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Detectability of shape deformation in short-period exoplanets

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ABSTRACT

Context. Short-period planets are influenced by the extreme tidal forces of their parent stars. These forces deform the planets causing them to attain nonspherical shapes. The nonspherical shapes, modeled here as triaxial ellipsoids, can have an impact on the observed transit light-curves and the parameters derived for these planets.

Aims. We investigate the detectability of tidal deformation in short-period planets from their transit light curves and the instrumental precision needed. We also aim to show how detecting planet deformation allows us to obtain an observational estimate of the second fluid Love number from the light curve, which provides valuable information about the internal structure of the planet.

Methods. We adopted a model to calculate the shape of a planet due to the external potentials acting on it and used this model to modify the *ellc* transit tool. We used the modified *ellc* to generate the transit light curve for a deformed planet. Our model is parameterized by the Love number; therefore, for a given light curve we can derive the value of the Love number that best matches the observations.

Results. We simulated the known cases of WASP-103b and WASP-121b which are expected to be highly deformed. Our analyses show that instrumental precision ≤50 ppm min⁻¹ is required to reliably estimate the Love number and detect tidal deformation. This precision can be achieved for WASP-103b in ∼40 transits using the *Hubble* Space Telescope and in ∼300 transits using the forthcoming CHEOPS instrument. However, fewer transits will be required for short-period planets that may be found around bright stars in the TESS and PLATO survey missions. The unprecedented precisions expected from PLATO and JWST will permit the detection of shape deformation with a single transit observation. However, the effects of instrumental and astrophysical noise must be considered as they can increase the number of transits required to reach the 50 ppm min⁻¹ detection limit. We also show that improper modeling of limb darkening can act to bury signals related to the shape of the planet, thereby leading us to infer sphericity for a deformed planet. Accurate determination of the limb darkening coefficients is therefore required to confirm planet deformation.

Key words. methods: analytical – techniques: photometric – planets and satellites: interiors

1. Introduction

The existence of planets with short-period orbits around their stars came as a surprise at the inception of exoplanet discoveries especially because the first case was a gas giant (Mayor & [Queloz](#page-7-0) [1995\)](#page-7-0) bearing no resemblance to the planet configuration in our solar system. Several of these planets have now been found as they represent some of the most easily detected planets using both the transit and radial velocity methods. Planets reach their final shapes having attained hydrostatic equilibrium from balancing gravitational, pressure, and other external forces acting on them. Planet shapes are often assumed to be spherical for simplicity but they are triaxial in reality. For very-short-period planets (*P* < 1−2 days), the close proximity to their stars exposes them to strong tidal forces which deforms them and increases the triaxiality of their equilibrium shapes.

Contribution to deformation of a planet can also come from its rotation, making it oblate (Barnes & [Fortney](#page-7-1) [2003\)](#page-7-1).

Planet shape can have noticeable effects on the light curve obtained from transit observations [\(Seager](#page-7-2) & Hui [2002;](#page-7-2) [Carter](#page-7-3) & Winn [2010a](#page-7-3)[,b\)](#page-7-4). Analysis of the transit light curve of a planet assuming planet sphericity allows for a spherical radius R_{spr} to be obtained. However, [Leconte](#page-7-5) et al. [\(2011\)](#page-7-5) showed that planet deformation due to tidal and rotational forces lowers the observed transit depth in comparison to a spherical planet. This causes an underestimation of the radius when sphericity is assumed in the transit light curve analysis of a deformed planet. Since the density of a planet is calculated from the assumed spherical radius, the obtained density will consequently be over-estimated. [Burton](#page-7-6) et al. [\(2014\)](#page-7-6) therefore provided density corrections for some short-period planets expected to be tidally deformed based on the Roche approximation [\(Chandrasekhar](#page-7-7) [1969\)](#page-7-7). Tidal deformation is particularly significant for planets orbiting close to their stellar Roche limits and a number of planets have been discovered to orbit so close to this limit

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Fig. 1. Schematic of triaxial ellipsoid centered on the origin of the Cartesian coordinate system (X, Y, Z) with positive *X*-axis pointing towards the star.

that they are bordering on tidal disruption (e.g., [Gillon](#page-7-9) et al. [2014;](#page-7-9) [Delrez](#page-7-10) et al. [2016\)](#page-7-10). For some of these planets, theoretical calculations have been done using the Roche model by [Budaj](#page-7-11) [\(2011\)](#page-7-11) to estimate the planet shape and correct the derived spherical radii and densities for the expected planet deformation (e.g., [Southworth](#page-7-12) et al. [2015;](#page-7-12) [Delrez](#page-7-10) et al. [2016\)](#page-7-10). [Correia](#page-7-13) [\(2014\)](#page-7-13) formulated an analytical model for computing the shape of a deformed planet based on the fluid second Love number and also showed the difference between light curves of deformed and spherical planets.

