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H₂ emission from non-stationary magnetized bow shocks

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ABSTRACT

When a fast moving star or a protostellar jet hits an interstellar cloud, the surrounding gas gets heated and illuminated: a bow shock is born that delineates the wake of the impact. In such a process, the new molecules that are formed and excited in the gas phase become accessible to observations. In this paper, we revisit models of H₂ emission in these bow shocks. We approximate the bow shock by a statistical distribution of planar shocks computed with a magnetized shock model. We improve on previous works by considering arbitrary bow shapes, a finite irradiation field and by including the age effect of non-stationary C-type shocks on the excitation diagram and line profiles of H₂. We also examine the dependence of the line profiles on the shock velocity and on the viewing angle: we suggest that spectrally resolved observations may greatly help to probe the dynamics inside the bow shock. For reasonable bow shapes, our analysis shows that low-velocity shocks largely contribute to H₂ excitation diagram. This can result in an observational bias towards low velocities when planar shocks are used to interpret H₂ emission from an unresolved bow. We also report a large magnetization bias when the velocity of the planar model is set independently. Our 3D models reproduce excitation diagrams in BHR 71 and Orion bow shocks better than previous 1D models. Our 3D model is also able to reproduce the shape and width of the broad H₂ 1–0S(1) line profile in an Orion bow shock (Brand et al. 1989).

Key words: shock waves – Herbig–Haro objects – ISM: jets and outflows – ISM: molecules.

1 INTRODUCTION

Jets or winds are generated in the early stages and the late phases of stellar evolution. The impact of high-velocity flows on the interstellar medium (ISM) creates a shock. When the star moves with respect to the surrounding gas, or when the tip of a jet penetrates the ISM, the shock working surface assumes a curved shape called ‘bow shock’.

The angle between the impinging gas velocity and the normal to the shape can vary along this bow. It also affects the angle of the ambient magnetic field. As a result, the local effective entrance velocity and the transverse magnetic field change along the shock working surface. This leads to differences in the local physical and chemical conditions, which cause varying emission properties throughout the bow shock.

As a result, the global emission spectrum of a bow shock is expected to differ from that of a 1D plane-parallel shock. Accurate modelling of the emission properties of bow shocks is thus an important goal if we wish to retrieve essential properties of the sys-

tem from observations, such as the propagation speed, the age, the environment density and the magnetic field. Molecular hydrogen is a particularly important tracer, as it dominates the shock cooling up to the dissociation limit (if the pre-shock medium is molecular), and it emits numerous lines from a wide range of upper energy levels within a single spectrometer setting [in the *K*-band for rovibrational $\Delta v = 1$ lines; in the mid-infrared (IR) range 8–28 μm for the first pure rotational lines]. In principle, the H₂ emission originating from bow shocks can be predicted by performing 2D or 3D numerical simulations, but the latter have been so far limited to single-fluid ‘jump’ shocks, J-type (e.g. Suttner et al. 1997; Raga et al. 2002). Up to now they cannot treat ‘continuous’ C-type shocks, where ion–neutral decoupling occurs in a magnetic precursor (Draine & McKee 1993). Such situation is encountered in the bow shock whenever the entrance speed drops below the magnetosonic speed in the charged fluid. To address this case, a second approach to predict H₂ emission from bow shocks is to prescribe a bow shape and treat each surface element as an independent 1D plane-parallel J-type or C-type shock, assuming that the emission zone remains small with respect to the local curvature. This approach was first introduced by Smith & Brand (1990a) and Smith, Brand & Moorhouse (1991a) using simplified equations for the 1D

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shock structure and cooling. The validity of this approach was recently investigated by Kristensen et al. (2008) and Gustafsson et al. (2010) using refined 1D steady-state shock models that solve the full set of magnetohydrodynamical equations with non-equilibrium chemistry, ionization and cooling.

Kristensen et al. (2008) studied high angular resolution H_2 images of a bow shock in the Orion BN–KL outflow region, performing several 1D cuts orthogonal to the bow trace in the plane of the sky. They fitted each cut separately with 1D steady shock models proposed by Flower & Pineau des Forêts (2003). They found that the resolved width required C-shocks, and that the variation of the fitted shock velocity and transverse magnetic field along the bow surface was consistent with a steady bow shock propagating into a uniform medium. This result provided some validation for the ‘local 1D-shock approximation’ when modelling H_2 emission in bow shocks, at least in this parameter regime. Following this idea, Gustafsson et al. (2010) built 3D stationary models of bow shocks by stitching together 1D shock models. They then projected their models to produce maps of the H_2 emission in several lines that they compared directly to observations. They obtained better results than Kristensen et al. (2008) thanks to the ability of the 3D model to account both for the inclination of the shock surface, with respect to the line of sight, and the multiple shocks included in the depth of their 1D cuts. The width of the emission maps was better reproduced.

In this paper, we extend Gustafsson et al. (2010)’s works on H_2 emission by computing the excitation diagram and line profiles integrated over the bow, and by considering the effect of short ages where C-shocks have not yet reached steady state. Our method also increases the scope of Gustafsson et al. (2010) to arbitrary bow shapes (we do not restrict the bow shape profile to power laws). Using time-dependent simulations, Chièze, Pineau des Forêts & Flower (1998) discovered that young C-type shocks, the age of which is smaller than the ion crossing time, are composed of a magnetic precursor and a relaxation layer separated by an adiabatic J-type front. Lesaffre et al. (2004b) later showed that the magnetic precursor and the relaxation layer were truncated stationary models of C-type and J-type shocks, respectively. In this work, we make use of these CJ-type shocks to explore the age dependence of the H_2 emission. Non-steady shocks are more likely to occur in low-density media, where the time-scales are generally longer than those driving the mechanisms of these shocks: hence, we consider lower densities than Gustafsson et al. (2010), down to 100 cm^{-3} . As in Lesaffre et al. (2013), we include the grain component as part of the charged fluid, which significantly lowers the magnetosonic speed. In addition the Paris–Durham code (Flower et al. 2003; Flower & Pineau des Forêts 2015), recently improved by Lesaffre et al. (2013), now allows to consider finite ultraviolet (UV) irradiation conditions and we use a standard interstellar irradiation field of $G_0 = 1$ (Draine 1978) throughout this paper. This lowers slightly further the magnetosonic speed as the ionization degree/fraction increases but we checked it does not introduce critical changes for the H_2 emission properties. The lower magnetosonic speed above which no C-shock propagates and the truncated precursor in young CJ-type shocks both act in a way so that they give more weight to J-type shocks compared to Gustafsson et al. (2010), who had their J-type shocks H_2 emission dimmed by dissociation above $\simeq 15\text{--}20 \text{ km s}^{-1}$ due to the larger densities. Finally, we also investigate the line profiles that were not examined by Gustafsson et al. (2010).

We study how the geometry influences the distribution of shock entrance velocity and transverse magnetic field in Section 2. We

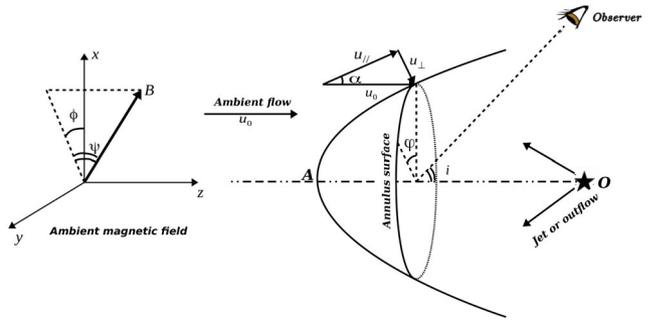


Figure 1. Morphology of a magnetized bow shock in the frame of a star or a jet. The direction of the magnetic field is expressed by the angles ψ and ϕ . The observer lies at an angle i to the z -axis in the Oxz plane.

present our grid of planar shock models at finite ages in Section 3. In Section 4, we combine the planar shock models to build 3D models of bow shocks. We examine the observable H_2 excitation diagram and the potential biases that arise when 1D models are fit to intrinsically 3D models. We apply our 3D model to constrain parameters of the BHR 71 bipolar outflow and for a bow shock in Orion. Finally, we study the properties of H_2 line profiles and show how it can be used to retrieve dynamical information. We summarize and conclude in Section 5.

2 THE MODEL

As in Gustafsson et al. (2010), we assume that the 3D bow shock is made of independent planar shocks. In fact, we neglect the curvature effects and the friction between different 1D shock layers, the gradients of entrance conditions in the planar shock models and the possible geometrical dilatation in the post-shock: our approximation is valid as long as the curvature radius of the bow shock is large with respect to the emitting thickness of the working surface.

2.1 Geometry and coordinate system

We consider an axisymmetric 3D bow shock around a supersonic star (or a jet) travelling at the speed of $-u_0$ relative to an ambient molecular cloud assumed to be at rest. In the frame of the star, the impinging velocity is therefore uniform and equal to u_0 . The apex of the bow shock is at position A and the star (or a reference point in the jet) at position O (Fig. 1). The axis of symmetry chosen as the z -axis is therefore along the direction (AO) . The observer is assumed to lie in the (Oxz) plane and the y -direction is chosen such that $(Oxyz)$ is direct. The axisymmetric shape of the bow shock is completely determined by the function $x = f(z)$. The local position along the planar shock can be specified by the angle between the incoming flow and the tangent to the surface $\alpha = \arccos(u_{\perp}/u_0)$ (see Smith & Brand 1990a, fig. 1), and by the angle ϕ between the radius and the x -axis in the (xy) plane of projection.

The impinging velocity can be expressed as $u_0 = \hat{t}u_{\parallel} + \hat{n}u_{\perp} = u_0(\hat{t} \cos \alpha + \hat{n} \sin \alpha)$, where $\hat{n}(-\cos \alpha \cos \phi, -\cos \alpha \sin \phi, \sin \alpha)$ is the unit normal vector pointing inside the bow and $\hat{t}(\sin \alpha \cos \phi, \sin \alpha \sin \phi, \cos \alpha)$ is the unit tangent vector along the working surface. The effective shock speed at the local point is $v_s = u_{\perp} = u_0 \sin \alpha$. Away from the axis of symmetry, the effective entrance velocity into the shock decreases down to the sound speed c_s in the ambient medium. Beyond this point, the shock working surface is a cone of opening angle $\alpha_0 = \arcsin(c_s/u_0)$, wider as the terminal velocity is closer to the sound speed. In this paper, we

mainly focus on the ‘nose’ of the bow shock where $u_{\perp} > c_s$, and we neglect the emission from these conical ‘wings’, or we simply assume that they fall outside the observing beam.

The orientation of the line of sight of the observer in the (xz) plane is defined by the inclination angle $i: \hat{\mathbf{l}}(\sin i, 0, \cos i)$. The ambient uniform magnetic field is identified by the obliqueness ψ and the rotation $\phi: \mathbf{B}/B_0 = (\cos \psi \cos \phi, \cos \psi \sin \phi, \sin \psi)$. For each bow shock, ψ and ϕ are fixed.

2.2 Distribution function of the local planar shock velocity

This section aims at computing the fraction $P(u_{\perp})du_{\perp}$ of planar shocks with an entrance planar shock u_{\perp} within du_{\perp} in a given bow shock shape. This will help us building a model for the full bow shock from a grid of planar shocks.

Considering the shock geometry as prescribed in Section 2.1, we aim at obtaining the formula for the unit area ds corresponding to these shocks as a function of du_{\perp} .

