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Molecular emulsions: from charge order to domain order

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Abstract

Aqueous mixtures of small molecules, such as lower n-alkanols for example, are known to be micro-segregated, with domains in the nanometer range. One consequence of this micro-segregation would be the existence of long range domain-domain oscillatory correlations in the various atom-atom pair correlation functions, and subsequent pre-peaks in the corresponding atom-atom structure factors, in the q-vector range corresponding to nano-sized domains. However, no such pre-peak have ever been observed in the large corpus of radiation scattering data published so far on aqueous mixtures of small n-alkanols. By using large scale simulations of aqueous-1propanol mixtures, it is shown herein that the origin for the absence of scattering pre-peak resides in the exact cancellation of the contributions of the various atom-atom correlation pre-peaks to the total scattered intensity. The mechanism for this cancellation is due to the differences in the long range oscillatory behaviour of the correlations (beyond 1nm), which are exactly out-of-phase between same species and cross species. This is similar to the charge order observed in ionic melts, but differs from room temperature ionic liquids, where the segregation is between charged and neutral groups, instead of species segregation. The consequences of such cancellation in the experimental scattering data are examined, in relation to the possibility of detecting micro-segregation through such methods. [In the particular case of aqueous-1propanol mixtures, it is shown the Xray scattering leads an exact cancellation, while this cancellation in neutron scattering is seen to depend on the deuteration ratio between solvent and solute.](#)

1 Introduction

Aqueous mixtures of small quantities of tbutanol or n-alkyl polyglycol ether (C_nE_m) show aggregation of these solute molecules in both cases[1, 2, 3, 4, 5, 6].

However, there is a considerable physico-chemical difference between these two types of aggregation. While tbutanol molecules form small aggregates about 1nm wide[3], C_nE_m molecules self-assemble into shapes called micelles about 5-10nm wide[5]. The latter type of mixtures are called emulsions, while the former is a solution. In both cases, it is the dual amphiphilic/hydrophobic nature of the two types of molecules that produces the aggregate formation[7]. The microscopic structural differences between these two mixtures can be probed by radiation scattering[8, 9], such as light, Xray or small angle neutron scattering. The intensity $I(k)$ scattered off the micro-emulsion will show a Teubner-Strey behaviour[10] with an important pre-peak for wave vector k_P in the range $k_P \approx 0.1 - 0.2 \text{ \AA}^{-1}$, while for aqueous tbutanol mixture $I(k)$ will show a typical Ornstein-Zernike like behaviour, with no such pre-peak. The existence of the pre-peak is only weakly dependent of the nature of the scattering radiation type (light, neutrons, Xray), and seems to depend more on the type of aggregates[8, 9]. The scattering data in both systems seems to suggest that the existence of a pre-peak could be related to the size of the surfactant.

Since a decade, however, a new property of the solution type mixtures has become apparent: the atom-atom pair correlation functions, *as obtained in computer simulations*, exhibit long range oscillations, which come from the existence of correlations between aggregated domains[11]. Consequently, the corresponding atom-atom structure factors exhibit a domain pre-peak at the wave vector corresponding to the size of these domains. This finding poses a problem: why this pre-peak does not contribute to the radiation scattered intensity $I(k)$?

One of the possible answers is that computer simulations could produce artifacts in the long range correlations, due to approximate molecular model, or statistical problems. However, this would be in variance with the fact that, for many neat liquids, computer simulations are able to predict scattering pre-peak in excellent agreement with experiments, for example neat alcohols[12] and neat room temperature ionic liquids[13, 14]. The origin of these latter pre-peaks has been related[13, 14, 15, 16] to the segregation of the charged (hydroxyl or ionic) and neutral (methyl or methylene) molecular groups. Furthermore, in such systems, the contribution of pre-peaks of the atom-atom structure factors to the total scattering pre-peak has been demonstrated[13, 16]. There is however an important difference between these neat systems and the mixtures mentioned above. As I have recently shown[17], the atom-atoms correlations of these neat systems do not show any long range domain oscillations corresponding to the segregation of the charged and neutral groups. Hence, the pre-peaks in such systems do not arise from segregated domain correlations, but correspond to the alternate disposition of the plus and minus charges *within* the charged group domain. This observation shows the principal difference between those neat systems, which show scattering pre-peak, and the case of mixtures presented here. Indeed, in the present case, both segregated species have atomic charges, such that, contrary to neat alcohols and ionic liquids, one cannot speak of charged group versus uncharged group segregation. What is even more problematic in the case of aqueous mixtures is precisely the absence of pre-peak in scattering experiments, versus their existence in atom-atom structure factors obtained

from computer simulations.

The answer we provide here clarifies the origin of this discrepancy. We show that these long range domain oscillations in the atom-atom correlations are genuine physical features, but their contributions to the radiation scattering intensity vanish, because the various atom-atom contributions cancel each other. This cancellation is similar to that found in simple ionic liquids, where the charge order imposes out-of-phase long range oscillations[17, 18], hence drawing an analogy between charge order and domain order. In addition, the same analogy equally explains the existence of a pre-peak in the scattering in micellar systems, through a mechanism similar that produces a scattering pre-peak in room-temperature ionic liquids, as compared to its absence in ordinary ionic liquids: the perturbation of the charge order by the uncharged methyl groups[17, 18]. The equivalent mechanism in the case of domain order would be the perturbation of this order by the large interface between the two types of components. This new explanation gives a better microscopic foundation to the previous argument based on size antagonism between types of aggregates. [In addition, we find interesting differences between Xray and neutron scattering, the latter being more flexible in order to detect domain ordering.](#)

In the presentation below, we first recall the important details of the charge ordering process in different types of ionic liquids. Then, we present the case of aqueous-1propanol as a prototype to show the nature of the domain order and the consequences on both the various atom-atom pair correlation function and the total scattering function. In the final part, we examine the consequences of the domain and charge order analogy for the understanding of the liquid-like order in complex liquids.

2 Charge ordering

Charge ordering is a crucial concept for this paper, since we want to show the appealing analogy between the way ionic species in a molten salt, and micro-segregated species domains in aqueous mixtures, are spatially positioned. Charge order is not a new concept[19, 20], but it seems to have been overshadowed by other properties of ionic liquids. It has known a recent renewal with room temperature ionic liquids[13, 16], as described in the Introduction. Since the presentation in this section has been covered in our previous publications[17, 18], we will be brief about it in the presentation below. Charge ordering describes the very special form of order in simple ionic liquids, such as high temperature molten salts, for example. This special form of order is apparent from the correlation functions between like and unlike charge atoms, namely $g_{++}(r)$, $g_{--}(r)$ and $g_{+-}(r)$, which are function of the atom-atom separation distance r . Fig.1 shows a typical example taken from a model simulation of a ionic liquid, made of soft spheres of same diameter, which bear the charges of valence $z_+ = +1$ and $z_- = -1$. In Fig.1a, it is seen that, past the details of the first neighbour correlations, the remainder of the correlations are exactly out of phase. This property translates into the following equality, which holds for

large distances only, $r > r_C \approx 3.6\text{\AA}$:

$$h_{++} = h_{--} = -h_{+-} \quad (1)$$

where $h_{ij} = g_{ij} - 1$. These equalities can be summarised in a unique one as

$$\sum_{ij} h_{ij} = 0 \quad r > r_C \quad (2)$$

Correlation functions for uncharged atoms never obey this property, and are usually more or less in phase at large distances. Charge order is therefore a remarkable form of order in a *disordered* liquid. The origin of this order is naturally coming from the fact that like charges repel each other, while unlike charges attract each other, and in a disordered liquid, these local constraint leads to this special form of order. Charge order can equally be defined through the atom-atom structure factors, which are related to the Fourier transform of the correlation functions[21]:

$$S_{ij}(k) = \delta_{ij} + \rho \sqrt{x_i x_j} \int d\mathbf{r} h_{ij}(r) \exp(i\mathbf{k} \cdot \mathbf{r}) \quad (3)$$

where x_i is the mole fraction of species i , and $\rho = N/V$ is the number density defined as the total number of atoms N in the volume V . The functions $S_{++}(k)$, $S_{--}(k)$ and $S_{+-}(k)$ are shown in the inset of Fig.1b. Charge order is visible through the exact opposition of the peaks (shown by the red arrow), at the k-vector $k \approx 1.67\text{\AA}^{-1}$, which corresponds to the period of the long range oscillation in the $g_{ij}(r)$. The fact that the charge order peaks are exactly opposite in sign comes naturally from the equalities in Eq.(1).

