

# (0001) Interfaces between M2O3 corundum oxides (M = Al, Ti, V, Cr, Fe).

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#### ACCEPTED MANUSCRIPT

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#### Highlights

- Fundamental analysis of transition metal corundum oxide interfaces with DFT+U calculations
- $\bullet$  Redox reaction at  $\rm Ti_2O_3/V_2O_3$  and  $\rm Ti_2O_3/Fe_2O_3$  interfaces driven by band off-sets
- Additional weaker electron transfer follows the difference of ionicity of parent oxides
- Interface stability can be deduced from energetics of corresponding mixed bulk oxides

## (0001) interfaces between $M_2O_3$ corundum oxides (M = Al, Ti, V, Cr, Fe).

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#### Abstract

The structural quality of oxide/oxide interfaces, their chemistry, and the nature of their electronic states are critical properties for new promising applications and require continuous advances in their fundamental understanding. To this goal, we have performed a theoretical study of a series of (0001) M<sub>2</sub>O<sub>3</sub>/M'<sub>2</sub>O<sub>3</sub> interfaces (M, M' = Al, Ti, V, Cr, Fe) between simple and transition metal oxides crystallizing in the corundum structure. Our DFT+U results reveal two qualitatively different mechanisms of interface charge redistribution: an interfacial oxidation-reduction reaction occurring at Ti<sub>2</sub>O<sub>3</sub>/V<sub>2</sub>O<sub>3</sub> and Ti<sub>2</sub>O<sub>3</sub>/Fe<sub>2</sub>O<sub>3</sub> contacts, and a much weaker electron transfer along anion-cation bonds which follows the difference of ionicity between the two constituting oxides at all interfaces. At variance with interfaces between *sp* semiconductors, the band bending does not propagate beyond one or two atomic layers. More generally, our results show that the nature of the interface electronic structure and the energetics of its formation can be tightly linked to the properties of the corresponding bulk oxides, thus providing a precious tool for designing oxide/oxide interfaces of required characteristics.

*Keywords:* transition metal corundum oxides; oxide/oxide interfaces; DFT+U calculations; interfacial redox reaction; band off-sets; ionicity

#### 1. Introduction

Oxides have long been used in a variety of applications, including catalysis, electronics and optoelectronics, or as thermal or electrical insulating barriers. More recently, all-oxide electronic devices have progressively replaced many of those traditionally based on semiconductors. In these fields, the structural quality of oxide/oxide interfaces, their precise composition, and the nature of their electronic states play a decisive role. It is also worth mentioning a more fundamental interest in oxide interfaces triggered by the discovery of emergent phenomena associating charge, spin and orbital degrees of freedom [1].

Despite this wide context, there are very few systematic studies of oxide/oxide interfaces which try to relate their characteristics to those of the constituting oxides. The most significant ones concern perovskite oxides [2] or the  $Cr_2O_3/Fe_2O_3$  interface [3, 4, 5, 6]. Here our goal was to perform a thorough and systematic study of six (0001) interfaces between transition metal corundum oxides, includ-

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ing Ti<sub>2</sub>O<sub>3</sub>, V<sub>2</sub>O<sub>3</sub>, Cr<sub>2</sub>O<sub>3</sub> and Fe<sub>2</sub>O<sub>3</sub>. We have also considered an hypothetical Ti<sub>2</sub>O<sub>3</sub>/Al<sub>2</sub>O<sub>3</sub> interface as to include a more ionic oxide with pure *sp* character. Using a DFT+U approach, we have analyzed the nature of the states close to the Fermi level, the interface charge transfers, and the formation of interfacial dipoles. We link these interface characteristics to the band alignment between the constituting oxides and their difference in ionicity. Moreover, we evidence strong similarities between the energetics of  $M_2O_3/M'_2O_3$  interfaces and the formation energies of mixed MM'O<sub>3</sub> oxides of corundum-type structures.

The paper is organized in the following way. After a section describing the computational methods and settings (Section 2), we summarize the results on anionic-type and cationic-type interfaces (Section 3). A discussion (Section 4) highlights two qualitatively different mechanisms of interface charge redistribution, both characterized by extremely short penetration lengths, and establishes a direct link between the interface stability and the tendency for cationic mixing in the corresponding bulk corundum-type oxides. A conclusion follows (Section 5).

#### 2. Computational details

DFT calculations are performed with the Vienna Ab-initio Simulation Package (VASP) [7, 8] using the Projector Augmented Wave (PAW) method [9, 10] to represent the electron-core interaction and a 400 eV energy cutoff in the development of Kohn-Sham orbitals on a plane-wave basis set. Transition metal 3p states are systematically considered as semi-core states. The DFT+U approach proposed by Dudarev [11, 12] is used together with the dispersion-corrected exchange-correlation functional (optB88-vdW) [13, 14, 15], as to improve the description of interfacial electronic structure and energetics. As in our previous work [16], we use U values equal to 1.0, 1.7, 3.0, and 3.0 for  $Ti_2O_3$ ,  $V_2O_3$ ,  $Cr_2O_3$ , and  $Fe_2O_3$ , respectively, which correctly account for the electronic characteristics of the bulk oxides. All calculations are spin-polarized and the non-magnetic (NM for  $Al_2O_3$  and  $Ti_2O_3$ ), G-type (for  $Cr_2O_3$  and  $V_2O_3$ ) and C-type (for  $Fe_2O_3$ ) antiferromagnetic (AF) ground state orderings computed for the corresponding bulk materials [16] are systematically preserved. Ionic charges are estimated with the partition scheme proposed by Bader [17, 18] and magnetic moments are obtained by integration of the spin density within the Bader's volumes. Bulk and interface configurations are plotted with VESTA [19]

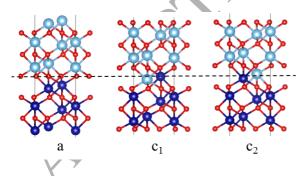


Figure 1: Atomic structure at anionic (a) and cationic  $(c_1 and c_2)$  interfaces. Oxygen and metal atoms are represented with red and blue (dark or light) balls, respectively.