The norm of a segment dl on the (x, z) section of the bow shock surface is

$$dl = \sqrt{dx^2 + dz^2} = \sqrt{1 + f'^2(x)}dx. \quad (1)$$

Now, we take that segment and rotate it around the z -axis, over a circle of radius x . The area (ds) of the bow shock’s surface swept by this segment can be expressed as

$$ds = 2\pi x dl = 2\pi x \sqrt{1 + f'^2(x)}dx. \quad (2)$$

Note that the angle α defined in Fig. 1 is also the angle between the segment dl and the differential length dz along the z -axis. Then, the tangent of the angle α can be set as

$$\tan \alpha = \frac{dx}{dz} = \frac{1}{f'(x)}. \quad (3)$$

In all generality, the relationship between α and u_{\perp} will be realized according to whether we consider the shock in the ambient medium or in the stellar wind or jet. Then, ds as a function of du_{\perp} can be obtained by replacing that relation into equation (2). However, we will only focus here on the bow shock in the ambient material. In that case, the norm of the effective velocity (i.e. the effective normal velocity u_{\perp}) is related to the norm of the incident velocity u_0 through the angle α as

$$u_{\perp} = u_0 \sin \alpha \rightarrow \alpha = \arcsin \left(\frac{u_{\perp}}{u_0} \right). \quad (4)$$

Now, x can be expressed as a function of u_{\perp} by substituting equation (4) into equation (3):

$$\begin{aligned} \tan \left[\arcsin \left(\frac{u_{\perp}}{u_0} \right) \right] &= \frac{1}{f'(x)} \rightarrow x = f'^{-1} \\ &\times \left\{ \cot \left[\arcsin \left(\frac{u_{\perp}}{u_0} \right) \right] \right\} = g(u_{\perp}). \end{aligned} \quad (5)$$

In equation (2), the unit area ds of the shock is a function of the coordinate x , while in equation (5), the coordinate x is a function of the effective shock velocity u_{\perp} . To sum up, we can obtain ds as a function of u_{\perp} :

$$\begin{aligned} ds(u_{\perp}) &= 2\pi g(u_{\perp}) \sqrt{1 + \cot^2 \left[\arcsin \left(\frac{u_{\perp}}{u_0} \right) \right]} g'(u_{\perp}) du_{\perp} \\ &= \pi \sqrt{1 + \cot^2 \left[\arcsin \left(\frac{u_{\perp}}{u_0} \right) \right]} d[g^2(u_{\perp})]. \end{aligned} \quad (6)$$

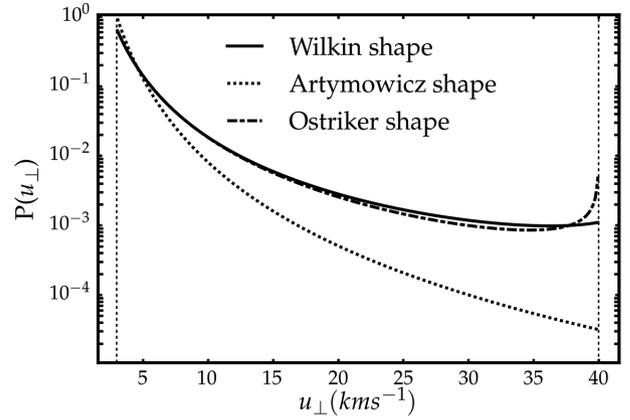


Figure 2. Statistical distributions of 1D planar shock along the bow shock obtained for various bow shock shapes. These distributions are dominated by low-velocity shocks.

Finally, the distribution function of shock velocities is simply defined as

$$P(u_{\perp}) = \frac{ds(u_{\perp})}{\int_{c_s}^{u_0} ds}, \quad (7)$$

so that the integral of $P(u_{\perp})$ is normalized to unity. Note that the lower limit of the integral is the sound speed in the ambient medium. This implicitly assumes that we only focus on the ‘nose’ of the bow shock, where $u_{\perp} < c_s$. One could include the conical ‘wings’ by adding a Dirac distribution $\delta(u_{\perp} = c_s)$. Conversely, one could also narrow down the integration domain if the beam intersects a smaller fraction of the bow. We implemented this mathematical formulation numerically to compute the distribution P from an arbitrary input function f . We obtained results that agree with those obtained using the analytical expressions when the shape assumes a power-law dependence $z \sim x^{\beta}$.

2.3 Example of bow shock shapes

In an elegant and concise paper, Wilkin (1996) derived an analytical description of the shape of a bow shock around a stellar wind when it is dominated by the ram pressure of the gas. When dust grains control the dynamics of the gas, the main forces are the gravitation pull and the radiation pressure from the star and the shape of the shock should then be very close to the grains avoidance parabola derived in Artymowicz & Clampin (1997). In fact, the ISM is a mixture between gas and dust grains, so the actual bow shock shape should lie in-between.

For the dust-dominated case, the bow shock shape is the Artymowicz parabola expressed as $z = \frac{1}{4R_0}x^2 - R_0$ with $R_c = 2R_0$ the curvature radius at apex, R_0 being the star–apex distance. In the gas-dominated case, the bow shock shape follows the Wilkin formula $R = \frac{R_0}{\sin \theta} \sqrt{3\sqrt{1 - \theta \cot \theta}}$ with $R_c = 5/4R_0$ the curvature radius.

Finally, in the case of the tip of a jet, Ostriker et al. (2001) showed that the shape of the bow shock should be cubic $z = x^3/R_0^2 - z_j$ with an infinite curvature radius (and R_0 and z_j are length-scales parameters). Fig. 2 displays the distributions obtained for various bow shock shapes. Note that low-velocity shocks ($u_{\perp} \leq 15 \text{ km s}^{-1}$) always dominate the distribution: this stems from the fact that the corresponding surface increases further away from the axis of symmetry, where entrance velocities decrease. The distribution for the

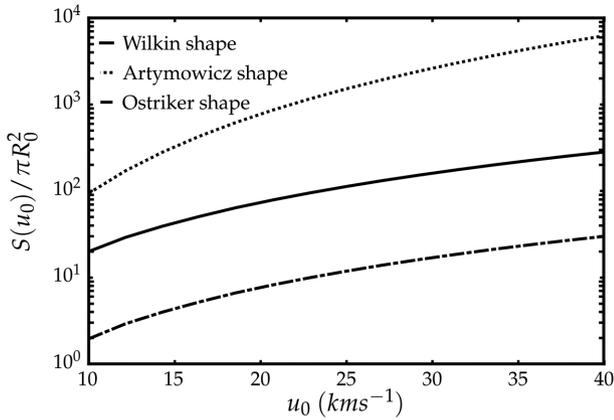


Figure 3. Total surface of the bow shock for various bow shock shapes and terminal velocities, in units of πR_0^2 , where R_0 is the length-scale parameter of the bow (on the order of the nose’s curvature radius).

cubic shape has a spike due to its flatness (infinite curvature radius) near the apex. The Wilkin shape has a cubic tail but a parabolic nose. In Fig. 3 we display the dimensionless surface $S/\pi R_0^2$, where S is the total surface of the bow shock and R_0 is an estimate of the radius of the nose of the bow. For elongated shapes such as the parabolic shape, the total surface can be much bigger than the nose cross-section πR_0^2 . We will subsequently essentially consider an ambient shock with a parabolic shape (Artymowicz shape), unless otherwise stated.

2.4 Orientation of the magnetic field

The magnetic field decouples the ions from the neutral fluid in the shock. However, as discussed in Smith (1992), the effective magnetic field is the component of the field parallel to the shock surface. If the homogeneous pre-shock density is n_H , the strength scale factor of the ambient uniform magnetic field is defined as $b_0 = B_0(\mu G)/\sqrt{n_H[\text{cm}^{-3}]}$. The component of the field parallel to the working surface b_{\parallel} is given by

$$\left(\frac{b_{\parallel}}{b_0}\right)^2 = \cos^2 \alpha \sin^2(\varphi - \phi) + [\sin \psi \sin \alpha + \cos \psi \cos \alpha \cos(\varphi - \phi)]^2, \quad (8)$$

where the angles α and φ monitor the position in the bow shock (this expression is actually valid regardless of the bow shock shape). Fig. 4 displays how this component (b_{\parallel}) changes along the shock surface in a few cases.

3 1D PLANAR SHOCK MODELS

We now compute the chemical composition and the emission properties of each local planar shock composing a bow shock.

3.1 Grid input parameters

We set all the parameters to values corresponding to typical conditions encountered in the molecular interstellar gas in our Galaxy,

as described in Table 1. We assume that the ambient gas is initially at chemical and thermal equilibrium and we compute this initial state as in Lesaffre et al. (2013) by evolving the gas at constant density during $10^{12}/n_H$ yr. Our initial elemental abundances in the gas, grain cores and ice mantles are the same in Flower & Pineau des Forêts (2003). We also include polycyclic aromatic hydrocarbons (PAHs) with ratio $n(\text{PAH})/n_H = 10^{-6}$. The irradiation conditions are for a standard external irradiation field ($G_0 = 1$) but an additional buffer of $A_{v,0} = 0.1$, $N_0(\text{H}_2) = 10^{20} \text{ cm}^{-2}$ and $N_0(\text{CO}) = 0 \text{ cm}^{-2}$ is set between the source and the shock so that the gas is actually mainly molecular (see Lesaffre et al. 2013, for details). In our calculations, the atomic hydrogen fractions $n(\text{H})/n_H$ are 7.85×10^{-2} , 5.94×10^{-4} and 5.89×10^{-6} : they correspond to pre-shock gas densities of 10^2 , 10^3 and 10^6 cm^{-3} , respectively. These initial conditions at steady state are then used as pre-shock conditions to compute the grid of planar shock models.

Our grid of models has a range of shock velocities between 3 and 40 km s^{-1} as in Lesaffre et al. (2013), with a velocity step of $\Delta u = 1 \text{ km s}^{-1}$. However, we take into account the effect of the finite shock age by taking snapshots at five different values of age: 10^2 , 10^3 , 10^4 and 10^5 yr for a density of $n_H = 10^2 \text{ cm}^{-3}$, and a hundred times shorter for a density of $n_H = 10^4 \text{ cm}^{-3}$. Note that the typical time to reach the steady state in a C-type shock with $G_0 = 1$ is about $t_s = 10^6 \text{ yr}/(n_H/10^2 \text{ cm}^{-3})$ (with little or no magnetic field dependence; see Lesaffre et al. 2004a).

The projected value of the magnetic field parallel to the shock B_{\parallel} varies along the shock surface, so we need to sample the range of attainable values in our grid. The first constraint for a shock to exist is that its entrance velocity u_{\perp} should be greater than the Alfvén velocity $v_A = \frac{B_{\parallel}}{\sqrt{4\pi\rho}} \simeq b_{\parallel} 1.85 \text{ km s}^{-1}$ where we defined the dimensionless value of the transverse magnetic field using the standard scaling $b_{\parallel} = B_{\parallel}/\mu G/(n_H/\text{cm}^{-3})^{1/2}$. The condition $u_{\perp} > v_A$ translates as $b_{\parallel} < u_{\perp}/1.85 \text{ km s}^{-1}$, and we use as upper limit of our grid $b_{\parallel} < b_{\parallel\text{max}} = u_{\perp}/3 \text{ km s}^{-1}$ (see Fig. 5).

Another important parameter is the magnetosonic speed in the charged fluid $v_m = \sqrt{c_s^2 + B_{\parallel}^2/4\pi\rho_c}$ (where c_s and $B_{\parallel}^2/4\pi\rho_c$ are the speed of sound and the Alfvén speed of the charged fluid). The magnetosonic speed is the fastest signal speed in a partially ionized medium. Because of the low ionization degree in the molecular ISM, it is almost proportional to the local magnetization parameter: $v_m \simeq B_{\parallel}^2/4\pi\rho_c = b_{\parallel} v_{m1}$, where v_{m1} is the magnetosonic speed obtained when the magnetization parameter is equal to unity. In our calculations, we find $v_{m1} = 18.5 \text{ km s}^{-1}$ or $v_{m1} = 19.2 \text{ km s}^{-1}$ for respective densities of $n_H = 10^2 \text{ cm}^{-3}$ or $n_H = 10^4 \text{ cm}^{-3}$. The charged fluid mass is dominated by the dust grains: the gas-to-dust ratio turns out to be $\rho/\rho_d = 180$ for the cores and mantle composition used in our simulations.