Despite these efforts, there has been no observational detection of tidal deformation in short-period planets which would provide better estimates of their parameters. We therefore investigate the possibility of detecting deformation in the transit light curve of short-period planets with some current and near-future observational instruments. We modify the *ellc* transit tool by [Maxted](#page-7-14) [\(2016\)](#page-7-14)^{[1](#page-2-0)} to incorporate the planet shape model by [Correia](#page-7-13) [\(2014\)](#page-7-13). The modified *ellc* is used to generate the light curve for a deformed planet based on its fluid second Love number. This allows us to obtain an estimate for the Love number of the planet that best matches the transit observations, which provides insights into the internal structure differentiation of the planet.

In Sect. [2,](#page-2-1) we summarize the model used to compute the shape of the planet and modification of the transit tool used to generate the light curves. In Sect. [3](#page-4-0) we apply the modified tool to investigate the detectability of planet deformation in a case study of a known short-period planet. In Sect. [4,](#page-5-0) we discuss the results and some useful considerations for detecting planet deformation. We present our conclusions in the last section.

2. Modeling transit of deformed planets

2.1. Planet shape

Modeling the shape of a deformed planet follows the analytical formulation by [Correia](#page-7-13) [\(2014\)](#page-7-13) in which the planet is described by a triaxial ellipsoid centered at the origin of a Cartesian coor-dinate. As shown in Fig. [1,](#page-2-3) the semi-principal axes (a, b, c) of the ellipsoid are aligned with the *X*, *Y*,*Z* axes of the coordinate system, respectively. The equilibrium shape and mass distribution of a planet depends on the forces acting on it, namely the planet's self gravity and other perturbing potentials. The planet

can deform under the influence of centrifugal and tidal potentials. For a tidally locked close-in planet with circularized orbit of radius *r*0, Correia & [Rodriguez](#page-7-8) [\(2013\)](#page-7-8) give the nonspherical contribution from the perturbing potential on the surface of the planet as

$$
V_p = \frac{1}{2}\Omega Z - 2r_0^3 \frac{3GM_*}{X},
$$
\n(1)

where G is the gravitational constant. The first term on the righthand-side is the deformation contribution from the centrifugal potential resulting from the planet's coplanar and synchronous rotation rate Ω about the *Z*-axis. The second term refers to the tidal contribution to the deformation along the *X*-axis by a star ofmass *M*∗.

Following [Love](#page-7-15) [\(1911\)](#page-7-15), [Correia](#page-7-13) [\(2014\)](#page-7-13) describes this deformation using a Love number approach such that the fluid second Love number for radial displacement h_f is related to the radial deformation of the planet ∆*R*. The equilibrium surface deformation is thus given by

$$
\Delta R = -h_f V_p / g, \qquad (2)
$$

where *g* is the average surface gravity of the planet, and h_f is a dimensionless quantity that quantifies the response (in terms of deformation) of a planet to a perturbing potential²[.](#page-2-2) The magnitude of h_f depends on the mass distribution of the planet. More homogeneous planets have higher *h^f* whereas planets that are more centrally condensed have lower h_f [\(Kramm](#page-7-16) et al. [2011,](#page-7-16) [2012\)](#page-7-17). For an incompressible homogeneous planet, $h_f = 2.5$ which is the theoretical maximum value [\(Leconte](#page-7-5) et al. [2011;](#page-7-5) [Correia](#page-7-13) [2014\)](#page-7-13). The physical values of h_f range from 1 to 2.5 where $h_f = 1$ would represent highly differentiated bodies with high core mass like FGK stars and $h_f = 2.5$ is only possible for significantly homogeneous bodies like asteroids. In comparison, Jupiter has $h_f \approx 1.5$ and Earth has $h_f \approx 2$ [\(Yoder](#page-7-18) et al. [1995\)](#page-7-18). A first observational measurement of the Love number of Saturn was recently obtained by [Lainey](#page-7-19) et al. [\(2017\)](#page-7-19) leading to a value of $h_f = 1.39$ (from $k_f = 0.39$).

