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Departure from the Wiedemann–Franz law in WP_2 driven by mismatch in T-square resistivity prefactors

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The Wiedemann–Franz law establishes a link between heat and charge transport due to electrons in solids. The extent of its validity in the presence of inelastic scattering is a question raised in different contexts. Here we report on a study of the electrical, σ, and thermal, κ , conductivities in WP₂ single crystals. The Wiedemann-Franz law holds at 2 K, but a downward deviation rapidly emerges upon warming. At 13 K, there is an exceptionally large mismatch between the Lorenz number and the Sommerfeld value. We show that this is driven by a fivefold discrepancy between the T-square prefactors of electrical and thermal resistivities, both caused by electron–electron scattering. This implies the existence of abundant small-scattering-angle collisions between electrons, due to strong screening. By quantifying the relative frequency of collisions conserving momentum flux, but degrading heat flux, we identify a narrow temperature window where the hierarchy of scattering times may correspond to the hydrodynamic regime.

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INTRODUCTION

The electrical conductivity of a metal σ and its thermal counterpart κ are linked to each other by the Wiedemann–Franz (WF) law, provided that the heat carried by phonons is negligible and electrons do not suffer inelastic scattering. This law states that the ratio of the two conductivities divided by temperature should be equal to a universal number set by fundamental constants. The validity of the WF law is expected both at very low temperatures, where elastic scattering by disorder dominates, and above the Debye temperature, where scattering by phonons becomes effectively elastic. At intermediate temperatures, inelastic scattering is known to degrade thermal current more efficiently than the electrical current.¹ Experiments have found a zero-temperature validity combined to a downward departure in elemental metals (due to electron–phonon scattering) 2,3 as well as in correlated metals (because of electron–electron scattering).^{4,5} During the past decade, the search for a possible breakdown of the WF law near a quantum critical point⁶ motivated high-resolution experiments, which verified its zero-temperature validity within experimental margin and quantified the deviation at finite temperature.⁷⁻¹⁰

Gooth et al.¹¹ have recently reported on thermal transport in micrometric samples of WP_2 down to 5K and found a drastic breakdown of the WF law. WP₂ is a type-II Weyl semimetal with a room-temperature residual resistivity ratio (RRR) expressed in five digits and an impressively large magnetoresistance.¹² The observation raised fundamental questions regarding the relevance of the scattering-based theory of charge and entropy transport by mobile electrons to this non-trivial solid. The possible link between WF breakdown and electron hydrodynamics is a subject of attention. $13-1$

In this paper, we present a study of thermal conductivity in bulk millimetric single crystals of WP_2 . By performing concomitant measurements of thermal and electrical transport between 2 and 40 K, we find that: (i) The WF law is obeyed at 2 K, but a drastic downward deviation of exceptional amplitude emerges at higher temperatures; (ii) Thanks to the low-temperature data, one can distinguish between the contributions to the thermal and electrical resistivities arising from electron–electron and electron–phonon scattering; (iii) The downward deviation arises because of a large (fivefold) difference between the amplitudes of the T-square prefactors in the two (electrical and thermal) resistivities due to electron–electron scattering. We conclude that electron–electron scattering is the origin of the exceptionally large downward deviation from the Wiedemann–Franz law. This can happen if small-angle momentum-relaxing scattering events are unusually frequent. Thus, the semi-classical transport theory is able to explain a large mismatch between Lorenz number and Sommerfeld number at finite temperature. However, the large Tsquare thermal resistivity caused by momentum-conserving scattering among electrons, together with the long mean-freepath of the electrons, opens a window for entering into the hydrodynamic regime.

RESULTS

Figure 1a shows the resistivity as a function of temperature in a WP₂ single crystal. The RRR for this sample is $\rho(300K)/\rho(2K) = 9600$. The residual resistivity ρ_0 of the different samples was found to lie