The exact cancellation of the structure factors charge order peaks can be highlighted through the Bhatia-Thornton transformation[22], which holds only for binary mixtures. It consists in defining 2 new microscopic densities, the total local density $\rho_N(\mathbf{r}) = \rho_+(\mathbf{r}) + \rho_-(\mathbf{r})$ and the charge density $\rho_Z(\mathbf{r}) = [z_+ \rho_+(\mathbf{r}) + z_- \rho_-(\mathbf{r})]/2$, and introducing corresponding new structure factors $S_{AB}(k) = \langle \tilde{\rho}_A(k) \tilde{\rho}_B(-k) \rangle$ through ensemble averages of the correlations of their Fourier transforms. In particular, one has for the density-density structure factor

$$S_{NN} = \frac{1}{2} [S_{++} + S_{--} + 2S_{+-}] \quad (4)$$

This structure factor S_{NN} is equally represented in the inset of Fig.1. It is seen that the opposing peaks in the S_{ij} do not appear in S_{NN} , due to their exact cancellation in the expression Eq.4. Conversely, these peaks appear in the charge-charge structure factor shown in Fig.1.

It is important to note that charge order is different from the global electroneutrality, although both are obviously related through the Coulomb interaction. Global electroneutrality is contained in the small-k limit of the structure factors, through the well-known Stillinger-Lovett sum rules[23]. Therefore, they concern $k = 0$ behaviour of the structure factor. In contrast, charge order concerns the local distribution, as witness by both the medium-to-long range

oscillations and the $k \neq 0$ wave vector where it manifests itself, and it may not necessarily obey electroneutrality, which is a global ($k = 0$) constraint.

The various features of the charge ordering process shown here, are now used to demonstrate how domain-ordering follows a similar pattern to charge ordering.

3 Domain ordering in aqueous 1propanol mixtures

3.1 Simulation details

We have studied by computer simulations the aqueous 1propanol mixtures, and in particular various atom-atom correlation functions and corresponding structure factors. This type of mixture corresponds to what we have named molecular emulsions[11], which show strong micro-heterogeneity, with water and solute segregated domains[24, 25]. SPC/E water model[26] and TraPPE 1propanol model[27] were chosen. We have focussed here on 1propanol mole fractions $x = 0.2$ and $x = 0.3$, since these values are close to the maximum of the experimental Kirkwood-Buff integrals[28, 29], where maximum segregation effects are expected. The structure of this mixture has been previously studied by Xray and small angle neutron scattering experiments[30, 31, 32, 33] as well as computer simulations[34, 35], and both approaches revealed the clustering properties of these mixtures. It is important to note that none of these works have reported the existence of scattering or atom-atom domain correlation pre-peaks. The present simulations have been conducted in the isobaric ensemble by using the GROMACS package[36]. The temperature was maintained at 300K through a Nosé-Hoover thermostat, and the pressure was set at 1atm using the Parrinello-Rahman barostat, with time constant 1ps. Various system sizes were investigated (see below). In each case, the system was equilibrated for 5ns, and production runs for 10ns. Several successive runs of 10ns were sampled, in order to ensure full convergence of the correlation functions. In order to properly sample long range oscillations due correlations between segregated domains, we have studied a system of $N = 128\,000$ molecules, which corresponds to box sizes of $L = 184\text{\AA}$ for $x = 0.2$ and $L = 195\text{\AA}$ for $x = 0.3$. This is an unusually large number, but it is required, since lower system sizes do not allow a proper sampling of these domain-domain correlations -as shown further below. Initial configurations were generated by the program PACKMOL, which are always random. Independence upon initial conditions were tested by inverting the components order in the configuration files, and the final configurations looked identically micro-segregated in all cases, and the calculated correlation functions identical. The atom-atom structure factors $S_{ij}(k)$ were computed by direct fast Fourier transform of the calculated $g_{ij}(r)$, as in our all our previous works. We discuss in Section 3.3 below system size dependance of these quantities.

3.2 Domain ordering

Fig.2a demonstrates in a single plot how all the 33 atom-atom correlation functions $g_{ab}(r)$ (where a and b stands for the various atoms), corresponding to the aqueous mixture with 30% 1propanol, merge at long distance in 3 distinct domain-domain correlation corresponding to the 3 species-species contributions. The water-water functions are shown in blue, the cross species atom correlations in magenta, and the propanol-propanol atom correlations in green. The left part of the plot shows all the correlations within the distance range $0 < r < 10\text{\AA}$. The right part shows the zoom of the correlations in the range $10 < r < 100\text{\AA}$. The inset shows the very short distance details of the first neighbour correlations for $0 < r < 5\text{\AA}$. The detail of the various functions is shown and labelled separately in Fig.3a-f. Despite the confusing aspect of the left side of the plot, due to the specific details of various individual atom-atom correlations, one sees how this messy detail thins out into 3 distinct branches at about $r \approx 8\text{\AA}$, which depend only on species pairs. The right panel continues the display, but with a different horizontal distance scale, and a different vertical scale displayed at the right vertical axis (as indicated by the blue arrow), which is a zoom in the region close to the asymptote 1. It shows clearly the domain oscillations of much weaker amplitude, but of half-period about $r_C \approx 25\text{\AA}$, which correspond to the mean domain size. It is seen that all atomic details are washed out into single species-species correlations, namely water-water (in blue), propanol-propanol (in green) and cross water-propanol correlations (in magenta). It is clearly seen that these 3 type of species-species correlations show out-of-phase correlations between the like and cross correlations. This long range part of Fig.2a bears a striking resemblance with charge-ordering displayed in Fig.1, and we will consider here that these out of phase oscillations represent a “domain ordering”, which is due to the micro-segregation of water and 1propanol(see snapshots in Fig.4). The domain oscillations are not quite damped at the end of the half-box (about 98\AA) indicating that even the $N=128000$ particle box is not enough to accommodate the description of such correlations.

Fig.2b shows the same information as Fig.2a, but from the structure factor point of view. The species-species color conventions are kept the same. The main panel shows the detail of the correlations for k-vector about the main peaks, which is $2 - 3\text{\AA}^{-1}$ for water and $1.5 - 1.8\text{\AA}^{-1}$ for 1propanol. The inset shows a zoom over the small-k behaviour, indicating clearly that all the details of the various site-site correlations have merged into 3 distinct species-species functions. These are a direct counter part of the long range domain correlations displayed on the right panel of Fig.2b. The pure 1propanol pre-peak is indicated by a red arrow, and is seen to occur at the k-vector larger than the domain pre-peak. Once again, we see that all the differences in the atomic details shows up essentially for $k > k_C = 2\pi/r_C \approx 0.5\text{\AA}^{-1}$, where $r_C \approx 12\text{\AA}$ corresponds to the region where atomic details are still seen (left part of Fig.2a); but for smaller k-values $k < k_C$ (inset), only the species-species specificity emerge into pre-peaks with opposing signs. This finding proves that the domain-domain correlations are independent of the atomic details of the various molecular con-

stituents. We have previously discussed such pre-peaks in the context of many other types of aqueous mixtures, and also non-aqueous mixtures[11]. But it is the first time that we relate such pre-peak to charge order, as seen in Fig.1, which they are clearly reminiscent of.

Fig.3(a-f) show the detail of the various atom-atom correlations functions, as well as the corresponding structure factors (in the insets), anonymously displayed in Fig.3a-b. These are the 3 functions $g_{O_w O_w}, g_{O_w H_w}$ and $g_{H_w H_w}$ (when the subscript “w” stands for water) shown in Fig.2a, the 15 functions between the propanol atoms, which are $g_{OO}, g_{OH}, g_{OC_1}, g_{OC_2}, g_{OC_3}$ shown in Fig.3b $g_{HH}, g_{HC_1}, g_{HC_2}, g_{HC_3}$ shown in Fig.2c and $g_{C_1 C_1}, g_{C_1 C_2}, g_{C_1 C_3}, g_{C_2 C_2}, g_{C_2 C_3}, g_{C_3 C_3}$ shown in Fig.3d as well as the 15 cross correlation functions between these atoms, which are $g_{O_w O}, g_{O_w H}, g_{O_w C_1}, g_{O_w C_2}, g_{O_w C_3}$ shown in Fig.3e, $g_{H_w O}, g_{H_w H}, g_{H_w C_1}, g_{H_w C_2}, g_{H_w C_3}$ shown in Fig.2f, and for a total of 33 functions.