Three types of interfaces are considered, involving either an interfacial oxygen layer (Figure 1, left, labeled *a* or *anionic* in the following), or an interfacial cationic bi-layer (Figure 1, right, labeled  $c_1$  and  $c_2$  or *cationic*). At a interfaces, the interfacial atoms are all equivalent, with two cation first neighbors of one type and two of the other. On each side of this layer, the two cations are nonequivalent. One is linked via a short inter-plane bond to a cation of its own type ("bulk-like" bond) and one with a cation of opposite type ("interfacial" bond). At c interfaces, a cation of a given type may occupy two inequivalent positions. In the configuration  $c_1$ , an interfacial cation has three in-plane first neighbors, zero inter-plane first neighbor and six inter-plane second neighbors with cations of opposite type. In the second configuration (noted  $c_2$ ) in which the two interfacial cations have exchange positions, an interfacial cation has three in-plane first neighbors, one inter-plane first neighbor and three inter-plane second neighbors with cations of opposite type. In both cases, the oxygen atoms which are the closest to the interface have three cations first neighbor of one type and one of the other type, instead of having four cations first neighbors of the same type in the bulk. It should be noted that all anionic and cationic interfaces are non-polar [20]. Indeed, their repeat units of respective composition  $O_{1.5}/M_2/O_{1.5}$  (for the anionic interface) and  $M/O_3/M$  (for the cationic interfaces) bear no dipole moment and thus do not produce a polarization discontinuity [21].

Interfaces are represented by superlattices with six  $M_2O_3$  formula units of each oxide, with an interface registry which preserves the corundum stacking. We have checked that alternative registries produce less stable configurations. The in-plane lattice parameters are fixed at the average values between those of the two corresponding bulks (4.80 Å, 5.14 Å, 5.05 Å, 5.04 Å, 5.06 Å, for bulk  $Al_2O_3$ ,  $Ti_2O_3$ ,  $V_2O_3$ ,  $Cr_2O_3$ , and  $Fe_2O_3$ , respectively [16]), and the out-of-plane parameters are optimized until the corresponding components of stress tensor are smaller than  $0.01 \text{ eV}^{\text{A}-3}$ . In addition, all atomic position are relaxed until maximum forces get smaller than 0.01 eV Å<sup>-1</sup>. The Brillouin zone of the  $(1 \times 1)$  interface unit cell is sampled on a  $\Gamma$ centered  $(8 \times 8 \times 1)$  Monkhorst-Pack grid [22].

The stability of an  $M_2O_3/M'_2O_3$  interface is estimated from the interface energy  $E_{int}$ :

$$E_{int} = \frac{(E_{M_2O_3/M'_2O_3} - (E'_{M_2O_3} + E'_{M'_2O_3}))}{2S} \quad (1)$$

in which  $E_{M_2O_3}$ ,  $E_{M'_2O_3}$  are the energies of six formula units of bulk  $M_2O_3$  and  $M'_2O_3$  materials (at the average in-plane lattice parameter),  $E_{M_2O_3/M'_2O_3}$  is the energy of the constituted heterostructure, and S is the interface area. Factor 2 accounts for the two equivalent interfaces in the unit cell.

#### 3. Results

In this section, the numerical results for the anionic and cationic interface structures are reported. We start by a comprehensive description of the cationic interfaces, and, in a second step, we highlight their similarities and differences with the anionic interfaces.

#### 3.1. Cationic interfaces

Table 1 summarizes the electronic, magnetic and energetic properties of the most stable cationic configurations for all interfaces under consideration. Figures 2 and 3 display their local density of states (LDOS) projected on the cations at the interface and in bulk-like positions.

All interfaces are subject to similarly weak structural distortions since the lattice mismatch between the constituent oxides never exceeds 1.5%, except between Ti<sub>2</sub>O<sub>3</sub> and Al<sub>2</sub>O<sub>3</sub> for which it reaches 7%. At variance, the interface electronic structures display much bigger differences with respect to their bulk counterparts. On the one hand, at the  $Ti_2O_3/V_2O_3$  and  $Ti_2O_3/Fe_2O_3$  interfaces, a strong charge redistribution takes place between the two interfacial cations. It changes their oxidation states and thus can be seen as a local reduction-oxidation (redox) reaction. These two interfaces are also characterized by large negative interface energies. On the other hand, much smaller but not negligible interface charge rearrangements are also present at the five other interfaces. They principally reflect the charge modifications of the anions and systematically produce positive interface energies. A detailed presentation of the results for these two sets of interfaces is given in the following.

In the case of  $\text{Ti}_2\text{O}_3/\text{V}_2\text{O}_3$  and  $\text{Ti}_2\text{O}_3/\text{Fe}_2\text{O}_3$  interfaces which are characterized by a strong electron redistribution, the clearest and most consistent information can be deduced from the LDOS, Fig. 2, and magnetic moments, Tab. 1. Indeed, in the  $\text{Ti}_2\text{O}_3/\text{Fe}_2\text{O}_3$  LDOS, the bulk-like Ti LDOS peak just below  $E_F$  has lost most of its weight on the interface Ti, implying a loss of formally one electron and thus a formal Ti<sup>+4</sup> oxidation state. In parallel, the interfacial Fe-projected LDOS displays an additional filled peak compared to the bulk one, thus

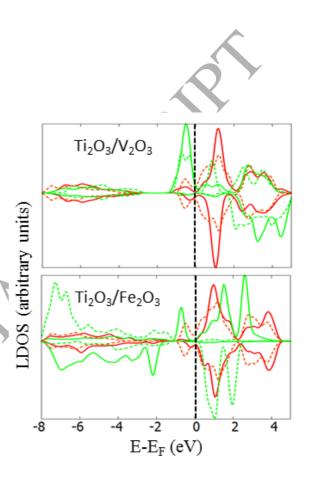


Figure 2: Densities of states projected on interfacial (plain lines) and bulk-like (dashed lines) cations at cationic  $M_2O_3/M'_2O_3$  interfaces:  $Ti_2O_3/V_2O_3$  and  $Ti_2O_3/Fe_2O_3$ . Red and green colors refer to M and M' cations, respectively.