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Fig. 1 a Resistivity of WP₂, ρ, measured along the *a*-axis, as a function of temperature. **b** Thermal conductivity divided by temperature, $\frac{\kappa}{f}$ (*j_Q*//*a*-
axis) as a function of temperature in the same sampl axis) as a function of temperature in the same sample with the same electrodes. c Ratio of Lorenz, $L(T) = \frac{\kappa}{T\sigma}$ to Sommerfeld $L_0 = 2.44 \times 10^{-8}$ W Ω K $^-$, numbers as a function of temperature (red). The data reported for a micro-ribbon of WP2 11 are shown in green. **d** L(T)/L₀ as a function of temperature in CeRhIn₅.⁴ e L(T)/L₀ as a function of temperature for an Ag wire with a 50 μm diameter and 99.99% purity. WP₂ and Ag were measured with the same experimental set-up. Error bars are due to the error on the measurement of the resistance of the thermometers, which are used to evaluate the temperature gradient in the sample

between 4 and 6 n Ω cm. With a carrier density of 2.5 \times 10²¹ cm⁻³,¹¹ this implies a mean-free-path in the range of 70 to , 140 μm, and, given the dimensions of the sample, a proximity to the ballistic limit.

The temperature dependence of κ/T , the thermal conductivity divided by temperature, is plotted in panel (b) of the Fig. 1. Note that in our whole temperature range of study, the phonon contribution to heat transport is negligible (see Supplemental Material). The extracted Lorenz number, $L(T) = \frac{\kappa \rho}{Z}$ is to be compared with the Sommerfeld number $L_0 = \frac{\pi^2}{3} \left(\frac{k_B}{e}\right)^2$. As seen in Fig. 1c, according to our data, L/L_0 is close to 0.5 at 40 K and decreases with decreasing temperature until it becomes as low as 0.25 at 13 K, in qualitative agreement with the observation originally reported by Gooth et al., $¹¹$ who first reported on a very</sup> low magnitude of the L/L_0 ratio in WP₂. As seen in the Fig. 1c, however, the two sets of data diverge at low temperature and we recover the expected equality between L and L_0 at low temperature.

Comparison with two other metals, Ag and CeRhIn₅, is instructive. Figure 1d displays the temperature dependence of L/ L_0 in the heavy-fermion antiferromagnet, CeRhIn₅ as reported by Paglione et al.⁴ The L/L_0 ratio, close to unity at 8 K, decreases with decreasing temperature and becomes as low as 0.5 at 2 K, before shooting upwards and attaining unity around 100 mK. In Ag, as seen in Fig. 1e, which presents our data obtained on a silver wire, a similar downward deviation of the L/L_0 ratio is detectable. Close to unity below 8 K, it decreases with warming and attains a minimum of 0.6 at 30 K before increasing again.

It is also instructive to recall the case of semi-metallic bismuth, in which thermal transport is dominated by phonons. In such a compensated system, an ambipolar contribution to the thermal conductivity, arising from a counter-flow of heat-carrying electrons and holes, was expected to be present.^{18,19} An ambipolar diffusion would have led to an upward deviation of L/L_0 from unity. However, Uher and Goldsmid¹⁸ found (after subtracting the lattice contribution) that $L/L_0 < 1$ in bismuth, which indicates that there is no ambipolar contribution to the thermal conductivity.

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Fig. 2 a A schematic representation highlighting the difference between horizontal and vertical inelastic scattering. Both kind of processes degrade heat transport. Their effect on momentum transport is, however, very different. Arrows indicate scattering from one state to another. b A sketch of Normal and Umklapp scattering in the case of a simple circular Fermi surface (blue), inside a rectangular Brillouin zone (red). They differ by the balance of quasimomentum exchange after collision. $\vec{d}Q = \vec{k}_{2f} + \vec{k}_{1f} - \vec{k}_{2i} - \vec{k}_{1i}$ is zero in a normal process and equal to a unit vector of the reciprocal lattice in an Umklapp one

The absence of a significant phononic contribution in our data makes the interpretation even more straightforward, and we also find no evidence for ambipolar heat transport in WP_2 . The reason is that the electron and hole gases are degenerate both in Bi (below room-temperature) and $WP₂$ (for all temperatures of interest), and thus the ambipolar contribution is small in proportion to T/E_F .

