 10 km from the English Channel shoreline (Figure 1), in a landscape of grass-land, forest and farmland, with a smooth relief. In the middle of the studied site stands a 90 m ASL hill, surrounded by the Arguenon River at 10 m ASL flowing toward the English Channel (Figure 1). The migmatites that constitute the rocks in this area belong to the Saint-Malo dome, exhumed at the end of the Cadomian Orogeny (540 Ma).

These partially melted rocks originated from detrital sediments interbedded with graphitic cherts, composed of quartz. They now form a folded gneiss with relict bands of cherts. They were later intruded by dolerite dykes during the Hercynian period (330 Ma). The associated hard-rock aquifer is located mostly in the sub-surface stratiform weathered layers (Durand et al., 2006), which consist of: (i) a cover of unconsolidated weathered rocks (saprolite), several tens of meters thick where it has
been preserved from erosion, consisting mainly of clay or sandy clay, that are the weakly permeable
transformation products of the initial minerals; (ii) beneath this layer, and above the unweathered
bedrock, a fractured layer, some 50 m thick or more, resulting from rock shattering under the
influence of stress generated by the swelling of certain minerals during the early stages of
weathering (Dewandel et al., 2006; Lachassagne et al., 2011; Wyns et al., 2004). Field surveys and
geophysical mapping of the two weathered-fractured layers and of the various geological
heterogeneities, such as graphitic cherts and dolerite dykes, are described in a previous study
(Durand et al., 2006). In an area covering only 4 km², six pumping wells and 36 piezometers (Error!
Reference source not found.), owned and monitored by the Nestlé Waters Company for bottled
natural mineral and spring water, provide an unusually rich set of hydrogeological data. While most
piezometers (26) are located where the saprolite is saturated, and will thus help to quantify the
storage in this layer, 10 of them are located where the saprolite is either eroded, or unsaturated, and
will consequently help the storage quantification in the fractured layer.

Figure 1. Location of the study area (within the grey-shaded polygon), the meteorological
stations (stars), and the only gauging station (square)

Figure 2. Geometry of the finite-difference model, boundary conditions, thickness of layer 1
(white: zero thickness) and location of the piezometers with their respective numbers

2.2 Recharge estimation

The daily rainfall was measured directly at the Plancoët bottling plant (Figure 1). The mean annual
rainfall (R) is on average 800 mm, with a typical oceanic climate. Around Plancoët, three weather
stations belonging to Météo France, located in Pleurtuit, Quinténic and Trémeur (Figure 1), also
provided data on rainfall and daily potential evapotranspiration (PET) estimated with Penman’s
relation (Penman, 1948). Daily river flow measurements were available at the Jugon-les-Lacs gauging
station (Figure 1) on the Arguenon River, which drains the studied area. Over the eight years of the monitored period, a mean annual river discharge of 253 mm/y was found at the Jugon-les-Lacs gauging station, for the area of its catchment (see Durand (2005) for more details). Thornthwaite’s method (Castany, 1967; Maidment, 1993; Vittecoq et al., 2010) was used at a daily time step and during the eight-year monitored period to compute the effective rainfall (Eff), equal to P minus Real EvapoTranspiration (RET), or to the sum of the aquifer recharge plus the surface runoff over the catchment. The computation used the rainfall data measured directly on the Plancoët site, and the weighted average of PET data from the three Météo France weather stations calculated for the site. The maximum soil storage capacity (MSC), the parameter used in Thornthwaite’s method to temporarily store rainfall in the soil before it is taken up by RET and Eff, was calibrated so that the Eff value would be as close as possible to the available annual catchment flow in the area. In this hydrogeological context, both runoff and aquifer recharge reach the river in a year (Molénat et al., 1999). Rounding off the value, the best fit for MSC was obtained with 100 mm, leading to a mean real evapotranspiration of 530 mm/y and an annual effective rainfall of 247 mm/y, quite close to the average river discharge. Figure 3 presents the meteorological data (P, RET and Eff) averaged for each model time step in mm/day. It shows that Eff is positive only during the winter season, when RET is sufficiently low. Considering the landscape, smooth relief and grassy hills, the field observations during the winter rainy season (no runoff observed even during the most intense rainy periods), and for simplicity reasons, the recharge was fixed at 100% Eff. This will be discussed in the final discussion part below.