0	,	$(P^*D)^*$			
		$\mathrm{Ti}_{2}\mathrm{O}_{3}$	$Al_2O_3$	$\mathrm{Ti}_{2}\mathrm{O}_{3}/\mathrm{Al}_{2}\mathrm{O}_{3}$ $(c_{1})$	$Ti_2O_3/Al_2O_3$ (a)
	$Q_M$	1.90	2.49	1.84, 1.98/2.50	1.97, 1.93/2.50
	$\mu_M$	0.0	0.0	0.0, 0.0/0.0	0.0/0.0
	$Q_O$	-1.27	-1.66	-1.39/-1.56	-1.48
	$Q_{int}$	-	-	-0.33/+0.33	-0.29/+0.29
	$E_{int}$	-	-	0.25	0.27
	ine	$\mathrm{Ti}_{2}\mathrm{O}_{3}$	$V_2O_3$	$Ti_2O_3/V_2O_3(c_1)$	$Ti_2O_3/V_2O_3$ (a)
	$Q_M$	1.91	1.84	2.02, 2.10/1.62, 1.72	2.01, 2.02 / 1.75, 1.86
	$\mu_M$	0.0	1.8	0.3,  0.0/2.3, 2.1	$0.3,  0.1 \neq 2.0,  2.0$
	$Q_O$	-1.27	-1.23	-1.26/-1.24	-1.28
	$Q_{int}$	-	-	+0.44/-0.44	+0.27 / -0.27
	$E_{int}$	-	-	-0.28	-0.18
	ine	$Ti_2O_3$	$Cr_2O_3$	$Ti_2O_3/Cr_2O_3(c_1)$	$Ti_2O_3/Cr_2O_3$ (a)
	$Q_M$	1.91	1.77	2.01/1.69	1.96 / 1.73, 1.77
	$\mu_M$	0.0	2.9	0.4/3.0	0.7, 0.5 / 3.0, 2.8
	$Q_O$	-1.27	-1.18	-1.25/-1.21	-1.24
	$Q_{int}$	-	-	+0.20/-0.20	+0.14/-0.14
	$E_{int}$	-	-	0.15	0.10
	ine	$\mathrm{Ti}_{2}\mathrm{O}_{3}$	$\mathrm{Fe}_2\mathrm{O}_3$	$Ti_2O_3/Fe_2O_3(c_2)$	$Ti_2O_3/Fe_2O_3$ (a)
	$Q_M$	1.92	1.74	2.03, 2.15 / 1.44, 1.49	2.08, 2.05 / 1.66, 1.50
	$\mu_M$	0.0	4.1	0.1 / 3.7	0.2, 0.1 / 3.9, 3.7
	$Q_O$	-1.28	-1.16	-1.23/-1.18	-1.21
	$Q_{int}$	-	-	+0.68/-0.68	+0.47/-0.47
	$E_{int}$	-	-	-0.65	-0.45
	ine	$V_2O_3$	$Cr_2O_3$	$V_2O_3/Cr_2O_3(c_1)$	$V_2O_3/Cr_2O_3$ (a)
	$Q_M$	1.84	1.77	1.86 / 1.76	1.86, 1.87 / 1.77, 1.77
	$\mu_M$	1.7	2.9	1.8 / 2.8	$1.7,  1.8 \ / \ 2.9$
	$Q_O$	-1.22	-1.18	-1.22 /-1.20	-1.21
	$Q_{int}$	-	<b>Y</b> -	+0.08/-0.08	+0.06/-0.06
	$E_{int}$		-	0.02	0.01
	ine	$V_2O_3$	$\mathrm{Fe}_2\mathrm{O}_3$	$V_2O_3/Fe_2O_3~(c_2)$	$V_2O_3/Fe_2O_3$ (a)
	$\dot{Q}_M$	1.85	1.74	1.96 / 1.66	$1.90,  1.84 \ / \ 1.76,  1.74$
	$\mu_M$	1.7	4.1	1.5 / 4.0	1.6, 1.8 / 4.1, 4.1
	$Q_O$	-1.23	-1.16	-1.22/-1.19	-1.21
(	$Q_{int}$	-	-	+0.15/-0.15	+0.08/-0.08
	$E_{int}$	-	-	0.10	0.13
	ine	$Cr_2O_3$	$Fe_2O_3$	$\operatorname{Cr}_2\operatorname{O}_3/\operatorname{Fe}_2\operatorname{O}_3(c_2)$	$Cr_2O_3/Fe_2O_3$ (a)
	$Q_M$	1.77	1.74	1.79 / 1.76	1.79, 1.77 / 1.78, 1.76
	$\mu_M$	2.9	4.1	2.9/4.1	2.8, 2.9 / 4.1, 4.1
	$Q_O$	-1.18	-1.16	-1.18 /-1.18	-1.19/-1.17
	$Q_{int}$	-	-	+0.02/-0.02	-0.00/+0.00
	$E_{int}$	-	-	0.12	0.16
	ine				

Table 1: Characteristics of constituting bulk  $M_2O_3$  and  $M'_2O_3$  oxides (at average in-plane lattice parameter) and of the most stable cationic  $(c_1 \text{ or } c_2)$  and anionic (a)  $M_2O_3/M'_2O_3$  interfaces: Bader charges of cations  $Q_M$  and oxygen atoms  $Q_O(e)$ , cation magnetic moments  $\mu_M(\mu_B)$ . Total Bader charges  $Q_{int}$  of each side of the interface (e) and interface energies  $E_{int}(J/m^2)$ .

