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How pulse disturbances shape size-abundance pyramids

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Abstract

Ecological pyramids represent the distribution of abundance and biomass of living organisms across body-sizes. Our understanding of their expected shape relies on the assumption of invariant steady-state conditions. However, most of the world’s ecosystems experience disturbances that keep them far from such a steady state. Here, using the allometric scaling between population growth rate and body-size, we predict the response of size-abundance pyramids within a trophic guild to any combination of disturbance frequency and intensity affecting all species in a similar way. We show that disturbances narrow the base of size-abundance pyramids, lower their height and decrease total community biomass in a nonlinear way. An experimental test using microbial communities demonstrates that the model captures well the effect of disturbances on empirical pyramids. Overall, we demonstrate both theoretically and experimentally how disturbances that are not size-selective can nonetheless have disproportionate impacts on large species.
INTRODUCTION

Ecological pyramids, which represent the distribution of abundance and biomass of organisms across body-sizes or trophic levels, reveal one of the most striking regularities among communities (Elton 1927; Lindeman 1942; Trebilco et al. 2013). Several types of pyramids have been reported in ecological research, as well as distinct underlying mechanisms to explain their shape. For example, trophic pyramids describe the distribution of abundance or biomass along discrete trophic levels (Fig. 1a). The inefficiency in energy transfer from resources to consumers as well as strong self-regulation within trophic levels provide the main explanation for their shape (Lindeman 1942; Barbier & Loreau 2019). Alternatively, size-abundance pyramids (Fig. 1b,c), also known as the pyramid of numbers (Elton 1927), the Damuth law (Damuth 1981), or the abundance size spectrum (Sprules & Barth 2016), describe the distribution of abundance across body-sizes and can be studied both within and across trophic guilds (Elton 1927; Trebilco et al. 2013). The energetic equivalence rule, along with the metabolic theory of ecology, provide theoretical expectations regarding the shape of such size-abundance pyramids: in a community where all individuals feed on a common resource (i.e. within a trophic group), population abundance should be proportional to $M^{-0.75}$, where $M$ is body-size, and biomass should be proportional to $M^{0.25}$ (Damuth 1981; Brown et al. 2004; White et al. 2007).

As with most concepts in ecology, these relationships correspond to theoretical baselines that are predicted under steady-state conditions, which are rarely met in nature (DeAngelis & Waterhouse 1987; Hastings 2004, 2010). Most natural ecosystems and communities are exposed to a wide range of environmental fluctuations and disturbances, ranging from harvesting to extreme weather events. Furthermore, many of these disturbances are expected to increase in frequency and intensity in the context of global change, as illustrated by recent large scale wildfires, floods or...

Despite the extensive literature on disturbance ecology (Sousa 1984; Yodzis 1988; Petraitis et al. 1989; Fox 2013; Dantas et al. 2016; Thom & Seidl 2016), the effects of disturbances on community structure and biomass distribution remain poorly understood (Donohue et al. 2016). On the one hand, ecologists have often focused on the consequences of environmental disturbances on species richness (Huston 1979; Haddad et al. 2008; Bongers et al. 2009) and the coexistence of competing species (Violle et al. 2010; Miller et al. 2011; Fox 2013), rather than on body-size and biomass distribution (but see Woodward et al. (2016)). As such, the specific identity of species resistant (or not) to disturbances has received ample attention, with various definitions of disturbance-resistant species groups (Sousa 1980, 1984; Lavorel et al. 1997). These studies have pointed out key demographic traits, notably population growth rate and carrying capacity, that determine species’ capacities to persist in a disturbed environment (McGill et al. 2006; Haddad et al. 2008; Enquist et al. 2015; Woodward et al. 2016). On the other hand, the metabolic theory of ecology uses the scaling of metabolic rate with body-size to predict a set of structural and functional characteristics across biological scales (Brown et al. 2004). At the community level, it demonstrates how size-abundance pyramids emerge from the scaling of population growth rate and abundance with body-size (Trebilco et al. 2013). Surprisingly, a formal integration of the theory on disturbances with the metabolic theory of ecology is still lacking, but would allow ecologists to generalize and predict the effect of environmental disturbances on the shape of size-abundance pyramids.
Here, we integrate these two disconnected fields by developing a size-based model for population persistence, assuming that the scaling of population growth rate with body-size is the leading mechanism determining the response of size-abundance pyramids to disturbances. We predict the shape of size-abundance pyramids within a trophic guild in response to repeated pulse disturbances of varying frequency and intensity affecting all species in a similar way, regardless of their size. Such disturbances represent a wide range of environmental pressures that increase species mortality, such as floods, wildfires, or hurricanes. They differ from the disturbance studies developed in fishery sciences, that specifically addressed the effect of a press, size-selective disturbance (i.e. fishing) on the abundance size spectrum (Jennings et al. 2002; Shin et al. 2005; Petchey & Belgrano 2010; Sprules & Barth 2016). We then experimentally test the predicted responses of size-abundance pyramids and standing biomass to disturbances, using microbial communities composed of aquatic species with body-sizes and populations densities varying over several orders of magnitudes. We finally discuss the general implications of our findings for the structure and functioning of communities exposed to environmental disturbances.

MATERIALS AND METHODS

A model for size-abundance pyramids exposed to disturbances

We build a mechanistic model to predict how disturbance frequency and intensity modulate the shape of size-abundance pyramids and community total biomass. We describe the dynamics of population abundance \( N \) with a logistic model:

\[
\frac{dN}{dt} = rN \left(1 - \frac{N}{K}\right)
\]

(1)

where \( r \) is population growth rate and \( K \) is population carrying capacity. We model a disturbance regime, corresponding to a recurrent abundance reduction, of intensity \( I \) (fraction of abundance).
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and frequency $f$ or period $T=1/f$ (time between two disturbances, Fig. 2a). We can demonstrate that a population persists in a disturbed environment only if its growth rate balances the long-term effect of the disturbance regime (adapted from Harvey et al. 2016), that is:

$$r > -\frac{\ln(1-l)}{T}$$  \hspace{1cm} (2)$$

From equation (2), we can predict the set of disturbance regimes a population can sustain according to its growth rate (Fig. 2b), as well as the minimum generation time ($1/r$) needed to maintain a viable population (Fig. S1). We then use the allometric relationship between population growth rate $r$ and average body-size $M$, that is $r = c \times M^a$ with $a = -\frac{1}{4}$ (Brown et al. 2004; Savage et al. 2004) and $c$ a positive constant, to derive the following size-specific criterion for population persistence under a disturbance regime:

$$M \leq \left(\frac{\ln(1-l)}{T \times c}\right)^{-4}$$  \hspace{1cm} (3)$$

Equation (3) indicates that a species can persist in a disturbed environment only if its average body-size is below a certain value. Note that this analytical criterion is applicable to any biological and temporal scale. Indeed, the disturbance frequency and population growth rate are expressed with the same time unit and can range from hours (e.g. fast-growing microbial organisms) to years (e.g. slow-growing organisms such as large mammals). To investigate the effect of disturbances on the shape of size-abundance pyramids, we derive the mean abundance at dynamical equilibrium $N_B$ of a population under a given disturbance regime (i.e. averaged over a time period, see Appendix 1 for detailed steps), that is:

$$\bar{N} = K \left(\frac{\ln(1-l)}{T \times c} + 1\right)$$  \hspace{1cm} (4)$$

where $K$ corresponds to the carrying capacity of the population, which also scales with body-size on a logarithmic scale (Brown & Gillooly 2003; Brown et al. 2004): $\ln(K) = a_K \ln(M) + b_K$. 


where \( a_K \) and \( b_K \) are normalizing constants. We use this allometric relationship to express mean abundance as a function of mean population body-size and finally obtain:

\[
\ln(\bar{N}) = a_K \ln(M) + b_K + \ln\left(\frac{\ln(1-t)}{Te^{a_r\ln(M)+b_r}} + 1\right)
\] (5)

The formula is valid when the expression in parentheses in the right-hand term is positive, which corresponds to the persistence criteria given in equations (2) and (3). We express population biomass, \( B \), as the product of mean abundance at dynamical equilibrium, \( \bar{N} \), and the average individual body-size in the population, \( M \), that is \( B = \bar{N}M \).