2.3 Water table variations

The piezometric signals in this type of aquifer, in a temperate climate, have a pseudo-sinusoidal shape with an annual period, where the highest levels are observed at the end of winter and the
lowest at the end of summer. The amplitude of the head variations between the high and low levels
depends both on the time distribution of the recharge and on the Sy values (Maréchal et al., 2006).
As the specific yield plays an active role only for an unconfined layer, it is either Sy in the saprolite
layer 1 (Sy1) or Sy in the fractured layer 2 (Sy2) that is effective, depending on the piezometer
location: Sy1 is effective where layer 1 (saprolite layer) is present and saturated (26 piezometers),
and Sy2 will be effective where layer 1 has been eroded or is unsaturated (10 piezometers). In the
data set, both piezometer types are well represented, and it is interesting to compare the signals
obtained for each type. The piezometric head was measured manually in each observation hole from
1/1/1996 to 30/11/2003, with a time step of approximately 15 days. From these data, one can see
that the mean annual amplitude variation of the piezometric levels is higher in the piezometers
representing layer 2, the fractured layer (6.1 ± 2.3 m in average) than in those representing layer 1,
the saprolite (3.4 ± 1.3 m in average). An example is shown in Figure 4.

3 Model description
The finite-difference PMWIN model (Chiang and Kinzelbach, 2000) that uses the MODFLOW code
(Harbaugh and McDonald, 1996) was chosen for this work. The model was built with two parallel
layers in order to account for the assumed distinct hydrodynamic properties of the saprolite (layer 1),
and the underlying weathered fractured layer (layer 2).
The geometry of each of these layers (shape of top and bottom) was determined by extensive field
work over the entire 116 km² study area (Durand et al., 2006). The maximum thickness of layer 2,
where it is totally preserved from erosion, was found to be quite uniform across the studied area and
was estimated at 100 m, a thickness consistent with our experience of the Brittany geology and the
available borehole logs and geophysical data (Durand, 2005). Layer 2 is present over the whole modelled area (116 km²), as it has never been totally eroded, whereas layer 1, with a maximum thickness of 40 m, covers only 54 km², due to local patches of total erosion (Error! Reference source not found.).

In the centre of the modelled area, owned by Nestlé Waters and including the bottled-water exploitation zone, the accuracy of the structural map and the number of hydrogeological data are much higher than in the other areas. The rectangular grid of the model (Error! Reference source not found.) is therefore a compromise between good precision where the data are dense and relatively fast calculations: consequently, the width of the rectangular model cells varies from 400 m on the borders to 40 m in the exploitation zone. Each of the two layers is modelled vertically by a single cell whose height is equal to the thickness of the corresponding layer. The layers are connected vertically, as they are assumed to be in reality. Layer 1 is modelled as an unconfined aquifer and layer 2 can be either confined or unconfined, depending on the potential lowering of the piezometric head below the bottom of layer 1.

The simulations were performed in a transient flow regime which allowed the time-dependent seasonal and yearly piezometric variations observed in the aquifer to be reproduced. The modelling runs from 1/1/1996 to 30/11/2003, with a time step of 15 days, similar to the frequency of the piezometric head measurements.

Six pumping wells in the exploitation zone (Error! Reference source not found.) are used for bottled-water production and their time-varying discharges are precisely recorded and used in the model. No other significant pumping is known to occur in the whole modelled domain, except a few tens of litres per day, in the summer, from shallow wells, not considered in this study.

The total modelled domain, chosen much larger than the area exploited by the bottling plant, is limited by permanent rivers, considered to be prescribed-head boundaries, so no conductance parameter was set for these cells (Error! Reference source not found.). The river elevations were extracted from the 1/25 000 topographic map of the area (IGN, 2000) assuming a linear slope...
between known points (contour lines every 5 m). In the exploitation zone, the topographic
depression due to a disused quarry of graphitic cherts located near the top of a hill is at the origin of
a small perennial lake (Error! Reference source not found.). The level of this lake, generally higher
than that of the observed nearby piezometric levels, shows that it functions as an infiltration zone. It
is modelled as a reservoir in the MODFLOW code (Error! Reference source not found.), with a
prescribed constant level, a water depth of 1 m, and an underlying 1 m-thick sediment layer with a
vertical hydraulic conductivity of $1.2 \times 10^{-5}$ m/s. This value was calibrated so that the infiltration from
the lake is consistent with its hydrological balance. Two small temporary rivers (Error! Reference
source not found.) surrounding the hill are considered as drains in the model, because they drain the
aquifer during high-water periods and are dry during the rest of the year. A calibrated hydraulic
conductance of $5.8 \times 10^{-4}$ m$^2$/s was assigned to the contact area between the aquifer and these drains.
The initial value of the piezometric heads on January 1st, 1996 was estimated as follows: a
preliminary run of the model over the whole 8-year period started with heads at the ground surface;
the calculated heads on November 3rd, 2003 at the end of this preliminary run were then taken as the
initial conditions for January 1st, 1996.