The scattering-based Boltzmann picture provides an explanation for such downward deviations. Thermal and electrical transport are affected in different ways by inelastic collisions labeled as "horizontal" and "vertical" (See Fig. 2a). In a horizontal scattering event, the change in the energy of the scattered carrier is accompanied by a drastic change of its momentum. Such a large-q process degrades both charge and heat currents. A vertical process, on the other hand, is a small-q scattering event, which marginally affects the carrier momentum, but modifies its energy as strongly as a horizontal process of similar intensity. In the case of momentum transport, the presence of a (1 – cos θ) pondering factor disfavors small-angle scattering. No such term exists for energy transport. This unequal importance of vertical events for electrical and thermal conductivities, pulls down the $L(T)/L_0$ ratio at finite temperature and generates a finite temperature breakdown of the Wiedemann–Franz law.¹ Such a behavior was observed in high-purity Cu half a century $ago_r²$ in other elements, such as Al and Zn_i^3 in heavy-fermion metals such as UPt₃, CeRhIn₅⁴ or CeCoIn₅⁷ as well as in magnetically ordered elements like Ni 20 or Co.²¹

On the microscopic level, two distinct types of vertical scattering have been identified. The first is electron–phonon scattering, $¹$ relevant in elemental metals. At low-temperatures, the</sup> 3

Bloch-Grüneisen picture of electron–phonon scattering yields a T^5 electric resistivity and a T^3 thermal resistivity. The higher exponent for charge transport is due to the variation of the typical wavevector of the thermally excited phonons with temperature: $q_{ph} = \frac{k_B T}{\hbar v_s}$. Small-angle phonon scattering becomes more frequent with cooling. Therefore, phonons' capacity to degrade a momentum current declines faster than their ability to impede energy transport. This power law difference leads to $L(T)/L_0 < 1$ in the intermediate temperature window (below the Debye temperature), when phonon scattering dominates over impurity scattering, but all phonons are not thermally excited. A second source of qselectivity concerns momentum-relaxing electron–electron scattering (See Fig. 2b). The quadratic temperature dependence of resistivity in a Fermi liquid is a manifestation of such scattering.²² This is because the phase space for collision between two fermionic quasi-particles scales with the square of temperature. Since the total momentum before and after collision is conserved, electron–electron collisions degrade the flow of momentum only when the scattering is accompanied by losing part of the total momentum to the lattice. Two known ways for such a momentum transfer are often invoked.²³ The first is Baber mechanism, in which electrons exchanging momentum belong to two distinct reservoirs and have different masses. The second is an Umklapp process, where the change in the momentum of the colliding electrons is accompanied by the loss of one reciprocal lattice wave-vector (Fig. 2b). Abundant small-angle electron–electron scattering (which could be either Umklapp or Baber-like) would generate a mismatch in prefactors of the T-square resistivities with the electrical prefactor lower than the thermal one. This is a second route towards $L(T)/L_0 < 1$, prominent in correlated metals.^{24,25}

In order to determine what set of microscopic collisions causes the downward deviation from the WF law in WP₂, we identified and quantified various contributions to the thermal and electrical resistivities of the system.

Figure 3 shows the electrical resistivity, ρ , and thermal resistivity, WT, as a function of T^2 . In order to keep the two resistivities in the same units and comparable to each other, we define $WT = \frac{T_{0}}{\kappa}$, as in ref. ⁴. One can see that at low temperatures, the temperature-induced increase in ρ and WT is linear in T^2 , , confirming the presence of a T-square component in both quantities. The intercept is equal in both plots, which means that the WF law is valid in the zero-temperature limit. But the two slopes are different and the deviation from the low-temperature quadratic behavior occurs at different temperatures and in different fashions.

DISCUSSION

Admitting three distinct contributions (scattering by defects, electrons and phonons) to the electrical and thermal resistivities, the expressions for ρ and WT become:

$$
\rho = \rho_0 + A_2 T^2 + A_5 T^5 \tag{1}
$$

$$
WT = W_0 T + B_2 T^2 + B_3 T^3
$$
 (2)

We assume these scattering mechanisms to be additive. Note that since the data are limited to a temperature window in which $T>\frac{\hbar}{kT}$ no Altshuler-Aronov corrections are expected.²⁶ As seen $k_{B}t'$ no Aleshure-Aronov corrections are expected. As seen
above, $\rho_0 = W_0 T$, but $A_2 \neq B_2$. The insets in Fig. 3 show that $\rho - \rho_0$ $-A_2T^2$ is linear in T^5 and $WT - W_0T - B_2T^2$ is proportional to T^3 , in agreement with what is expected from Eqs. (1) and (2).