We extend this approach to multispecies assemblages composed of potentially hundreds of co-occurring species with different body-sizes (see detailed method in Appendix 2 and Table S1 for parameter values). We assume that all species’ populations follow a logistic growth and are constrained by intraspecific competition only (an assumption relaxed in Appendix 3). From equation (3) and (5), we expect that disturbances will decrease the maximum size observed in the community as well as total biomass. We use this analytical approach to explore how community size-structure, a more tractable representation of abundance distribution across size-classes compared to pyramids (Fig. 1b), and total community biomass will respond to a whole landscape of disturbance frequencies and intensities (Fig. 3).

**Disturbance experiment on microbial communities**

We conducted an experiment in aquatic microcosms inoculated with 13 protist species and a set of common freshwater bacteria as a food resource. The protist species cover a wide range of body-sizes (from 10–10³ µm) and densities (10–10⁵ individuals/ml, Giometto et al. 2013). General lab procedures follow the protocols described in Altermatt et al. (2015), and build upon previous work on pulse disturbance effects on diversity (Altermatt et al. 2011; Harvey et al. 2016) and
invasion dynamics (Mächler & Altermatt 2012). Detailed microcosm description and set-up are presented in Appendix 4. In short, we performed a factorial experiment in which we varied disturbance frequency and intensity, resulting in a total of twenty different disturbance regimes. Disturbance was achieved by boiling a subsampled fraction of the well-mixed community in a microwave so that all species experience the same level of density reduction. All protists were killed by the microwaving process. We let the medium cool down before putting it back into the microcosm. We disturbed microcosms at five intensities: 10, 30, 50, 70 and 90 % and at four frequencies: \( f = 0.08, 0.11, 0.16 \) and 0.33, corresponding to a disturbance every 12, 9, 6 and 3 days, respectively. The experiment lasted for 21 days, or about 10–50 generations depending on species. Each disturbance regime was replicated six times. To control for the intrinsic variability of community size-structure, we cultured eight undisturbed microcosms under the same conditions. We sampled 0.2 ml of each microcosm daily to quantify individual body-sizes (i.e. cell area in \( \mu \text{m}^2 \)), protist abundances (individuals/\( \mu \text{l} \)) and total community biomass (i.e. total bioarea in \( \mu \text{m}^2/\mu \text{l} \)) using a standardized video procedure (Altermatt et al. 2015; Pennekamp et al. 2017). We binned the observed individuals into twelve size-classes ranging from 0 to \( 1.6 \times 10^5 \ \mu \text{m}^2 \) in order to get statistically comparable community size-structures. Mean protist abundance and its standard deviation in each size-class were calculated over 21 time points and 6 replicates (total of 126 observations) for each treatment and over 21 time points and 8 replicates (total of 168 observations) for the control communities. We performed Welch two sample t-tests of mean comparison (treatment versus control) to determine which disturbance regime had a significant effect on community size-structure and total community biomass (Table S2).

Model parameterization
We parameterized the model using the experimental data in order to test the capacity of the model to predict the effect of a given disturbance regime on the size-structure of real communities. The model required the following input parameters: the carrying capacities of each size-class as well as the slope and the intercept of the allometric relationship between growth rate and body-size. We took the average abundances of the undisturbed communities (8 controls) to estimate carrying capacities in each size-class. We fitted a logistic growth model to the recovery dynamics of each size-class after one disturbance (I = 90%) to obtain growth rate estimations. Specifically, we used the data from the treatment \{I=90\%, f =0.08\} (i.e. highest intensity, lowest frequency) to estimate the parameters of a logistic growth model over 12 time points using the function nls() of the stats package in R (R Core Team 2019). We determined the relationship between growth rate and body-size in our experimental communities using the 13 time-series (covering 6 size-classes) that displayed a logistic growth. We obtained the following allometric relationship: 

\[ \ln(r) = -0.37 \times \ln(M) + 3.75 \] (p-value = 0.005, \( R^2 = 0.47 \)).

Using this parameterization, we produced theoretical predictions on the size-abundance pyramids expected in the experimental disturbance regimes. We then quantitatively compared these predictions with the size-abundance pyramids observed in the experimental communities. We performed ordinary least-squares regressions to characterize the relationship between observed and predicted log-transformed mean abundances among size-classes for all the disturbance regimes.

**RESULTS**

**Model predictions**

We first explore the effects of increasing disturbance frequency (Fig. 3a, c). Infrequent disturbances do not strongly affect community size-structure and only decrease the mean abundance of the largest size-classes (Fig. 3a, \( f = 0.1 \) in dark blue). Maximum body-size gradually
decreases as disturbance frequency increases, corresponding to the extinction of large, slow-growing species (Fig. 3a, $f = 0.25$ in light blue). Disturbance frequency also affects the community size-structure through its effect on mean abundance. For frequent disturbance events, the mean abundance of all size-class decreases (Fig. 3a, $f = 0.5$ and $1$ in orange and red respectively). The effect of disturbance frequency on community-size structure have direct consequences for community-level properties: we indeed observe an approximately linear decrease in total community biomass (log) along a gradient of disturbance frequency, followed by an abrupt collapse of the community for extreme disturbance regimes (Fig. 3c).

We then investigate the effect of increasing disturbance intensity (Fig. 3b, d). Similarly, low intensity disturbances marginally affect community size-structure (Fig. 3c, $I = 30\%$ in blue) and increasing disturbance intensity decreases maximum body-size and population mean abundance. (Fig. 3b). Interestingly, the effect of disturbance intensity on community total biomass is clearly nonlinear (Fig. 3d). Low to intermediate disturbance intensities do not affect total biomass when disturbance frequency is low (e.g. $f = 0.1$ or $0.25$ in Fig. 3d). However, strong intensities affect all population abundances and trigger a sharp decrease in total biomass, culminating in a crash of the system (e.g. $\{I > 90\%, f = 0.25\}$ in Fig 3d).

**Experimental results**

We experimentally investigated the effect of disturbance frequency and intensity on the size-structure of microbial communities. For a fixed intensity (set to $I = 90\%$ in Fig. 4a, see Fig. S2 for other intensities), infrequent disturbances (i.e. $f = 0.08$ and $f = 0.11$) had a significant negative impact only on the mean abundance of intermediate size-classes (between $\text{exp}(9.6)$ and $\text{exp}(10.5)$ $\mu m^2$, Welch two sample t-tests: $t \geq 2.6$, p-values $\leq 0.02$, Table S2). When disturbance
frequency increased to $f = 0.16$, the mean abundance of the smallest size-class also decreased ($t = 3.6$, p-value = 0.01, Table S2). Finally, at even more frequent disturbances ($f = 0.33$), all size-classes were negatively impacted, except the smallest one (Fig 5a and Table S3). Overall, increasing disturbance frequency led to an abundance depletion at intermediate sizes compared to undisturbed control communities.

Similarly, for a fixed frequency (set to $f = 0.33$ in Fig. 4b, see Fig. S3 for other frequencies), a low disturbance intensity $I = 10\%$ (Fig. 4b) only affected intermediate size-classes (between exp(10) and exp(10.5) $\mu$m$^2$, $t \geq 4.5$, p-values $\leq 0.001$, Table S2). Disturbance intensities $I = 30\%$ and $50\%$ had a negative effect on the mean abundance of larger size-classes (between exp(10) and exp(11) $\mu$m$^2$, $t \geq 2.8$, p-values $\leq 0.03$, Table S2). Finally, intensities $I = 70\%$ and $I = 90\%$ had an impact on all size-classes, except the smallest size-class that were not negatively impacted by change in disturbance intensity (Fig. 4b, Table S2). Interestingly, the following disturbance regimes had a positive effect of on the mean abundance of the smallest size-class: \{I = 30\%, f = 0.33\}, $t = -6.1$, p-value $< 0.001$, (Fig. 4b), as well as \{I = 50\%, f = 0.16\} and \{I = 70\%, f = 0.11\} (Table S2, Fig. S2 and S3).

At the community-level, total biomass gradually decreased with disturbance frequency as expected by theory (Fig. 4c). All frequencies had a significant negative effect on total biomass compared to controls ($t \geq 8$, p-value $< 0.001$, Fig 4c). Disturbance intensities $I = 10\%$ and $30\%$ had no significant effects on total community biomass ($I_{10\%}$: $t = 0.75$, p-value = 0.48, $I_{30\%}$: $t = 0.5$, p-value = 0.63), while total biomass strongly decreased for intensities above $I = 50\%$ ($I_{50\%}$: $t = 6.1$, p-value $< 0.001$, $I_{70\%}$: $t = 12.7$, p-value $< 0.001$, $I_{90\%}$: $t = 14.2$, p-value $< 0.001$, Fig. 4d).