The micro-segregation of this system is illustrated in Fig.4, through snapshots for the 30% mixture of various sizes $N = 2000, N = 16000$ and $N = 128000$ (each system is exactly the double of the size of the previous one). In all these three cases, the local segregation of domains is quite obvious, and these domains show an alternated dispositions, which strikingly resembles that of the charge ordering in the ionic liquid of the previous section, as shown in Fig.1a. There are important differences though. While the charges in the ionic liquid are localised within the atoms, the water and 1propanol domains do have such sharp localisation. This feature has important heuristic implications that we will discuss later in Section 5. Although this “domain order” is much more loose than the strict charge order of the ionic liquid, the long range correlations hold an appealing analogy through the fact they appear to obey out-of-phase behaviour reminiscent of that captured through Eqs.(1,2) for the case of ionic liquids. This type of equality can be illustrated further through the analysis of the atom-atom structure factors $S_{ab}(k)$, shown in Fig.2b.

It is important to underline that the micro-segregation reported in these snapshots has nothing to do with macroscopic phase separation. The lengthy run of several of tens of nanoseconds never lead to full demixing. In addition, as reported below in Section 3.3, the correlation functions from the 3 different sizes converge to the same data, independently of the system sizes, and within the mean domain size, which is below 10\AA .

The domain order displayed in Figs.4 has also a striking similarity with the so-called bi-continuous and plumber phases found in micro-emulsions[37], which exhibit segregation of molecular species at a larger scales, but which occurs more often in presence of an water-oil-surfactant context. The important difference that these have with the actual system is the presence of better defined interface area, separating water-rich and oil-rich domains, and which is saturated with the surfactant[37]. We conjecture that it is this segregation of a component into a lower dimensional area, which is responsible to the scattering Teubner Strey pre-peak[10] observed in such systems. We revisit this argument below in Section 5.

3.3 System size dependence

The system size dependence is further illustrated in Fig.5a-b, for $x = 0.2$, where we show the 3 oxygen atom correlation functions $g_{O_wO_w}$, g_{OO} and g_{O_wO} (Fig.5a), as well as the corresponding structure factors (Fig.5b), calculated for the different system sizes shown in Fig.4. In both Fig.5a and Fig.5b, the insets focus on the respective domain-domain contributions. These figures show that the system size does not matter so much for the short range features, since all curves are nearly superimposed. This superposition of the correlations from 3 different system sizes is also a proof that our calculations for each size are perfectly converged to thermodynamical equilibrium. However, both insets show the dramatic differences coming from the long range part, which is sensitive to correct description of domain-domain correlations. For example, system size $N = 2000$ shows that the correlations are not settled to 1 at the truncation distance corresponding to half-box size $L \approx 20 \text{ \AA}$ for this particular system size. This leads to incorrect and too large $k = 0$ predictions of the structure factors in the left-inset Fig.4b. This well known problem has been previously reported by us [24, 25]. The $N = 16000$ system seems appropriate since it gives results nearly similar to the $N = 128000$ system, although the r-range does not extend beyond 48AA. We would like to point out that, since the calculated correlations have twice the range for each increased system size, any arguments about the large distance truncation errors are totally irrelevant, as can be observed in the inset of Fig.4b. Only genuine physical effects due to approximate description of the micro-segregation are noticeable in this figure.

3.4 Water force field model dependence

The degree of domain segregation depends on the type of water models. In order to test the universality of the domain-domain correlations in case of micro-segregation, we have simulated the 30% 1propanol mixture with the TIP4P 2005 water model [38], which is particularly known to reproduce the density anomaly [39] among other water anomalous properties. The three oxygen atom correlation functions for the $N = 128000$ system are shown in Fig.6. For comparison, the differences with the SPC/E model for the short range correlations are displayed for distances smaller than 10 \AA . These differences are seen to be quite small for the main peak (inset). However, the long range domain oscillations beyond 10 \AA are present for both models, clearly illustrating that the micro-segregation is independent of the selected water model. Interestingly, it is seen that the domain oscillations for the TIP4P-2005 model are smaller in amplitude than those of the SPC/E water model. In addition, these domain oscillations decrease faster for the TIP4P model than for the SPC/E model. These observations are consistent with the empirical fact that the TIP4P water models are more compatible with the OPLS/TraPPE solute models than the SPC/E model, due to modeling similarities. As a consequence, one expects that compatible models exhibit lesser segregation. Micro-heterogeneity differs between models, just like for thermodynamic properties. The data displayed in

Fig.5 demonstrates that, despite these differences, micro-segregation and subsequent oscillatory correlations in the correlation functions are robust universal features of aqueous mixtures.

4 Absence of radiation scattering pre-peak in domain-ordered systems

4.1 Expression for the scattered intensity

One of the problem of predicting domain pre-peaks in the atom-atom structure factors is to explain why such pre-peaks are not experimentally observed in radiation scattering experiments[11]. In order to answer this question in a self-consistent manner, it is necessary to go through a short reminder of textbook knowledge[1] about this topic. The radiation scattering intensity $I(k)$ is formally defined through the Debye formula[40]

$$I(k) = \langle \sum_{i,j} f_i(k) f_j(k) \exp(i\mathbf{k} \cdot (\mathbf{r}_i - \mathbf{r}_j)) \rangle \quad (5)$$

where the sum runs over all pairs of scattering atoms i,j , which are at respective spatial positions \mathbf{r}_i and \mathbf{r}_j , the functions $f_i(k)$ are the atomic form factor for atom i and depend on the type of radiation which is scattered, and the symbol $\langle \dots \rangle$ designates an average over all possible positions of these atoms, which corresponds to a thermal average, or an ensemble average for calculational purposes. In practice, it is convenient to rewrite this expression in terms of the molecular species which contains the atoms[41]. For a binary mixture, we introduce symbols i, j to designate the molecular species index, and a_i, b_j to designate the atoms of types a and b in respective molecules. Using the definition of the atom-atom structure factor :

$$\rho \sqrt{x_i x_j} S_{a_i b_j}^{(M)}(k) = \langle \sum_{m_{a_i} m_{b_j}} \exp(i\mathbf{k} \cdot (\mathbf{r}_{m_{a_i}} - \mathbf{r}_{m_{b_j}})) \rangle \quad (6)$$

where the sum runs over all atoms of type a_i, b_j , and $x_i = N_i/N$ is the mole fraction of molecular species i . In the equation above, the atom-atom structure factor $S_{ab}^{(M)}(k)$ is not the same as that which appears in Eq.(3), since it contains contributions from the intra-molecular contributions as well, hence the superscript (M) for molecular. Indeed, the sum in Eq.(6) contains also atom pairs in the same molecule. It can be shown, in case of atoms rigidly bound inside a molecule, that this contribution in Eq.(6) comes down to the Bessel function $j_0(kd_{ab}) = \sin(kd_{ab})/kd_{ab}$, where $d_{ab} = |\mathbf{r}_a - \mathbf{r}_b|$. This function is the same as the W-matrix, with elements $w_{ab}(k) = j_0(kd_{ab})$, which appears in the Site-Site Ornstein-Zernike theory[21], and which contain the intra-molecular contribution to the pair correlation function. The link with the structure factor defined through Eq.(3) and the atom-atom pair correlation function $g_{a_i b_j}(r)$ is then

$$S_{a_i b_j}^{(M)}(k) = w_{a_i b_j}(k) + \rho \sqrt{x_i x_j} \int d\mathbf{r} [g_{a_i b_j}(r) - 1] \exp(i\mathbf{k} \cdot \mathbf{r}) \quad (7)$$

which represents a generalisation of Eq.(3) to molecular systems. By noting that the form factors $f_i(k)$ do not depend on the thermal average $\langle . \rangle$, we can rewrite the Debye formula into:

$$I(k) = \rho \sum_{ij} \sqrt{x_i x_j} \sum_{a_i b_j} f_{a_i}(k) f_{b_j}(k) S_{a_i b_j}^{(M)}(k) \quad (8)$$

which is convenient to recalculate the scattered intensity from the atom-atom pair correlation functions and the corresponding atom-atom structure factors. It is interesting to note that this expression is similar to the Pings-Waser (PW) formula[41] generically used by many authors, but which does not contain the intra-molecular part $w_{ab}(k)$. The present derivation shows both the origin of this term and how to incorporate this contribution into the PW expression through the correct expression Eq.(7). The strict PW formula is recovered by setting $W_{ab}(k) = \delta_{ab}$. The expression in Eq.(8) applies both for Xray and neutron scattering, when appropriate form factors are used. In the case of neutron scattering, $I(k)$ represents only the [inelastic](#) part of the scattering.