3.2 J- and C-type shocks at early age

Depending on the value of the entrance speed relative to the entrance magnetosonic speed v_m , one can consider different kinds of shocks. When the magnetic field is weak and/or when the ionization fraction is large, the shocks behave like hydrodynamic shocks with an extra contribution from the magnetic pressure. Such shocks are faster than the signal speed in the pre-shock medium. Therefore, the latter cannot ‘feel’ the shock wave before it arrives. Across the shock front, the variables (pressure, density, velocity, etc.) of the fluid vary as a viscous discontinuity jump (the so-called J-type shock). When the ionization fraction is small, the magnetosonic speed v_m in the charges can be greater than the shock entrance velocity, then

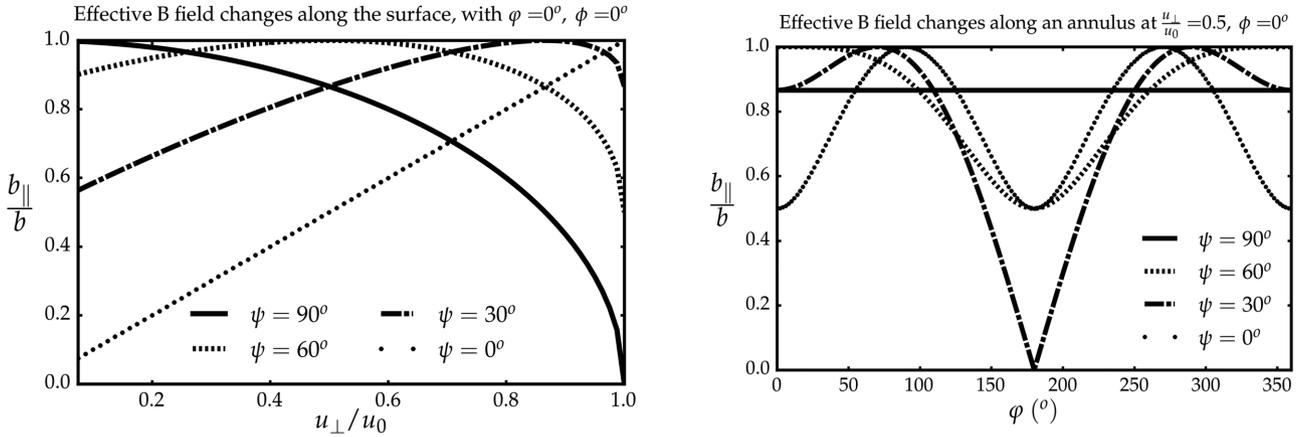


Figure 4. Variation of the effective transverse magnetic field b_{\parallel} along the bow shock surface: for various directions of b (left) and based on the position of fixed direction of b on an annulus circle (right).

a magnetic precursor forms upstream of the discontinuity where the charged and neutral fluids dynamically decouple. The resulting friction between the two fluids heats up and accelerates the neutral fluid. At early ages, the shock is actually composed of a magnetic precursor and a J-type tail (it is a time-dependent CJ-type shock). Chièze et al. (1998) remarked that time-dependent shocks looked like steady state: this yielded techniques to produce time-dependent snapshots from pieces of steady-state models (Flower & Pineau des Forêts 1999; Lesaffre et al. 2004b). We follow the approach of Lesaffre et al. (2004b) in the large compression case. The J-type front in a young C-type shock is thus inserted when the flow time in the charged fluid is equal to the age of the shock. The J-type shock ends when the total neutral flow time across the J-type part reaches the age of the shock (the same holds for young J-type shocks). As the shock gets older, the magnetic precursor grows larger and the velocity entrance into the J-type front decreases due to the ion–neutral drag. As a result, the maximum temperature at the beginning of the J-type front decreases with age, as illustrated in Fig. 6. If the magnetic field is strong enough, the J-type tail eventually disappears and the shock becomes stationary. The resulting structure forms a continuous transition between the pre-shock and the post-shock gas (a stationary C-type shock).

For each value of the entrance velocity u_{\perp} , we compute five CJ-type shock models with varying transverse magnetic field b equally spaced between 0 and u_{\perp}/v_{m1} , and we compute five J-type shocks models with varying transverse magnetic field b equally spaced between u_{\perp}/v_{m1} and $b_{\parallel\max} = u_{\perp}/3 \text{ km s}^{-1}$. That way, we homogeneously sample the possible shock magnetizations that are likely to occur in the 3D bow shock (see Fig. 5).

The main input parameters of the model are gathered in Table 1.

3.3 H₂ excitation in C- and J-type shocks

An H₂ rovibrational level (v, J) can be populated after a collision with another species provided that the temperature yields more energy per particle than the energy level $E_{v,J}$. In a J-type shock, the sudden surge of viscous heat in the adiabatic shock front easily leads to large temperatures ($T_J = 53 \text{ K}(u/\text{km s}^{-1})^2$; see Lesaffre et al. 2013, equation 10) that are able to excite high energy levels. Figs 7(a) and (b) show the level populations for young ages, where even CJ-type shocks are dominated by their J-type tail contribution. These figures illustrate the threshold effect for two different energy

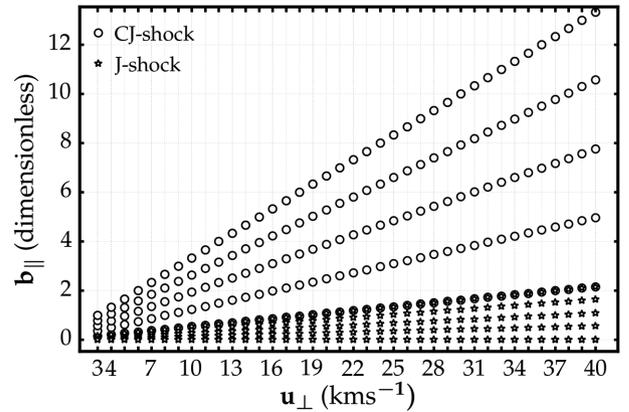


Figure 5. Grid of 1D models in the parameter space (u_{\perp}, b_{\parallel}).

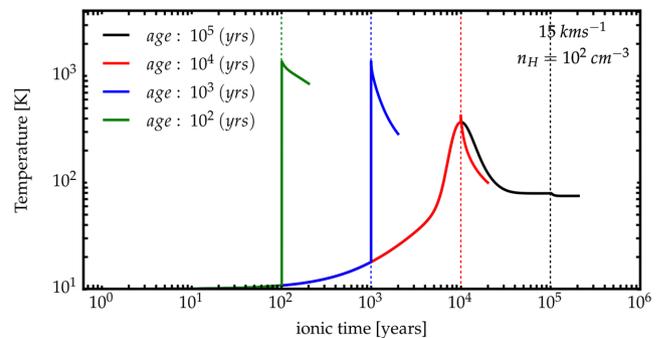


Figure 6. Temperature profile of CJ-type shocks at various shock ages for $n_{\text{H}} = 10^2 \text{ cm}^{-3}$ and $b = 5$.

levels: their population rises quickly and reaches a plateau when $u > u_{v,J}$, with $u_{v,J}$ a critical velocity depending on the energy level. Note the weak dependence of the plateau on the shock magnetization for J-type shocks, as magnetic pressure only marginally affects their thermal properties. The critical velocity $u_{v,J}$ mainly depends on the energy level ($E_{v,J} \simeq k_{\text{B}} T_J$) and only weakly depends on the magnetization.

Table 1. Main input parameters of model.

Parameter	Value	Note
n_H	$10^2 \text{ cm}^{-3}, 10^4 \text{ cm}^{-3}$	Pre-shock density of H nuclei
A_V	0.1	Extinction shield
$N_0(H_2)$	10^{20} cm^{-2}	Buffer H_2 column density
$N_0(CO)$	0 cm^{-2}	Buffer CO column density
G_0	1	External radiation field
ζ	$3 \times 10^{-17} \text{ s}^{-1}$	Cosmic ray flux
OPR	3	Pre-shock H_2 ortho/para ratio
u_\perp	3, 4, 5, ..., 40 km s^{-1}	Effective shock velocity
$b_\parallel v_{m1}/u_\perp$	0, ..., 1	Range of b_\parallel parameter for J-type shocks
$b_\parallel v_{m1}/u_\perp$	1, ..., $\frac{v_{m1}}{3 \text{ km s}^{-1}}$	Range of b_\parallel parameter for CJ-type shocks
$\text{Age} \times n_H/100 \text{ cm}^{-3} \text{ yr}^{-1}$	$10^2, 10^3, 10^4, 10^5$	Shock age

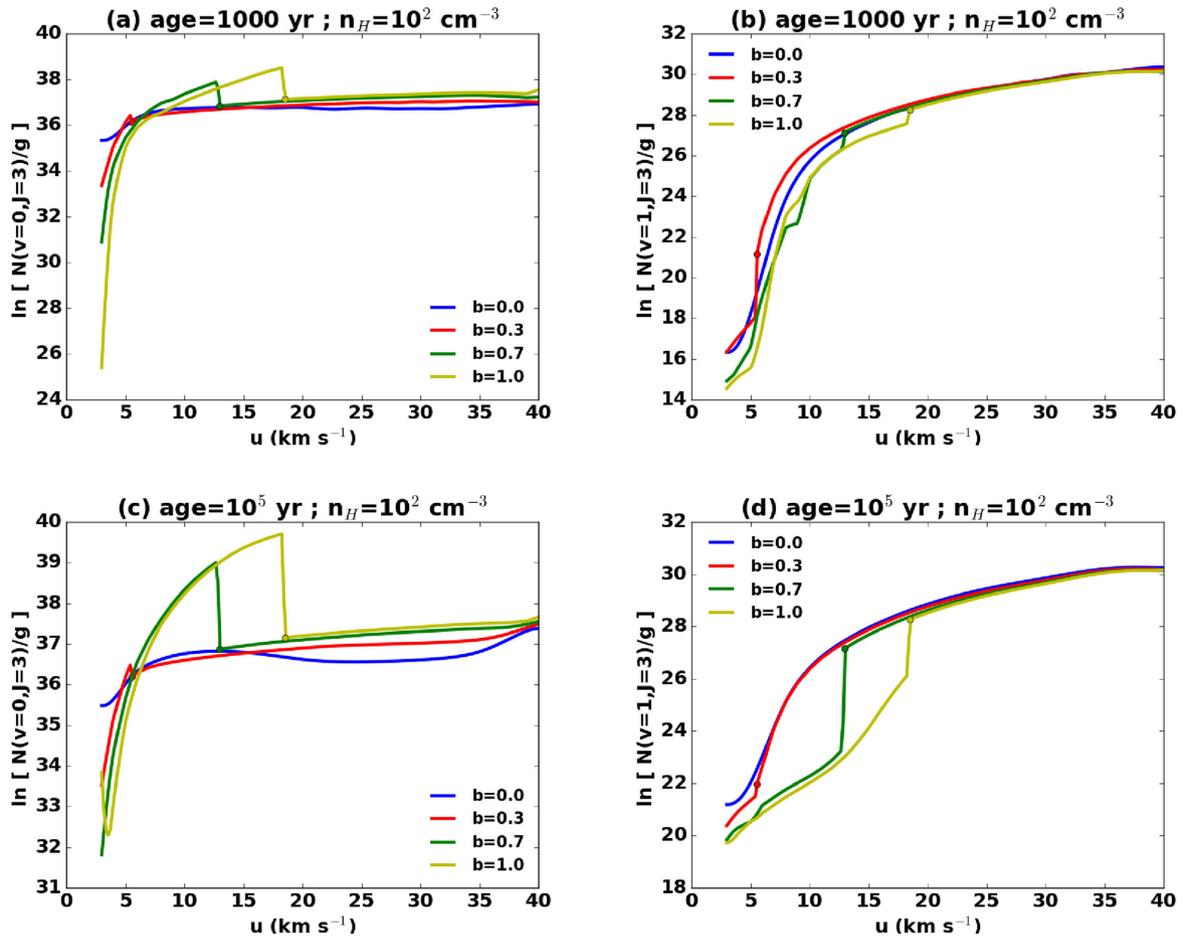


Figure 7. Overview of results from our models for a pre-shock density $n_H = 10^2 \text{ cm}^{-3}$. We show the natural logarithm of the integrated column densities of H_2 populations normalized by their statistical weight. They are given as a function of the velocity u for various values of the magnetic field parameter b_\parallel . Left-hand panels are for the level $(v, J) = (0, 3)$, the upper level of the 0–0S(1) line, and the right-hand panels are for the level $(v, J) = (1, 3)$, the upper level of the 1–0S(1) line. Upper panels are for a young age of 10^3 yr , while bottom panels are nearly steady state at an age of 10^5 yr . In each panel, the symbol ‘o’ marks the transition between CJ-type shocks (on the left-hand side) and J-type shocks (on the right-hand side), when the velocity u is equal to the magnetosonic speed bv_{m1} .