**Observed versus predicted effect of disturbances on size-abundance pyramids**
We then compared our experimental results with the predictions of the model parameterized for our freshwater microbial communities (Figure 5). The model predicted well the observed mean abundances relative to carrying capacity for all the disturbance regimes in most of the size-classes. The slope of the linear regression between observed and predicted log mean abundances, including all size-classes in all disturbance regimes (240 points), was very close to the 1:1 line, which indicates a very good fit (Figure 5a, linear regression: $y = -0.012 + 1.01x$, $R^2 = 0.96$, p-value < 0.001). Additionally, the intercept of the linear regression was not significantly different from zero ($t = 0.95$, p-value = 0.34). We illustrate in Figure 5b-d the similarities as well as the differences between the predicted and observed community size-structures for varying disturbance frequencies with a disturbance intensity fixed to $I = 90\%$ (other disturbance regimes are shown in Figs. S4-S5).

Overall, the predicted community structures were very similar to the observed ones. The model, however, often underestimated the mean abundance in the smallest size-class (Figure 5d). Furthermore, as mentioned in the previous section, some disturbance regimes had a positive effect of on the mean abundance of the smallest size-class, which cannot, by construction, be predicted by our model. We discuss below how this pattern can be explained by a disruption of biotic interactions following a disturbance and present further analyses using a predator-prey model to support this possible explanation (Fig. 6c, Appendix 3).

**DISCUSSION**

Most theories in community ecology have been developed under the assumption of steady-state conditions (Hastings 2010). Yet, most of the world’s ecosystems – specifically ≥75% of land/freshwater and 50% of marine systems – have been altered by human activities and are facing disturbances that put them clearly outside of such a steady state (IPBES 2018). Thus, to meet the societal demand for an ecological science able to predict how ecosystems will respond to global
change (Petchey et al. 2015; Urban et al. 2016), this assumption needs to be relaxed. The challenge is to develop models that make quantitative predictions regarding the impact of fluctuating environmental conditions on the structural and functional characteristics of biological systems.

Consequences of the growth-size relationship for communities exposed to disturbances

Here, we provide a robust and simple approach for predicting the size-structure of communities exposed to any combination of disturbance frequency and intensity affecting all species in a similar way, regardless of their body-size. We combine theory on disturbances with the metabolic theory of ecology and assume that the scaling of population growth rate with body-size is the leading mechanism determining the response of size-abundance pyramids to disturbances. The model makes an important advance over the steady-state predictions of the metabolic theory of ecology as it links quantitatively the shape of a size-abundance pyramid to the disturbance regime experienced by the community (Fig. 6a–b). Overall, increasing disturbance frequency or intensity narrows the bases of size-abundance pyramids and lowers their height. This corresponds to the extinction of the largest species and a general reduction of population mean abundances in all size-classes. Hence, we demonstrate that disturbances that are not size-selective and do not target large species have nonetheless a higher impact on large species than on smaller ones.

The model is applicable across all biological and temporal scales as population growth rate and disturbance frequency are expressed with the same time units. Equation (2) can also apply to populations that do not show a scaling relationship between growth rate and body-size and predicts which disturbance regimes a species can sustain, or not, based on its generation time (Figs. 2 and S1). Importantly, our results are not specific to repeated pulse disturbances but also hold for press
disturbances, which will affect the shape of size-abundance pyramids in an equivalent way (see Appendix 1 for a mathematical demonstration).

Our model offers a new perspective on community responses to disturbances by exploring the effect of repeated pulse disturbances of varying frequency and intensity on community size structure. The majority of theoretical studies on community stability have focused on local stability, which examine community’s response to small pulse disturbances around one single equilibrium (Donohue et al. 2016), reflecting the great interest for the so-called diversity-stability debate (May 1972; McCann 2000; Allesina & Tang 2012; Jacquet et al. 2016). Our approach goes beyond local stability measures at the vicinity of one single attractor and is applicable to any combination of disturbance frequency or intensity. It predicts which species, based on its growth rate, can persist or not and how the abundances of the remaining species will be affected by a whole gradient of disturbances.

Note that the model depends on a number of technical assumptions. First, we restricted our theoretical approach to disturbance regimes where pulse disturbances are applied at fixed intervals with a fixed intensity. This choice, though relatively simplistic, allowed us to mirror the disturbance regimes applied to the experimental communities. To generalize, we also performed simulations where we added stochasticity in the frequency and intensity of the disturbance regime to test the sensitivity of the theoretical results to variability in the periodicity and intensity of disturbances (Appendix 2). Our results were qualitatively robust to the addition of noise around average values of disturbance frequency and intensity, which simply increased the negative effect of one given disturbance regime on the largest size-classes (Fig. S6). Second, we consider that the allometric parameters of the relationships between population growth rate, carrying capacity and body-size are the same for all species (i.e. same slopes and intercepts). We therefore performed sensitivity
analyses of Equation (5) and demonstrate that our results are robust to variation in these allometric parameters (Appendix 2, Fig. S7-8).

**Experimental test of the theory**

The disturbance experiment on microbial communities showed some similarities but also some departures from the theoretical predictions (Figure 5b-d). As expected from the analytical model, total community biomass gradually decreased with disturbance frequency and in a more nonlinear way with disturbance intensity (Fig. 4c–d, and Fig. 3c–d for the theoretical predictions). Interestingly, it was the intermediate and not the largest size-classes that were the most sensitive to disturbances in the microbial community. We provide below two possible explanations for this observation. Most likely, the abundances of the largest size-class might be already too low, and therefore too close to the methodologically-defined detection threshold, in the control communities to observe a significant effect of the disturbances of these size-classes. Second, this might be explained by the duration of the experiment (21 days), which was not long enough to capture the extinction of the largest species. We estimated the time to reach the dynamical equilibrium in the experiment with the model parameterized with experimental data (see Table S3). The model predicted that equilibrium is reached by the end of the experiment (21 days) for the size-classes considered in all disturbance regimes but the strongest. With the highest frequency and intensity \{I=90\%; f=0.33\} the equilibrium is reached by the three smallest size-classes (in 12, 18, and 21 days respectively).

Additionally, some combinations of disturbance frequency and intensity had a positive effect on the smallest size-class of microbes compared to controls, which corresponded to the main departure from the theoretical predictions (Figure 4a-b and Figure 5d). This could be explained by a disruption of biotic interactions (predation or competition) following a disturbance, allowing the
remaining small species to grow in higher densities in the absence of other species (Cox & Ricklefs 1977; Ritchie & Johnson 2009; Bolnick et al. 2010). Such “interaction-release” mechanism could not be captured by our model of co-occurring species. We discuss below how interspecific interactions, such as competition, predation or parasitism, could modulate the shape of size-abundance pyramids exposed to disturbances.

Extending the model to communities of interacting species

To observe an “interaction-release” effect that will widen the pyramid’s base, two conditions are required (but not sufficient): (i) the existence of a significant mismatch between the growth rates of the two interacting species, leading to differential response to disturbances, and (ii) the species with the slowest growth rate has a negative effect on the other species (i.e. predator, competitor or parasite). The latter condition seems unlikely for parasitism. For competitive interactions, a “competition-release” effect can potentially increase the abundance of small, fast-growing species that will recover faster from a disturbance event compared to larger competitors (e.g. Xi et al. (2019)). Finally, the existence of a “predation-release” effect is very likely as predators are generally larger than their prey and have slower growth rates (Brose et al. 2006, 2016; Barnes et al. 2010). In an additional analysis, we performed simulations using a predator-prey model to explore in which conditions a “predation-release” effect could increase the abundance of small prey species (see Appendix 3 for detailed methods). We found that small to intermediate disturbance regimes can increase average prey abundance through a “predation-release” effect, which should generate size-abundance pyramids with a wider base (Fig. 6c). This effect vanishes above some disturbance thresholds, where prey species are also negatively impacted by disturbances (Fig. 6c and Figs. S9-S11).
Our model cannot capture cascading effects triggered by complex interactions networks in its current form. A promising future direction is the extension of the model to multitrophic communities, which will allow further explorations of the potential of interspecific interactions to modulate the impact of disturbances on size-abundance pyramids and community biomass. Indeed, it is likely that predator species will also be impacted indirectly through a bottom-up transmission of the disturbances (i.e. decrease in prey availability).