It is now instructive to compare $WP₂$ and Ag to examine the possible role played by inelastic phonon scattering. Figure 4 compares the amplitude of the T^5 terms in WP₂ and Ag. As seen in the Fig. 4, the amplitude of both A_5 and B_3 is larger in WP₂. More quantitatively, $A_5(WP_2)/A_5(Ag) = 3.4$ and $B_3(WP_2)/B_3(Ag) = 3.6$. In other words, the B_3 and A_5 ratios of WP₂ and Ag are similar in

magnitude, which implies that phonon scattering is not the origin of the unusually low magnitude of the Lorenz number in WP_2 .

Having ruled out a major role played by phonon scattering in setting the low magnitude of L/L_0 , let us turn our attention to electron–electron scattering. As stated above, the prefactors of the

Fig. 3 a Electrical resistivity, ρ , as a function of T^2 . The dotted line is a linear fit to the $T < 10$ K data. The inset shows $\delta \rho = \rho - \rho_0 - A T^2$ as a linear fit to the T < 10 K data. The inset shows $\delta \rho = \rho - \rho_0 - A T^2$ as a function of T^5 expressed in n Ω cm. **b** Thermal resistivity, $WT = \frac{L_0 T}{\kappa}$, as a function of 7^2 . The dotted line is a linear fit to the $1 < 8$ K data. The inset shows $\delta WT = WT - W_0T - BT^2$ as a function of T^3 expressed

T-square terms in ρ and WT, namely A_2 and B_2 , are unequal. The ratio A_2/B_2 is as low as 0.22, well below what was observed in other metals, such as CeRhIn₅ (A₂/B₂ \simeq 0.4),⁴ UPt₃ (A₂/B₂ \simeq 0.65),⁵ or nickel $(A_2/B_2 \simeq 0.4).^{20}$ This feature, which pulls down the magnitude of the L/L_0 ratio in WP₂, may be due to unusually abundant vertical events (involving a small change in the wavevector of one of the colliding electrons), which could be either Umklapp or inter-band involving collisions between hole-like and electron-like carriers belonging to different pockets.

To have electron–electron collisions, which are simultaneously small-angle, Umklapp, and intra-band, one needs a Fermi surface component located at the zone boundary.²⁷ Interestingly, as seen in Fig. 5 , this is the case of WP₂. The figure shows the Fermi surface obtained by our Density Functional Theory (DFT) calculations (see Supplemental Material), consistent with previous reports.^{28,29} It is composed of two hole-like and two electron-like pockets, each located at the boundary of the Brillouin zone. Such a configuration allows abundant intra-band low-q Umklapp scattering. According to previous theoretical calculations, ^{24,25} the weight of small-angle scattering can pull down the A_2/B_2 (and the L/L_0) ratio. However, the lowest number found by these theories (\simeq 0.38) is well above what was found here by our experiment on WP₂ ($A_2/B_2 \simeq 0.22$), as well as what was reported long ago in the case of tungsten 30 (see Supplemental Material).

Following the present experimental observation, Li and Maslov showed 31 that in a compensated metal with a long-range Coulomb interaction among the charge carriers, the Lorenz ratio is given by

$$
L/L_0 = (\kappa/k_\text{F})^2/2
$$
 (3)

Fig. 5 a DFT-computed 3D Fermi Surface of WP₂. **b** Top view of the Fermi surface. Arrows illustrate wave-vectors during an inter-band Umklapp and small-angle scattering event. $\vec{k}_{i,n}$ and $\vec{k}_{f,n}$ are carrier momenta, $\vec{k}_{f,2} - \vec{k}_{i,2} = \vec{q}$ and $\vec{k}_{f,1} - \vec{k}_{i,1} = \vec{G} + \vec{q}$

Fig. 4 a Inelastic electrical resistivity $\delta \rho$ caused by phonon scattering in WP₂ (black) and Ag (red) as a function of T^5 . **b** Inelastic thermal resistivity, δW , in WP₂ (black) and Ag (red) as a functio resistivity, δWT , in WP₂ (black) and Ag (red) as a function of T^3 . The ratio of the two slopes is similar for heat and charge transport

in nΩ cm
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Fig. 6 a The Kadowaki–Woods plot with A_2 and B_2 plotted as a function of fermionic specific heat γ (C = γT). To the plot compiled by Tsujii et al., 43 we have added the data for 3 He, 32,44,45 WP₂ (this work), W³⁰ and CeRhIn₅.^{4,46} These compounds are indicated by boxes

where κ is the (inverse) screening length and k_F is the (common) Fermi momentum of the electron and hole pockets. By assumption, $\kappa \ll k_F$ and thus L/L_0 can be arbitrarily small in this model.