On the other hand, C-type shocks dissipate their energy through ion–neutral friction, a process much slower than viscous dissipation: at identical velocity, C-type shocks are much cooler than J-type shocks, but their thickness is much larger. C-type shocks dominate the emission of old CJ-type shocks, when the J-type front

contribution almost disappears (Fig. 7c of the ‘o’ symbols). Because of their low temperature, high energy levels can never be populated (Fig. 7d). This enhances the threshold effect, with a discontinuous jump at $u = bv_{m1}$. On the contrary, energy levels of energy lower than $k_B T_C$, with T_C the typical temperature of a

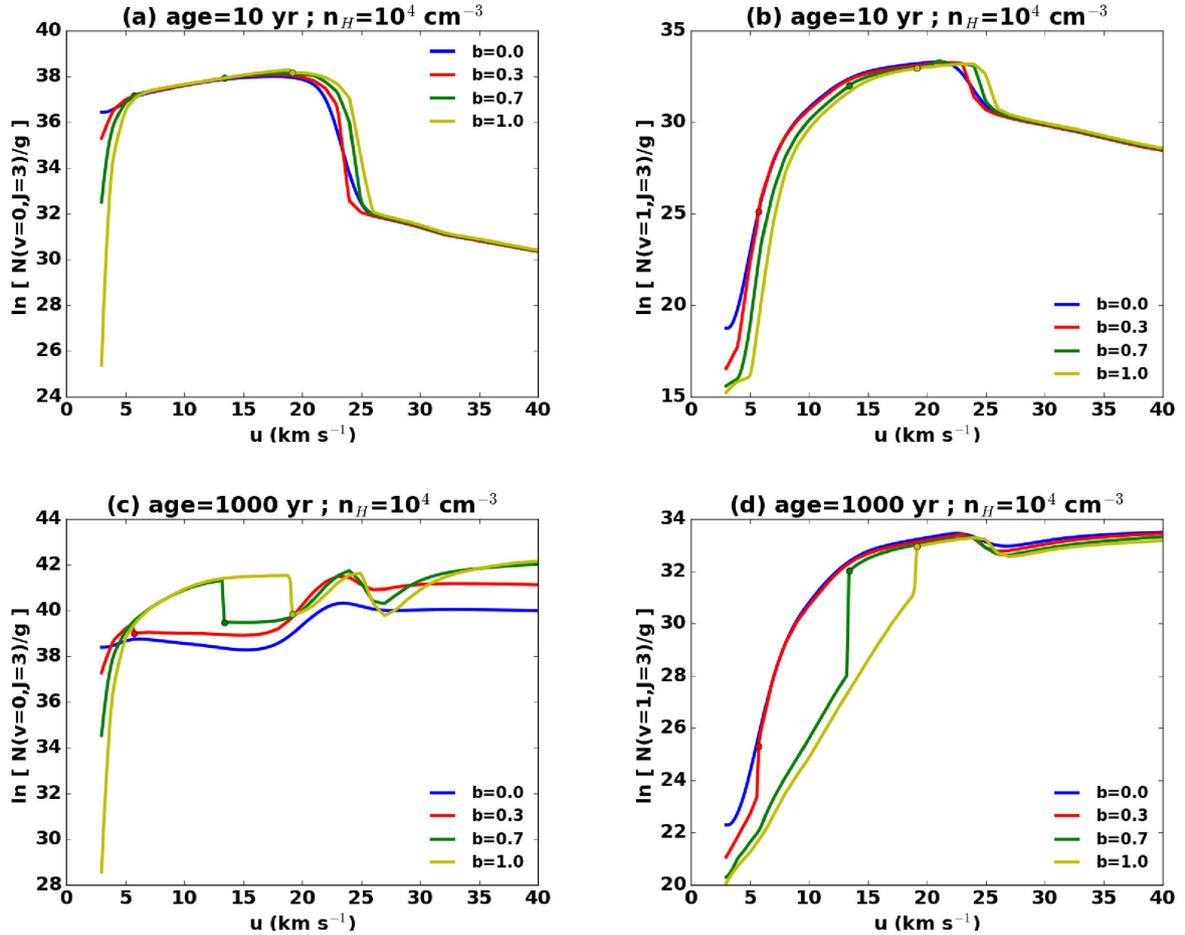


Figure 8. Same as Fig. 7 but for the denser case $n_{\text{H}} = 10^4 \text{ cm}^{-3}$. The corresponding ages are: upper panels at a young age of 10 yr, while the bottom panels are nearly steady state at an age of 10^3 yr.

C-type shock, will be much more populated in a C-type shock than in a J-type shock due to the overall larger column density. This is illustrated in the Fig. 7(c) for a low energy level. The discontinuous jump at $u = bv_{m1}$ becomes a drop instead of a surge and a peak appears in the level population. Magnetization in C-type shocks controls the compressive heating which, in turn, impacts the temperature: excitation of H_2 low-energy levels in C-type shocks decreases systematically with larger magnetization, but the effect remains weak within C-type shocks. However, the magnetization is important insofar as it controls the transition between C-type and J-type shocks, which have very different emission properties.

To summarize, at a density of $n_{\text{H}} = 10^2 \text{ cm}^{-3}$, the excitation of a given H_2 level follows a threshold in velocity after which a plateau is reached, with little or no magnetic field dependence. However, low energy levels at old ages, for velocities below the magnetosonic speed, can be dominated by C-type shock emission. In that case, the H_2 level population peaks at the magnetosonic speed before reaching a plateau. Therefore, H_2 emission in bow shocks is likely to be mostly dominated by J-type shocks.

At high density, the picture is essentially unchanged, except for the effect of H_2 dissociation that is felt when the velocity is larger than the H_2 dissociation velocity: the value of the plateau decreases beyond this velocity (see the right half of each panel in Fig. 8, which is in other respects similar to Fig. 7). At even

higher densities, H_2 dissociation completely shuts off H_2 emission in J-type shocks, and we reach a situation where the bow shock emission is dominated by C-type shocks, as in Gustafsson et al. (2010).

4 3D BOW SHOCK MODELS

In this section, we combine the grid of planar shocks and the statistics of planar shock velocity u_{\perp} computed in the previous sections to produce observable diagnostics of 3D bow shocks.

4.1 H_2 excitation diagram

4.1.1 Excitation of a given H_2 level

The average column density of a given excited level of H_2 along the bow shock can be expressed as

$$N_{vJ}^{\text{tot}}(\text{age}, u_0, b_0, \psi) = \int_0^{2\pi} \frac{d\varphi}{2\pi} \times \int_{c_s}^{u_0} P_{u_0}(u_{\perp}) N_{vJ}(\text{age}, u_{\perp}, b_{\parallel}) du_{\perp}, \quad (9)$$

where $P_{u_0}(u_{\perp})$ is the distribution computed in Section 2 and N_{vJ}^{tot} and N_{vJ} are the column densities of H_2 in the excited level (v, J) in the whole bow shock and in each planar shock, respectively.

As noted in Section 3.3, $N_{v,J}$ sharply increases as a function of u_{\perp} at a given threshold velocity $u_{v,J}$ before reaching a plateau. We also showed that the statistical distribution was steeply decreasing as a function of u_{\perp} . As a result, the product of the two peaks at around $u_{v,J}$ and its integral over u_{\perp} is a step function around $u_{v,J}$ (see Fig. 9). This situation is reminiscent of the Gamow peak for nuclear reactions. Then, $N_{v,J}^{\text{tot}}(u_0)$ tends to a finite value when u_0 is much greater than the threshold velocity $u_{v,J}$. The final value depends both on magnetization and age.

4.1.2 Resulting H_2 excitation diagram

The excitation diagram displays the column densities in each excited level (normalized by their statistical weight) as a function of their corresponding excitation energy. This is an observational diagnostic widely used to estimate the physical conditions in the emitting gas.

Fig. 10(a) shows the influence of the terminal velocity on the excitation diagrams of H_2 at an age of 10^4 yr. As expected, the excitation diagram saturates at large velocity, when u_0 is larger than all the individual $u_{v,J}$ of the levels considered. That saturation occurs quicker at low energy levels, as the corresponding critical velocity is lower.

Fig. 10(b) illustrates the effect of density on the excitation diagram. Roughly speaking, the column densities are proportional to the density, but in this example (40 km s^{-1} bow shock), higher energy levels are subject to H_2 collisional dissociation, and they are slightly less populated relative to their low energy counterpart.

At young ages, shocks are dominated by the emission properties of J-shock: as time passes, C-type shocks increase the emission of low energy levels and the excitation diagram of the bow shock is slightly steeper at the origin (Fig. 10c). Interestingly, the energy level just above 2000 K does not seem to be affected by age (it is also weakly affected by all the other parameters, the safe density) and all the curves converge on this point.

As mentioned in Section 2.3, the shape of bow shocks affects the velocity distribution and the relative weight between of the large velocities increases when one moves from a parabola to a Wilkin shape. As a result, a bow shock with a Wilkin shape has more excited high energy levels than a parabolic bow shock (Fig. 10d).

Finally, the magnetic field tends to shift the transition between C-type and J-type shocks in the bow shock to larger velocities. At early age, it does not matter much, since both C-type and J-type shocks are dominated by J-type shock emission. At later ages, though, the low energy levels get an increasing contribution from C-type shocks and see their excitation increase. Conversely, high energy levels are less excited because the overall temperature of the shock decreases, as seen in Fig. 10(e). The orientation of the magnetic field azimuthally affects the range of values of b (as φ varies) but its main systematic effect is to shift the magnetization from low velocities to large velocities as it gets more and more parallel to the axis of symmetry (Fig. 4). Fig. 10(f) shows the differential effect caused by varying the angle Ψ : tending Ψ to 0° amounts to increasing b (high energy levels are less excited, whereas low energy levels are more excited). The resulting change is subtle but we show below that it might still be probed by observations.

4.1.3 Using 1D models to fit 3D excitation diagrams

Observations often consider low energy transitions (pure rotational or low vibrotational levels): although we included the first 150 levels in our calculations, here we mainly consider the levels with an

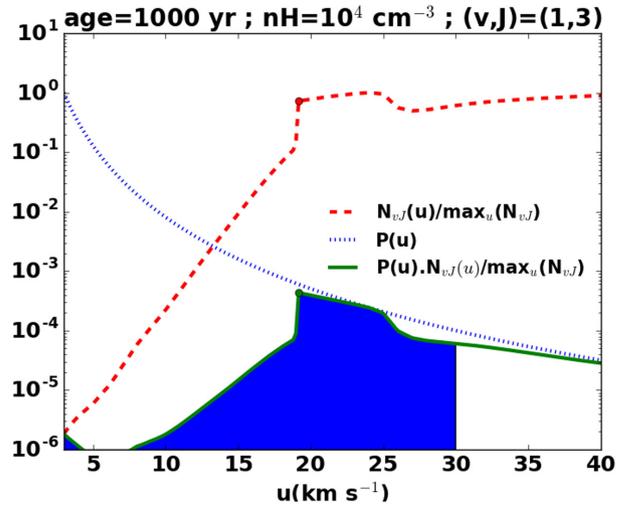


Figure 9. Illustration of the ‘‘Gamow-peak’’ effect on the integration of the total column densities of the H_2 level $(v, J) = (1, 3)$ in a bow shock with terminal velocity $u_0 = 30 \text{ km s}^{-1}$, $n_H = 10^2 \text{ cm}^{-3}$ and the age is 10^5 yr.

energy up to 10^4 K. The two lowest rotational states ($J = 0$ and 1) are, of course, unobservable in emission. The *James Webb Space Telescope* (*JWST*) will observe pure rotational transitions up to energies of about 5900 K (seven levels involved). This is similar to the performances of its predecessors: the *Infrared Space Observatory* (*ISO*) and the *Spitzer* telescope. These two IR telescopes have been used to observe shocked regions, generate excitation diagrams and maps around young stellar objects (YSOs; e.g. Giannini et al. 2004; Neufeld et al. 2009) or supernova remnants (SNRs; e.g. Cesarsky et al. 1999; Neufeld et al. 2014) shocks. The *Akari* mission has also been used for similar purposes in SNRs environments (e.g. Shinn et al. 2011). In addition, note that the *JWST* will also target rovibrational transitions. Finally, the Echelon-Cross-Echelle Spectrograph (*EXES*; operating between 4.5 and $28.3 \mu\text{m}$; DeWitt et al. 2014) on-board the *Stratospheric Observatory For Infrared Astronomy* (*SOFIA*) should allow observations of pure rotational transitions of H_2 , but no program has been explicitly dedicated to the observation of shocked H_2 with this instrument so far.