Additional mechanisms shaping size-abundance pyramids exposed to disturbances

Here, we propose a systematic approach, based on the metabolic theory of ecology, to predict the response of size-abundance pyramids to persistent disturbances. Our results are specific to a class of persistent disturbances (i.e. pulse or press) that affect the abundance of all species in a similar way, regardless of their specific body-size or growth rate. We also assume that the leading mechanism that determines the response of size-abundance pyramids to this type of disturbances is the allometric relationship between species growth rate and body-size. However, additional mechanisms can generate size-dependent abundances or size-dependent responses to disturbances in real world ecosystems. First, species sensitivity to disturbances that are not size-selective can be nonetheless unequal among size classes, with particular size-classes being more resistant to a given disturbance intensity. For example, strong windstorms or droughts generally cause greater mortality among larger or taller trees (Woods 2004; Hurst et al. 2011; Bennett et al. 2015). Second, from a spatial perspective, size-specific mobility and immigration-extinction dynamics could largely affect the relationship between species recovery dynamics and their size (McCann et al. 2005; Jacquet et al. 2017). It would be interesting to extend our approach to metacommunities, where the depletion of large species in a disturbed habitat patch could be balanced by immigration from undisturbed neighboring patches (Pawar 2015).
Finally, some disturbances can be size-selective, as illustrated by studies on abundance size spectra that specifically addressed the effect of a press, size-selective disturbance, often reflecting disturbances expected under commercial fishing (Shin et al. 2005; Sprules & Barth 2016). Our model can easily be refined to more specific cases, in which disturbances have unequal effects on species, by adding size-specific disturbance intensities to the model. The abundance size spectra of harvested fish communities are generally characterized by steeper slopes than unfished communities, and are used as a size-based indicator of fisheries exploitation (Shin et al. 2005; Petchey & Belgrano 2010; Sprules & Barth 2016). We demonstrate that size-abundance pyramids are also predictably affected by more general pulse disturbances that are not size-selective such as floods or wildfires. Hence, when compared to a reference state, size-abundance pyramids provide information on the level of disturbances an ecosystem is facing and could be used as “universal indicators of ecological status”, as advocated in Petchey & Belgrano (2010).

Conclusion

Our findings have direct implications regarding the effects of disturbances on ecosystem functioning. Indeed, the model makes predictions on total biomass and demographic traits correlated to productivity rate and energy flows, which are among the most relevant metrics to quantify ecosystem functioning (Oliver et al. 2015; Schramski et al. 2015; Brose et al. 2016; Barnes et al. 2018). In the current context of global change, we demonstrate that the expected increase in disturbance frequency and intensity should accelerate the extinction of the largest species, leading to an increasing proportion of communities dominated by small, fast-growing species and lower levels of standing biomass. Importantly, the effect of increasing disturbance regimes will be nonlinear and abrupt changes in community structure and functioning are expected once a disturbance threshold affecting the equilibrium abundances of smaller species is reached.
DATA AVAILABILITY STATEMENT

The data supporting the experimental results as well as a Rmarkdown document, which explains in detail the theoretical approach and produces the figures, are archived in the Dryad Digital Repository: https://doi.org/10.5061/dryad.95x69p8g7.

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Figure 1: A trophic pyramid (a) describes the distribution of biomass along discrete trophic levels, and assumes that all species within a trophic level have the same functional traits. The community size-structure (b) and the size-abundance pyramid (c) are equivalent size-centric representations of ecological communities and are the focus of this study. They describe the distribution of abundance across body-sizes and can be studied both within and across trophic levels. b) the community size-structure depicts log(body-size) on the x-axis and log(abundance) on the y-axis, while c) the size-abundance pyramid shows log(abundance) on the x-axis and log(body-size) on the y-axis. Note that the area $A$ is the same in both panels. We use the community size-structure representation throughout the paper as it facilitates comparisons between theory and experimental data, but see Fig. 6 for a synthesis of our findings using the pyramid representation.
Figure 2: Population dynamics and persistence according to disturbance regime. a) Temporal dynamics of two species experiencing the same disturbance regime. Species 1 has a smaller body-size and therefore a higher growth rate than species 2. A population can persist only if its growth rate balances the long-term effect of the disturbance regime. We derive in equation (4) the mean abundance at dynamical equilibrium (i.e. temporal mean) of the persisting species experiencing varying disturbance regimes. b) Isoclines of the persistence criterion in the disturbance regime landscape according to population growth rate (numbers): on and above the line, the population of a given growth rate goes extinct. Lines with the same color code as in panel (a) correspond to the same growth rate.
Figure 3: Effects of disturbance frequency and intensity on community size-structure and average total biomass at dynamical steady state. Analytical results derived from Equation (5). a) Effect of disturbance frequency (disturbance intensity is fixed to 50% abundance reduction), and b) disturbance intensity (disturbance frequency is fixed to 0.25) on community size-structure. c) Effect of disturbance frequency and d) intensity on average total biomass (in log), for different intensities (c) and frequencies (d), respectively. Points on the black lines in (c) and (d) show the disturbance regimes corresponding to community size-structures of the respective colors displayed in panels (a) and (b).
**Figure 4:** Experimental results. a) Effect of disturbance frequency on community size-structure. Vertical bars illustrate mean abundance (individuals/µl) and its standard deviation over 21 time points and 6 replicates for each size-class (µm²). Disturbance intensity is fixed to $I = 90\%$; other intensities are shown in Fig. S2 and statistics in Table S2. b) Effect of disturbance intensity on community size-structure. Disturbance frequency is fixed to $f = 0.33$, other frequencies are shown in Fig. S3 and statistics in Table S2. Controls are in grey (undisturbed environment) and axes are on a logarithmic scale. c) Effect of disturbance frequency on total community biomass (temporal mean, $n = 6$ for treatments, $n = 8$ for controls, in µm²/µl). Disturbance intensity is fixed...
to \( I = 90\% \) as in panel (a); other intensities are shown in Fig. S2. All frequencies have a

significant negative effect on total biomass compared to controls: Welch two sample t-tests: \( f_{0.08} \):

\[ t = 8, \ p\text{-value} < 0.001, \]

\[ f_{0.11} : t = 8.5, \ p\text{-value} < 0.001, \]

\[ f_{0.16} : t = 13.2, \ p\text{-value} < 0.001, \]

\[ f_{0.33} : t = 14.2, \ p\text{-value} < 0.001. \]

d) Effect of disturbance intensity on total community biomass (temporal mean, \( n = 6 \) for treatments, \( n = 8 \) for controls, in \( \mu m^2/\mu l \)). Disturbance frequency is fixed to \( f = 0.33 \) as in panel (b); other frequencies are shown in Fig. S3. All intensities except \( I = 10\% \) and 30\% have a significant negative effect on total biomass compared to controls: \( I_{10\%} : t = 0.75, \ p\text{-value} = 0.48, \]

\( I_{30\%} : t = 0.5, \ p\text{-value} = 0.63, \)

\( I_{50\%} : t = 6.1, \ p\text{-value} < 0.001, \)

\( I_{70\%} : t = 12.7, \ p\text{-value} < 0.001, \)

\( I_{90\%} : t = 14.2, \ p\text{-value} < 0.001. \)
Figure 5: Comparison between experimental results and model predictions. a) Predicted vs. observed mean abundance $N$ relative to carrying capacity $K$ in the twelve size-classes for all the disturbance regimes ($n=240$). Solid line: linear regression $[y = -0.012 + 1.01x; R^2 = 0.96, p\text{-value} < 0.001]$. Standard error for slope: 0.01, intercept: 0.02. Dashed line indicates a 1:1 relationship. 

b) Predicted effect of disturbance frequency on the community size-structure of experimental communities. Disturbance intensity is fixed to $I = 90\%$; other disturbance regimes are shown in Figs. S4-S5. Controls are in black (undisturbed environment) and axes are on a logarithmic scale.