4 Calibration

4.1 Homogeneous model calibration

In this type of aquifer, the hydraulic conductivity might be very heterogeneous; but the
heterogeneity does not depend primarily on the geometry of the two layers, but rather on the
location of fractures and other spatial discontinuities. As this type of heterogeneities was not the
main focus here, a homogeneous hydraulic conductivity was chosen for each layer, and the PEST
automatic calibration method in transient state (Doherty, 2004), within the PMWIN interface, was
used to provide the best possible average fit. In a first approximation, the hydraulic conductivity and
the specific yield, considered here to be uniform in space and identical for the two layers, were
calibrated simultaneously: the best calibrated hydraulic conductivity was $8.1 \times 10^{-7}$ m/s, and the
specific yield was 6%. An arbitrary value of the storage coefficient for the confined layer was set at 10⁻⁴. As the hydraulic conductivity is only roughly calibrated on the whole model, the simulated heads are therefore shifted locally, as compared to the observed ones. It is considered that this shift does not influence the further calibration of Sy1 and Sy2, based on a good amplitude variation fit. This specific point is discussed in the final discussion part of the article.

4.2 Classical calibration of the specific yield using the variance criterion

In a second step, a model with distinct storage properties in the two layers was used to obtain a better calibration of the specific yield (Sy). This hydraulic parameter may be considered the most important one in the two-layer model. Contrary to the hydraulic conductivity, which influences the average hydraulic heads, this parameter influences primarily the amplitude of the hydraulic-head variations. We used PEST for an automatic calibration of Sy1 and Sy2, fixing the previously calibrated value for the hydraulic conductivity. Sy1 was found to be optimum at 3%, but the Sy2 calibrated values were always the maximum defined ones, even when amounting to 50%. This can be explained by the fact that, due to the imperfect calibration of the hydraulic conductivity of the model, the average simulated head values are shifted as compared to observed data, and that the quality-of-fit criterion used in PEST is the least squares of the differences between modelled and observed heads.

As a high Sy tends to reduce the amplitude variation of the signal, the quality-of-fit criterion is better with a “flat” signal than a varying one in the case where the general average is very different from the true one. In order to understand the automatic calibration process, and to quantify the performance of each model, various combinations of Sy parameters were tested manually. Nine values of Sy1 and Sy2 were thus tested (1%, 2%, 3%, 4%, 5%, 6%, 7%, 10% and 15%), leading to 81 model runs. The classical head squared deviation variance (Var, Equation 1) between the calculated (calc) and observed heads (obs) on each measurement day of the data set was calculated for all 36 piezometers and this variance was averaged over the whole data set for each model.

$$\text{Var} = \frac{\sum_{i=1}^{n} (\text{calc}_i - \text{obs}_i)^2}{n}$$

(1)

with n the number of data points for each piezometer.
Note that in PEST, the sum of squared deviation is used, but here we take into account the number of measurements over periods of varying lengths in order to compare the results obtained for each piezometer. Considering all piezometers, the best Var value was 97 m² for Sy1=3% and Sy2=15%.

Nevertheless, it appeared that these statistics might be biased by the fact that some simulated heads concerned another layer than the one of the observed data (for instance, the observed piezometry is in the saprolite while the computed one is in the fractured layer, or vice-versa). As the hydraulic conductivity was not calibrated, this was observed on 7 piezometers representative of the saprolite, and on 4 from the fractured layer. In order to avoid this specific bias and improve the results, we chose to remove these piezometers and re-calculate the average Var values. The results obtained for the various Sy values are given in matrix form (Table 1), the values of Var are shown with Sy1 values in columns and Sy2 values in rows. The minimum Var values are highlighted (corresponding to the better fit). Table 1 shows that the coloured cells are below the diagonal matrix, i.e. for Sy2>Sy1, and that the maximum chosen Sy2 value (15% here) leads to the better Var value. This confirms that, for the same reasons as explained above, the Var criterion, or any criterion based on squared head deviations, as in PEST, is not appropriate for the calibration of Sy. It is therefore necessary to develop another criterion better adapted to calibrate Sy in each layer.

Table 1. Var values (in m²) obtained for all Sy1 and Sy2 values. Yellow: minimum values; orange, red and light brown respectively: classes around the minimum, with an increase of Var of 5% of the total variation range between two successive classes.