Due to the synchronous rotation, the semi-principal axis *a* of the planet always points in the direction of the star leading to a tidal deformation along *a*. The shape of the planet is such that $a > b > c$ and the deformation is kept constant along the circularized orbit. For the ellipsoid, we can define also the radius of a sphere that will enclose the same volume as the ellipsoid so that $R_v = (abc)^{1/3}$. According to the formulation by [Correia](#page-7-13) [\(2014\)](#page-7-13), the semi-principal axes are related as $a = b(1 + 3q)$ and $c = b(1 - q)$. We can then write *b* as a function of R_v to first order in the parameter *q* as

$$
b \bigotimes_{V} \frac{I}{1 - \frac{2}{3}q}, \tag{3}
$$

so that

$$
a = b(1+3q)\bigotimes R_{v} \frac{I_{1}}{1+\frac{7}{3}q}\bigg\}
$$
 (4)

and

$$
c = b(1-q)\bigotimes R_{\nu} \frac{1}{1-\frac{5}{3}q}, \qquad (5)
$$

Available at <https://pypi.org/project/ellc/>

 $h_f = 1 + k_f$ where k_f is the fluid second Love number for potential [\(Correia](#page-7-20) et al. [2014\)](#page-7-20). Calculation of the different Love numbers can be found in Sabadini & [Vermeersen](#page-7-21) [\(2004\)](#page-7-21).

Fig. 2. Quantification of tidal deformation as a function of distance to the star for two different h_f values.

where q is an asymmetry parameter that relates to h_f according to

$$
q = \frac{h_f M_*}{2 m_p} \frac{I_{R_v}}{r_0} \tag{6}
$$

The asymmetry parameter *q* quantifies the deformation of a planet, and is a measure of the difference between the semiprincipal axes of the ellipsoid. Maximum deformation (hence maximum *q*) is attained for a given planet when it orbits at the Roche radius ($r_0 = r_R = 2.46 R_v[M_*/m_p]$). Therefore, for maximum $h_f = 2.5$, we have $q_{\text{max}} \otimes 0.083$. The equilibrium shape of a planet therefore depends on its radius, its fluid second Love number h_f , the mass ratio between star and planet M_*/m_p , and also the distance from the planet to the star, *r*₀. Figure [2](#page-3-0) shows how tidal deformation becomes negligible with semi-major axis (in units of its Roche radii) for a given body with $h_f = 2.5$ and again with Jupiter's $h_f = 1.5$. We see that far away from the star, irrespective of the value of h_f , the planet does not deform $(q \blacklozenge 0)$ and so its shape remains largely spherical (*a* \bigcirc *b* \bigcirc *c* from Eqs. [\(3\)](#page-2-4)–[\(5\)](#page-2-5)). In general, Eq. [\(6\)](#page-3-1) shows that tidal deformation is more relevant for large planets orbiting very close to their Roche radii. Planets with the highest absolute deformation (highest product $q \times R_v$) provide the best chance to detect deformation.

2.2. Transit model

Planetary features that change the shape of a planet (oblateness or rings) have the effect of modifying the transit light curves (e.g., Barnes & [Fortney](#page-7-1) [2003;](#page-7-1) [Akinsanmi](#page-7-22) et al. [2018\)](#page-7-22). In the same vein, tidal deformation of a planet can modify the observed transit light curve. To model the transit of a deformed planet, the above ellipsoidal shape model by [Correia](#page-7-13) [\(2014\)](#page-7-13) was incorporated as a subroutine into a new version of the *ellc* transit tool by [Maxted](#page-7-14) [\(2016\)](#page-7-14). The *ellc* light curve model allows the projection of the ellipsoid and generation of the corresponding transit light curve. The projected shape of the ellipsoid on the stellar disk is an ellipse whose dimensions depend on the phase of the planet due to rotation of the ellipsoid with phase (*see* Fig. A.1 in [Correia](#page-7-13) [2014\)](#page-7-13). The rotation of the ellipsoid causes the crosssection of the planet to vary during transit. It should be noted that the shape correction model by [Budaj](#page-7-11) [\(2011\)](#page-7-11) does not account for the varying ellipsoidal cross-section during transit, thereby

Fig. 3. Comparison of ellipsoidal model light curves of different h_f values with spherical model light curve for WASP-103b.

Table 1. System parameters for WASP-103b.

Quantity (Unit)	Symbol	Value
Planet radius (R_0)	R_{spr}	0.1604
Planet mass (M_0)	m_p	0.0014
Stellar radius (R)	R_{*}	1.4130
Stellar mass (M)	M	1.2050
Semi-major axis (R_0) Roche radius (R_0)	r_0 r p	4.2555 3.7534

making *ellc* a more complete model involving this observational effect. Detailed descriptions of the *ellc* tool and the input parameters can be found in [Maxted](#page-7-14) [\(2016\)](#page-7-14).