c) Observed effect of disturbance frequency on the community size-structure of experimental communities (similar to Fig. 4a). d) Difference between observed and predicted mean abundance for each size-class.
Figure 6: Graphical summary of the effects of disturbances on the shape of size-abundance pyramids. Panels (a) and (b) show size-abundance pyramids for increasing disturbance frequency and intensity, respectively (same analytical results as in Fig. 3a-b). Panel (c) illustrates the expected change in the shape of size-abundance pyramids resulting from a predator-prey dynamic. Lines and points in panel (c) represent isoclines of disturbance regimes \( \{ I, T \} \) under which we can expect a predation-release effect leading to wider bases of size-abundance pyramids. Points represent the disturbance intensity for which prey species switch from higher to lower mean abundances at dynamical equilibrium in presence compared to in absence of disturbances, for a given disturbance frequency and a set of predator parameters. Black points are estimated for a smaller prey, i.e. with higher growth rate, than grey points (see detailed method in Appendix 3 and Table S4 for parameter values).
Supporting Information

How pulse disturbances shape size-abundance pyramids

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7. Supplementary References
1. Appendix 1: Analytical derivation of population mean abundance

To investigate the change in community size-structure with disturbances, we derive analytically the equilibrium mean abundance, $\bar{N}$, of a model in which a population displaying a logistic growth is submitted to recurrent pulse disturbances affecting all species in a similar way. This simple model is described in the methods section (see Fig. 2). The minimal abundance at equilibrium, $N_-$, that is the abundance just after a disturbance, is provided in Harvey et al. (2016), and gives, after simplification:

$$N_- = K \left(1 - \frac{I}{1 - e^{-rt}}\right) \quad (6)$$

with $r$ and $K$ the growth rate and the carrying capacity of the population, respectively. $I$ and $T$ are the intensity (proportion of abundance reduction) and the period (inverse frequency) of the disturbance regime, respectively.

To get the mean abundance, $\bar{N}$, we calculate the integral of the abundances between two disturbances at equilibrium, that is between 0 and $T$, the period of the disturbance regime:

$$\bar{N} = \frac{1}{T} \int_0^T f(t)\,dt \quad (7)$$

Here, the function $f(t)$ is the logistic solution, with $t$ the time and $N_0$ the initial abundance:

$$f(t) = \frac{K}{1 + \left(\frac{K}{N_0} - 1\right)e^{-rt}} \quad (8)$$

To calculate $\bar{N}$, we note that equation (7) is equivalent to:

$$\bar{N} = \frac{1}{T} \left(F(T) - F(0)\right) \quad (9)$$

where $F(x)$ is a primitive of $f(t)$. It can be shown by calculating its derivative that the following function is a primitive of the logistic solution (8):

$$f(t) = \frac{K}{1 + \left(\frac{K}{N_0} - 1\right)e^{-rt}} \quad (8)$$
\[ F(t) = \frac{K \ln(K + N_0 e^{rt} - N_0)}{r} \quad (10) \]

In our case, \( N_0 \) is the minimal abundance after a disturbance at equilibrium, \( N_- \). By replacing equation (6) in (10), and then equation (10) in (9), we obtain the following expression:

\[ \bar{N} = K \left( \frac{\ln(1 - I)}{Tr} + 1 \right) \quad (11) \]

Since we are interested into community size-structure, we want to express mean abundance in function of mean population body-size on a log scale. For that, we assume the following allometric log-linear relationship between growth rate, \( r \), and mean body-size, \( M \), in accordance with the metabolic theory of ecology (Brown et al. 2004; Savage et al. 2004):

\[ \ln(r) = a_r \ln(M) + b_r \quad (12) \]

With \( a_r \) and \( b_r \) being the slope and the intercept of this allometric relationship.

Abundance also scales with body-size on a logarithmic scale (Brown & Gillooly 2003; Brown et al. 2004), then we can assume for carrying capacity:

\[ \ln(K) = a_K \ln(M) + b_K \quad (13) \]

With \( a_K \) and \( b_K \) being the slope and the intercept of this second allometric relationship.

By replacing (12) and (13) into (11), we finally obtain:

\[ \ln(\bar{N}) = a_K \ln(M) + b_K + \ln \left( \frac{\ln(1 - I)}{Te \ a_r \ \ln(M) + b_r} + 1 \right) \quad (14) \]

The formula is valid when the expression in parentheses in the right-hand term is positive, which corresponds to the persistence criteria given in equations (2) and (3) of the main text.

We focus here on pulse disturbances to compare the theoretical predictions with the experimental results. However, press disturbances would have similar effects on size-abundance pyramids. Indeed, if we consider a constant additional mortality rate \( m \) on the logistic growth, such that population dynamics are described by:
\[ \frac{dN}{dt} = rN \left( 1 - \frac{N}{K} \right) - mN \quad (15) \]

Then the abundance at equilibrium is \( \bar{N} = K \left( 1 - \frac{m}{r} \right) \) and the critical growth rate is \( r > m \).

This result demonstrates that press disturbances that are not size-selective will also exclude the large, slow growing species.


2. Appendix 2: Detailed methods to produce the theoretical results

We consider a community made of different co-occurring species constrained by intraspecific competition only. The species populations grow according to logistic functions (equation (1)) with specific growth rates, \( r \) and carrying capacities \( K \), and are submitted to disturbances which recurrently reduce population abundances (every \( T \) units of time, the period) by destructing a proportion \( I \) (the intensity) of all species populations.

Equations (2) and (3) of the main text give the analytical derivation of the critical growth rate above which a population can persist under a given disturbance regime (combination of \( I \) and \( T \)). This allows to predict the set of disturbance regimes that a population can sustain (Fig. 2b) according to its growth rate, as well as the minimum generation time \((1/r)\) needed to maintain a viable population under a given disturbance regime (Fig. S1).

To analyze the changes in community size-structure driven by disturbance regimes, we consider a set of 1000 co-occurring species, which body-sizes are randomly drawn from a lognormal distribution of mean 6 and standard deviation 1.5. This provides a range of sizes between 2 and 10 on a logarithmic scale. In an aquatic community for instance, it could correspond to a set of species from bacteria to planktivorous ranging from sizes of 5 µm to 22 mm. We assume a negative allometric relationship between growth rate and body-size (equation 12) with \( a_r = -0.25 \), a widely observed value for multiple taxa (Brown et al. 2004), and \( b_r = 0.4 \), a value which makes our growth rate gradient ranging approximately from 0.1 to 1, corresponding to common values for microorganisms when day is the time unit. We also derive the carrying capacity \( K \) of each species from its body-size assuming a log-linear relationship (equation (13)), with the slope \( a_K = -0.75 \), following a commonly observed value (Brown & Gillooly 2003; Brown et al. 2004), and the intercept \( b_K = 10 \), chosen to have values from 10 to 5000 for \( K \).
which are, for instance, common values for microorganisms in terms of number of individuals per µl. We then calculate the mean abundance at equilibrium, $\bar{N}$, for each species population using equation (14), for different disturbance regimes $\{I, T\}$, to produce Figs. 3a and 3b and the abundance pyramids in Figs. 6a and 6b (same values). In the figures, $f$ corresponds to the disturbance frequency: $f = 1/T$. Parameter values are summarized in Table S1.

Then, we calculate community total biomass by summing the biomass of each of the 1000 species populations within the community, with species biomass, $B$, calculated as the product of mean abundance at equilibrium, $\bar{N}$, and the average individual body-size in the population, $M$:

$$B = \bar{N}M$$

We provide total biomass of the community for scenarios covering a whole landscape of disturbance regimes $\{I, T\}$ in Figs. 3c and 3d.

**Addition of stochasticity in intensity and frequency of disturbances**

The above analysis was first conducted for strictly regular disturbances of the same magnitude. We then investigate the effect of variability of disturbance period and intensity on the community size-structure. We run simulations of the same 1000 co-occurring species than previously but with sequences of disturbance periods and intensities drawn from a uniform distribution within an interval defined by a percentage of deviation from the mean (see Table S5). Results are robust to this variation for weak to relatively strong regimes of disturbances. For very high disturbance intensities and frequencies, the variability of disturbances characteristics increases by drift the extinction of the larger species (Figure S6). The effect is more pronounced for intensity variability, while for periods, increase in extinction occur only for very large variations around
already short periods (mean±100%). In that case, consecutive very short periods selected by chance can prevent recovery.

For instance, let’s take the case shown in Fig. S6 in the top right panel, for which pulse disturbances were of mean intensity 80% with a variability of 25% (in terms of deviation from the mean) and a mean period of 3 days with a variability of 100%. This means that we created sequences of disturbances (one for each replicate simulation applied to all species of the community) with the intensity of each disturbance and the period between each pair of disturbances being randomly drawn from the intervals [60%,100%] and [0,6], respectively.