Most observations are unable to resolve all details of a bow shock, and the beam of the telescope often encompass large portions of it, therefore mixing together planar shocks with a large range of parameters. However, it is customary to use 1D models to interpret observed excitation diagrams. Previous work (Neufeld & Yuan 2008, hereafter NY08; Neufeld et al. 2009, 2014) have also shown that statistical equilibrium for a power-law temperature distribution $T^{-b_{SE}} dT$ can be quite efficient at reproducing the observed H_2 pure rotational lines. We thus seek to explore how accurately these two simple models perform as compared to 3D bow shocks. We consider the worst-case scenario where the whole nose of a parabolic bow shock is seen by the telescope: the effective entrance velocity u_{\perp} varies from the speed of sound c_s (in the wings of the bow shock) to the terminal velocity u_0 (at the apex of the bow shock).

The following χ function is used to estimate the distance between 1D and 3D models:

$$\chi^2 = \frac{1}{L} \sum_{vj} \left[\ln \left(\frac{N_{vj}^{\text{tot}}}{g_{vj}} \right) - \ln \left(\frac{N_{vj}^{u_{\perp}}}{g_{vj}} \right) - C \right]^2, \quad (10)$$

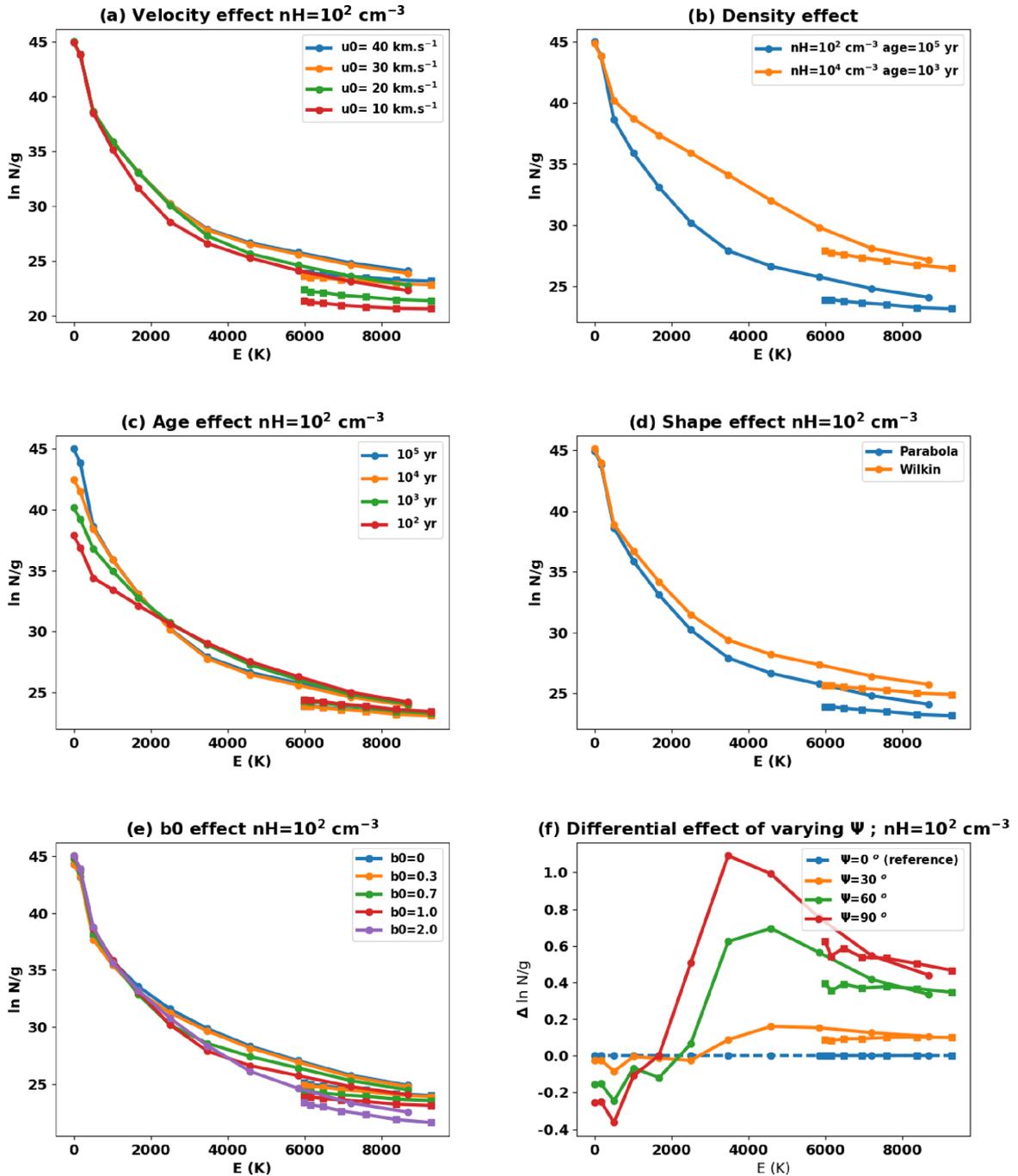


Figure 10. Excitation diagrams of H₂ showing the effect of varying some of the parameters of the model. The reference model is $n_{\text{H}} = 10^2 \text{ cm}^{-3}$, age = 10^5 yr, $b_0 = 1$, $\Psi = 0$, shape = parabola, $u_0 = 40 \text{ km s}^{-1}$. It is always displayed in solid blue. Connected circle symbols have all $v = 0$ (pure rotational levels), while square symbols have $v = 1$.

with L the number of observed vibrotational levels (v, j), and g_{vj} the statistical weight of each level (v, j). The constant C reflects the fact that the beam surface at the distance of the object may not match the actual emitting surface of the bow shock, partly because of a beam filling factor effect and partly because the bow shock surface is curved. We assume here that the observer has a perfect knowledge of the geometry and we take $C = 0$, which means that the 1D shock model has the same surface as the 3D bow shock

to which it is compared with. The best 1D model and power-law assumption selected is the one yielding the smallest χ^2 value on our grid of 1D models.

Fig. 11 shows the result of the fit on a 30 km s^{-1} bow shock at age 10^5 yr, density $n_{\text{H}} = 10^2 \text{ cm}^{-3}$ and magnetization parameter $b_0 = 1$ ($\Psi = 90^\circ$). 1D models have the same parameters (same age, pre-shock density and $b_{\parallel} = 1$) except the entrance velocity u_{\perp} . We find that the best velocity is either 8 or 13 km s^{-1} depending on the

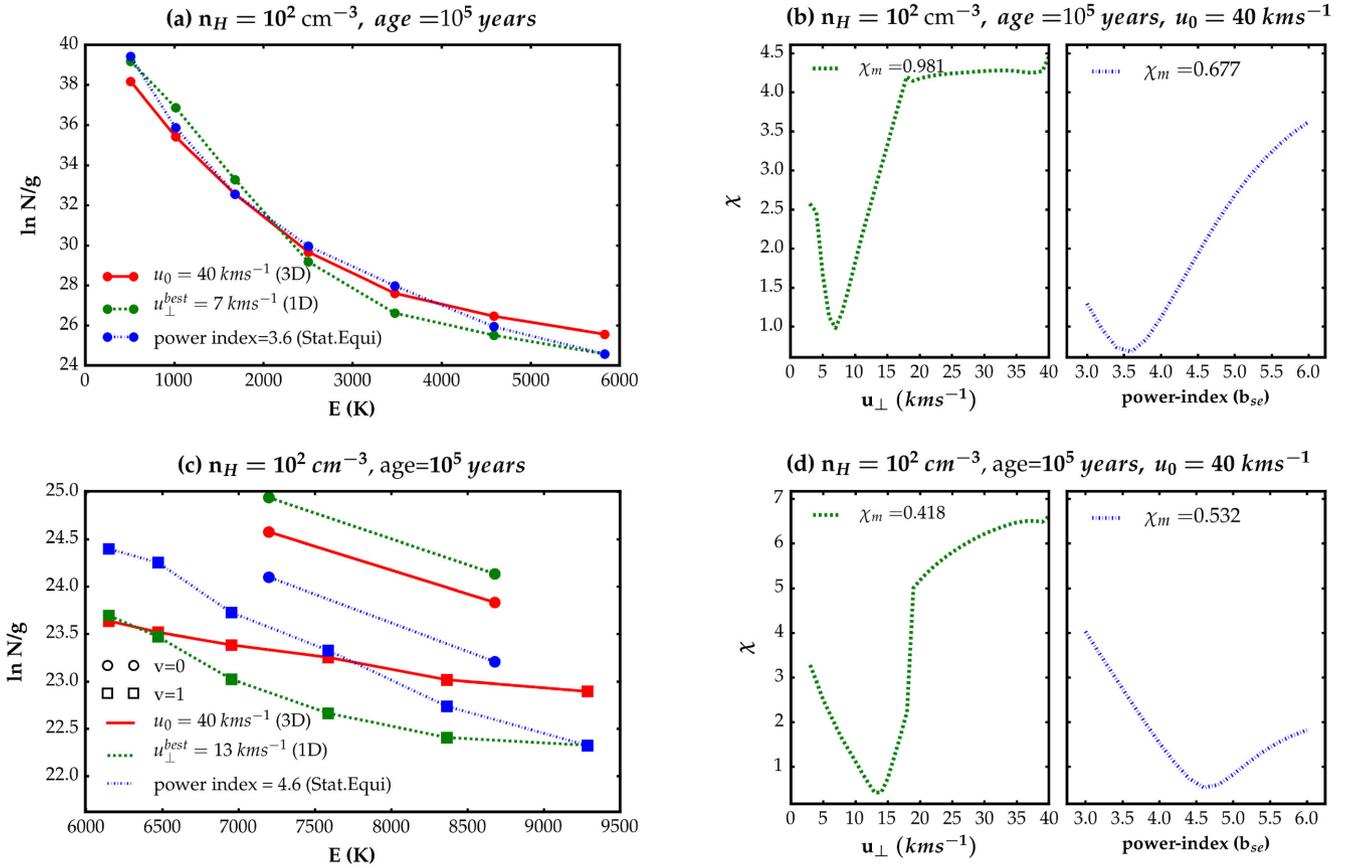


Figure 11. Results of the fit of 1D models and statistical equilibrium approximations to a 3D bow shock. (a)-(b): transitions with upper level $E_{vj} < 5900$ K (JWST-like) are used. (c)-(d): fitted transitions have $5900 < E_{vj} < 10000$ K. (a)-(c): comparison of the excitation diagrams of the bow shock to the best 1D fit and the best NY08 fit. (b)-(d): standard deviation of the natural logarithm difference between the two diagrams ($\chi = \sqrt{\chi^2}$) as the entrance velocity in the 1D model and the power index in NY08 assumption vary. The bow shock parameters are: pre-shock density 10^2 cm^{-3} , $b_0 = 1$, $\psi = 90^\circ$ and the age is 10^5 yr. Connected circle symbols all have $v = 0$ (pure rotational levels), while square symbols have $v = 1$.

range of lines considered. This is way below the terminal velocity and this illustrates again the fact that the resulting 3D excitation diagram is dominated by low-velocity shocks. As a consequence, the use of higher energy lines reduces the bias, and a cubic shape for the bow shock yields less bias towards low velocity than a parabolic shape (not shown here). In the left-hand sides of the panels (b)–(d), the resulting χ^2 is around one in all cases: it corresponds to an average mismatch of about a factor of 3 between the 3D and 1D column densities, a common result when comparing 1D models and observations.

Fig. 12 systematically explores this bias as a function of the bow shock terminal velocity: the best 1D model usually has an entrance velocity smaller than the terminal velocity of the 3D bow shock. Moreover, when the 3D excitation diagram saturates at large u_0 , the best 1D model does not change.

Following the approach of NY08, we calculate the H_2 levels population in statistical equilibrium for a range of temperatures (100–4000 K) and convolve this with a power-law distribution of the gas temperature. We explore power indices (b_{se}) varying from 3 to 6 (as in NY08) in steps of 0.2. We recover the fact that the NY08 approximation performs very well in the low-energy regime of pure rotation. In the case displayed in Fig. 11(a), our best-fitting power index is 3.6, close to the estimation of 3.78 for parabolic bow shocks calculated by equation (4) in NY08. However, Fig. 11(c) shows that this simple approach fails for vibrational levels, or rotational levels of higher energy.