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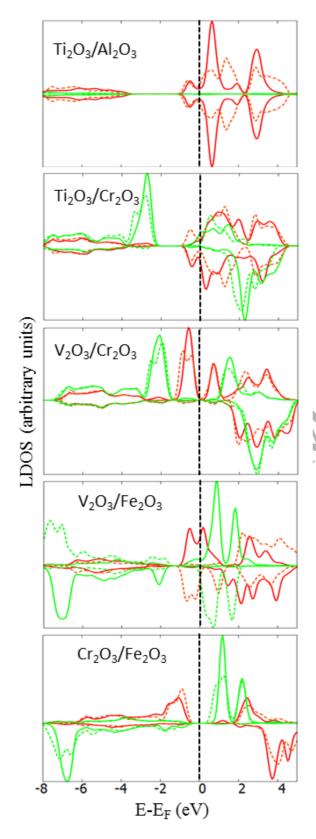


Figure 3: Same as Fig. 2 for cationic  $M_2O_3/M'_2O_3$  interfaces:  $Ti_2O_3/Al_2O_3$ ,  $Ti_2O_3/Cr_2O_3$ ,  $V_2O_3/Cr_2O_3$ ,  $6V_2O_3/Fe_2O_3$ , and  $Cr_2O_3/Fe_2O_3$ .

pointing to a  $Fe^{2+}$  formal oxidation state. This analysis is further confirmed by the vanishing value of  $\mu_{Ti}$ , characteristic of Ti<sup>+4</sup> in the absence of the Ti-Ti bonding responsible for the NM ground state in bulk  $Ti_2O_3[16]$ , and by the reduced magnetic moment on the interfacial Fe cation. Interestingly, a second cation on each side of the interface also experiences a change of oxidation state. The modifications of electronic structure lead to similar conclusions at the  $Ti_2O_3/V_2O_3$  interface, with a strong increase of  $\mu_V$  from 1.8  $\mu_B$  in the bulk to 2.3  $\mu_B$  on the interfacial vanadium atom and to 2.1  $\mu_B$  on one of the sub-interfacial vanadium atom. One should note that, at variance with sp-type semiconductor interfaces, an overlap between the narrow d states at the gap edges of these Mott-Hubbard oxides easily induces correlated shifts of whole d states across the Fermi level and, consequently, an actual oxydoreduction process. In that case, it is thus legitimate to talk of a change of cation oxidation states.

Consistently with this change, the titanium charges increase at these two interfaces and those of vanadium and iron atoms are reduced ( $\approx \pm 0.2$  at Ti<sub>2</sub>O<sub>3</sub>/V<sub>2</sub>O<sub>3</sub> and  $\pm 0.25 - 0.30$  at Ti<sub>2</sub>O<sub>3</sub>/Fe<sub>2</sub>O<sub>3</sub>). While the Bader charges do not give a direct information on formal charges, these variations are much larger than those at any of the remaining interfaces.

Finally, the changes of cation oxidation states deduced from the interface electronic structure are consistent with local structural modifications. Indeed, the interfacial Ti-O bond-lengths are shortened and the V-O and Fe-O expanded by  $\approx \pm 0.1$ Å, respectively, in line with the dependence of ionic radii on ionic charges  $(r_{M^{4+}} < r_{M^{3+}} < r_{M^{2+}})$  [23].

In the second set of interfaces, characterized by weaker electron redistributions, the cation oxidation states can also be deduced from the LDOS, Fig.3, and magnetic moments, Tab. 1. In particular, at the Ti<sub>2</sub>O<sub>3</sub>/Al<sub>2</sub>O<sub>3</sub>, V<sub>2</sub>O<sub>3</sub>/Cr<sub>2</sub>O<sub>3</sub> and Cr<sub>2</sub>O<sub>3</sub>/Fe<sub>2</sub>O<sub>3</sub> interfaces, the interfacial and bulk cations have quasi-identical LDOS in the Fermi level vicinity and their magnetic moments are very close to each other, clearly showing that the cation bulk 3+ oxidation state is maintained at both sides of the interface.

At the Ti<sub>2</sub>O<sub>3</sub>/Cr<sub>2</sub>O<sub>3</sub> and V<sub>2</sub>O<sub>3</sub>/Fe<sub>2</sub>O<sub>3</sub> interfaces, the metallic character of the electronic structure originating from hybridized cation states at  $E_F$ does not allow to unambiguously assign oxidation states to the interfacial cations. For example, at the Ti<sub>2</sub>O<sub>3</sub>/Cr<sub>2</sub>O<sub>3</sub> interface, the filled Ti peak below the Fermi level is up-shifted and partially depleted while, concomitantly, the Cr peak localized above  $E_F$  in bulk Cr<sub>2</sub>O<sub>3</sub> moves to lower energies, suggesting a small but non-vanishing electron redistribution between Ti and Cr, associated to small variations of the cation magnetic moments ( $\approx 0.15$  $\mu_B$ ) and Bader charges ( $\approx 0.1$  e).

Interestingly, while the cation charges are hardly modified at these five interfaces except when a small cation-cation hybridization takes place, the charges of interfacial oxygen atoms display larger variations. At each  $M_2O_3/M'_2O_3$  interface, they are close to an average of the bulk charges,  $Q_O \approx (3Q_O(M_2O_3) + Q_O(M'_2O_3))/4$  on the  $M_2O_3$  side and  $Q_O \approx (Q_O(M_2O_3) + 3Q_O(M'_2O_3))/4$  on the  $M'_2O_3$  side, consistently with their numbers of O-M and O-M' bonds.