**Sensitivity analyses**

We consider that the allometric parameters of the relationships between population growth rate, carrying capacity and body-size are the same for all species (i.e. same slopes and intercepts). However, the intercepts can be variable between taxonomic groups (Brown *et al.* 2004). Moreover, while multicellular organisms have growth rates that scale with body-size with a slope of -1/4, a slope of -1 has been reported for unicellular organisms (DeLong *et al.* 2010). We therefore perform sensitivity analyses of Equation (5) to assess the robustness of our results to variation in these allometric parameters. Increasing the slope (toward more negative values) or decreasing the intercept of the relationship between population growth rate and body-size has the same qualitative impact on community size-structure: it decreases the size-specific criterion for population persistence (equation 3) and therefore truncates the community size-structure from its largest species (Fig. S7). Small species are not impacted by changes in the slope, except when disturbances are very strong. Finally, the slope and intercept of the allometric relationship between carrying capacity and body-size essentially change the steepness of a pyramid’s sides, but not their qualitative response to disturbances (Fig. S8). Note that this slope is modulated by
additional variables in multitrophic communities, namely predator-prey mass ratio and predator trophic efficiency (Jennings & Mackinson 2003; Blanchard et al. 2009; Trebilco et al. 2013). A further step will be to integrate these variables into the model to capture the effect of disturbances on the size-structure of multitrophic communities.
3. Appendix 3: Predator-prey model and interaction-release effect

We focus here on the effect of predator-prey dynamics on the shape of size-abundance pyramids exposed to disturbances. We hypothesize that specific disturbance regimes could trigger a predation release after a disturbance event that would allow small, fast-growing prey species to reach higher abundances compared to the undisturbed case. We investigate this hypothesis using a Lotka-Volterra predator-prey model, where the dynamics of prey and predator abundances, $N$ and $P$, are described by the following system of differential equations:

$$\frac{dN}{dt} = \left(1 - \frac{N}{K}\right) r N - aPN$$  \hspace{1cm} (15)

$$\frac{dP}{dt} = (\epsilon N - m)P$$  \hspace{1cm} (16)

with $K$ and $r$ the carrying capacity and the intrinsic growth rate of the prey, respectively, and $\epsilon$, $a$, and $m$ the conversion efficiency, attack and mortality rates of the predator, respectively. We added recurrent disturbances to this dynamic as described in the previous section.

We examine the effects of recurrent pulse disturbances on a predator-prey system by means of simulations (see Table S6 for parameter values). To avoid issues arising from synchrony between intrinsic oscillations of the system and disturbance regime, species parameters are chosen to have stable equilibrium for the case without disturbance, and simulations start with species abundances set to their equilibrium without disturbances, which are easily derived analytically. After 1000 units of time, disturbances start and dynamics are run until 50,000 units of time, which was sufficient to reach equilibrium in the parameter space explored. Dynamics are calculated in a C++ code (see html file). For numerical integration, we use an adaptive step solver provided in the GNU Scientific Library, GSL version 2.5 (Galassi et al. 2011), using the Runge-Kutta Kash-Carp method. We estimate mean abundances at equilibrium by averaging prey or predator abundances over ten disturbance periods (time between eleven disturbances).
We hypothesize that specific disturbance regimes could trigger a transient predation release after a disturbance event that would allow small, fast-growing prey species to reach higher abundances compared to the undisturbed case. To test this hypothesis, we focus on how change in disturbance regime modulates the equilibrium abundance of a specific predator-prey system. Predator parameters are chosen to have prey abundance without disturbance of 100 individuals per area unit (see Tables S4 and S6). As we are also interested into understanding if faster prey benefit from a higher predation release effect, we vary prey body-size, and thus prey growth rate through equation (12), while keeping predator parameters constant (this is equivalent to varying the predator-prey size ratio). We choose prey carrying capacity such that the predator persists for a wide range of disturbance regimes, but eventually goes extinct in too harsh disturbance regimes. Figs. S9 to S11 show the results for an extended parameter space of disturbance regimes and prey body-sizes (see Table S6 for parameter values).

Finally, we are interested in linking this result to change in the shape of size-abundance pyramids. For that, we summarize the results of the predation-release effect for two prey body-sizes in Fig. 6c. Overall, disturbances always have a positive effect on prey abundance for low to intermediate disturbances regimes. Then, when increasing the strength of disturbances, a case happens for which disturbances are so strong that prey mean abundance is also negatively affected. We determine the critical disturbance intensity for which prey mean abundance drops below the case without disturbances for a given disturbance period (or frequency). For that, we run a set of simulations with a small increment of disturbance intensity (see Table S4) and estimate this threshold via a linear approximation between the two closest points to the threshold (see provided code). Under the isoclines representing the threshold intensity for different disturbance frequencies, the predator-release effect operates and is stronger than the negative impact of disturbances on prey species. In that case we might observe a widening of abundance.
pyramid’ bases with disturbance in trophic communities (Fig. 6c). Larger prey sizes (or lower predator-prey size ratio) bring down the predator-release isocline to weaker disturbance regimes, reducing the disturbance regime space in which disturbance might lead to pyramids with wider bases.

**Code release**

We will release the code through a Rmarkdown document and an associated C++ source code file. We thank the developers of R version 3.6.1 (R Core Team 2019), Rmarkdown, and those of the R-C++ interface, that we used in the script. Specifically, we used R version 3.5.1 and the following R-packages: "**Rcpp**" version 1.0.0 (Eddelbuettel and Francois 2011, Eddelbuettel 2013, Eddelbuettel and Balamuta 2017), and "**RcppGSL**" version 0.3.6 (Eddelbuettel and Francois 2018). “Rmisc” version 1.5 (Hope 2013) has been used to calculate confidence intervals in Figure S6.
4. Appendix 4: Full experimental methods

We conducted an experiment in aquatic microcosms inoculated with 13 protist species (*Blepharisma* sp., *Cephalodella* sp. *Chilomonas* sp., *Chlorogonium euchlorum*, *Colpidium* sp., *Cyclidium* sp., *Euglena gracilis*, *Euplotes aediculatus*, *Loxocephalus* sp., *Paramecium aurelia*, *Paramecium caudatum*, *Spirostomum* sp. and *Tetrahymena* sp.) and a set of common freshwater bacteria (*Serratia fonticola*, *Bacillus subtilis* and *Brevibacillus brevis*) as a food resource. These protist species cover a wide range of body-sizes (from 10–10$^3$ microns) and densities (10–10$^5$ individuals/ml, Giometto *et al.* 2013). All species are bacterivores whereas three of them can also photosynthesize and two species can feed on smaller protists (Table S7). General lab procedures follow the protocols described in (Altermatt *et al.* 2015). The microcosms consisted of a 250 ml Schott bottle filled to 100 ml. They were assembled by first filling each Schott bottle with 30 ml of pre-autoclaved standard protist medium (Carolina Biological Supply, Burlington NC, USA), and 5 ml of a bacteria solution. After 24 h, to allow time for bacteria growth, we added 65 ml of protist solution mixing 5 ml of each protist species at carrying capacity. All communities were allowed to grow for one week before disturbance treatments started.

**Experimental design**

We performed a factorial experiment in which we varied disturbance frequency and intensity, resulting in a total of twenty different disturbance regimes. Disturbance was achieved by boiling a fraction of the well-mixed community in a microwave. We let the medium cool down before putting it back into the microcosm. This procedure allowed to keep the composition of the microcosm constant and to avoid nutrient addition or loss. It mimics disturbances such as fire and flooding, that initially reduce population abundance but may also enhance the regeneration of
nutrients (Haddad et al. 2008). Disturbance intensities ranged from 10, 30, 50, 70 to 90%. We disturbed microcosms at four frequencies: \( f = 0.08, 0.11, 0.16 \) and 0.33, corresponding to a disturbance every 12, 9, 6 and 3 days respectively. The experiment lasted for 21 days, or 10–50 generations depending on species. Each disturbance regime was replicated six times. To control for the intrinsic variability of abundance pyramids, we cultured eight undisturbed microcosms under the same conditions.