4.2 Application to the aqueous-1propanol mixtures

4.2.1 X-Ray scattering

We now compute the Xray scattering intensity from various atom-atom pair correlation functions and structure factors shown in Fig.2. The form factors are taken from the scattering data[42]. Fig.7 shows the total $I(k)$, as well as the 3 species-species contributions, namely water-water (blue), propanol-propanol (green) and water-propanol (magenta) contributions to $I(k)$. The dashed red line represent the negative of the sum of water-water and propanol-propanol contributions, which should match the magenta curve if exact cancellation should occur, which is seen to be the case in the pre-peak region. From the main panel of Fig.6, it is clearly seen that each of these contributions in the pre-peak region are 2 orders of magnitude larger than the total $I(k)$. However, the total contribution totally cancels the pre-peak, as can be seen in the expanded view of $I(k)$ reported in the top inset. This inset shows that only the 1propanol and water main peak are dominant, at $k \approx 0.65 \text{\AA}^{-1}$ and $k \approx 1.45 \text{\AA}^{-1}$, respectively. This cancellation is a striking result for several reasons. First of all, it is consistent with the known absence of pre-peak in the experimental Xray scattering data for this particular system Ref.[33]. Secondly, in order for the cancellation of such huge pre-peak contribution to happen, despite the fact that experimental form factors are used in conjunction with calculated structure factors, there must be a fine tuned adjustment of these cancellations. This fact proves that domain order is a very robust physical phenomena.

Then, if one considers the relative good agreement between the calculated $I(k)$ and the experimental one, as shown in the lower inset of Fig.7, and con-

sidering the fact that the form factors are taken from the experimental data, this agreement enforces the hypothesis that the simulated atom-atom structure factors must be close to the experimental data - if such data could be measured. Indirectly, it confirms that the classical model representation must be good enough to provide the observed cancellation. Finally, it is important to realise that the absence of the pre-peak in the experimental data does not allow to infer the existence of domain correlations in each of the partial contributions, since these cannot be directly observed individually. It would then seem that the existence of the domain-domain correlations can only be predicted from theory and apparently against direct experimental observation.

The lower inset of Fig.7 shows a comparison between the calculated $\Delta I(k)$ and the Xray data from Ref.[33] (shown in blue). It is seen that the agreement is quite fair, including in the pre-peak region. The agreement is better on the various peak positions than in the data itself, which implies that the size of the molecules are well described by the models but their distribution is slightly dephased with respect to real one. The data reported in Ref.[33] is $\Delta I(k) = I(k)/I_{id}(k) - 1$, where $I_{id}(k)$ corresponds to the ideal part of the expression in Eq.(8), in other words when the structure factors $S_{ab}(k)$ in Eq.(7) are replaced by the first term in this equation, namely $w_{ab}(k)$.

It is interesting to see how domain order affect the scattered intensity. For this, we select in Eq.(8) the k-vectors under the pre-peak contributions, where only the species-species contributions are seen and all atom-atom details are washed out. For this range of k-vectors, the various atom-atom structure factors of a given species pair are strictly similar:

$$S_{a_i b_j}(k) = S_{i_j}(k) \quad \text{for } 0 < k < k_D \quad (9)$$

where k_C is the maximum k-vector for which the domain order pre-peak is numerically distinctively defined. For this k-vector range, the Debye expression in Eq.(8) becomes

$$I(k) = \rho \sum_{ij} \sqrt{x_i x_j} F_i(k) F_j(k) S_{i_j}(k) \quad \text{for } 0 < k < k_C \quad (10)$$

where the effective form factor functions $F_i(k)$, which depend now on species, rather than atoms are defined as:

$$F_i(k) = \sum_{a_i} f_{a_i}(k) \quad (11)$$

This expression is very similar to the form factor one would get in case of approximating a super-atom made of all the atoms inside a single molecule[46]. This type of transformation is used to describe the methyl and methylene group as super atoms, where the form factor of the united atom is approximated as $f_M = f_C + n f_H$, and f_C and f_H are the form factors of the carbon and hydrogen atoms, respectively, with $n = 2, 3$ for the methylene and methyl pseudo atoms, respectively.

What Eq.(10) tells us is that pre-peak k-vector region is dominated by scattering of the molecular species as pseudo-atoms, indifferently to the atomic details. In that, it is strictly similar to the ionic liquid model, with only 2 mono-atomic species, with the appropriate pseudo-atom form factor $F_i(k)$. It is interesting to see that, for a binary component, the expression in Eq.(10) is similar to the Bathia-Thornton structure factor S_{NN} in Eq.(4), with $I(k) = \rho [F_1^2 S_{11} + F_2^2 S_{22} + 2F_1 F_2 S_{12}]$, for $0 < k < k_D$.

4.2.2 Neutron scattering

Neutron scattering necessitates that some of the atoms are replaced by their heavier isotopes, which is easier to perform when it is the hydrogen atom which is replaced by deuterium (or tritium). A specificity of form factors for neutron scattering is that these are constants independent of k-vector. This can be explained by the fact that, in r-space, the spread of form factor is so small that it can be considered a Dirac delta function, which makes its Fourier transform a k-independent constant, weighted by the atom-dependent amplitude[42].

In our case, we have tried the 4 possible combinations, when the water hydrogens H_W and/or the 1propanol hydroxyl group hydrogen H, can be replaced by their deuterated version D_w and D , respectively. Their scattering amplitudes are, -3.739 and 6.671[42]. Fig.8 shows the 4 neutron scattering intensities for cases when both the water and 1propanol hydrogens are deuterated, shown in full lines labelled (D_W, D) , when water is deuterated but not 1propanol, (D_w, H) in dotted lines, when water is not deuterated but 1propanol is, (H, D) in dashed lines and finally when none are deuterated, (H, H) in big dashed lines. In all 4 cases, there is a clear compensation between the various species-species contributions, as illustrated by the main panel, but not all of them lead to a total compensation of the pre-peak contributions, as illustrated in the inset. Only the 2 cases where water is deuterated, namely (D_W, D) and (D_w, H) , lead to an $I(k)$ without pre-peak and with the Orstein-Zernike like Lorentzian shape predicted by small angle neutron scattering experiments [43] when only water is deuterated. Conversely, the cases (H_W, D) and (H_W, H) where water is not deuterated lead to an observable pre-peak in the scattered intensity. Since there is no experimental data for the case when the 1propanol is deuterated, the present finding is theoretical. However, we note that most experimental cases are conducted when water is deuterated[5, 43, 44], hence supporting the finding in the present case. The incomplete cancellation of the pre-peak in case when water is not deuterated does not outrule the mechanism of domain ordering suggested in the present work, since Fig.8 shows that considerable compensation still happens. Rather, it suggests that the local inhomogeneity of the mixture could be detected by neutron scattering through appropriate weighting of the deuteration ratios.

5 Discussion

Several important consequences of the present study are worth re-considering.

The results above indicate that atom-atom correlations contain important information about domain-segregation which do not appear in the $I(k)$ obtained from scattering experiments. However, atom-atom correlation functions are not primary experimental observables, unlike $I(k)$. Although there are several strategies to uncover partial atomic structure factors $S_{ij}(k)$ from combining different types of $I(k)$, such as deuteration techniques for example, one wonders how the missing information in $I(k)$ can be restituted in the $S_{ij}(k)$ by any of such procedures. This shortcoming may explain why long range domain oscillatory correlations were never been reported from experimental $I(k)$. This observation implies that very specific types of scattering experiments might be required, and this could represent potentially important future studies.

Micro-segregation is analogous to charge order, in that the segregated domains are disposed in quasi alternate fashion -a checker board type order, in order to maximize the segregation, without leading to full phase separation. However, charge order concerns particle with fixed shapes, and occurs at the level of the particles themselves. In contrast, domain order concerns fuzzy molecular domains, with a certain degree of cross mixing which depends on the nature of the interactions. This is the reason why domain order is only observed in the long range part of the pair correlation functions. One can imagine domain order as being a smooth distortion of charged particles into fuzzy domain, hence going from a particle representation into a field representation. Strictly speaking, domain order is the field representation of charge order.

There is an important difference concerning the valence of the particle charges, which dictates charge order, and the domain valence, which dictates domain ordering. Indeed, like-charges repel each other while unlike-charges attract each other, leading to a large peak in the cross correlation function (Fig.1) . Conversely, in domain ordering, it is the like-correlations which exhibit the high peak at atomic contact, while cross correlations are depressed at contact. In terms of interactions, if a strict mapping with the Coulomb interactions should be made, this behaviour would correspond to *pure imaginary charges*. If a ionic liquid with imaginary charges would be used, it will lead to immediate demixing of each valence. Therefore, one requires a supplementary mechanism to maintain the particles into charge order. This mechanism is provided here through the hydrophobic-hydrophilic interaction balances, which maintain the domain order. Moreover, domain ordering is seen as a part of the atom-atom correlations, namely the long range part. In order to describe this contribution, one could resort to a field theory description, by assigning a phase to each of the fields corresponding to atom-atom distribution functions.