To summarize, we find that structural distortions at cationic interfaces are systematically small, except in the case of  $\text{Ti}_2\text{O}_3/\text{Al}_2\text{O}_3$ , where the lattice mismatch between the two oxides is larger or when a redox reaction takes place. The latter occurs only at the  $\text{Ti}_2\text{O}_3/\text{V}_2\text{O}_3$  and  $\text{Ti}_2\text{O}_3/\text{Fe}_2\text{O}_3$  interfaces. The local redox reaction  $Ti^{3+} + M^{3+} \rightarrow Ti^{4+} + M^{2+}$  (M = V, Fe) results in strong modifications of the interfacial cation characteristics, and is associated with negative interface energies. At variance, at all other interfaces, the electronic rearrangements are much weaker. They mainly affect the charges on the interfacial oxygen atoms, and are associated with positive interface energies.

#### 3.2. Anionic interfaces

Despite their different atomic structure, Fig. 1, anionic interfaces share many common characteristics with the cationic ones, Tab. 1. In particular, this concerns the presence of the interfacial redox reaction and the negative interface energy at the very same two interfaces ( $Ti_2O_3/V_2O_3$  and  $Ti_2O_3/Fe_2O_3$ ), and the nuch weaker electronic rearrangements associated with positive interface energies in all the remaining cases. In the following we describe the features which are specific to these two sets of anionic interfaces.

At the Ti<sub>2</sub>O<sub>3</sub>/V<sub>2</sub>O<sub>3</sub> and Ti<sub>2</sub>O<sub>3</sub>/Fe<sub>2</sub>O<sub>3</sub> interfaces, the redox reaction only induces a partial cation-tocation electron exchange. At the Ti<sub>2</sub>O<sub>3</sub>/Fe<sub>2</sub>O<sub>3</sub> interface, the LDOS of the two interfacial Ti atoms are nearly identical, Fig. 4, each with approximately a half-emptied peak at the Fermi level. Similarly, the additional Fe state below  $E_F$  involves the two interfacial Fe ions, although unequally. This suggests that a single electron is exchanged across the anionic interface, and that the transferred charge is shared between the two Ti and the two Fe on each side of the interface. Conversely, at the  $Ti_2O_3/V_2O_3$  interface, the filling of the Ti state just below  $E_F$  is slightly larger than at the  $Ti_2O_3/Fe_2O_3$  junction, and the Fermi level intercepts a vanadium state localized on a single interfacial vanadium atom. At both interfaces, the Ti-O bond-lengths are shortened and the V-O or Fe-O bondlengths are expanded by  $\approx 0.1$  Å. However, the variations of the cation magnetic moments with respect to the bulks are less pronounced than at the cationic interfaces. Due to the metallic character of the  $Ti_2O_3/V_2O_3$  electronic structure and the sharing of the transferred electron between two Ti and two Fe atoms at the  $Ti_2O_3/Fe_2O_3$  interface, it is not possible to assign formal oxidation states to the interfacial cations as unambiguously as at the corresponding cationic interfaces.

Electronic and magnetic characteristics of the other five anionic interfaces (Ti<sub>2</sub>O<sub>3</sub>/Al<sub>2</sub>O<sub>3</sub>, Ti<sub>2</sub>O<sub>3</sub>/Cr<sub>2</sub>O<sub>3</sub> V<sub>2</sub>O<sub>3</sub>/Cr<sub>2</sub>O<sub>3</sub>, V<sub>2</sub>O<sub>3</sub>/Fe<sub>2</sub>O<sub>3</sub>, and Cr<sub>2</sub>O<sub>3</sub>/Fe<sub>2</sub>O<sub>3</sub>) are extremely close to those at the corresponding cationic interfaces. Only the interfacial oxygen charges are visibly different, due to their different local environment. They are close to the average of bulk values  $Q_O \approx (Q_O(M_2O_3) + Q_O(M'_2O_3))/2$  with a 1:1 ratio corresponding to their equal number of O-M and O-M' bonds with the neighboring cations.

To summarize, anionic interfaces present many electronic and energetic similarities with cationic interfaces. However, the strong electron transfer occurring at the  $Ti_2O_3/V_2O_3$  and  $Ti_2O_3/Fe_2O_3$  interfaces remains limited to one electron per unit cell or less, shared between two cations of each type. At variance with cationic interfaces, it cannot be unambiguously transcribed into well-defined changes of cation oxidation states.

#### 4. Discussion

In this section, we highlight two qualitatively different mechanisms of interface charge redistribution, both characterized by extremely short penetration lengths, and we establish a direct link between the interface stability and the tendency for cationic mixing in the corresponding bulk corundum-type oxides.

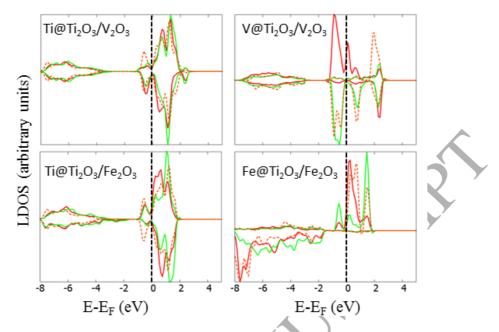


Figure 4: Densities of states projected on interfacial (plain lines) and bulk-like (dashed lines) cations at  $Ti_2O_3/V_2O_3$  and  $Ti_2O_3/Fe_2O_3$  oxygen interfaces. Red and green colors refer to the two inequivalent interface cations of each type.

