

# Supplementary Material for “Relativistic short-range exchange energy functionals beyond the local-density approximation”

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(Dated: February 14, 2020)

## I. EVEN-TEMPERED BASIS SETS CONSTRUCTED IN THIS WORK

TABLE I. Parameters  $\zeta_1$  and  $q$  for generating all the exponents  $\zeta_v = \zeta_1 q^{v-1}$  of our uncontracted even-tempered large-component basis functions for the Yb<sup>68+</sup> and U<sup>90+</sup> systems of the helium isoelectronic series. We use ten s basis functions, two sets of p basis functions, and one set of d basis functions. The small-component basis functions are generated from the unrestricted kinetic-balance scheme.

	Ten s basis functions		Two p basis functions		One d basis function
	$\zeta_1$	$q$	$\zeta_1$	$q$	$\zeta_1$
Yb <sup>68+</sup>	1.39601904E+07	0.30	3.39128349E+06	0.25	4.75587491E+03
U <sup>90+</sup>	5.58567332E+07	0.295	2.64721605E+07	0.25	3.34172062E+04

TABLE II. Parameters  $\zeta_1$  and  $q$  for generating all the exponents  $\zeta_v = \zeta_1 q^{v-1}$  of our uncontracted even-tempered large-component basis functions for the beryllium isoelectronic series. We use ten s basis functions, six sets of p basis functions, and one set of d basis functions. The small-component basis functions are generated from the unrestricted kinetic-balance scheme.

	Ten s basis functions		Six p basis functions		One d basis function
	$\zeta_1$	$q$	$\zeta_1$	$q$	$\zeta_1$
Be	6.40943779E+03	0.25	1.31800101E+01	0.25	2.71217265E-01
Ne <sup>6+</sup>	2.63937466E+04	0.30	1.01356529E+02	0.25	2.16640868E+00
Ar <sup>14+</sup>	2.16279421E+05	0.26	4.94782136E+02	0.25	1.13941141E+01
Kr <sup>32+</sup>	4.14098736E+06	0.23	9.01590791E+03	0.25	2.25939509E+02
Xe <sup>50+</sup>	9.04292743E+06	0.23	2.81773747E+05	0.25	1.95959651E+03
Yb <sup>66+</sup>	1.39601904E+07	0.236	3.39128349E+06	0.25	4.75587491E+03
Rn <sup>82+</sup>	1.46794059E+07	0.25	1.72824122E+07	0.25	1.25385658E+03
U <sup>88+</sup>	1.46346866E+07	0.26	2.64721605E+07	0.25	3.34172062E+04

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TABLE III. Parameters  $\zeta_1$  and  $q$  for generating all the exponents  $\zeta_v = \zeta_1 q^{v-1}$  of our uncontracted even-tempered large-component basis functions for the neon isoelectronic series. We use ten s basis functions, six sets of p basis functions, and one set of d basis functions. The small-component basis functions are generated from the unrestricted kinetic-balance scheme.

	Ten s basis functions		Six p basis functions		One d basis function
	$\zeta_1$	$q$	$\zeta_1$	$q$	$\zeta_1$
Ne	2.63937466E+04	0.30	1.01356529E+02	0.30	2.16640868E+00
Ar <sup>8+</sup>	2.16279421E+05	0.29	4.94782136E+02	0.32	1.13941141E+01
Kr <sup>26+</sup>	4.14098736E+06	0.25	9.01590791E+03	0.25	2.25939509E+02
Xe <sup>44+</sup>	9.04292743E+06	0.255	9.36856349E+03	0.31	1.95959651E+03
Yb <sup>60+</sup>	1.39601904E+07	0.235	2.61264417E+04	0.32	4.75587491E+03
Rn <sup>76+</sup>	1.46794059E+07	0.25	5.70898829E+04	0.30	1.25385658E+03
U <sup>82+</sup>	1.46346866E+07	0.26	1.22880210E+05	0.28	3.34172062E+04

TABLE IV. Parameters  $\zeta_1$  and  $q$  for generating all the exponents  $\zeta_v = \zeta_1 q^{v-1}$  of our uncontracted even-tempered large-component basis functions for the argon isoelectronic series. We use twelve s basis functions, eight sets of p basis functions, and three set of d basis functions. The small-component basis functions are generated from the unrestricted kinetic-balance scheme.

	Twelve s basis functions		Eight p basis functions		Three d basis functions	
	$\zeta_1$	$q$	$\zeta_1$	$q$	$\zeta_1$	$q$
Ar	2.16279421E+05	0.30	4.94782136E+02	0.325	1.13941141E+01	0.25
Kr <sup>18+</sup>	4.14098736E+06	0.25	9.01590791E+03	0.30	2.25939509E+02	0.25
Xe <sup>36+</sup>	9.04292743E+06	0.25	9.36856349E+03	0.36	1.95959651E+03	0.25
Yb <sup>52+</sup>	1.39601904E+07	0.26	2.61264417E+04	0.33	4.75587491E+03	0.25
Rn <sup>68+</sup>	1.46794059E+07	0.30	1.92412503E+05	0.30	1.25385658E+03	0.25
U <sup>74+</sup>	1.46346866E+07	0.29	1.22880210E+05	0.29	4.95593590E+02	0.25