4.3 New calibration of the specific yield taking the amplitude variation into account

To better fit the specific yield, a new performance criterion, named "AdVar", was developed, based on the seasonal piezometric amplitude variations. For each piezometer, and for each available measurement on day d, a moving interval of one year after d was defined both for the observed and
the calculated heads. Then for that one-year interval, each piezometer amplitude-deviation variance

\[ \text{AdVar} = \frac{\sum_{d=1}^{n_{\text{day}}}(\text{max}_{\text{calcd}} - \text{min}_{\text{calcd}})(\text{max}_{\text{obsd}} - \text{min}_{\text{obsd}}))^2}{n_{\text{day}}} \]  

(2)

with \( \text{max}_{\text{calcd}}, \text{min}_{\text{calcd}}, \text{max}_{\text{obsd}}, \text{min}_{\text{obsd}} \) respectively the maximum-minimum values of the calculated and observed heads over the one-year interval after day \( d \), and \( n_{\text{day}} \) the number of measurement dates \( d \) available, i.e. the total number of data points less those of the last year of data. Like the variance, AdVar is always positive and the smaller values indicate a better fit. For a better visualisation of the AdVar behaviour compared to Var, when quantifying the fit between theoretical sinusoidal curves, please refer to Appendix 1.

Considering all piezometers, the best AdVar value was 9.7 m² for \( Sy1=10\% \) and \( Sy2=4\% \). Removing the biased piezometers as previously, and re-calculating the average AdVar values, the same matrix form as for Var was used for AdVar in 2, with \( Sy1 \) values in columns and \( Sy2 \) values in rows. 2 shows that the coloured cells are above the diagonal matrix, i.e. for \( Sy1>Sy2 \), with AdVar, which seems more realistic from a hydrogeological viewpoint than the results obtained with Var. Following this criterion, the specific yield is about 10% in the saprolite (\( Sy1 \)) and 2% in the fractured layer (\( Sy2 \)). The uncertainty intervals are 7%<\( Sy1<15\% \) and 1%<\( Sy2<3\% \).

Table 2. AdVar values (in m²) obtained for all \( Sy1 \) and \( Sy2 \) values. Yellow: minimum values; orange, red and light brown respectively: classes around the minimum, with an increase of AdVar of 0.5% of the total variation range between two successive classes

4.4 Comparison of the simulated water tables from the best adjustments of Var and AdVar

To give a better view of the results obtained in each of the two layers of the model, Figure 5 shows the observed piezometric variations compared with two simulations in P26, a piezometer...
representative of the saprolite layer, and in P17, representative of the fractured layer. The first
model, with Sy1=2% and Sy2=15%, corresponds to the best performance for the Var criterion, and
the second model, with Sy1=10% and Sy2=2%, to the best performance for the AdVar criterion.
Even if the hydraulic conductivity, and thus the mean value of the piezometric head is not perfectly
fitted, the second model with the lowest Sy2 and the highest Sy1 better mimics the observed
amplitude variations than the first one, with low Sy1 and high Sy2 values.
The Var and AdVar values are given in Table 3 for each of these piezometers with the two above
models. Except for Var in P17, the values follow the same trend as the average Var and AdVar
values: the first model gives a better Var, and the second a better AdVar. Between two distinct
models, an expert eye would choose in accordance with the AdVar criterion, not with the Var one.
As a conclusion to this part of the work, the obtained calibration of Sy can be considered very
satisfactory, particularly when one considers that, for this study, no spatial variations neither of the
hydraulic conductivity, nor of the specific-yield, were considered.

Figure 5. Examples of piezometric variations for P26 within the saprolite and P17 within the
fractured layer. Two model results corresponding to the best Var and AdVar values are
compared to the observed data

Table 3. Var and AdVar values (in m²) for piezometers P26 and P17 with two Sy set of values

<table>
<thead>
<tr>
<th></th>
<th>Sy1=2%, Sy2=15%</th>
<th></th>
<th>Sy1=10%, Sy2=2%</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Var</td>
<td>AdVar</td>
<td>Var</td>
</tr>
<tr>
<td>P17</td>
<td>16.0</td>
<td>22.9</td>
<td>13.3</td>
</tr>
<tr>
<td>P26</td>
<td>6.2</td>
<td>14.2</td>
<td>16.1</td>
</tr>
</tbody>
</table>
5 Discussion

5.1 Comparison of specific yield values with other studies

These results of specific yield values are consistent with the conceptual model developed by Lachassagne et al. (2001) and Dewandel et al. (2010), notably with a decrease of Sy with depth. The obtained Sy values (Sy1=10% and Sy2=4% for the best AdVar values) are higher than those given by Rushton and Weller (1985) for a granite in India and by Compaore et al. (1997) for a granite in Burkina Faso. These authors estimated the specific yield of the saprolite layer at between 1 and 2%.