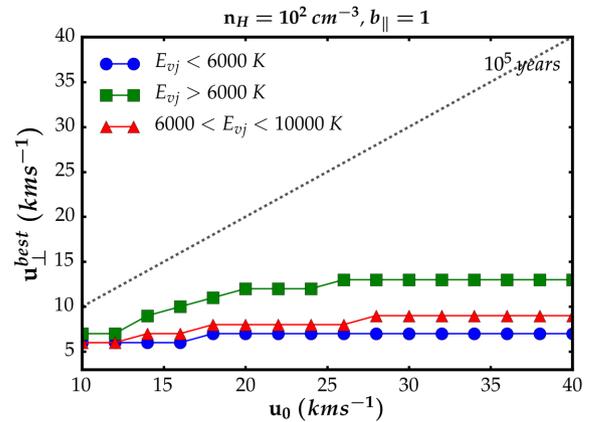


Figure 12. Velocity bias between 1D and 3D model. Blue circle symbols fit only $E_{vj} < 5900$ K (JWST-like), the Green square symbols fit only $E_{vj} > 5900$ K (ground based) and the red triangles fit $5900 < E_{vj} < 10000$ K. The parameters of the bow shock are the same as for Fig. 11. The dotted black line is $u_{\perp}^{best} = u_0$.

We then turn on recovering magnetization from 1D models. We first fix the terminal velocity of the bow shock to $u_0 = 40 \text{ km s}^{-1}$ and explore several values of the magnetization b_0 , while keeping $\Psi = 90^\circ$. Once the best-matching 1D velocity is found, we further let the magnetization parameter b of the 1D model vary freely and explore which value best fits the 3D model (while keeping u_{\perp} fixed).

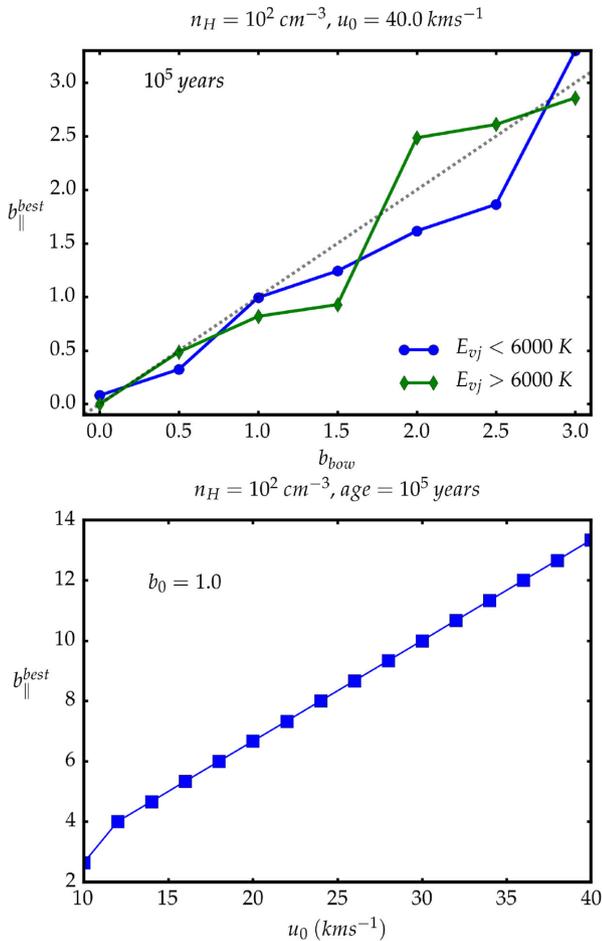


Figure 13. Magnetization bias between 1D and 3D models. The top panel is at $u_0 = 40 \text{ km s}^{-1}$ and for each value of b_0 , it gives the best b_{\parallel} after the best u_{\perp} has been determined. The bottom panel is at $b_0 = 1$ and for each value of u_0 , it gives the best-matching b_{\parallel} when $u_{\perp} = u_0$ is assumed. Symbols are the same as in Fig. 12. The remaining parameters of the bow shock are the same as for Fig. 11.

The result of this second adjustment is shown in Fig. 13: the magnetization parameter of the best 1D model is only slightly below and represents a good match to the original magnetization parameter of the bow shock. Next, we assume that a priori information about the bow shock velocity (usually by looking at some molecular line width, for example) is available. We now fix $b_0 = 1$ for the underlying 3D model and assume $u_{\perp} = u_0$ in the 1D models while searching for the best b_{\parallel} value. The retrieved magnetization parameter is usually too high, which may lead to overestimations of the magnetization parameter when the dynamics have been constrained independently.

4.1.4 Applications and prospects

In this section, we briefly show how to use the 3D bow shock to interpret and constrain the parameters of bow shock observations.

BHR 71

Located at a distance of about 175 pc (Bourke et al. 1995), BHR 71 is a double bipolar outflow (Bourke et al. 1997; Bourke 2001)

Table 2. Parameters that best reproduce the excitation diagram in BHR 71. We also give a 3σ uncertainty range for the parameter Ψ (see text).

Parameter	Value	Note
n_{H}	10^4 cm^{-3}	Pre-shock density of H nuclei
Age	10^3 yr	Shock age
Δu_{\perp}	$21\text{--}23 \text{ km s}^{-1}$	Range of u_{bot}
b_0	1.5	Strength of the magnetic field
ψ	$-50^{\circ} \pm 20^{\circ}$	Orientation of the magnetic field
u_0 and β	NA	Bow shock terminal velocity and shape are irrelevant because of the narrow range of velocities

emerging from a Bok globule visible in the Southern sky. The two outflows are spectrally distinguishable (Parise et al. 2006). Their driving protostars, IRS 1 and IRS 2 have luminosities of 13.5 and $0.5 L_{\odot}$ (Chen et al. 2008) and are separated by about 3400 au. For this double star system, the time since collapse has been evaluated to about 36 000 yr (Yang et al. 2017). Multiple observations of this outflow system have been performed from IR to submillimetre wavelength ranges. Bright Herbig–Harro (HH) objects HH 320 and HH 321 (Corporon & Reipurth 1997) have been detected, as well as chemical enhancement spots (Garay et al. 1998) and several other knots of shocked gas (Giannini et al. 2004). By combining H_2 observations performed by *Spitzer* (Neufeld et al. 2009; Giannini et al. 2011) and SiO observations obtained from the Atacama Pathfinder Experiment (APEX) telescope, Gusdorf et al. (2011) were able to characterize the non-stationary CJ-type shock waves propagating in the northern lobe of the biggest outflow. They more tightly constrained the input parameters of Paris–Durham shock models by means of successive observations of lower to higher J_{up} CO (Gusdorf et al. 2015) using APEX and *SOFIA*. The most recent studies based on *Herschel* observation hint at the presence of an atomic jet arising from the driving IRS 1 protostar (Nisini et al. 2015; Benedettini et al. 2017). This does not challenge the existence of a molecular bow shock around the so-called SiO knot position in the northern lobe of the main outflow, where most attempts have been made to compare shock models with observations (Gusdorf et al. 2011, 2015; Benedettini et al. 2017). In particular, the last three studies have placed constraints on shock models of the H_2 emission over a beam of 24 arcsec centred on this position: pre-shock density $n_{\text{H}} = 10^4 \text{ cm}^{-3}$, magnetic field parameter $b = 1.5$, shock velocity $v_s = 22 \text{ km s}^{-1}$ and age of 3800 yr. In these studies, the influence of the external interstellar radiation field (ISRF) or from the driving protostar was neglected, with an equivalent G_0 factor set to 0. The excitation diagram that was used can be seen in Fig. 14, where the large error bars reflect the uncertainty on the filling factor and the proximity of the targeted region to the edge of the *Spitzer*-InfraRed Spectrograph (IRS) H_2 map.

Here we attempt to reproduce the same H_2 emission data around the SiO knot position as in Gusdorf et al. (2015). To fit a 3D model to this data, we should in principle adjust all the parameters in Table 2, which would be a bit tedious, and very likely underconstrained by the observations. Instead, we started up from already published parameters and expanded around these values. Hence, we use a narrow range of velocities around $u_0 = 22 \text{ km s}^{-1}$, $b_0 = 1.5$ and $n_{\text{H}} = 10^4 \text{ cm}^{-3}$ as indicated by Gusdorf et al. (2015). These authors found an age of 3800 yr, so we took our grid models at an age of 1000 yr, as 10^4 yr would not be compatible with the extent of the shock. A speed of 22 km s^{-1} during 1000 yr already results in a shock width of 0.02 pc, about the same size of the beam (24 arcsec

at 200 pc according to Gusdorf et al. 2015), although the H_2 lines emission region is a factor of a few smaller.

Fig. 14 illustrates the comparison between our models and the observational values. We first restrict the velocity range in the bow shock velocity distribution to the narrow interval [21,23] km s⁻¹ that is close to the original best solution of Gusdorf et al. (2015). This also accounts for the fact that the beam selects a local portion of the bow shock and one might expect to find a privileged velocity.

First, we examine the case $\Psi = 90^\circ$ when the magnetization is close to b_0 and uniform throughout a transverse annulus of the bow shock. Technically this is still a 3D model, but it is very close to the model in our grid of planar shocks with similar parameters because we use a very narrow range of velocities combined with uniform magnetization. The excitation diagram for this model is noted as the green diamonds in Fig. 14. Although it slightly differs from the best model of Gusdorf et al. (2015), it is not much further away from the observational constraints ($\chi = 1.0$ in the model in Gusdorf et al. 2015 and $\chi = 1.5$ in our model at $\Psi = 90^\circ$).

Second, we leave the orientation of the magnetic field Ψ free and we find the best model at $\Psi = -44^\circ$: this greatly improves the comparison with observations ($\chi = 0.2$). In particular, the curvature of the excitation diagram that was difficult to model, is now almost perfectly reproduced. At this orientation, the model is a mixture of planar shocks with transverse magnetization between b_0 and a small minimum value. Because we limited the velocity to such a narrow range, this model is effectively a 2D model.

Third, we checked that increasing the velocity range, changing the shock shape or limiting the integration range for the angle φ (to account for the fact that the observational beam probably intersects only one flank of the bow shock) did not improve the fit: the interpretation capabilities of our 3D model seem to be reached. Table 2 sums up our constraints on the parameters of our model. We estimate 3σ error bars for Ψ by investigating the shape of the χ^2 well around the best value: we vary Ψ with all other parameters kept fixed and we quote the range of values where χ^2 is below four times its minimum value.

Finally, we checked the NY08 approximation. As mentioned in the previous section that simple assumption works surprisingly well in the case of low pure rotational excitation. We find a best value of the power index at $b_{SE} = 2.6$, consistent with the value 2.5 in Neufeld et al. (2009) for the same object, with $\chi = 0.2$: as close to the data as our 3D model.

Orion molecular cloud

The Orion molecular cloud (OMC-1) is one of the well-studied star-forming regions. A central young stellar object generates a strong outflow that shocks the surrounding gas and yields a wealth of H_2 IR emission lines that have been observed by Rosenthal et al. (2000). These authors however indicated that the full range of H_2 level population could not be reproduced by a single shock model. In fact, Le Bourlot et al. (2002) showed that only a mixture between one J-type shock and one C-type shock model was able to account for the population of both the low and the high energy levels. In this work, we try to reproduce the observed excitation diagram of H_2 and strongest H_2 1-0S(1) line profile from the OMC-1 Peak 1 with one of our bow shock models.

We ran a new grid of models at the pre-shock conditions in Orion, $n_H = 10^6$ cm⁻³ (White et al. 1986; Brand et al. 1988; Hollenbach & McKee 1989; Kaufman & Neufeld 1996; Kristensen et al. 2008). We limited the age to 1000 yr, which roughly corresponds to the

Table 3. Best-fitting parameters of the OMC-1 Peak 1 (see Fig. 15) with our model. We give an estimation of the 3σ uncertainty range for parameters ψ and b_0 (see text).