It is interesting that the demonstration of domain order requires extensive computer simulations, nearly at the edge of what can be done in desktop PC-type workstations. Moreover, it seems reasonable to think that most of soft-matter system experience such domain order at various degrees of extent. In view of the computer power required in the present case of aqueous-1propanol

mixture, a system which cannot be considered as particularly challenging, one wonders at the type of resources that could be required to account for domain order in simulation of realistic systems as those found in soft-matter. Conversely, one wonders how much importance domain order can have in such system, and to what extent it can be neglected. These are subjects for subsequent investigations, which are newly opened by the present investigation.

Eqs.(10,11) contain the important information concerning pre-peak cancellation. It is interesting to observe that, in the present calculations, the structure factors have been obtained from computer simulation using approximate force fields, while the form factors are experimental one, corresponding to the real atomic groups in the molecules. Yet, the cancellation is as effective as in the experimental $I(k)$. This implies that there is an element of reality in the calculated atomic structure factors. The cancellation in $I(k)$ could provide an alternative new method to fine tune force fields directly with the experimental $I(k)$.

In the present paper, we have report the cancellation effects only for one concentration, namely $x=0.3$, in order to have a thorough analysis. However, this effect is universal for every concentration showing micro-segregation of the species. For the particular system studied here, micro-segregation with oscillatory long range tail of the correlations, is observed for all concentrations ranging from 0.1 to 0.7. This is less apparent for $x > 0.7$, since one observes small water clusters, as those we have reported in similar cases for other mixtures[11, 24, 25]. The scattering function $I(k)$ is very similar to that of pure 1propanol, as confirmed from experimental results[32, 33]. In addition, we would like to point out that homogeneous species micro-segregation happens also for non-aqueous mixtures, such as benzene-ethanol mixtures[45], for example. A detailed report grouping different cases is in the works.

When going from simple ionic liquids, such as molten NaCl, to room temperature ionic liquids, such as ethylammonium-nitrate, for example, the particles change from simple charged atoms to complex molecules, which contain uncharged methyl and methylene groups[47, 48]. These groups perturb the global homogeneity of the charge ordering found in simple ionic liquids, and the loss of global homogeneity gives rise to a pre-peak both in the atom-atom structure factors and the total scattered intensity[17, 18, 47, 48]. Similarly, when going from molecular emulsions to micro-emulsions, we conjecture that the global domain order is perturbed by the change in the nature of the aggregates. Direct micelles contain extended water impregnated outer interface, sharply separated from the inner oily core[4]. Inverse micelles also have well separated polar inner cores from the fuzzy and hairy outer core made of the hydrophobic tails[7]. This is a sharp change in the nature of the type of aggregates found in molecular emulsions. We conjecture here that is this change which produces a non canceling pre-peak in the total scattered intensity. Demonstrating this conjecture would require computer simulations beyond desktop capabilities. Yet, many systems found in soft-matter or biomaterial context, contain structural aggregates similar to micelles[49, 50, 51]. The fact that scattering experiments in such systems are able to predict scattering pre-peak[51] does not necessarily imply that they can provide a better microscopic description. Indeed, there

are probably hidden cancellation mechanisms beneath the apparent pre-peak of micro-emulsions, which would require further investigations similar to that conducted herein. The microscopic relation between micelle structure and scattering data remains to be re-investigated in the light of the present finding. We conjecture that the present theoretical descriptions of micelle formation, which never take into account domain ordering, are analogous to the Debye-Huckel description of ionic liquids, which does not account for charge order, but describes correctly the screening of charges. A new theory of micro-emulsions, which accounts for domain order, is yet to be developed.

6 Conclusion

The most important conclusion of this work is the fact that micro-segregation in molecular emulsions induces domain order, which is a form of macroscopic homogeneity, rescaled at the level of the segregated domains as pseudo-molecular grains. Radiation scattering is sensitive to individual molecules, but not this homogeneous nanoscale heterogeneity, which is the principal reason why many scattering experiments cannot detect any pre-peak feature underlying the domain segregation. This apparent homogeneity is similar to that found in atomic ionic liquid, where the particles do not experience the random disordered distribution seen in simple binary mixtures, but the charge order dictated by the Coulomb interactions. It is this form of order-within-disorder, which produces the apparent homogeneity of these systems. Micro-segregated mixtures have the same type of order, hence they look more homogeneous than they actually are at molecular level, at least from the point of view of scattered radiations. This apparent homogeneity can be destroyed by super-structures such as micelles, which appear when going from molecular emulsions to micro-emulsions. This is not a simple change in the size of aggregates, as reported in the literature, but a topological change in the conformal structure of the aggregate, which in particular induces a change in the homogeneity of the system. **In addition, it would seem that selected deuteration could equally influence the status of the global homogeneity, as perceived by neutron scattering experiments.** Finally, we have emphasized the difference between computer simulations of aqueous mixtures, which are able to describe domain-segregation through the pre-peaks in the atom-atom structure factors, and the scattering experiments, **in particular Xray scattering**, where these pre-peaks get canceled, hence preventing the recovery of these features in the atom-atom structure factors which can be deduced from these experiments.

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Figure captions

- Fig.1 (a) Snapshot of charge order for the ionic liquid characterized by the parameters below the picture. (b) Pair correlation functions and corresponding BT functions (inset; see text). (c) Structure factors and corresponding BT functions (inset; see text). The red arrows indicates the pre-peak position.
- Fig.2 (a) Atom-atom pair correlation functions of the aqueous-1propanol 30% mixture. The functions are displayed into 2 different distance scale (as indicated by the blue arrows) separating the short and long range parts. the inset shows details of the correlations at atomic contact. Blue is for water-water correlations, magenta for propanol-propanol and green for cross correlations. The functions $g_{O_wO_w}(r)$, $g_{O_P O_P}(r)$ and $g_{O_W O_P}(r)$, corresponding to the correlations between the oxygen atoms of water and 1propanol, are highlighted in thicker lines. (b) Corresponding atom-atom structure factors with same line and color conventions. The red arrow indicates the position of the neat propanol pre-peak. The inset represent a zoom over the pre-peak part.
- Fig.3a-b The atom-atom functions and structure factors (inset) for (a) water-water and (b) oxygen(1propanol)-1propanol atoms.
- Fig3c-d The atom-atom functions and structure factors (inset) for (c) hydrogen(1propanol)-1propanol atoms and (d) methyl-methyl of 1propanol.
- Fig3e-f The atom-atom functions and structure factors (inset) for (e) oxygen(water)-1propanol atoms and (f) hydrogen(water)-1propanol atoms
- Fig.4 Snapshots of the systems for various sizes, for 30% 1propanol: (a) $N=2000$, (b) $N=16000$ and (c) $N=128000$, showing the segregation of the polar OH groups and the oily methyl groups (in cyan). The water oxygen and hydrogen atoms are shown in red and white, respectively, those of 1propanol in blue and gray, respectively, and the methyl/methylene groups are shown in cyan.
- Fig.5 System size dependence of the atom-atom pair correlation functions for 20% 1propanol (a) and corresponding structure factors (b), illustrated for the three oxygen-oxygen correlations, namely water-water (WW), 1propanol-1propanol (PP) and cross (WP). The data for system size $N=128000$ is shown in full lines, $N=16000$ in dotted lines and $N=2000$ in dashed lines. Corresponding WW correlations are colored in blue, cyan and purple, respectively, for PP correlations in green, yellow and grass, and cross WP correlations in magenta, red and brown, respectively. In (b), the structure factor of pure water is shown as thin black curve.

- Fig.6 Water model dependence illustrated for the oxygen atom correlation functions of the 30% 1propanol mixtures. The short and long range parts of the functions are shown in the left and right panels, respectively, with 2-different scales (as in Fig.2). For the TIP4P-2005 and SPC/E models, respectively, the functions $g_{O_w O_w}(r)$ are shown in blue and cyan, the functions $g_{O_w O_P}(r)$ in magenta and red, and the functions $g_{O_P O_P}(r)$ in green and jade. The inset in the right panel is a zoom on the first peaks.
- Fig.7 Xray scattering intensity for the 30% 1propanol in the aqueous mixture, as computed from collecting the atom-atom structure functions calculated in the N=128000 particles simulations, through Eq.(8). The main panel shows the 3 partial species-species contributions to $I(k)$ (blue for water, green for propanol and magenta for cross) and the calculated $I(k)$ in black (for the dotted red line, see text). The calculated I(k) is reproduced in magnified scale in the upper inset. The lower inset shows a comparison with experiments (shown in blue from Ref.[33]) in blue of the quantities $\Delta I(k) = k [I(k)/I_{Id}(k) - 1]$ (see text).
- Fig.8 Neutron scattering intensities for the 30% 1propanol in the aqueous mixture, for various deuteration cases, as computed from the atom-atom structure function calculated in the N=128000 particles simulations, through Eq.(8). The main panel shows the 3 partial species-species contributions to $I(k)$ (blue for water, green for propanol and magenta for cross) and the calculated $I(k)$ in black. The full, dotted, dashed and big-dashed lines are for the combination (D_w, DA) , (D_w, H_A) , (H_w, D_A) , (H_w, H_A) , respectively (notations explained in the text). The inset shows a zoom on the total I(k) for the various cases.