Let us now turn our attention to the possibility that $WP₂$ enters the hydrodynamic regime. 11 In order to address this question, let us first recall what is known in the case of normal-liquid ³He. The latter presents a thermal conductivity inversely proportional to temperature³² (strictly equivalent to our WT being proportional to T^2) and a viscosity proportional to T^{-233} at very low temperatures. Both features are caused by fermion-fermion collisions, 34 which are normal and conserve total momentum. As one can see in Fig. 6, the magnitude of B_2 (prefactor of the thermal T-square resistivity) in ³He, in CeRhIn₅, in WP₂ and in W plotted vs. γ , the fermionic specific heat, lies close to the universal Kadowaki–Woods plot. This means that while A_2 quantifies the size of momentum-relaxing collisions and B_2 is a measure of energy-relaxing, yet momentum-conserving collisions, both scale roughly with the size of the phase space for fermion-fermion scattering, which (provided a constant fermion density) is set by γ^2 . As a consequence, the magnitude of B_2 opens a new window to determine where one may expect electron hydrodynamics.

The hydrodynamic regime^{35,36} of electronic transport (identified long ago by Gurzhi³⁷) requires a specific hierarchy of scattering times. Momentum-conserving collisions should be more frequent than boundary scattering and the latter more abundant than momentum-relaxing collisions. Let us show that this hierarchy can be satisfied in our system thanks to the combination of an unusually low A_2/B_2 ratio and low disorder. The combination of a residual resistivity as low as 4 n Ω cm and a carrier density of 2.5 \times 10^{21} cm⁻³ according to¹¹ (compared to 2.9 × 10²¹ cm⁻³ according to our DFT calculations) implies that we are at the onset of the ballistic limit. It yields a mean-free-path of 140 μm. This is to be compared to the sample width and thickness of 0.1 mm.

Like in many other cases, 38 the Dingle temperature of quantum oscillations yields a mean-free-path much shorter than this. A particularly large discrepancy between the Dingle and transport mobilities has been observed in low-density semi-metals such as $Sb³⁹$ In the system under study, the difference is as large as three

Fig. 7 The magnitude of B_2T^2 , proportional to momentum-
conserving (MC) electron-electron collisions is compared to ρ_{max} conserving (MC) electron–electron collisions is compared to ρ_{im} $+A_2T^2+\tilde{A_5}T^5$, which is proportional to momentum-relaxing (MR) collisions by electrons and phonons and ρ_0 , which is a measure of boundary scattering. In a limited temperature window $(7 < T < 13$ K), the hierarchy for hydrodynamic regime is satisfied

orders of magnitude.¹² This is presumably because of a very long screening length, weakening large-angle scattering, and helping momentum conservation along long distances.

This feature, combined with the fact that momentumconserving collisions are 4–5 times more frequent than momentum-relaxing ones, implies that the system satisfies the required hierarchy of scattering times in a limited temperature window, as one can seen in Fig. 7. This figure compares the temperature dependence of momentum-relaxing collisions (with other electrons and phonons), momentum-conserving collisions (among electrons) and the boundary scattering. The three terms are represented by their contributions to resistivity, convertible to scattering rates by the same material-dependent factor. Note the narrowness of the temperature window and the modesty of the difference between the three scattering rates. Note, also that the hydrodynamic regime coincides with the observed minimum in L/ L_0 representing an excess of momentum flow in comparison to energy flow. In the hydrodynamic scenario, this coincidence is not an accident. However, the position and the width of this window are not solidly set. Assuming that the residual resistivity is not entirely fixed by the boundary scattering (i.e., $\rho_0 = \rho_{00} + \rho_{\rm imp}$) would shift this temperature window and beyond a threshold ρ_{imp} , the window will close up (see Supplemental Material).