**Sampling**

We sampled 0.2 ml of each microcosm daily to quantify individual body-sizes (i.e. mean cell area in \( \mu m^2 \)), protist abundances (individuals/\( \mu l \)) and total community biomass (i.e. total bioarea in \( \mu m^2/\mu l \)) using a standardized video procedure (Altermatt et al. 2015; Pennekamp et al. 2017). A constant volume (14.9 \( \mu l \)) of each sample was placed under a dissecting microscope connected to a camera and a computer for the recording of videos (4 seconds per video). Then, using image processing software (IMAGEJ, National Institute of Health, USA) and the R-package *bemovi* (Pennekamp et al. 2015) we extracted the number of moving organisms per video frame and the size of each individual (mean cell area in \( \mu m^2 \)). We estimate total biomass as the sum area of all individuals averaged by video frames, assuming proportionality between area and mass. Other traits such as organisms’ speed and shape were used to filter out background movement noise (e.g. particles from the medium).

**Statistical analyses**

We binned the observed individuals into twelve size-classes ranging from 0 to \( 1.6 \times 10^5 \mu m^2 \) in order to get statistically comparable community size-structures. The mean abundance and its standard
deviation in each size-class were calculated over 21 time points and 6 replicates (total of 126 observations) for each treatment and over 21 time points and 8 replicates (total of 168 observations) for the control communities. We performed Welch two sample t-tests of mean comparison (treatment versus control) to determine which disturbance regime had a significant effect on community size-structure and total community biomass. Results are presented in Table S2, Fig.4, Fig. S2 and Fig. S3.
## 5. Supplementary Tables

### Table S1: Model parameters for the results showed in Fig. 3.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
<th>Values</th>
<th>Dimension</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\mu_{size}$</td>
<td>Mean of the log-normal distribution of community body-size</td>
<td>6</td>
<td>L</td>
<td></td>
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<tr>
<td>$\sigma_{size}$</td>
<td>Standard deviation of the log-normal distribution of community body-size</td>
<td>1.5</td>
<td>L</td>
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<tr>
<td>$a_r$</td>
<td>Slope of the relationship between body-size and growth rate in a log space</td>
<td>-0.25</td>
<td>$T^{-1}L^{-1}$</td>
<td>Brown et al 2004</td>
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<tr>
<td>$b_r$</td>
<td>Intercept of the relationship between body-size and growth rate in a log space</td>
<td>0.4</td>
<td>$T^{-1}$</td>
<td></td>
</tr>
<tr>
<td>$a_K$</td>
<td>Slope of the relationship between body-size and carrying capacity in a log space</td>
<td>-0.75</td>
<td>$L^{-2}L^{-1}$</td>
<td>Brown et al 2004</td>
</tr>
<tr>
<td>$b_K$</td>
<td>Intercept of the relationship between body-size and carrying capacity in a log space</td>
<td>10</td>
<td>$L^{-2}$</td>
<td>Log number of individuals per area</td>
</tr>
<tr>
<td>$I$</td>
<td>Disturbance intensity</td>
<td>$0.001–0.999$</td>
<td>$\phi$</td>
<td>Proportion of punctual abundance reduction</td>
</tr>
<tr>
<td>$T$</td>
<td>Disturbance period</td>
<td>1–100</td>
<td>$T$</td>
<td>Time between two disturbances</td>
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Dimensions L and T mean length and time, respectively.
Table S2: **Statistics for the effect of all disturbance regimes on community size-structure.**

Effects of disturbance frequency $f = 1/T$ and intensity $I$ on the community size-structures presented in Figs. 4, S2 and S3. Statistics of Welch two-sample t-tests of mean comparison (treatment versus control). Values in blue and red indicate a significant positive and negative effect of the disturbance regime on the mean abundance compared to controls, respectively (i.e., p-value ≤ 0.05). The twelve size-classes (S1 to S12) range from 0 to $1.6 \times 10^5 \mu m^2$ and all have a width of $1.4 \times 10^4 \mu m^2$.