Nevertheless, as shown by Wyns et al. (2004), Sy in the saprolite is sensitive to the type of lithology: for instance, Sy increases with the coarsening of the minerals of the parent rock and also with the quartz content. The interval of specific-yield values measured by Wyns et al. (2004) on several types of hard-rock lithologies in Brittany (France) includes the values estimated in the present study.

5.2 Recharge sensitivity

In order to simplify the results, the recharge value was fixed arbitrarily in this study, considering that runoff is negligible. Previous work done elsewhere in Brittany (Durand and Juan Torres, 1996; Jiménez-Martinez et al., 2013; Molénéat et al., 1999) using other methods, such as isotope and natural tracer analyses, river discharge recession-curve analysis, or temporal groundwater head variations in response to recharge inputs, has arrived at similar conclusions. Nevertheless, it is possible to explore the sensitivity of the model to the recharge, testing various recharge values.

Figure 6 shows the observed and simulated heads at P26, for the reference model (Sy1=10%, Sy2=4%, Recharge=100% EffR), and for two other models, keeping the same Sy values, and testing Recharge=70% EffR and Recharge=30% EffR. Note that the simulated heads with low recharge values never stop decreasing from the beginning to the end of the simulation, and even drop below the observed values. They also decrease a little with the maximum recharge, due to a problem in the initial head, difficult to calibrate here, but it appears that the average heads tend to stabilize at the end of the modelled period. It is not the case with lower recharge values, leading to the conclusion that these values are too low to provide enough water to the aquifer, compared to the real natural
discharge and pumping rate on the site. Some graphics showing the Var and AdVar results with a complete parameter set (8 recharge values for each Sy combination) are presented in Appendix 2.

**Figure 6. Observed and modelled heads for P26, testing various recharge values**

### 5.3 Hydraulic conductivity sensitivity

In this study, an arbitrary choice was made to leave out the hydraulic conductivity calibration. Although it is the main parameter of the flow budget within the aquifer, this choice was made in order to focus attention on the storage parameter, a crucial parameter in HRA to quantify the exploitable water resources. The aim was to quantify the specific yield in the two layers of an HRA, highlighting their differences, and not to build a fully calibrated model for water-resource management purposes. A local adjustment of hydraulic conductivities may induce some minor modification of the temporal head amplitude variations. This is shown in Figure 7 with the example of P26: the reference model (black plain line), with K=8.1 \(10^{-7}\) m/s, is compared to models with K=8.1 \(10^{-6}\) m/s (light grey) and K=1.2 \(10^{-7}\) m/s (dark grey). Changes of K highly influence the mean interannual piezometric values, but influence in a minimal way the amplitude variations. One can conclude that more reasonable changes in K than those of this sensitivity analysis, to better fit the local data, would not seriously impact the amplitude variations. It is considered that, in the high-density data zone where the piezometers are located, the amplitude variations would not be much affected, as the chosen homogenous K value is already quite well fitted. It is possible, however, that the calibrated Sy values for both layers might not be quite exact, due to the local K variations. But the general tendency toward a higher storage capacity in the saprolite layer than in the fractured one will stay the same, whatever the local K values.

**Figure 7. Observed and modelled heads on P26, testing various K values**
5.4 Synthesis

Figure 8 synthesises these results in a qualitative way, presenting the respective behaviours of the saprolite and the fractured layer in two columns. In the case where the water table stays in the saprolite layer (first column), the observed water table (dotted blue line) varies with a low amplitude. The model M1 (in orange), with a high specific yield, well reproduces this low amplitude variation, but presents a computed average head value different from the observed one (lower here), as a consequence of the imperfect K calibration. Therefore, the variance calculated between the M1 computed red curve and the observed data is high, whereas the AdVar criterion is very good. Still in the first column, the inverse is shown for the model M2 (in green), with a low specific yield: its amplitude variation is too high compared to the observed data, leading to a high AdVar criterion. But as M2 presents an average value very similar to the observed data, the variance is better than for M1. This first column shows a higher efficiency of the Advar quality-of-fit criterion (rather than the Variance) in identifying the best Sy (here M1 with a high Sy), even if the average head is not well calibrated (for instance because of a locally imperfect calibration of K). Inversely, in the case where the water table stays in the fractured rock (second column), the observed water table varies with a high amplitude. The same M1 model as previously, well fitted for the average head, shows here a good variance criterion, but a weak AdVar criterion. And the same M2 model as previously, with a distinct average head but an amplitude variation similar to the data, shows a weak variance but a good Advar criterion. Again, this second column shows a greater efficiency of the Advar quality-of-fit criterion in identifying the best Sy (here M2 with a low Sy). This emphasises that the ideal model combines M1 and M2, with a relatively high specific yield in the saprolite layer, and a lower specific yield in the fractured layer, which are the two main conclusions of this paper. Moreover, the AdVar criterion is better adapted to quantifying the amplitude variation (thus to fit the specific yield) than the Var criterion.
Figure 8. Schematic view of the main results showing the observed and simulated piezometric amplitude variation for the two cases of a water table in the saprolite and in the fractured layer.