In purely hydrodynamic transport, momentum relaxation occurs only at the boundary of the system. Momentum-conserving collisions then set the magnitude of the viscosity and the fluid drifts in presence of an external force. However, this does not happen in WP₂ or in any other metal, because the finite B_2/A_2 ratio means that momentum-relaxing events are not absent. In our hydrodynamic regime, an electron traveling from one end of the sample to the other suffers few collisions and four-out-of-five of them conserve momentum. Because the three scattering times (momentum-conserving, momentum-relaxing and boundary) are of the same order of magnitude, any hydrodynamic signature would lead to modest corrections to what can be described in the diffusive or ballistic regimes, such as subtle departures in sizedependent transport properties.³⁶

One message of this study is that a finite temperature departure from the WF law by itself cannot be a signature of hydrodynamic

transport, but thermal transport can be used to quantify the relative weight of momentum-conserving collisions and to identify where to expect eventual hydrodynamic features. Specifically, our study highlights two features, which were not explicitly considered in previous discussions about the hydrodynamics of electrons. First, as for phonons,⁴⁰ the hydrodynamic regime for electrons is expected to occur in a finite temperature window squeezed between the ballistic and diffusive regimes. Second, the phase spaces for momentum-relaxing and momentum-conserving collisions for electrons follow the same (T-square) temperature dependence. This is in a contrast to the case of phonons where Umklapp scattering vanishes exponentially with temperature whereas normal scattering follows a power law.⁴¹ This difference makes electron hydrodynamics more elusive in comparison with its phononic counterpart.⁴²

We note also that the two solids showing anomalously low L/L_0 (W and WP₂) are those in which the $T=0$ ballistic limit is accessible and a hydrodynamic window can open up. Future studies on samples with different dimensions¹¹ using a fourcontact measurement set-up are necessary to reach a definite conclusion.

In summary, we found that $WP₂$ obeys the Wiedemann–Franz law at 2 K, but there is a large downward deviation, which emerges at higher temperatures. We recalled that the dichotomy between charge and heat transport is ubiquitous in metallic systems, since low-q scattering affects heat conduction more drastically than charge transport. The exceptionally low magnitude of L/L_0 ratio mirrors the discrepancy between the amplitude of T-square prefactors in thermal and electrical resistivities. The large difference between momentum-conserving and momentum-relaxing collisions among electrons opens a narrow temperature window where the hierarchy of scattering times conforms to hydrodynamic requirements.

METHODS

The samples used in this study were needle-like single crystals (grown along the *a*-axis). Their typical dimensions were $1-2 \times 0.1 \times 0.1$ mm³. The samples are similar to those detailed in ref. 12 they were grown by chemical vapor transport. Starting materials were red phosphorous (Alfa-Aesar, 99.999%) and tungsten trioxide (Alfa-Aesar, 99.998%) with iodine as a transport agent. The materials were taken in an evacuated fused silica ampoule. The transport reaction was carried out in a two-zone-furnace with a temperature gradient of 1000 °C (T_1) to 900 °C (T_2) for several weeks. After reaction, the ampoule was removed from the furnace and quenched in water. The metallic needle-like crystals were later characterized by X-ray diffraction. The measurements were performed with a standard oneheater-two-thermometers set-up, with Cernox chips, allowing to measure thermal conductivity κ and the electrical resistivity ρ with the same electrodes and the same geometrical factor. Contacts were made with 25 μm Pt wires connected via silver paste with a contact resistance ranging from 1 to 10 Ω . The electric and heat currents were injected along the a axis of the sample. By studying three different samples with different RRRs, we checked the reproducibility of our results (see the Supplemental Material).

DATA AVAILABILITY

All data supporting the findings of this study are available from the corresponding authors A.J. and K.B. upon request.

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AUTHOR CONTRIBUTIONS

A.J. carried out the thermal and electrical conductivity measurements. W.R., A.J., and B. F. built the probe. V.S. made the sample. C.F. and N.K. performed specific heat measurements. C.F., J.G., and K.B. initiated the collaboration. A.S. carried out the DFT calculations. A.J., B.F., and K.B. analyzed the data with input from D.M. All authors participated in the discussions leading to the paper, which was written by K.B. and A.J.

ADDITIONAL INFORMATION

Supplementary information accompanies the paper on the npj Quantum Materials website [\(https://doi.org/10.1038/s41535-018-0136-x](https://doi.org/10.1038/s41535-018-0136-x)).

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