Parameter	Value	Note
n_H	10^6 cm ⁻³	Pre-shock density of H nuclei
b_0	4.5 ± 0.9	Strength of the magnetic field
u_0	≥ 30 km s ⁻¹	3D terminal velocity
Age	10^3 yr	Shock's age
ψ	$90^\circ \pm 30^\circ$	Orientation of the magnetic field
β	2.1 ± 0.2	Shock shape

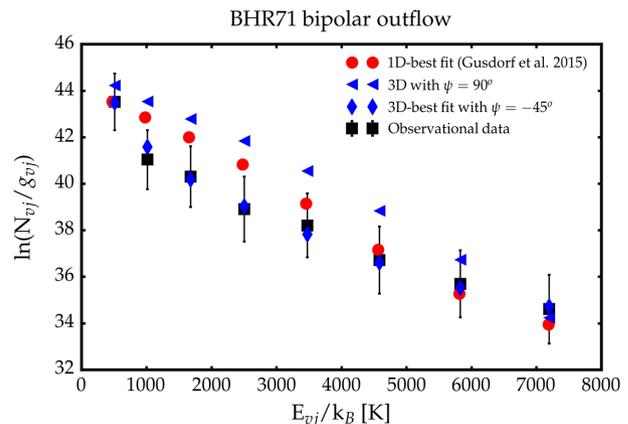


Figure 14. Comparison between BHR 71 observations and several bow shock models. Red circles: best fit with the 1D model of Gusdorf et al. (2015); green diamonds: our own corresponding 1D model (a 3D model with velocity close to 22 km s⁻¹ and $\Psi = 90^\circ$ so that the transverse magnetic field is uniform); blue diamonds: best fit with our 3D model (same as the previous model, but with magnetic field orientation $\Psi = -44^\circ$).

dynamical age of the outflow (Kristensen et al. 2008). At these densities, the shocks should have reached steady state since long.

Then we explore the parameter space of possible bow shocks and seek the best-fitting model. We considered u_0 between 20 and 100 km s⁻¹ and we varied b_0 from 1 to 6 with step 0.5. For each value of b_0 , we let the angle ψ vary from 0° to 90° with step 5°. Finally, we explore the shape of the shock for β in the interval from 1.0 to 3.0 with step of 0.2.

We compute the χ^2 for the 17 transitions with $v = 0$ among the 55 transitions that have been measured, discarding the upper limits (table 3 of Rosenthal et al. 2000). The parameters that best fit the excitation diagram are listed in Table 3. We also provide an estimation of the 3σ uncertainty range for some parameters by investigating the shape of the χ^2 well around the best value, as we did above for parameter Ψ in the case of BHR 71. The best model convincingly reproduces nearly all the lines ($\chi = 0.4$), as long as the terminal velocity is greater than 30 km s⁻¹. The comparison to the observations is displayed in Fig. 15: both the low- and high-energy regimes of the excitation diagram are obtained with the same model. The best-matching models found by Rosenthal et al. (2000) are also displayed for comparison. On the other hand, they consist in a mixture of two C-type shock models from Kaufman & Neufeld (1996) that reproduce well low energy levels, and on the other hand, in a single J-type shock model from Brand et al. (1988) for high energy levels. We also checked the NY08 approximation. Our best-fitting value is obtained at $b_{SE} = 3.2$ for $\chi = 0.6$. Again, this

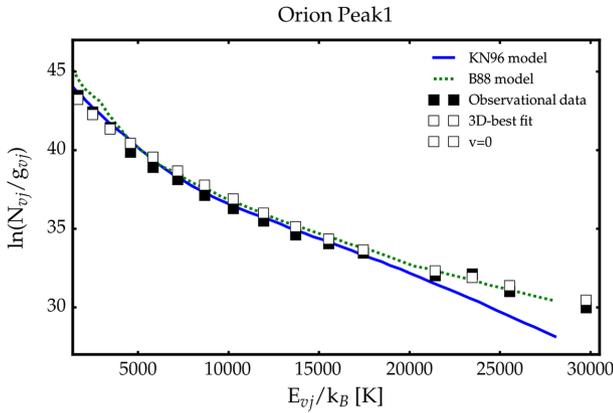


Figure 15. H_2 excitation diagram observed in OMC-1 Peak 1 (Rosenthal, Bertoldi & Drapatz 2000) compared with various models: our best-fitting 3D model of bow shock (open symbols), and the best-fitting models from Rosenthal et al. (2000): a combination of two planar C-shocks models from Kaufman & Neufeld (1996) (KN96) and one J-type shock model from Brand et al. (1988) (B88).

approach yields satisfying results for levels with a low excitation energy but tends to deviate at high excitation energy.

4.2 H_2 emission line profiles

Smith & Brand (1990b) pioneered the study of the emission-line profile of molecular hydrogen from a simple C-type bow shock. We revisit their work using our models that improve on the treatment of shock age, charge/neutrals momentum exchange, cooling/heating functions, the coupling of chemistry to dynamics and the time-dependent treatment of the excitation of H_2 molecules. We also introduce line broadening due to the thermal Doppler effect.

In the shock's frame, the gas flows with velocity $\mathbf{v}(r, u_\perp, \varphi) = (\hat{\mathbf{l}} u_\parallel + \hat{\mathbf{n}} u(r, u_\perp, b_\parallel))$, where r is the distance within the shock thickness (orthogonal to the bow shock surface) and $u(r, u_\perp, b_\parallel)$ is the shock orthogonal velocity profile as computed in the 1D model. In the observer's frame, the emission velocity becomes $\mathbf{v}_{\text{obs}} = \mathbf{v} - \mathbf{u}_0$. However the observer only senses the component along the line of sight: $\mathbf{v}_{\text{obs}} \cdot \hat{\mathbf{l}}$ with $\hat{\mathbf{l}}$ a unit vector on the line of sight, pointing towards the observer. When this is expressed in the observer's frame, the emission velocity becomes $v_{\text{rad}} = -\mathbf{v}_{\text{obs}} \cdot \hat{\mathbf{l}}$.

We assume the H_2 emission to be optically thin. Then the line profile is defined by integration over the whole volume of the bow shock, including the emission coming from each unit volume inside each planar shock composing the bow shock. The line emission at velocity v_r can be computed as follows:

$$f(V_r, i) = \int_{u_\perp} P(u_\perp) du_\perp \int_{\varphi} \frac{d\varphi}{2\pi} \times \int_r dr \frac{R_0^2}{\sqrt{2\pi}\sigma_T(r, u_\perp, b_\parallel)} \epsilon(r, u_\perp, b_\parallel) e^{-\frac{[v_{\text{rad}}(r, u_\perp, b_\parallel) - V_r]^2}{2\sigma_T^2(r, u_\perp, b_\parallel)}}, \quad (11)$$

which includes Doppler broadening with $\sigma_T^2(r, \alpha) = k_B/m_{\text{H}_2} T_{\text{H}_2}(r, u_\perp, b_\parallel)$, the thermal velocity of the H_2 molecule. Note that the dependence on the azimuthal angle φ occurs both in the expression of b_\parallel (see equation 8) and the projection of \mathbf{v}_{obs} on to the line-of-sight direction $\hat{\mathbf{l}}$.

Fig. 16(a) shows the effect of varying the viewing angle i on the 1–OS(1) line shape. When the observer looks at the bow shock from the point of view of the star ($i = 0^\circ$), all the emission is blueshifted,

with a stronger emission at a slightly positive velocity, coming from the part of the shock structure closest to the star, close to the J-type front where this line is excited. As the viewing angle turns more to the flank (i increases), the line of sight intercepts two sides of the working surface, one going away and the other going towards the observer. The line profile then becomes doubly peaked. We checked that the integrated line emission did not vary with the viewing angle i .

Fig. 17(a) shows how the age affects the 1–OS(1) line profile at a given viewing angle of 60° . As the shock becomes older, the J-tail entrance velocity decreases: this explains why the two peaks of the line profile get closer to each other as age proceeds. The velocity interval between the two peaks is proportional to the entrance velocity in the J-type tail of the shocks. Furthermore, as the entrance velocity decreases, the temperature inside the J-shock decreases accordingly and the Doppler broadening follows suit: the line gets narrower as time progresses. The width of the 1–OS(1) could thus serve as an age indicator, provided that the shock velocity is well known.

The 0–OS(1) line corresponds to a much lower energy level than the 1–OS(1) line: while the 1–OS(1) is sensitive to temperature and shines mostly around the J-type front, the 0–OS(1) line emits in the bulk of the shock, where gas is cooler. Since the 0–OS(1) line probes a colder medium, the resulting profiles are much narrower (Fig. 16b). For early ages (100 and 1000 yr), one can however still notice the double peak signature of the J-front (Fig. 17b). Because the temperature in the magnetic precursor is much colder than the transition's upper level temperature of 1015 K for level (0,3). At these early ages, the 0–OS(1) line is shut off in the magnetic precursor (see Fig. 6, for example) and it therefore probes the J-shock part.

These results show that a wealth of dynamical information is contained in the line shapes. However, this information is hard to retrieve, as the line shaping process is quite convoluted. In particular, each line probes different regions of the shock depending on the upper level sensitivity to temperature. As an illustration, we plot the normalized line shapes for three different transitions in a 20 km s^{-1} bow shock with pre-shock density 10^4 cm^{-3} , age 1000 yr and $b_0 = 1$ (Fig. 18). This figure is meant to be compared with fig. 2's top panel in Santangelo et al. (2014), which plots resolved observations of H_2 lines in HH 54. These observations come from two different slit positions: a CRIRES slit for 1–OS(1) and 0–OS(9) near the tip of the bow, orthogonal to the outflow axis, and a VISIR slit for the 0–OS(4) line along this axis. On the other hand, our models cover the whole extent of our bow shock, which questions the validity of the comparison. Despite this, some similarities are striking: the two lines 1–OS(1) and 0–OS(9) match perfectly and are blueshifted. The insight from our computations allows us to link the good match between the line profiles of 1–OS(1) and 0–OS(9) to the very similar energy of the upper level of the two transitions. Furthermore, we checked in our models that the emission from the low-energy 0–OS(4) is completely dominated by the C-type parts of our shocks, where the velocity is still close to the ambient medium velocity: this explains why this line peaks around $v_r = 0$. This C-type component should shine all over the working surface of the bow shock, and the VISIR slit along the axis probably samples it adequately. Conversely, we checked that the emission coming from both lines 1–OS(1) and 0–OS(9) is completely dominated by the J-type parts of our shocks. Hence they should shine near the tip of the bow shock (traversed by the CRIRES slit) at a velocity close to that of the star and its observed radial speed should lie around $-u_0 \cos(i)$, blueshifted for an acute angle i .

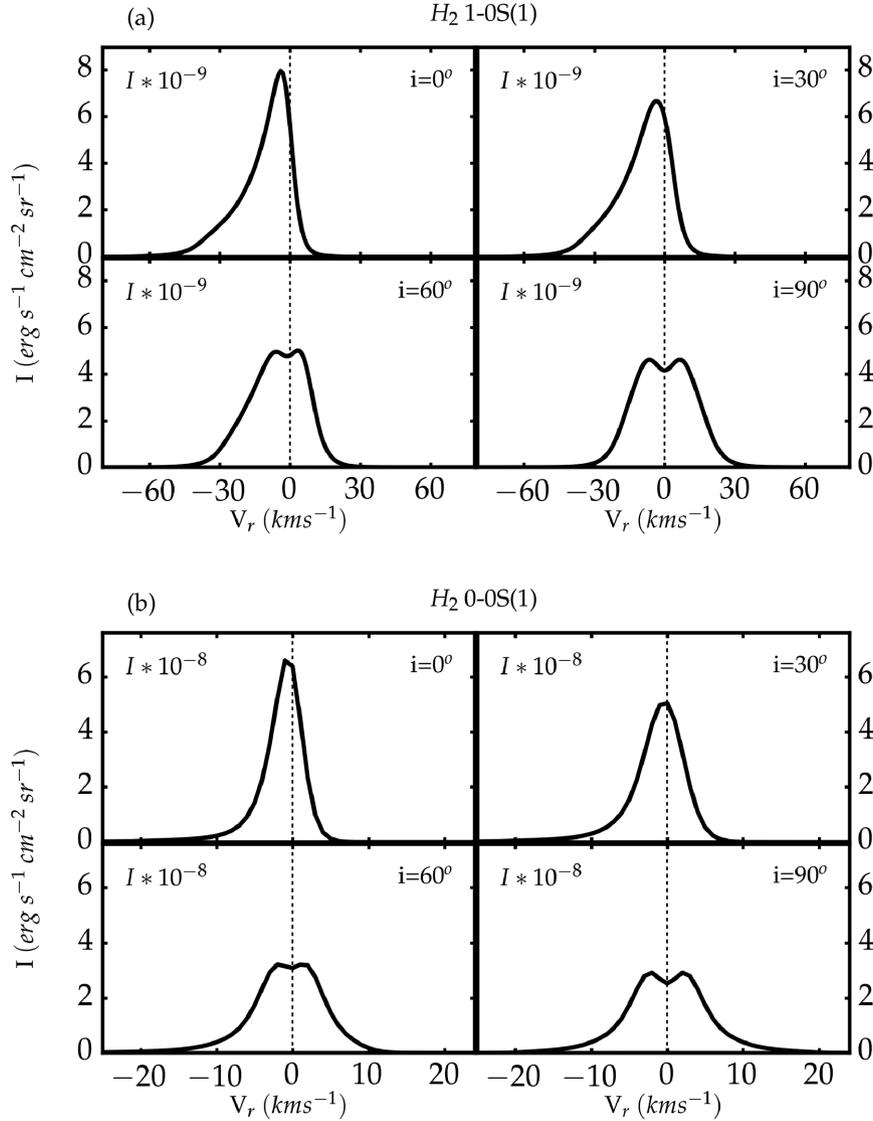


Figure 16. Line profiles of a whole bow shock parametrized by $u_0 = 40 \text{ km s}^{-1}$, age = 10^2 years, $b_0 = 1$ and $\phi = 0^\circ$. (a) for the H_2 1–0S(1) line and (b) for the H_2 0–0S(1) line. This figure shows the effect of the viewing angle on the line profile.