#### 4.1. Cation-to-cation interfacial charge transfer

An understanding of charge transfers and dipole formation at interfaces is usually obtained by aligning the band structures of the two materials with respect to a common reference energy [2, 24, 25, 26, 27, 28, 29, 30, 31]. In the present case of  $M_2O_3/M'_2O_3$  interfaces, the most natural choice is the energy of the oxygen 1s states of the two oxides.

Actually, we have recently used a similar strategy to tackle the question of cation-to-cation electron transfer in a different context. We have considered mixed MM'O<sub>3</sub> compounds involving the same cations (M, M' = Al, Ti, V, Cr, and Fe) in bulk corundum-like structures, such as the ilmenite and the LiNbO<sub>3</sub> ones [16]. By comparing the electronic characteristics of the mixed MM'O<sub>3</sub> oxides with those of their M<sub>2</sub>O<sub>3</sub> and M'<sub>2</sub>O<sub>3</sub> pure parents, we have unambiguously identified the presence of a mixing-induced redox reaction in the case of  $TiVO_3$  and  $TiFeO_3$ , leading to  $Ti^{4+}$ ,  $V^{2+}$  and  $Fe^{2+}$ oxidation states. Conversely, in all other mixed MM'O<sub>3</sub> compounds, the cations remained in the 3+ oxidation state characteristic of the pure oxides. In the same study, relying on an alignment of the oxygen 1s levels of the parent oxides, we have pointed out that the existence of the redox reaction in  $TiVO_3$  and  $TiFeO_3$  only, results from the particularly elevated position of the valence band

maximum of  $Ti_2O_3$  associated with its strong Mott-Hubbard character, which overlaps the conduction band minima of  $V_2O_3$  and  $Fe_2O_3$  [16].

These results are perfectly consistent with the present ones and show that, despite the misfitinduced distortions, the specificity of the Ti<sub>2</sub>O<sub>3</sub> electronic structure remains the principal factor which determines the occurrence of a redox reaction at the Ti<sub>2</sub>O<sub>3</sub>/M'<sub>2</sub>O<sub>3</sub> interfaces (M'=V, Fe), for which the offset between the parent materials is the largest [16]. At these cationic interfaces, two electrons are transferred per unit cell, leading to a change of oxidation state of two cations on each side of the interface. The electron transfer, limited to a single electron per unit cell, is smaller at the corresponding anionic interfaces.

#### 4.2. Anion-to-cation interfacial charge transfer

Aside from the strong cation-to-cation electron exchange found at the  $\text{Ti}_2\text{O}_3/\text{V}_2\text{O}_3$  and  $\text{Ti}_2\text{O}_3/\text{Fe}_2\text{O}_3$  junctions, a second mechanism of charge redistribution exists at oxide/oxide interfaces. Indeed, as summarized in Tab.1, a smaller, but non-vanishing interfacial charge transfer  $\pm Q_{int}$ , is also systematically present, even in the absence of redox reaction. It is mainly due to the charge modifications of the oxygen atoms bound to both M and M' cations with respect to their values in

pure  $M_2O_3$  and  $M'_2O_3$  oxides, as noted in Section 3. For example, at the cationic  $Ti_2O_3/Al_2O_3$  junction, the interfacial oxygen atoms on the  $Ti_2O_3$  side bear more negative charges than in bulk  $Ti_2O_3$  due to their bonding to Al ions, Tab. 1. This is the main reason for a significant electron transfer from  $Al_2O_3$  towards  $Ti_2O_3$  ( $Q_{int} < 0$ ). Such a mechanism of charge redistribution exists at all interfaces but is partially hidden by the stronger cation-tocation charge transfer when a redox reaction takes place.

Interestingly, the variations of  $Q_{int}$  along the series of  $M_2O_3/M'_2O_3$  interfaces display similar trends, independently of the cationic or anionic character of the junctions. This concerns both the amplitude and the sign of  $Q_{int}$ , and suggests that it results from the difference between intrinsic characteristics of the two materials. Indeed, as highlighted in Tab. 2, we find that the values of  $Q_{int}$  correlate well with the difference  $\delta Q_O$  between the oxygen charge values in the two constituent bulk materials. It is thus the ionicity difference between the two oxides which drives the interfacial charge transfer  $Q_{int}$ . For example, the larger ionicity of Al<sub>2</sub>O<sub>3</sub> compared to Ti<sub>2</sub>O<sub>3</sub>, is responsible for negative  $Q_{int}$  at the Ti<sub>2</sub>O<sub>3</sub>/Al<sub>2</sub>O<sub>3</sub> interface. Conversely, at other  $M_2O_3/M'_2O_3$  interfaces, since  $M_2O_3$  is always somewhat more ionic than  $M'_2O_3$ [16],  $Q_{int}$  is positive and much smaller. Small deviations from this general trend occur at the cationic  $V_2O_3/Fe_2O_3$  interface due to a non-negligible V-Fe hybridization resulting in a small cationic contribution to  $Q_{int}$ .

#### 4.3. Band bending at the interface

The band offsets at the interface or the difference in ionicity of the two oxides only drive the first step towards the formation of the interfacial dipole. Subsequent electron rearrangements take place in response to the electron transfers, so that the character and the penetration length of the overall dipolar layer are the result of a self-consistent procedure involving the band bending of electrostatic origin in the two materials.