6 Conclusion

In this study, a hard-rock aquifer system in Brittany (France) was simulated with a two-layer deterministic hydrogeological model at the catchment scale, each layer representing a specific weathering horizon (saprolite and fractured layer). The storage capacities of each layer can be quantified thanks to a rich data set, with piezometers representing the two types of layers, when unconfined. The specific yield values are calibrated using a new quality-of-fit criterion, AdVar, based on the seasonal piezometric amplitude variations. The saprolite layer is proved to be more capacitive than the fractured layer, with a calibrated specific yield 2.5 times greater than that of the fractured layer: $\text{Sy}_1=10\% \ (7\%<\text{Sy}_1<15\%)$ against $\text{Sy}_2=4\% \ (3\%<\text{Sy}_2<5\%)$, in this particular example.

Acknowledgment

We are grateful to the Nestlé Waters Company for financial support from 2002 to 2005 and for making the data available.

References


New submission of HYDROL21465 / HYDROL21465R1 to “Journal of Hydrology”


New submission of HYDROL21465 / HYDROL21465R1 to “Journal of Hydrology”


Harbaugh, A. W., and M. G. McDonald (1996), User’s documentation for MODFLOW-96, an update to the U.S. Geological Survey modular finite-difference ground-water flow model, 56 pp, USGS.


Appendix 1

In order to validate this new AdVar criterion, the respective behaviours of Var and AdVar were compared on a theoretical example. Perfect sinusoidal curves of heads (h) as a function of time in days (d) with different amplitudes were compared. From the equation of a sinusoid (Equation 3), a reference curve was calculated with an amplitude (a) of 10 m and a mean value (m) of 0 m, to act as the "observed data".

\[ h = a \cdot \sin\left(\frac{2\pi}{P} d\right) + m \]  

The period (P) was fixed at 365.25 days to follow an annual variation, and the total duration was set at 30 years. This reference curve was then compared to various "model" curves, with varying m and a. The "m" parameter varied between 0 and 10 m, and the "a" parameter between 0 and 20 m. With m=0 and a=10, the model curve is identical to the reference curve, and the quality-of-fit-criterion should be equal to zero, both for AdVar and for Var. The distinct behaviours of Var and AdVar with varying "m" and "a" are shown in Figure 9.

*Figure 9. Var (grey line) and AdVar (black line) values obtained by comparing perfect sinusoidal shapes to a reference sinusoidal curve with a zero mean (m) and an amplitude (a) of 10 m. Results are shown as a function of "a" from 0 to 20 (first line) and of "m" from 0 to 10 (second line), changing the values of "m" (first line) and of "a" (second line) in each column.*

It is clear that AdVar is sensitive only to a variation of "a", not of "m", which is due to the way this criterion has been defined, as it depends only on the amplitude variation, which is particularly useful for the purpose of our research. On the contrary, Var depends on both parameters: whereas the minimum Var value increases with "m", the AdVar minimum value is always zero when "a" is equal to the observed one. Furthermore, the AdVar values are much more variable when "a" varies than the
Var values: on the first plot with m=0, AdVar varies between 0 and 400 as "a" varies between 0 and 20, and Var between 0 and 50. This shows the advantage of AdVar with respect to Var: it is more precise on amplitude variations than Var. When all values of Var and AdVar are averaged over the total number of piezometers for each model, it is easier to compare two distinct models when these quality-of-fit values are clearly distinct from one model to another.
Appendix 2

The results of the two quality-of-fit criteria for the 36 piezometers (average Var and AdVar values for each simulation) are presented exhaustively: Figure 10 and Figure 11, show the evolution of Var (first line) and AdVar (second line) as a function of Rech (Figure 10) and Sy2 (Figure 11). Each column corresponds to a distinct value of Sy1 and each curve to a distinct value of Sy2 (Figure 10) and Rech (Figure 11). The scale of the Y axis is chosen identical for all Var, and for all AdVar, thus some curves that are too high for the scale disappear from the plots: the focus is on low criterion values.