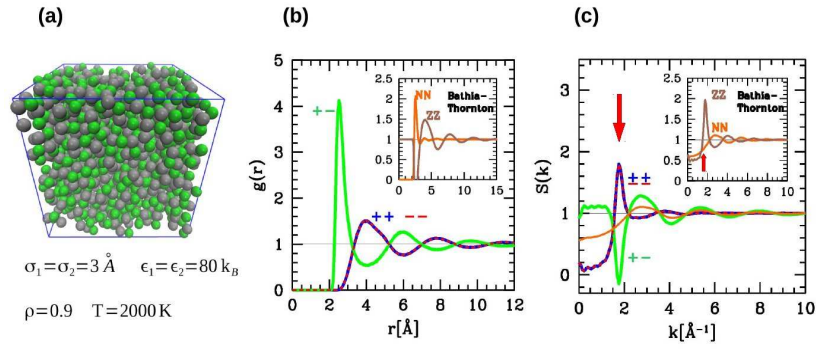


Fig.1. (a) snapshot of charge order for the ionic liquid characterized by the parameters below the picture. (b) Pair correlation functions and corresponding BT functions (inset; see text). (c) Structure factors and corresponding BT functions (inset; see text). The red arrows indicates the pre-peak position.

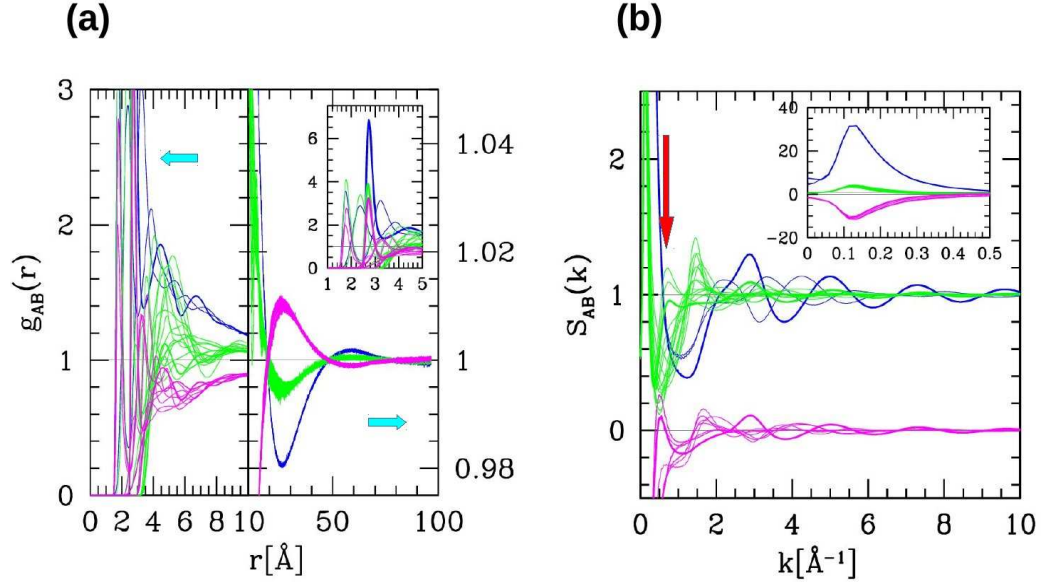


Fig.2. (a) Atom-atom pair correlation functions of the aqueous-1propanol 30% mixture. The functions are displayed into 2 different distance scale (as indicated by the arrows) separating the short and long range parts. the inset shows details of the correlations at atomic contact. Blue is for water-water correlations, green for propanol-propanol and magenta for cross correlations. The functions $g_{O_w O_w}(r)$, $g_{O_P O_P}(r)$ and $g_{O_W O_P}(r)$, corresponding to the correlations between the oxygen atoms of water and 1propanol, are highlighted in thicker lines. (b) Corresponding atom-atom structure factors with same line and color conventions. The inset represent a zoom over the pre-peak part.

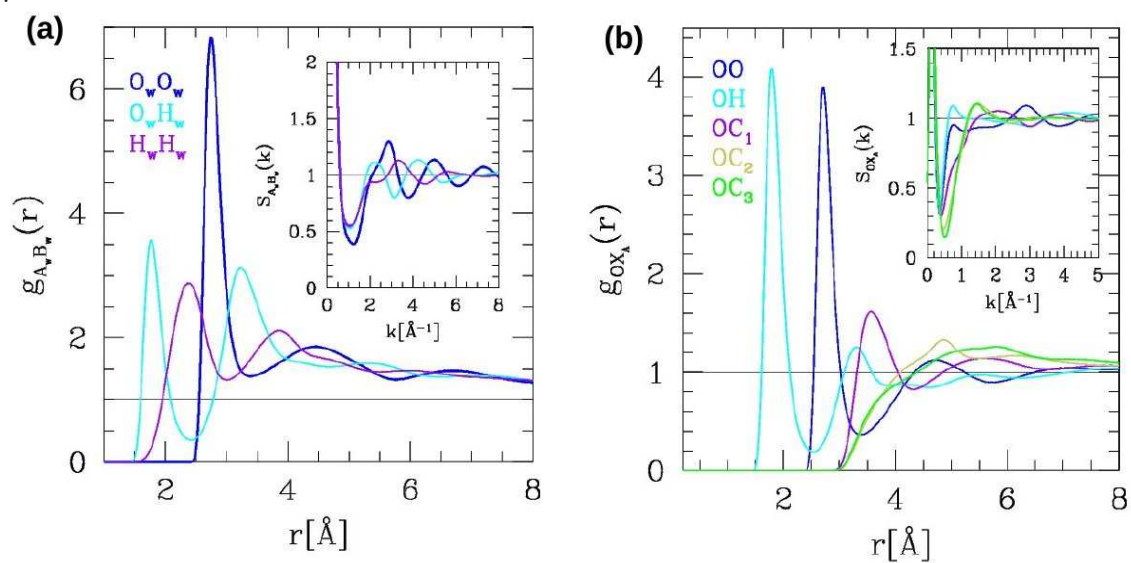


Fig.3a-b. The atom-atom functions and structure factors (inset) for (a) water-water and (b) oxygen(1propanol)-1propanol atoms.

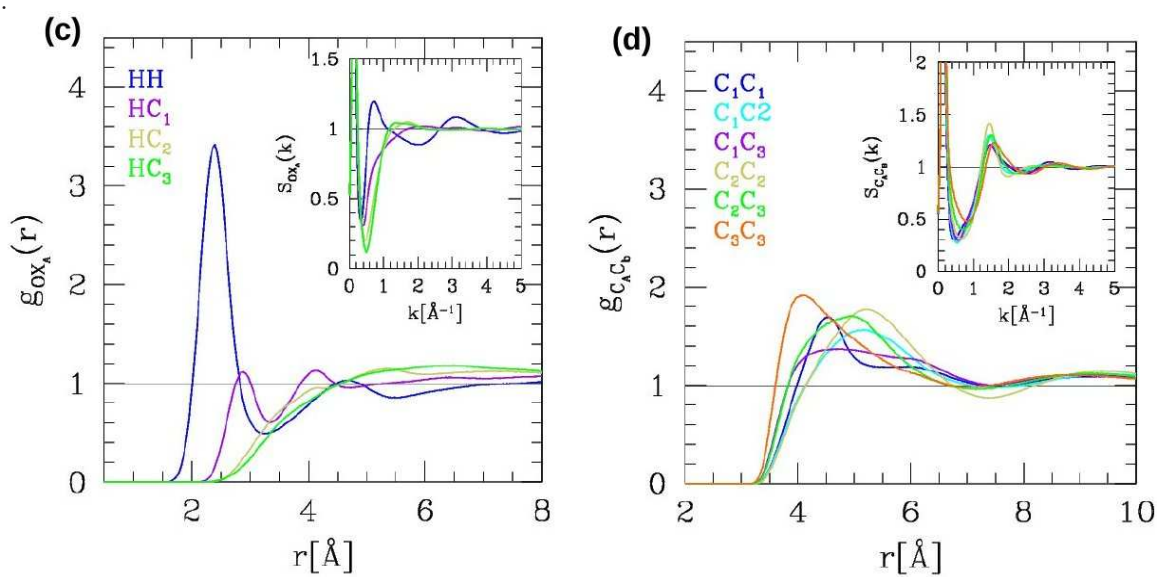


Fig.3c-d. The atom-atom functions and structure factors (inset) for (c) hydrogen(1propanol)-1propanol atoms and (d) methyl-methyl of 1propanol.