The modified transit model, in addition to the usual transit parameters, takes the value of h_f and the ellipsoid's volumetric radius R_v as inputs. Therefore, by fitting the ellipsoidal model to the transit observation, all the parameters of the transit can be obtained, including the shape of the planet, and *h^f* is estimated from the best fit of the model. Therefore, rather than obtaining the usual transit radius R_{spr} from spherical planet models, we obtain the best-match dimensions *a*, *b*, *c* of the ellipsoidal planet and calculate *Rv*.

2.3. The case of WASP-103b

To illustrate the output of *ellc* for an ellipsoidal planet, we take the case of WASP-103b, an ultra-short-period planet ($P =$ 22.2 hr) reported to be bordering on tidal disruption [\(Gillon](#page-7-9) et al. [2014\)](#page-7-9) making it an ideal candidate to detect deformation. Based on revised parameters by [Southworth](#page-7-23) & Evans [\(2016\)](#page-7-23), WASP-103b has an average radius of 1.596 *R*Jup and mass of 1.47 *M*Jup (Table [1\)](#page-3-2). It orbits its star at a semi-major axis (r_0) of 0.01979 AU and an inclination (*inc*) of 88.2°. It is assumed to be on the edge of tidal disruption due to its semi-major axis of only 1.13 times its Roche radius. Taking the quoted radius as the volumetric radius of the ellipsoid, Fig. [3](#page-3-3) compares the spherical planet light curve for WASP-103b to its ellipsoidal counterparts with different h_f values. It is seen that the light-curve of the ellipsoidal model changes noticeably for different values of h_f and also compared to the spherical case. This is because the ellipsoidal **Example 12**
 Cannetizy (Unit)
 Cannetizy (Unit)
 Cannetizy (Unit)
 Cannetizy (Unit)

Fig. 4. Spherical fit to simulated deformed WASP-103b light curve. The *bottom plot* shows the residual representing the signature of deformation with amplitude quoted as the maximum absolute residual (max_abs_res). All length measurements are given in units of solar radii.

ellipsoidal cross-section of *bc* $\bigotimes R^2(1 - 7q/3)$ which is less than the cross-section R_{sp}^2 r fore, if a spherical model is used to make a fit to the observation transit thereby leading to a lower transit depth when compared to the spherical planet. The mid-transit phase has the smallest of an ellipsoidal planet, the spherical radius R_{spr} derived will be smaller than the actual volumetric radius $R_v = (abc)^{1/3}$ of the ellipsoid (see Fig. [4\)](#page-4-1). This is in agreement with the result from [Leconte](#page-7-5) et al. (2011) . Differences in transit depth as h_f varies in Fig. [3](#page-3-3) are due to the fact that higher h_f for the same planet causes more deformation, which leads to even smaller projected crosssectional area. In our code, we allow for a case where $h_f = 0$ (although not physical) to imply no deformation for the planet so that the ellipsoidal planet model is equivalent to that of a spherical planet and they produce the same light-curve with $R_v = R_{spr}$. This is important for the analysis we perform in the following section and allows us to use the same model to explain both a deformed and a spherical planet. [Maxted](#page-7-14) [\(2016\)](#page-7-14) already showed that the spherical light curve of *ellc* is in agreement with other transit tools like BATMAN [\(Kreidberg](#page-7-24) [2015\)](#page-7-24).

2.4. Signature of deformation in transit light curves

Figure 1 in [Correia](#page-7-13) [\(2014\)](#page-7-13) showed difference plots between ellipsoidal and spherical light curves assuming both planets cover the same stellar area at the start of transit (full ingress). This perfectly captures the flux variation induced by deformation as both planets transit but is not the signature one would obtain from real observations, since the transit parameters would initially be unknown and would be determined from a fitting process. The observable signature of planet deformation is the residual between the light curve of the deformed planet and the best-fit spherical model. In Fig. [4,](#page-4-1) we simulated the light curve of deformed WASP-103b using our ellipsoidal model with parameters given in Table [1](#page-3-2) and performed least-squares fitting using a spherical planet model. The residual from the fit is shown in the

Fig. 5. Residuals from spherical fit to ellipsoidal simulations of different short-period planets in comparison to WASP-19b, 12b, and 4b from [Correia](#page-7-13) [\(2014\)](#page-7-13).

bottom panel and represents the signature of deformation for the simulated planet. The parameters derived from the fitting process are systematically incorrect as they adjust to mimic the signature of deformation. This also shows that the assumption of sphericity for a planet affects not only the radius derived but also the other transit parameters, and models that adjust only this radius are incomplete. We see in the residuals that the signature of deformation manifests in two regions. The first is at ingress and egress phases owing to oblateness $(b > c)$ of the planet as identified in previous studies (e.g., [Seager](#page-7-2) & Hui [2002;](#page-7-2) Barnes & [Fortney](#page-7-1) [2003\)](#page-7-1). A second prominent feature is seen as a bump centered on the mid-transit phase due to the varying star eclipsed area caused by ellipsoid rotation as it transits. This second feature is as a result of tidal deformation which was not accounted for in the previous studies mentioned but manisfests in our model due to full projection of the ellipsoidal shape as it rotates with phase [\(Correia](#page-7-13) [2014\)](#page-7-13).