In order to estimate the characteristic length at which the electronic structure of the two materials is affected by the presence of the interface, in Fig. 5 we have represented the variations of the total electrostatic potential at the oxygen cores across the anionic interfaces. In all cases, we find that the electron redistribution and the band bending are very strongly localized in the closest vicinity

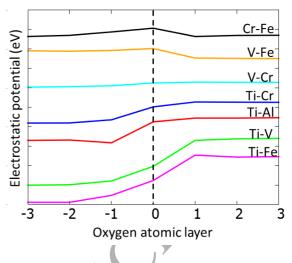


Figure 5: Variations of the electrostatic potential on oxygen atoms (three atoms on each side of the oxygen interfacial layer) across anionic  $M_2O_3/M'_2O_3$  interfaces: Ti/Al (red), Ti/V (green), Ti/Cr (blue), Ti/Fe (pink), V/Cr (cyan), V/Fe (orange) Cr/Fe (black). The curves have been vertically shifted for the sake of clarity and the unit on the vertical energy scale is 1 eV. Lines are drawn to guide the eves.

of the interface, so that the penetration length of the dipolar layer never exceeds one or two atomic layers. This is at variance with interfaces between sp semiconductors, and can be related to the ionic character of the oxides under consideration and the localized nature of their d orbitals compared to the sp ones.

#### 4.4. Interface energies and mixing properties

In Tab. 3 we summarize the values of the interface energies  $E_{int}^c$  and  $E_{int}^a$  at the M<sub>2</sub>O<sub>3</sub>/M'<sub>2</sub>O<sub>3</sub> cationic and anionic interfaces. We also recall the values of the bulk formation energies of mixed MM'O<sub>3</sub> oxides involving the same pairs of cations and estimated within the same DFT+U approach [16].

The reason to compare the energetics of mixed oxides and oxide/oxide interfaces lies in the similarity of their atomic structure and composition. Bulk ilmenite-type and LiNbO<sub>3</sub>-type structures, which are represented in Fig. 6, are sub-groups of the bulk corundum structure, with M and M' cations ordered either into alternating pure {M,M} and {M',M'} bilayers (Fig. 6, left panel) or with mixed {M,M'} bilayers (Fig. 6, right panel) along the hexagonal c-axis. The layer structure in the vicinity of the anionic and cationic interfaces is reminiscent of a part of ilmenite and LiNbO<sub>3</sub> bulks, respectively.

Table 2: Charge transfers across cationic (c) and anionic (a)  $M_2O_3/M'_2O_3$  interfaces (e/unit cell). Positive  $Q_{int}$  correspond to electron transfer from  $M_2O_3$  to  $M'_2O_3$ . The Bader charges of the corresponding bulk oxygen atoms  $Q_O$  and  $Q'_O$  (e) [16] and their difference  $\delta Q_O = Q_O - Q'_O$  (e) are recalled.

$M_2O_3/M'_2O_3$	$\mathbf{Q}_{int}^{c}$	$\mathbf{Q}^a_{int}$	$\delta Q_O$	$Q_O$	$Q'_O$
$\mathrm{Ti}_{2}\mathrm{O}_{3}/\mathrm{Cr}_{2}\mathrm{O}_{3}$	+0.20	+0.14	+0.09	-1.27	-1.18
$V_2O_3/Fe_2O_3$	+0.15	+0.08	+0.07	-1.23	-1.16
$V_2O_3/Cr_2O_3$	+0.08	+0.06	+0.05	-1.23	-1.18
$\mathrm{Cr}_2\mathrm{O}_3/\mathrm{Fe}_2\mathrm{O}_3$	+0.02	0.00	+0.02	-1.18	-1.16
$\mathrm{Ti}_{2}\mathrm{O}_{3}/\mathrm{Al}_{2}\mathrm{O}_{3}$	-0.33	-0.29	-0.39	-1.27	-1.66

Table 3: Calculated interface energies of cationic  $E_{int}^{c_1}$ ,  $E_{int}^{c_2}$  and anionic  $E_{int}^a$  M<sub>2</sub>O<sub>3</sub>/M'<sub>2</sub>O<sub>3</sub> interfaces (eV/cell), formation energies of mixed MM'O<sub>3</sub> compounds in ilmenite-type  $E_{form}^{ilm}$  and LiNbO<sub>3</sub>-type  $E_{form}^{LNO}$  structures (eV/formula unit), and the corresponding effective cation-cation mixing parameters  $W_1$ ,  $W_2$  and  $W_3$  (see text) (eV), from Ref. [16].

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	$TiFeO_3$	$TiVO_3$	$VFeO_3$	$VCrO_3$	$TiCrO_3$	CrFeO <sub>3</sub>	TiAlO <sub>3</sub>
ine $E_{int}^{c_1}$	-0.88	-0.40	0.36	0.02	0.21	0.28	0.33
$E_{int}^{c_2}$	-0.91	-0.31	0.13	0.06	0.35	0.17	0.70
$E^a_{int}$	-0.63	-0.25	0.18	0.01	0.14	0.22	0.36
ine $E_{form}^{ilm}$	-0.79	-0.35	-0.10	0.00	0.04	0.08	0.29
$E_{form}^{LNO}$	-0.73	-0.33	-0.01	0.02	0.16	0.06	0.60
ine $W_1$	-0.083	-0.043	0.017	0.010	0.052	0.022	0.118
$W_2$	-0.325	-0.125	-0.040	-0.015	-0.013	-0.048	0.223
$W_3$	-0.052	-0.025	-0.007	0.002	0.006	0.014	0.008

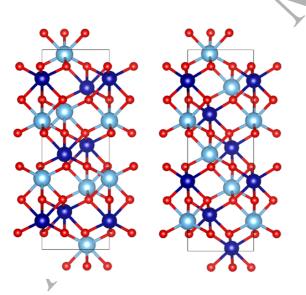


Figure 6: Unit cells for bulk MM'O<sub>3</sub> in the ilmenite (left) and LiNbO<sub>3</sub> (right) structures. Cations are represented as blue (light and dark) balls and oxygen atoms as red ones.