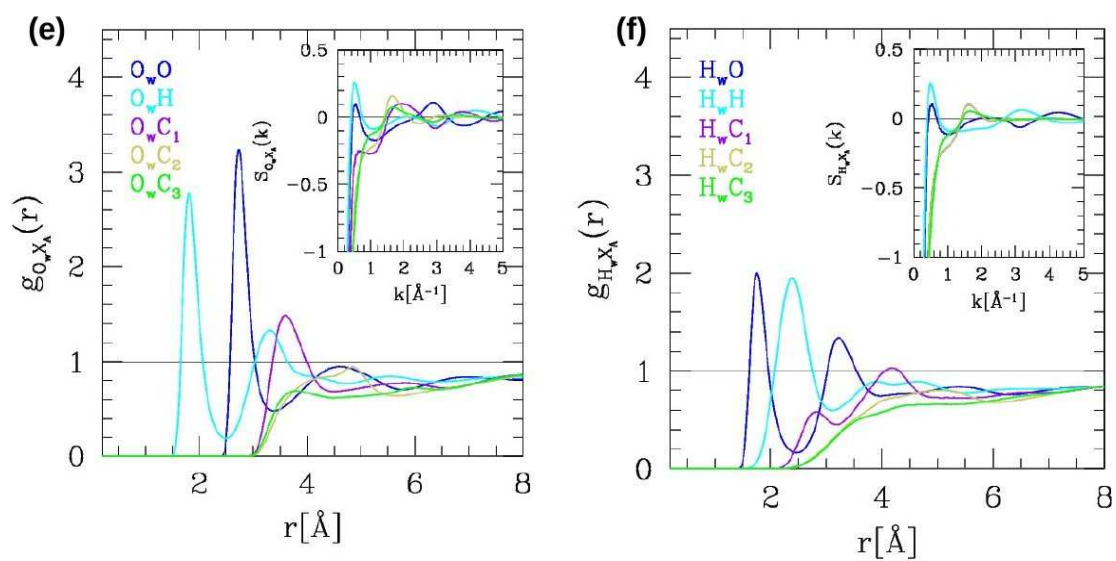


Fig.3e-f. The atom-atom functions and structure factors (inset) for (e) oxygen(water)-1propanol atoms and (f) hydrogen(water)-1propanol atoms

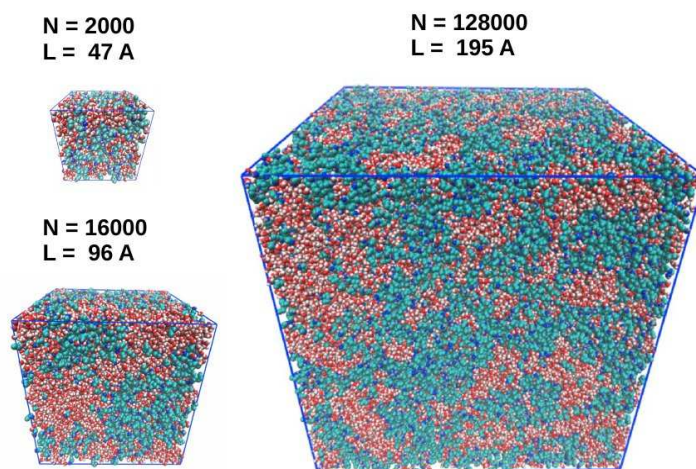


Fig.4. Snapshots of the systems for various sizes, for 30% 1propanol: (a) $N=2000$, (b) $N=16000$ and (c) $N=128000$, shown the segregation of the polar OH groups and the oily methyl groups (in cyan). The water oxygen and hydrogen atoms are shown in red and white, respectively, those of 1propanol in blue and gray, respectively, and the methyl/methylene groups are shown in cyan.

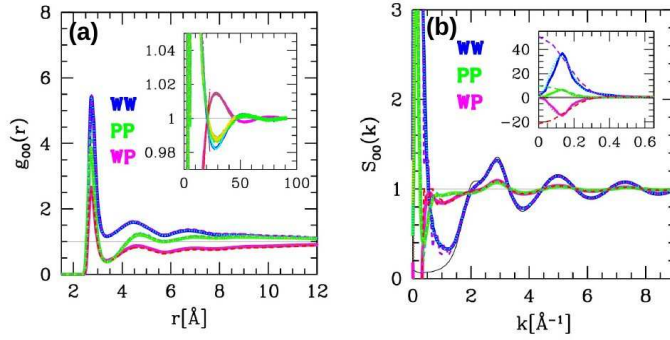


Fig.5. System size dependence of the atom-atom pair correlation functions for 20% 1propanol (a) and corresponding structure factors (b), illustrated for the three oxygen-oxygen correlations, namely water-water (WW), 1propanol-1propanol (PP) and cross (WP). The data for system size $N=128000$ is shown in full lines, $N=16000$ in dotted lines and $N=2000$ in dashed lines. Corresponding WW correlations are colored in blue, cyan and purple, respectively, for PP correlations in green, yellow and grass, and cross WP correlations in magenta, red and brown, respectively. In (b), the structure factor of pure water is shown as thin black curve.