To compare the deformation signal obtained from the fitting process with the flux difference plot in [Correia](#page-7-13) [\(2014\)](#page-7-13), we perform spherical fits to the ellipsoidal simulation of other shortperiod giant planets WASP-19b, WASP-12b, WASP-4b, and WASP-121b that were presented in the study and were expected to be deformed. The residuals are shown in Fig. [5.](#page-4-2) We see from Figs. [4](#page-4-1) and [5](#page-4-2) that the amplitude of the deformation signature is just about 40 ppm for the most deformed planets (WASP-103b and WASP-121b) while the amplitudes from the difference curves in [Correia](#page-7-13) [\(2014\)](#page-7-13) are up to 100 ppm. We reiterate that the latter should not be taken to imply high signal detectability.

WASP-103b, WASP-121b, and WASP-12b have the highest residual amplitudes and therefore present the best possibility of detecting deformation. Other planets likely to be deformed are HATS-18b, WASP-76b, and WASP-33b, but they have lower residual amplitudes of 20, 14, and 12 ppm, respectively.

3. Detectability of planet deformation and measurement of planet Love number

The residuals of the spherical fit to the light curve of a deformed planet is informative in detecting deformation as it shows that the

spherical model does not fully explain the observation. However, $\frac{2.5}{\sqrt{25}}$ Detectability plot for WASP-103b some of the signature of the deformation is masked in the errors some of the signature of the deformation is masked in the errors of the parameters obtained. To correctly estimate the planet transit parameters, our ellipsoidal model can be used to fit the transit observation. In doing so, we also obtain a value for the Love number that best fits the observation if there is enough precision in the data. The benefit of this approach is that we can fit the ellipsoidal model to any transit observation and, by the value of *h^f* recovered, ascertain if planet deformation is detectable or not. If we cannot detect the deformation, we get $h_f \approx 0$ which as shown in Fig. [3](#page-3-3) is equivalent to the fit of a spherical planet model.

Therefore, detectability of tidal deformation using the ellipsoidal model relies on the ability to recover a nonzero value of *h^f* with statistical significance from a fitting process. Despite being able to infer deformation with only detection of $h_f \gg 0$, we will need to have $h_f \geq 1$ with some significance where the values give actual physical interpretation to astronomical bodies. To illustrate the detectability, we created simulated observations of deformed WASP-103b with one-minute cadence using its parameters as stated above with $h_f = 1.5$. We used the Limb darkening toolkit (ldtk) by [Parviainen](#page-7-25) & Aigrain [\(2015\)](#page-7-25) to compute quadratic limb darkening coefficients of [0.5343, 0.1299] and their uncertainties [0.0012, 0.0027] in the CHEOPS bandpass for the star with stellar parameters given in [Gillon](#page-7-9) et al. [\(2014\)](#page-7-9). We added random Gaussian noise of different levels to the simulated data in each test run. We then investigated how well we can recover the value of h_f and at what noise level it would be impossible to distinguish between the light curve of a spherical planet and that of a deformed planet. This is important to know the instrumental precision necessary to detect deformation in close-in planets.

We performed Markov Chain Monte Carlo (MCMC) analysisto estimate the transit parameters and their uncertainties using the *emcee* package [\(Foreman-Mackey](#page-7-26) et al. [2013\)](#page-7-26) with uniform priors on h_f in the range [0, 2.5]. As shown in Appendix [A.1,](#page-8-0) when a noise level of 30 ppm is added to the simulated observation, h_f is reliably recovered, with 99.7% of its samples (within \triangle ±3 σ) greater than 1. This proves that the result is statistically significant and implies that the planet is indeed deformed. Moreover, the residual from the fit does not show any structure related to the deformation signal. However, when a noise level of 100 ppm is added to the observation the median of the distribution suggests a deformed planet, but because its width encompasses $h_f = 0$ (spherical model), planet deformation can-not be asserted (Appendix [A.2\)](#page-8-1). Figure 6 shows the detectability plot summarizing the results for the different noise levels added to the observation. We see that the significance of h_f detection above 1 reduces as the noise level of the observation increases. For instance, at 50 ppm noise level, *h^f* samples are well above zero, implying that the ellipsoidal model provides a better fit than the spherical model. However, the samples with $h_f < 1$ do not represent physical values for a planet but the detection still gives ∼95% of the samples above 1. Beyond 50 ppm, fitting the observation with a spherical model becomes increasingly more probable. With noise levels as high as 100 ppm, the spherical and ellipsoidal models produce comparable fits.