Note that the lowest Var and AdVar values are obtained mostly for the highest recharge (Rech) parameter.

For Var, the curve shapes in Figure 10 are very similar, generally showing a better fit towards the high recharge values and for the highest Sy2. For Sy1 up to 3 %, the best fit is obtained for a recharge of 100 % EffR, but for higher Sy1 values, this recharge is lower and varies between 80 and 100 % EffR.

For AdVar, the analysis is more delicate, as the Sy2 curves in Figure 10 do not show a homogeneous behaviour. For Sy1 up to 3 %, the lowest AdVar values are obtained for the lowest recharge. On the contrary, when Sy1 increases, except for the lowest Sy2 values, most of the lowest AdVar values are obtained with the maximum recharge, and here the difference between 80, 90 and 100 % EffR is greater than for Var.

Figure 11 shows distinct behaviours for Var and AdVar as functions of Sy2. Judging by the Var criterion only, one might conclude that the best fit would be obtained with the highest values of Sy2, even above 15 %, as shown in section 4.3. With the AdVar criterion however, the best fit for Sy2 is between 4 and 5 %, which, although quite high for a fractured layer, is more realistic.

Figure 10. Results of the quality-of-fit criteria Var and AdVar as functions of the recharge values on the X axis, each curve representing a distinct Sy2 value, and each column a distinct Sy1 value
Figure 11. Results of the quality-of-fit criteria Var and AdVar as functions of the Sy2 values on the X axis, each curve representing a distinct recharge value, and each column a distinct Sy1 value.
Figures

Figure 12. Location of the study area (within the grey-shaded polygon), the meteorological stations (stars), and the only gauging station (square).

Figure 13. Geometry of the finite-difference model, boundary conditions, thickness of layer 1 (white: zero thickness) and location of the piezometers with their respective numbers.

Figure 14. Precipitation (P), calculated real evapotranspiration (RET) and effective rainfall (EffR) used for each model time-step.

Figure 15. Measured water table in two types of piezometers: P17 in the fractured layer and P26 in the saprolite.

Figure 16. Examples of piezometric variations for P26 within the saprolite and P17 within the fractured layer. Two model results corresponding to the best Var and AdVar values are compared to the observed data.

Figure 17. Observed and modelled heads for P26, testing various recharge values.

Figure 18. Observed and modelled heads on P26, testing various K values.

Figure 19. Schematic view of the main results showing the observed and simulated piezometric amplitude variation for the two cases of a water table in the saprolite and in the fractured layer.
Figure 20. Var (grey line) and AdVar (black line) values obtained by comparing perfect sinusoidal shapes to a reference sinusoidal curve with a zero mean (m) and an amplitude (a) of 10 m. Results are shown as a function of "a" from 0 to 20 (first line) and of "m" from 0 to 10 (second line), changing the values of "m" (first line) and of "a" (second line) in each column.

Figure 21. Results of the quality-of-fit criteria Var and AdVar as functions of the recharge values on the X axis, each curve representing a distinct Sy2 value, and each column a distinct Sy1 value.

Figure 22. Results of the quality-of-fit criteria Var and AdVar as functions of the Sy2 values on the X axis, each curve representing a distinct recharge value, and each column a distinct Sy1 value.

Tables

Table 4. Var values (in m²) obtained for all Sy1 and Sy2 values. Yellow: minimum values; orange, red and light brown respectively: classes around the minimum, with an increase of Var of 5% of the total variation range between two successive classes.

Table 5. AdVar values (in m²) obtained for all Sy1 and Sy2 values. Yellow: minimum values; orange, red and light brown respectively: classes around the minimum, with an increase of AdVar of 0.5% of the total variation range between two successive classes.

Table 6. Var and AdVar values (in m²) for piezometers P26 and P17 with two Sy set of values.
New submission of HYDROL21465 / HYDROL21465R1 to “Journal of Hydrology”