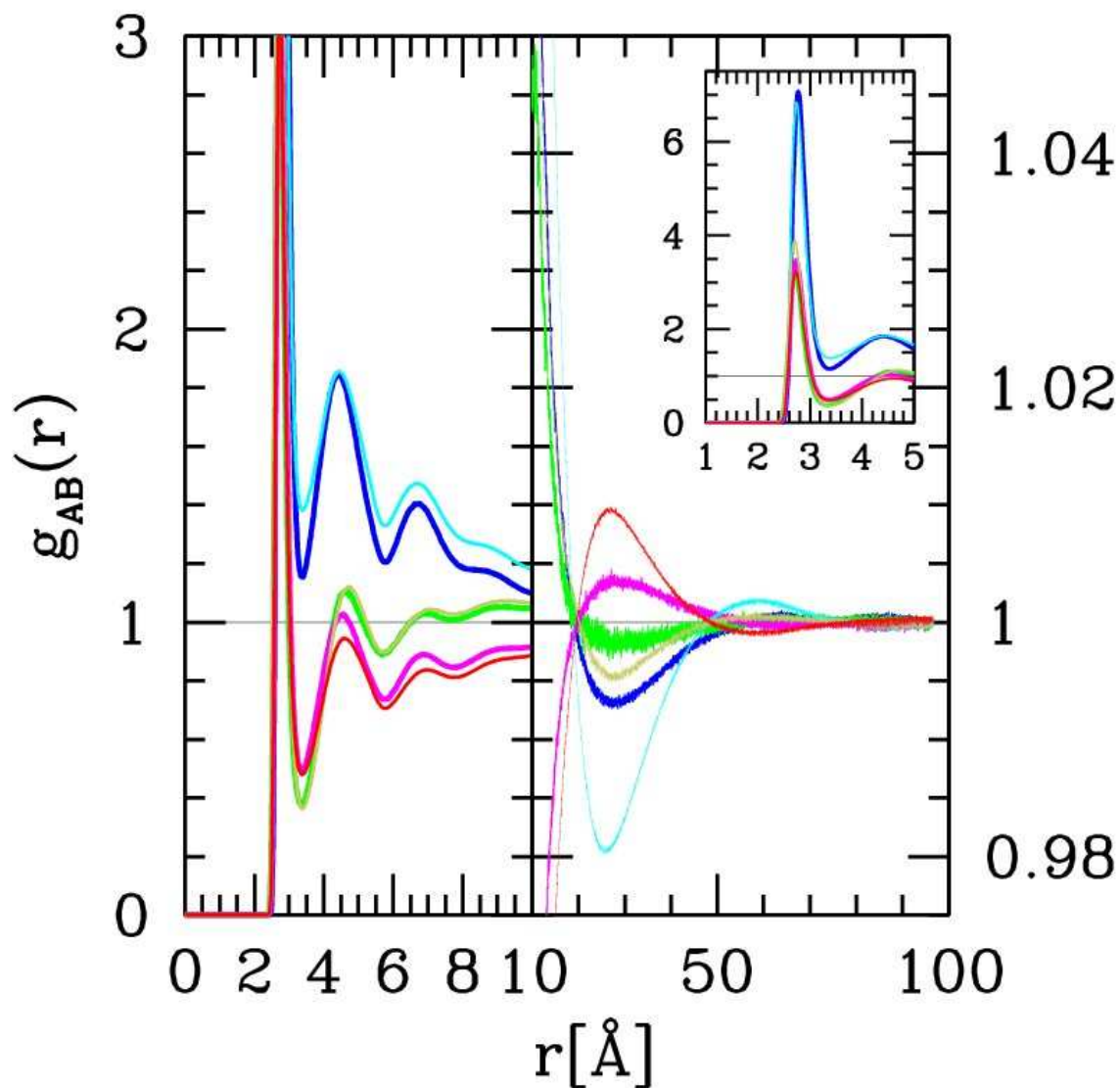


Fig.6. Water model dependence illustrated for the oxygen atom correlation functions of the 30% 1propanol mixtures. The short and long range parts of the functions are shown in the left and right panels, respectively, with 2-different scales (as in Fig.2). For the TIP4P-2005 and SPC/E models, respectively, the functions $g_{O_w O_w}(r)$ are shown in blue and cyan, the functions $g_{O_w O_P}(r)$ in magenta and red, and the functions $g_{O_P O_P}(r)$ in green and jade. The inset in the right panel is a zoom on the first peaks.

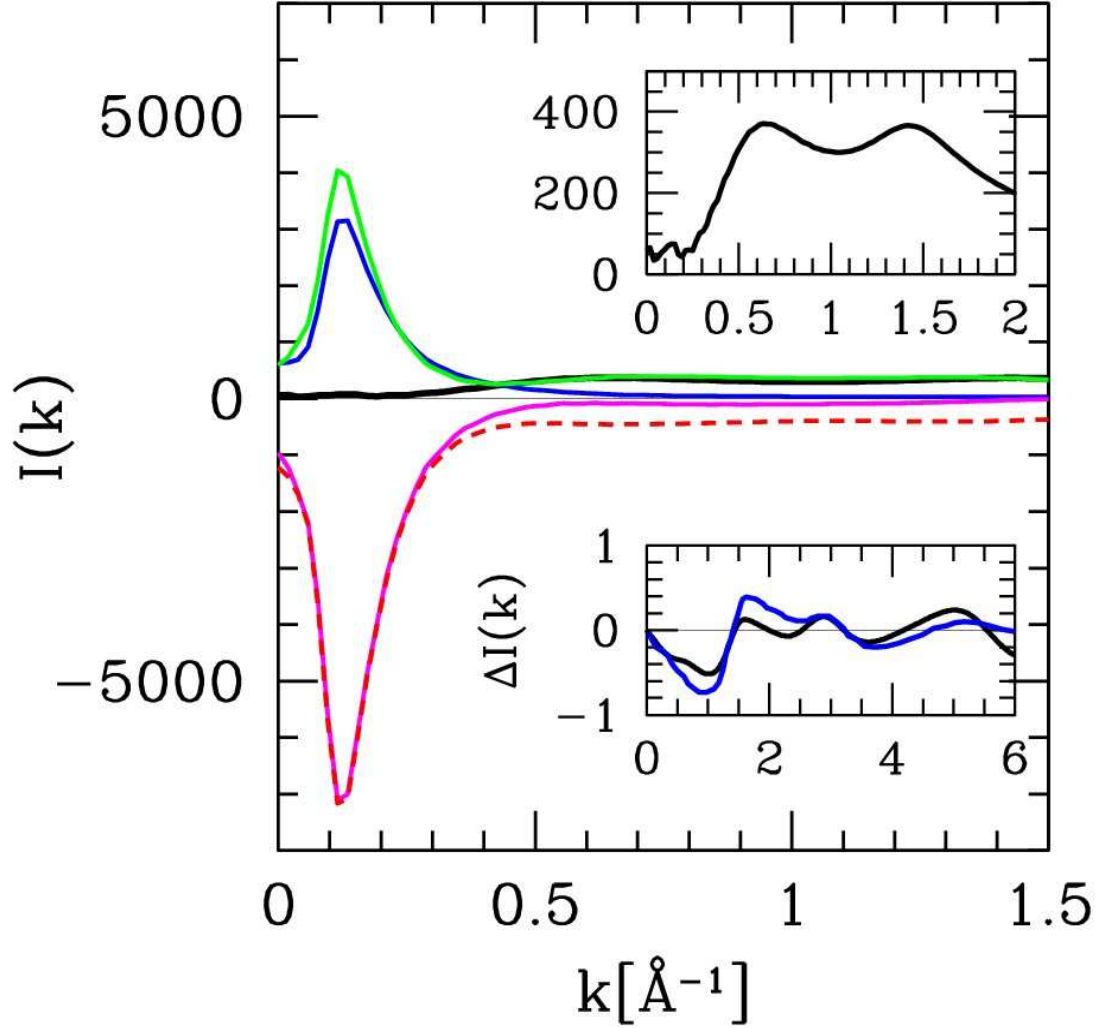


Fig.7. X-ray scattering intensity for the 30% 1propanol in the aqueous mixture, as computed from collecting the atom-atom structure functions calculated in the simulations, through Eq.(8). The main panel shows the 3 partial species-species contributions to $I(k)$ (blue for water, green for propanol and magenta for cross) and the calculated $I(k)$ in black (for the dotted red line, see text). The calculated $I(k)$ is reproduced in magnified scale in the upper inset. The lower inset shows a comparison with experiments (shown in blue from Ref.[33]) of the quantities $\Delta I(k) = k [I(k)/I_{Id}(k) - 1]$ (see text).

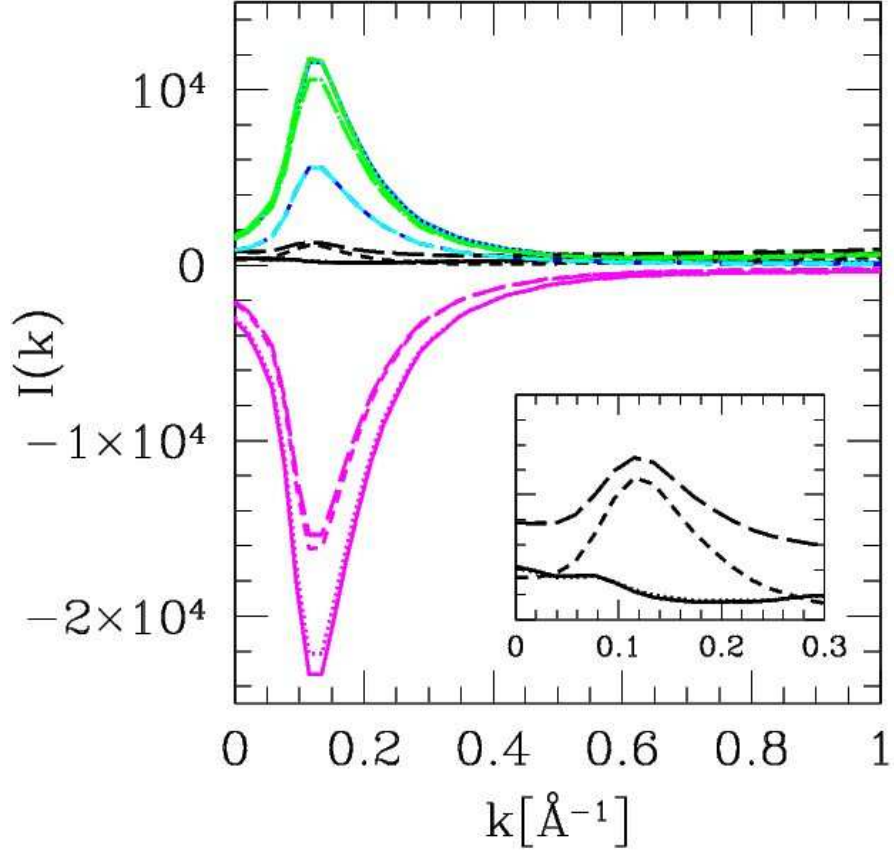


Fig.8. Neutron scattering intensities for the 30% 1propanol in the aqueous mixture, for various deuteration cases, as computed from the atom-atom structure function calculated in the $N=128000$ particles simulations, through Eq.(8). The main panel shows the 3 partial species-species contributions to $I(k)$ (blue for water, green for propanol and magenta for cross) and the calculated $I(k)$ in black. The full, dotted, dashed and big-dashed lines are for the combination (D_w, DA) , (D_w, H_A) , (H_w, D_A) , (H_w, H_A) , respectively (notations explained in the text). The inset shows a zoom on the total $I(k)$ for the various cases.