Brand et al. (1989) managed to observe a few wide H_2 line profiles from OMC-1 Peak 1 by using the United Kingdom Infrared Telescope (UKIRT), configured at a 5 arcsec sky aperture and with a resolution of 12 km s^{-1} full width at half-maximum (FWHM). A single shock model was not able to reproduce these wide observed lines (as indicated by Brand et al. 1989; Rosenthal et al. 2000). A C-type bow shock model of Smith, Brand & Moorhouse (1991b) could reproduce these lines and widths, but this assumed an extremely high magnetic field strength of $\geq 50 \text{ mG}$ (which amounts to $b_{||} \geq 50$), while independent measurements in the same region gave much lower values: 3 mG by Zeeman splitting (Norris 1984) or 10 mG by polarization (Chrysostomou et al. 1994). Here we use the best parameters listed in Table 3 to try and reproduce the profile of the H_2 1–0S(1) line with a more reasonable magnetization. As mentioned in the previous subsection, the excitation diagram alone did not allow to constrain the terminal shock velocity. Now, the width of the profile allows us to constrain the velocity to about $u_0 = 100 \text{ km s}^{-1}$ as illustrated by Fig. 19. The viewing angle $i \simeq 90^\circ$ can be adjusted to the position of the peak of the line profile.

Note that shock models with $u_{\perp} > 40 \text{ km s}^{-1}$ are not included in these line shape models. They should contribute little to the emission since H_2 molecules are dissociated at high shock velocities (both due to the high temperatures experienced in these shocks and to their radiative precursors).

5 DISCUSSION AND CONCLUSION

In this study, we provide a mathematical formulation that arbitrarily links the shape of a bow shock to a distribution of planar shocks. Then, a simple convolution of this distribution with a grid of planar shocks allows to produce intensities and line shapes for any transition of the H_2 molecule.

We used that property to explain the dependence of the excitation diagram of a bow shock to its parameters: terminal velocity, density, shape, age and magnetization properties (magnitude and orientation). The combination of a steeply decreasing distribution with a threshold effect linked to the energy of the upper level of each transition yields a ‘Gamow-peak’ effect. A given H_2

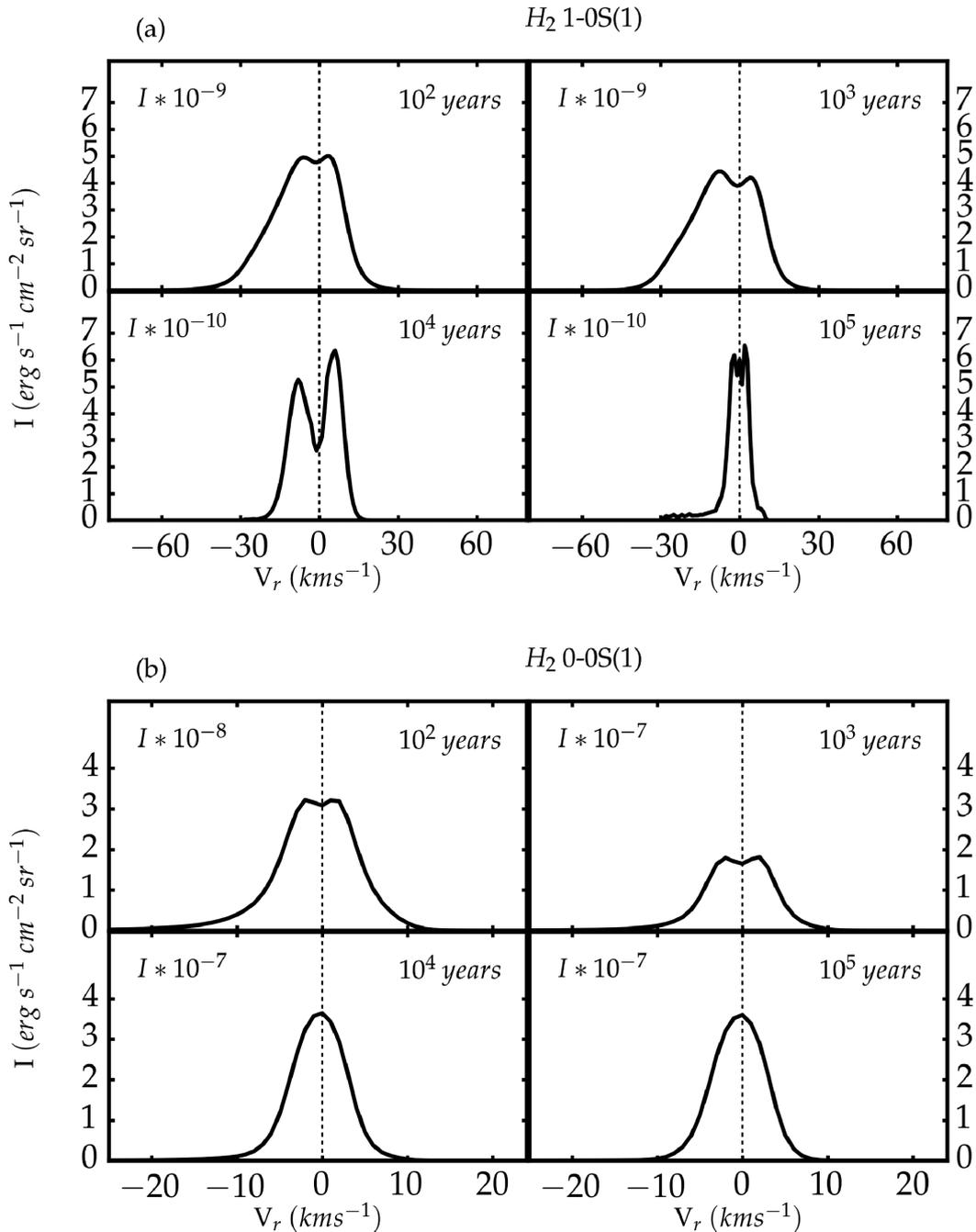


Figure 17. Line profiles of a whole bow shock parametrized by $u_0 = 40 \text{ km s}^{-1}$, $i = 60^\circ$, $b_0 = 1$ and $\phi = 0^\circ$. (a) for the H_2 1-0S(1) line and (b) for the H_2 0-0S(1) line. This figure shows the effect of the age on the line profile. Note the factor 10 change in flux scale between some panels.

level then reaches a saturation value when the terminal velocity is above a threshold that depends directly on the energy of the level. The magnetic field and the age dependence enter through the transition between the J-type and the C-type part of a time-dependent magnetized shock.

The wings of a bow shock usually have a larger surface than its nose. From this, it follows that the distribution and hence the global emission properties of a bow shock are generally dominated by low-velocity shocks. A direct consequence is that the excitation diagram of a whole bow shock resembles a 1D planar shock with a lower velocity: data interpretation with 1D models is likely

to be biased towards low velocity. However, if the terminal velocity of the bow shock was estimated independently (from line Doppler broadening measurements, for example), we suggest that a magnetization adjustment from 1D models to the excitation diagram will overestimate the magnetization parameter. Previous authors (NY08; Neufeld et al. 2009) have suggested that the statistical equilibrium approximation could accurately reproduce observed intensities of low-energy pure rotational levels. We confirm this result, and its probable link to the distribution of entrance velocities as pointed out by NY08. However, we remark that this simple model does not satisfyingly reproduce the observations of the higher lying

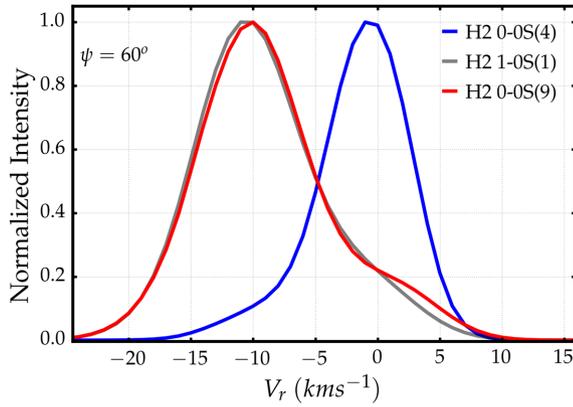


Figure 18. Line profiles of three different transitions in a bow shock at age 100 yr with parameters $u_0 = 20 \text{ km s}^{-1}$, $n_H = 10^4 \text{ cm}^{-3}$, $b_0=1$ and viewing angle $i = 60^\circ$.

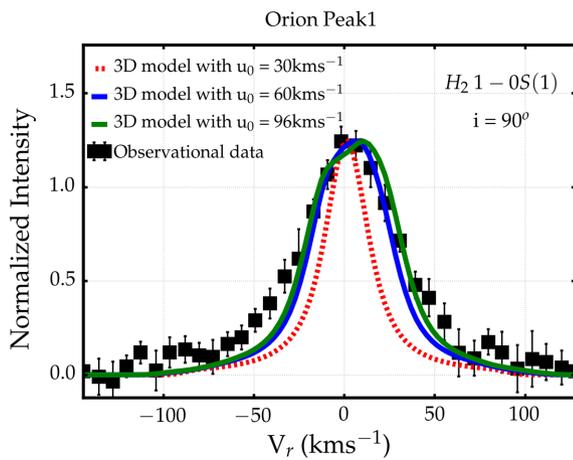


Figure 19. Comparison of the H_2 line profile between OMC-1 Peak 1 observation and bow shock model. Black square: the observational data (Brand et al. 1989). Solid lines: our 3D model using parameters in Table 3 with different values of u_0 . The best 3D model constrains the terminal shock velocity to about 100 km s^{-1} .

transitions. A possible interpretation is that these levels are more sensitive to J-type shocks, where the sudden temperature jump is more likely to put the gas away from statistical equilibrium.

We provide some illustrations of how our results could improve the match between model and observations in BHR 71 and Orion OMC-1. We show that 3D models largely improve the interpretation. In particular, we are able to obtain much better match than in previous works with relatively little effort (and with the addition of only one or two parameters compared to the 1D models: the magnetic field orientation and the shape of the bow shock).

We compute line shapes with an unprecedented care and examine their dependence to age and viewing angle. Although line shapes result from a convoluted process, they contain a wealth of dynamical information. In particular, we link the double-peaked structure of 1–0S(1) in young bow shocks to the dynamics of their J-type part components. The line width results from the combined effects of geometry, terminal velocity and thermal Doppler effect. We show how different lines probe different parts of the shocks depending on the temperature sensitivity of the excitation of their upper level. We show how our 3D model can reproduce the broad velocity profile of the H_2 1–0S(1) line in Orion Peak 1 with a magnetization compatible with other measurements. The excitation diagram fails

to recover dynamical information on the velocity (it only gives a minimum value), but the line shape width provides the missing constraint.

Further work will address some of the shortcomings of our method. First, it will be straightforward to apply similar techniques to the shocked stellar wind side of the bow shock working surface. Second, the different tangential velocities experienced on the outside and on the inner side of the working surface will very likely lead to turbulence and hence mixing, as multidimensional simulations of J-type bow shocks show. A challenge of the simplified models such as the ones presented here will be to include the mixing inside the working surface. All models presented here were run for a pre-shock ortho–para ratio of 3: the dilute ISM is known to experience much lower ratios and we will explore the effect of this parameter on the excitation diagrams of bow shocks in further work. Finally, our methods could be used to model other molecules of interest, provided that we know their excitation properties throughout the shock and that their emission remains optically thin. We expect that such developments will improve considerably the predictive and interpretative power of shock models in a number of astrophysical cases.

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