4. Discussion

The results show that noise levels below 30 ppm offer the best chance at detecting deformation for our test case of WASP-103b since we retrieve h_f with $\geq 3\sigma$ significance above 1. However, we could define a lower limit on our detection confirmation such

Fig. 6. Detectability of deformation in WASP-103b considering different noise levels. The black dashed line is the simulated h_f value. The points are the median of the *h^f* samples at each noise level. The red error bars show the 68% credible interval $(\bigotimes \pm 1\sigma)$ while the blue error bars show the 99.7% credible interval ($\bigcirc \pm 3\sigma$).

that we require to have $(h_f - 10) \ge 1$ which puts 84% of the recovered *h^f* samples in physical values expected for planets. This is satisfied for noise levels of 50 ppm and below.

A photometric precision of 50 ppm min[−]¹ is not yet attainable using current observational instruments. For our case system, WASP-103 is a twelfth-magnitude star and the photometric precision to be attained by the near-future instrument CHEOPS for this star is 855 ppm min[−]¹ . Attaining a reduced photon noise level of 50 ppm min⁻¹ for this star using CHEOPS requires ~293 transit observations of WASP-103b. For the interesting candidate WASP-121b, which orbits its star of magnitude $m_V = 10$ [\(Delrez](#page-7-10) et al. [2016\)](#page-7-10), our analysis also showed detectability of deformation with 50 ppm min[−]¹ noise level. CHEOPS precision for a tenth-magnitude star is 319 ppm min[−]¹ thereby requiring only 40 transit observations to detect deformation in this planet. Although information from the CHEOPS consortium indicates that WASP-121 might not be in the visibility region, new interesting planet candidates with short period orbits may appear from future surveys targeting bright stars, such as PLATO [\(Rauer](#page-7-27) et al. [2014\)](#page-7-27) and TESS [\(Ricker](#page-7-28) et al. [2015\)](#page-7-28). For these planets around stars brighter than $m_V = 9$, we expect photon noise levels as low as 150 ppm min⁻¹ with CHEOPS [\(Broeg](#page-7-29) et al. [2013\)](#page-7-29) and ≤ 62 ppm min⁻¹ with PLATO [\(Rauer](#page-7-27) et al. [2014\)](#page-7-27) and thus require fewer transits to reach the 50 ppm limit needed to detect planet deformation as reported in Table [2.](#page-6-0) For these stars, TESS will have a relatively higher noise level of 464 ppm min⁻¹ [\(Sullivan](#page-7-30) et al. [2015\)](#page-7-30) which is not desirable for detecting deformation. Observations with the forthcoming JWST will also be immensely beneficial as it is expected to attain photon-noise floor ∼40 ppm (65 s) on its NIRCam instrument amongst others [\(Beichman](#page-7-31) et al. [2014\)](#page-7-31). Attainment of this noise level implies that only one transit observation will be required in order to detect tidal deformation in a suitable shortperiod planet.

Unfortunately, interesting short-period planets expected to be significantly deformed were not found within the original *Kepler* survey field which would have allowed several transit observations of any found target. The WFC3 instrument on the *Hubble* Space Telescope (HST) achieved a noise level of 172 ppm(103 s)

Table 2. Number of transits required to reach 50 ppm min⁻¹ noise level with CHEOPS and PLATO for different stellar magnitudes.

CHEOPS		PLATO			
m_V	Noise/min	$#$ transits	mv	Noise/min	# transits
6.5	150 ppm		8	62 ppm	
8	186 ppm	14	10	209 ppm	17
10	319 ppm	40	11	263 ppm	28
12	855 ppm	293	13	619 ppm	153

Notes. Noise levels of CHEOPS were obtained from CHEOPS science team (priv. comm.) and that for PLATO was converted to ppm min[−]¹ from [Rauer](#page-7-27) et al. [2014](#page-7-27) (Table 2 and Fig. 14).

for two full-orbit observations of WASP-103 [\(Kreidberg](#page-7-32) et al. [2018\)](#page-7-32). Therefore, with ∼40 transits of WASP-103b using HST, we can attain the required precision of 50 ppm min^{-1} . However, some factors can still affect the detectability of deformation, some of which are mentioned below.