According to Tab. 3, the trends of interface and formation energies along the series of compounds show striking similarities. On the one hand, strongly negative energies are found for Ti<sub>2</sub>O<sub>3</sub>-Fe<sub>2</sub>O<sub>3</sub> and Ti<sub>2</sub>O<sub>3</sub>-V<sub>2</sub>O<sub>3</sub> systems, where redox reactions occur. Since negative interface energies indicate a preference to maximize the interface area, the mixed oxides in the ilmenite or LiNbO<sub>3</sub> structures can be seen as the ultimate limits of compounds uniquely composed of interfaces. These negative values are consistent with the fact that the ordered Ti<sub>2</sub>O<sub>3</sub>-Fe<sub>2</sub>O<sub>3</sub> alloy at 50% composition is a well-known mineral (ilmenite) of chemical formula TiFeO<sub>3</sub> [32]. Moreover, although TiVO<sub>3</sub> does not naturally exist, it has been recently synthesized as a thin film on c-cut sapphire [33]. On the other hand, the largest positive energies are characteristic of Ti<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub>, for which both the lattice mismatch and the difference of ionic character are the largest. In this case, much energy is required to form the interface and no mixing between the two oxides is expected, consistently with the absence of experimental evidence for TiAlO<sub>3</sub> alloys. Finally, smaller and mostly positive energies are systematically found in all other cases, where the electronic rearrangements upon interface or mixed compound formation are less noticeable.

In Ref. [16], we have analyzed the formation energies of the MM'O<sub>3</sub> compounds by introducing effective cation-cation mixing parameters  $W_i = 2V_i^{MM'} - V_i^{MM} - V_i^{M'M'}$  associated to interaction energies  $V_i$  between same (MM or M'M') and different (MM') cations in first (i = 1), second (i = 2), and third (i = 3) neighbor positions, Tab. 3 [16]. The structural similarity between mixed bulk and interface lattices makes it possible to express the interface energies in terms of the same mixing parameters:

$$E_{int}^{a} = W_{2} + 9W_{3}$$

$$E_{int}^{c_{1}} = 3W_{1} + 12W_{3}$$

$$E_{int}^{c_{2}} = 3W_{1} + 2W_{2} + 12W_{3}$$
(2)

Figure 7 shows a comparison between the values of  $E^a_{int},\,E^{c_1}_{int}$  and  $E^{c_2}_{int}$  obtained from the full DFT calculations and those approximated by Eq. 2, using the  $W_i$  values deduced from the MM'O<sub>3</sub> bulk simulations, Tab. 3. It turns out that, despite differences in the local environments of the atoms at the interface and in the mixed bulks, the overall trend is well reproduced, showing a good transferability of the effective cation-cation interactions. Due to the large number of first- (i = 1) and third-neighbor (i = 3) cation-cation pairs in the corundum structure, the formation energies of mixed bulks are principally driven by the  $W_1$  and  $W_3$  parameters. Equations 2 show that the same is true for the cationic and anionic interfaces, which explains the similar behaviors of  $E_{form}$  and  $E_{int}$  in the series, Tab. 3.

#### 5. Conclusion

Relying on a DFT+U approach, we have studied a series of non-polar (0001)  $M_2O_3/M'_2O_3$  interfaces between corundum bulk oxides of  $M_2O_3$  stoichiometry (M = Al, Ti, V, Cr, Fe), with either an anionic or a mixed cation interfacial composition. We find that, regardless of the precise interface structure, two qualitatively different mechanisms of charge redistribution operate.

At  $Ti_2O_3/V_2O_3$  and  $Ti_2O_3/Fe_2O_3$  interfaces a reduction-oxidation reaction takes place, associated with a substantial cation-to-cation charge transfer, and resulting in a change of oxidation states of the interfacial cations. The effect is traced back to the overlap of the valence band maximum of  $Ti_2O_3$  with the conduction band minima of  $V_2O_3$  and  $Fe_2O_3$ . It produces large negative interface energies, consistent with the known stability of mixed  $TiVO_3$  and  $TiFeO_3$  oxides.

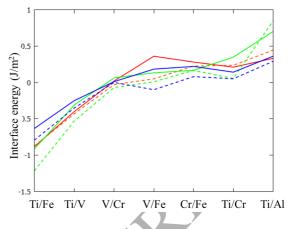


Figure 7: Calculated cationic  $c_1$  (red), cationic  $c_2$  (green) and anionic (blue) interface energies for the considered series of interfaces. Full and dashed lines represent the result of full DFT+U calculations and the estimation obtained with effective cation-cation mixing parameters  $W_i$ , Tab. 3, respectively.

While charge rearrangements are much less important at all the remaining interfaces, a non vanishing interface charge transfer is still found. It is mainly due to electron redistribution along anioncation bonds and its sign and amplitude scale with the difference of ionicity between the two constituting oxides. These interfaces are mostly characterized by small positive interface energies.

Contrary to interfaces between *sp* semiconductors and regardless of the precise nature of the charge transfer, the penetration length of the interfacial band bending is limited to one or two atomic layers.

Strong similarities between the M<sub>2</sub>O<sub>3</sub>/M'<sub>2</sub>O<sub>3</sub> interface energies and the energetics of formation of mixed MM'O<sub>3</sub> compounds in corundum-type structures have been demonstrated, and have been attributed to the transferable effective cation-cation interactions in these two types of systems. In particular, the substantially negative values of  $E_{int}$ at Ti<sub>2</sub>O<sub>3</sub>/V<sub>2</sub>O<sub>3</sub> and Ti<sub>2</sub>O<sub>3</sub>/Fe<sub>2</sub>O<sub>3</sub> interfaces are fully consistent with the known stability of ordered mixed TiVO<sub>3</sub> and TiFeO<sub>3</sub> compounds.

More generally, our results show that the nature of the interface electronic structure and the energetics of its formation can be tightly linked to the properties of the corresponding bulk oxides, thus providing a precious tool for designing oxide/oxide interfaces of required characteristics.

#### 6. References

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