<table>
<thead>
<tr>
<th></th>
<th>1%</th>
<th>2%</th>
<th>3%</th>
<th>4%</th>
<th>5%</th>
<th>6%</th>
<th>7%</th>
<th>10%</th>
<th>15%</th>
</tr>
</thead>
<tbody>
<tr>
<td>1%</td>
<td>116</td>
<td>95</td>
<td>90</td>
<td>90</td>
<td>94</td>
<td>99</td>
<td>106</td>
<td>128</td>
<td>161</td>
</tr>
<tr>
<td>2%</td>
<td>105</td>
<td>89</td>
<td>85</td>
<td>86</td>
<td>91</td>
<td>97</td>
<td>104</td>
<td>127</td>
<td>161</td>
</tr>
<tr>
<td>3%</td>
<td>99</td>
<td>85</td>
<td>82</td>
<td>85</td>
<td>90</td>
<td>96</td>
<td>103</td>
<td>126</td>
<td>161</td>
</tr>
<tr>
<td>4%</td>
<td>95</td>
<td>82</td>
<td>80</td>
<td>83</td>
<td>89</td>
<td>95</td>
<td>103</td>
<td>126</td>
<td>161</td>
</tr>
<tr>
<td>5%</td>
<td>92</td>
<td>80</td>
<td>79</td>
<td>82</td>
<td>88</td>
<td>95</td>
<td>102</td>
<td>126</td>
<td>161</td>
</tr>
<tr>
<td>6%</td>
<td>90</td>
<td>79</td>
<td>78</td>
<td>81</td>
<td>87</td>
<td>94</td>
<td>102</td>
<td>126</td>
<td>161</td>
</tr>
<tr>
<td>7%</td>
<td>88</td>
<td>77</td>
<td>77</td>
<td>80</td>
<td>86</td>
<td>94</td>
<td>101</td>
<td>126</td>
<td>161</td>
</tr>
<tr>
<td>10%</td>
<td>83</td>
<td>73</td>
<td>74</td>
<td>78</td>
<td>85</td>
<td>92</td>
<td>101</td>
<td>125</td>
<td>161</td>
</tr>
<tr>
<td>15%</td>
<td>78</td>
<td>69</td>
<td>70</td>
<td>75</td>
<td>83</td>
<td>91</td>
<td>99</td>
<td>125</td>
<td>161</td>
</tr>
</tbody>
</table>

647
648
New submission of HYDROL21465 / HYDROL21465R1 to “Journal of Hydrology”

<table>
<thead>
<tr>
<th>1%</th>
<th>2%</th>
<th>3%</th>
<th>4%</th>
<th>5%</th>
<th>6%</th>
<th>7%</th>
<th>10%</th>
<th>15%</th>
</tr>
</thead>
<tbody>
<tr>
<td>166.2</td>
<td>63.6</td>
<td>35.1</td>
<td>23.5</td>
<td>17.6</td>
<td>14.1</td>
<td>12.0</td>
<td>9.2</td>
<td>8.3</td>
</tr>
<tr>
<td>118.3</td>
<td>41.3</td>
<td>22.1</td>
<td>15.0</td>
<td>11.7</td>
<td>9.9</td>
<td>9.0</td>
<td>7.9</td>
<td>8.2</td>
</tr>
<tr>
<td>101.2</td>
<td>34.5</td>
<td>18.5</td>
<td>12.8</td>
<td>10.3</td>
<td>9.1</td>
<td>8.5</td>
<td>8.1</td>
<td>8.8</td>
</tr>
<tr>
<td>93.0</td>
<td>31.7</td>
<td>17.3</td>
<td>12.3</td>
<td>10.2</td>
<td>9.2</td>
<td>8.7</td>
<td>8.6</td>
<td>9.4</td>
</tr>
<tr>
<td>88.6</td>
<td>30.5</td>
<td>16.9</td>
<td>12.3</td>
<td>10.4</td>
<td>9.5</td>
<td>9.1</td>
<td>9.1</td>
<td>10.0</td>
</tr>
<tr>
<td>86.2</td>
<td>30.0</td>
<td>16.9</td>
<td>12.5</td>
<td>10.7</td>
<td>9.9</td>
<td>9.5</td>
<td>9.5</td>
<td>10.5</td>
</tr>
<tr>
<td>84.8</td>
<td>29.9</td>
<td>17.1</td>
<td>12.7</td>
<td>11.0</td>
<td>10.2</td>
<td>9.9</td>
<td>10.0</td>
<td>10.9</td>
</tr>
<tr>
<td>83.4</td>
<td>30.1</td>
<td>17.7</td>
<td>13.5</td>
<td>11.9</td>
<td>11.2</td>
<td>10.9</td>
<td>11.0</td>
<td>11.9</td>
</tr>
<tr>
<td>83.9</td>
<td>30.9</td>
<td>18.6</td>
<td>14.4</td>
<td>12.8</td>
<td>12.2</td>
<td>11.9</td>
<td>12.1</td>
<td>12.9</td>
</tr>
</tbody>
</table>

649
650
Highlights

- Quantitative evidence that the saprolite layer is more capacitive than the fractured one
- New quality-of-fit criterion, AdVar, based on the piezometric amplitude variations