Temporal resolution. We used one-minute cadence in our simulations to enable good resolution of the ingress and egress phases which have short durations especially for these shortperiod planets. A lower cadence than this reduces the precision with which h_f and other parameters are recovered. At the 30 ppm noise level, changing the cadence from 1 min to 4 mins and 8 mins increases the error on h_f from ± 0.12 to ± 0.23 and ± 0.38 , respectively.

Orbital inclination. The inclination of the orbit plays a role in the signature of deformation. Lower inclinations indicate a shorter transit duration so the effects referred to in residuals of Fig. [4](#page-4-1) and Sect. [2.4](#page-4-3) will be shorter in time, making them more difficult to temporally resolve, especially at the ingress and egress phases. In addition, a longer transit duration allows the projected ellipse area to vary more (longer phase rotation of ellipsoid) making the light-curve more markedly different from that of the spherical planet thereby leading to a higheramplitude bump around mid-transit (see also Fig. A.1 in [Correia](#page-7-13) [2014\)](#page-7-13). The effects of deformation in light curves is maximal at an inclination of 90 \degree where h_f is recovered with the best precision.

Limb darkening coefficients (LDCs). As shown in Fig. [4,](#page-4-1) the signature of deformation is prominent at ingress and egress phases with a bump centered around the mid-transit phase. The stellar limb-darkening affects light curves similarly in these regions (see effects of LDC modeling in [Neilson](#page-7-33) et al. [2017\)](#page-7-33), so we tested the impact of inaccurate estimation of limb-darkening coefficients on the recovery of h_f from the light curve. This was attempted on the 30 ppm noise level simulation in two ways and the results are summarized in Table [3.](#page-6-1) First we fixed the limb darkening coefficients to incorrect values that are slightly different from the true values used to generate the simulated observation. We found that for incorrectly fixed LDC values that are smaller than the true values, the signature of deformation gets damped as we recover lower h_f values than those simulated. When the values are fixed at values up to 0.01 smaller than the true values, the entire h_f distribution falls around zero and we infer a spherical planet (see left plot in Fig. [A.3\)](#page-9-0). On the other hand, *h^f* values are amplified when LDCs are fixed at values higher than the true values. For LDC values fixed at 0.015 higher than the true values, the recovered h_f distribution is pushed towards the maximum of 2.5. In the latter case, we can

Table 3. Results of LDC tests and *h^f* values recovered.

LDC tests	Values	h_f recovered
Fixed at 0.01 below	[0.5243, 0.1199]	$0.12^{+0.11}$
Fixed at 0.015 higher	[0.5493, 0.1449]	$2.44 \overline{)}0.04$
Gaussian priors	$Mean_{=}$ [0.5343,0.1299],	$1.56\frac{70.99}{-0.53}$
Gaussian priors	$\sigma = [0.01, 0.01]$ Mean = $[0.5343, 0.1299]$,	$1.59^{+0.18}_{-0.17}$
	$\sigma = [0.0012, 0.0027]$	

Notes. The plots are shown in Figs. [A.3](#page-9-0) and [A.4.](#page-9-1)

infer that the planet is deformed but cannot ascertain the extent of deformation due to inaccurate estimation of *h^f* which is evident from the obtained marginalized distribution (see right plot in Fig. $(A.3)$ $(A.3)$. The other attempt was to fit the LDCs by including them in the hyperparameters. We use a Gaussian prior with the true LDC values as mean and $\sigma = 0.01$. The MCMC sampling produced a wide *h^f* distribution centered close to the true value but with errors as large as ± 0.4 (left plot in Fig. [A.4\)](#page-9-1) making it difficult to ascertain planet shape. However, when tighter priors (e.g., using errors obtained from deriving LDCs with *ldtk*) are imposed on the LDCs, *h^f* is well-recovered with errors of just ± 0.18 to infer deformation (right plot in Fig. [A.4\)](#page-9-1). It should be noted that the LDC error estimates from *ldtk* are very small and have often had to be inflated in the literature during fitting to account for systematic errors in the atmospheric models (e.g., [Raynard](#page-7-34) et al. [2018;](#page-7-34) Maxted & [Hutcheon](#page-7-35) [2018\)](#page-7-35).

Alternatively, the power-2 limb darkening law has been recommended for the analysis of transit light curves as it has been shown to provide remarkable agreement between stellar atmospheric models and observations, particularly for cool stars [\(Morello](#page-7-36) et al. [2017;](#page-7-36) [Maxted](#page-7-37) [2018\)](#page-7-37). The transformation of the two parameters of the power-2 law in [Maxted](#page-7-37) [\(2018\)](#page-7-37) reduces the correlation between them during fitting and small errors of [0.011, 0.045] can be obtained on them. The fitting process can attempt different LDC laws so that the law with the best match to the observation and that produces the least errors on the derived parameters will be preferred.

Other noise sources. Our simulations considered the ideal situation where only photon (white) noise is present thereby allowing easy scaling of the noise with the number of observations/transits. However, in practice, other sources of noise [\(Pont](#page-7-38) et al. [2006\)](#page-7-38) will impact the estimates given above and act to increase the number of transits required to detect deformation. These other noise sources can be from instrumental effects (e.g., satellite jitter and thermal instability) and also from astrophysical sources such as stellar activity (occulted or unocculted active regions; [Oshagh](#page-7-39) et al. [2013\)](#page-7-39), stellar oscillations and granulation [\(Chiavassa](#page-7-40) et al. [2017\)](#page-7-40). These effects always have to be mitigated in transit analysis [\(Oshagh](#page-7-41) [2018;](#page-7-41) [Barros](#page-7-42) et al. [2014\)](#page-7-42) but will still impact the detectability of shape deformation. Recent developments in Gaussian process analysis also provide a method for tackling astrophysical noise (e.g., [Foreman-Mackey](#page-7-43) et al. [2017;](#page-7-43) [Serrano](#page-7-44) et al. [2018\)](#page-7-44).

5. Conclusion

Short-period planets, especially within two Roche radii from the host star, suffer from extreme tidal forces causing their shapes to depart from sphericity in a way that is difficult to detect in transit observations. With the increasing observational precision

of near-future instruments, detecting deformation becomes more feasible as planet shape will have a higher impact on the observed transit light curves. We demonstrate detectability of deformation for WASP-103b and WASP-121b (which have the highest deformation signatures as seen in Sect. [2.4](#page-4-3) and are regarded as some of the most deformed planets; [Delrez](#page-7-10) et al. [2016\)](#page-7-10) by employing a formulation from the literature in a way that allows an observational estimate of a planet's fluid Love number to be obtained. Because the Love number tells us how a planet deforms in response to perturbing potentials, we used it as a measure of deformation in the planet. Detecting and measuring planet deformation provides more accurate estimations of the radius and density of these planets as opposed to the estimates derived from spherical models or corrections calculated from only expectation of deformation. Additionally, measuring the Love number provides information about the interior structure of the planet. We showed that the instrumental precision needed to detect tidal deformation is ≤50 ppm which can be attained by CHEOPS with about 300 transits for WASP-103b and 40 transits for WASP-121b. The HST can also attain this precision for WASP-103b in approximately 40 transit observations. Fewer transit observations will be required if such short-period planets are found transiting very bright stars. Additionally, the precision expected from JWST will present the best opportunity to detect tidal deformation since only one transit of a suitable planet will be required.

The chances of detecting deformation are increased for planets with inclinations of 90◦ and also when the observations are taken with temporal resolution of ∼1 min. However detection can be severely hampered by improper modeling of the limb darkening which, in some cases, can cause the signature of deformation to be subdued, leading us to infer sphericity from the observations. Using the quadratic limb-darkening law, LDC errors smaller than 0.01 are required in order to confirm planet deformation. Proper treatment of noise sources will also be pertinent in order to identify the signature of shape deformation.

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Appendix A: Additional figures

Fig. A.1. *Left panel*: posterior distributions for parameters of simulated deformed WASP103b with 30 ppm noise added. The values quoted on the diagonal histograms indicate the median marginalized distribution of each parameter (red lines) with the surrounding 68% credible interval ($\pm 1\sigma$). The dashed vertical lines indicate the $\pm 3\sigma$ limits calculated as the 0.15th and 99.87th percentiles. Blue lines indicate the true simulated values. *Right panel*: fit of simulated light curve of ellipsoidal WASP-103b with parameters retrieved from the sampling.

Fig. A.2. As in Fig. [A.1](#page-8-0) but with 100 ppm noise added to the simulated observation.

Fig. A.3. *Left panel*: as in Fig[. A.1](#page-8-0) but with LDCs fixed at incorrect values 0.01 smaller than the true values. *Right panel*: as in Fig. [A.1](#page-8-0) but with LDCs fixed at values 0.015 higher than the true values.

Fig. A.4. *Left panel*: posterior distributions of parameters when Gaussian prior with $\sigma = 0.01$ is used on the LDCs (u_1, u_2). *Right panel*: posterior distributions of parameters when tighter Gaussian priors from *ldtk* errors are used for the LDCs.