<table>
<thead>
<tr>
<th>$I$</th>
<th>$f$</th>
<th>S1</th>
<th>S2</th>
<th>S3</th>
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<th>S5</th>
<th>S6</th>
<th>S7</th>
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<th>S9</th>
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<th>S11</th>
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<td>4.9</td>
<td>6.9</td>
<td>4.5</td>
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<td>1.1</td>
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<td>-0.5</td>
<td>0.9</td>
</tr>
<tr>
<td>10%</td>
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<td>0.9</td>
<td><strong>2.5</strong></td>
<td>1.2</td>
<td>4</td>
<td>1.1</td>
<td>1.1</td>
<td>-0.3</td>
<td>-0.3</td>
<td>-0.5</td>
<td>-1.4</td>
<td>-0.4</td>
<td>0.6</td>
</tr>
<tr>
<td>10%</td>
<td>0.11</td>
<td>-1</td>
<td>-0.8</td>
<td>1.7</td>
<td>0.6</td>
<td>0.7</td>
<td>-0.1</td>
<td>-0.7</td>
<td>0.8</td>
<td>0.6</td>
<td>1.3</td>
<td>0.4</td>
<td>1.2</td>
</tr>
<tr>
<td>10%</td>
<td>0.08</td>
<td>0.7</td>
<td>1.8</td>
<td><strong>2.9</strong></td>
<td><strong>5.2</strong></td>
<td>2</td>
<td>2.1</td>
<td>1.4</td>
<td><strong>2.7</strong></td>
<td>0.7</td>
<td>1.2</td>
<td>1</td>
<td>1.2</td>
</tr>
<tr>
<td>30%</td>
<td>0.33</td>
<td>-<strong>6.1</strong></td>
<td>0.8</td>
<td><strong>5.7</strong></td>
<td><strong>5.7</strong></td>
<td>5.3</td>
<td><strong>4.3</strong></td>
<td>2.8</td>
<td>3.8</td>
<td>-0.2</td>
<td>-1.1</td>
<td>-0.9</td>
<td>-0.1</td>
</tr>
<tr>
<td>30%</td>
<td>0.16</td>
<td>-0.6</td>
<td>0.7</td>
<td>2.1</td>
<td>1.7</td>
<td><strong>3.9</strong></td>
<td><strong>3.6</strong></td>
<td>1.8</td>
<td>1.8</td>
<td>-1.8</td>
<td>0</td>
<td>0</td>
<td>1.6</td>
</tr>
<tr>
<td>30%</td>
<td>0.11</td>
<td>-1.6</td>
<td>0.7</td>
<td>2.2</td>
<td><strong>2.4</strong></td>
<td><strong>2.5</strong></td>
<td>2.1</td>
<td>0.4</td>
<td>-0.9</td>
<td>-1.6</td>
<td>0</td>
<td>0.2</td>
<td>1.1</td>
</tr>
<tr>
<td>30%</td>
<td>0.08</td>
<td>-1.6</td>
<td>-0.9</td>
<td><strong>2.8</strong></td>
<td>2.4</td>
<td>1.9</td>
<td><strong>3.5</strong></td>
<td>1.3</td>
<td>0.5</td>
<td>-0.7</td>
<td>0</td>
<td>0.3</td>
<td>0</td>
</tr>
<tr>
<td>50%</td>
<td>0.33</td>
<td>-0.8</td>
<td>2.1</td>
<td><strong>8.6</strong></td>
<td><strong>11.1</strong></td>
<td>7.3</td>
<td><strong>4.6</strong></td>
<td><strong>3.1</strong></td>
<td><strong>3.7</strong></td>
<td>-1</td>
<td>-0.3</td>
<td>0.6</td>
<td>1.6</td>
</tr>
<tr>
<td>50%</td>
<td>0.16</td>
<td>-<strong>2.7</strong></td>
<td>1.4</td>
<td><strong>3.8</strong></td>
<td><strong>5.5</strong></td>
<td><strong>4.4</strong></td>
<td><strong>4.3</strong></td>
<td><strong>2.8</strong></td>
<td>1.1</td>
<td>-1.2</td>
<td>-0.8</td>
<td>-0.4</td>
<td>2.1</td>
</tr>
<tr>
<td>50%</td>
<td>0.11</td>
<td>-1.6</td>
<td>-0.7</td>
<td><strong>3.9</strong></td>
<td>7</td>
<td><strong>2.6</strong></td>
<td><strong>2.6</strong></td>
<td>-0.5</td>
<td>-0.5</td>
<td>-<strong>2.8</strong></td>
<td>-2</td>
<td>-0.7</td>
<td>0.7</td>
</tr>
<tr>
<td>50%</td>
<td>0.08</td>
<td>-0.3</td>
<td>1.8</td>
<td><strong>2.6</strong></td>
<td><strong>3.4</strong></td>
<td><strong>5.2</strong></td>
<td>3.8</td>
<td>2</td>
<td>-0.2</td>
<td>-1.3</td>
<td>-1.7</td>
<td>0</td>
<td><strong>2.6</strong></td>
</tr>
<tr>
<td>70%</td>
<td>0.33</td>
<td>0.1</td>
<td><strong>6.7</strong></td>
<td>10.5</td>
<td>9.2</td>
<td>7.5</td>
<td><strong>6.6</strong></td>
<td><strong>6.3</strong></td>
<td><strong>2.7</strong></td>
<td>0.2</td>
<td>1.1</td>
<td>1</td>
<td>1.5</td>
</tr>
<tr>
<td>70%</td>
<td>0.16</td>
<td>-2.1</td>
<td><strong>3.3</strong></td>
<td><strong>5.5</strong></td>
<td><strong>5.2</strong></td>
<td>3</td>
<td><strong>2.7</strong></td>
<td>0.7</td>
<td>-0.3</td>
<td>-1.5</td>
<td>-0.7</td>
<td>1.3</td>
<td><strong>0.3</strong></td>
</tr>
<tr>
<td>70%</td>
<td>0.11</td>
<td>-<strong>2.5</strong></td>
<td>-0.3</td>
<td>6</td>
<td><strong>8.9</strong></td>
<td><strong>5.6</strong></td>
<td><strong>4.3</strong></td>
<td><strong>2.6</strong></td>
<td>1.5</td>
<td>-1.3</td>
<td>-0.4</td>
<td>0.6</td>
<td>1.5</td>
</tr>
<tr>
<td>70%</td>
<td>0.08</td>
<td>-0.9</td>
<td><strong>2.7</strong></td>
<td><strong>3.8</strong></td>
<td><strong>2.7</strong></td>
<td><strong>3.8</strong></td>
<td><strong>3.5</strong></td>
<td>1</td>
<td>1.2</td>
<td>-1.4</td>
<td>-0.7</td>
<td>-0.4</td>
<td>0.3</td>
</tr>
<tr>
<td>90%</td>
<td>0.33</td>
<td>-1.7</td>
<td><strong>6.3</strong></td>
<td>10.4</td>
<td><strong>17.6</strong></td>
<td><strong>9.8</strong></td>
<td>9</td>
<td><strong>7.3</strong></td>
<td><strong>4.3</strong></td>
<td><strong>2.9</strong></td>
<td><strong>2.8</strong></td>
<td>1.1</td>
<td></td>
</tr>
<tr>
<td>90%</td>
<td>0.16</td>
<td><strong>3.6</strong></td>
<td><strong>6.6</strong></td>
<td>8.4</td>
<td><strong>10.2</strong></td>
<td><strong>4.7</strong></td>
<td><strong>6.4</strong></td>
<td>1.6</td>
<td>-0.1</td>
<td>-2.2</td>
<td>-0.5</td>
<td>0.4</td>
<td>1.6</td>
</tr>
<tr>
<td>90%</td>
<td>0.11</td>
<td>1.8</td>
<td><strong>2.9</strong></td>
<td><strong>6.8</strong></td>
<td><strong>6.8</strong></td>
<td><strong>3.4</strong></td>
<td>2.3</td>
<td>-1.9</td>
<td>-0.8</td>
<td>-<strong>2.8</strong></td>
<td>-1.7</td>
<td>0.1</td>
<td>0.9</td>
</tr>
<tr>
<td>90%</td>
<td>0.08</td>
<td>0.7</td>
<td><strong>2.6</strong></td>
<td><strong>5.9</strong></td>
<td><strong>9.7</strong></td>
<td><strong>3.5</strong></td>
<td>1.7</td>
<td>-0.3</td>
<td>-0.4</td>
<td>-1.6</td>
<td>-1.4</td>
<td>-0.4</td>
<td>1.8</td>
</tr>
</tbody>
</table>
Table S3: Model parameters for the results showed in Fig. 5.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
<th>Values</th>
<th>Units</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>$a_r$</td>
<td>Slope of the relationship between body-size and growth rate in a log space</td>
<td>-0.37</td>
<td>log($\mu$m$^2$)$^{-1}$ log(d$^{-1}$)</td>
<td>From experimental data</td>
</tr>
<tr>
<td>$b_r$</td>
<td>Intercept of the relationship between body-size and growth rate in a log space</td>
<td>3.75</td>
<td>log(d$^{-1}$)</td>
<td>From experimental data</td>
</tr>
<tr>
<td>$M$</td>
<td>Midpoints of size-classes (cell area)</td>
<td>7,182–86,185</td>
<td>$\mu$m$^2$</td>
<td>From experimental data</td>
</tr>
<tr>
<td>$K$</td>
<td>Carrying capacities per size-class</td>
<td>244–95,387</td>
<td>individuals/$\mu$L</td>
<td>From experimental data</td>
</tr>
<tr>
<td>$I$</td>
<td>Disturbance intensity</td>
<td>0.1–0.9</td>
<td>$\phi$</td>
<td>Proportion of punctual abundance reduction</td>
</tr>
<tr>
<td>$T$</td>
<td>Disturbance period</td>
<td>3–12</td>
<td>d</td>
<td>Time between two disturbances</td>
</tr>
</tbody>
</table>
Table S4: Predator-prey model parameters for the simulations showed in Fig. 6c.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
<th>Values</th>
<th>Dimension</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>$M$</td>
<td>Prey body-size</td>
<td>100, 10000</td>
<td>L</td>
<td></td>
</tr>
<tr>
<td>$a_r$</td>
<td>Slope of the relationship between body-size and growth rate in a log space</td>
<td>-0.25</td>
<td>T⁻¹L⁻¹</td>
<td>Brown et al 2004</td>
</tr>
<tr>
<td>$b_r$</td>
<td>Intercept of the relationship between body-size and growth rate in a log space</td>
<td>0.4</td>
<td>T⁻¹</td>
<td></td>
</tr>
<tr>
<td>$K$</td>
<td>Prey carrying capacity</td>
<td>5000</td>
<td>L⁻²</td>
<td>number of individuals per area</td>
</tr>
<tr>
<td>$a$</td>
<td>Predator attack rate</td>
<td>0.01</td>
<td>T⁻¹/L⁻²</td>
<td>attacks per predator (given their abundance per area) and per unit of time</td>
</tr>
<tr>
<td>$m$</td>
<td>Predator mortality rate</td>
<td>0.1</td>
<td>T⁻¹</td>
<td>Proportion of predator death per unit of time</td>
</tr>
<tr>
<td>$\varepsilon$</td>
<td>Predator conversion efficiency</td>
<td>0.1</td>
<td>$\varnothing$</td>
<td>Proportion of prey caught converted into predator</td>
</tr>
<tr>
<td>$I$</td>
<td>Disturbance intensity (in %)</td>
<td>0 to 99.9 by increment of 0.1</td>
<td>$\varnothing$</td>
<td>Percentage of punctual abundance reduction</td>
</tr>
<tr>
<td>$T$</td>
<td>Disturbance period</td>
<td>2, 3, 4, 5, 6, 7, 10, 20, 100</td>
<td>T</td>
<td>Time between two disturbances</td>
</tr>
</tbody>
</table>

Dimensions L and T mean length and time, respectively.
Table S5: Model parameters for the results showed in Fig. S6.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
<th>Values</th>
<th>Dimension</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\mu_{size}$</td>
<td>Mean of the log-normal distribution of community body-size</td>
<td>6</td>
<td>L</td>
<td></td>
</tr>
<tr>
<td>$\sigma_{size}$</td>
<td>Standard deviation of the log-normal distribution of community body-size</td>
<td>1.5</td>
<td>L</td>
<td></td>
</tr>
<tr>
<td>$a_r$</td>
<td>Slope of the relationship between body-size and growth rate in a log space</td>
<td>-0.25</td>
<td>T^{-1}L^{-1}</td>
<td>Brown et al 2004</td>
</tr>
<tr>
<td>$b_r$</td>
<td>Intercept of the relationship between body-size and growth rate in a log space</td>
<td>0.4</td>
<td>T^{-1}</td>
<td></td>
</tr>
<tr>
<td>$a_K$</td>
<td>Slope of the relationship between body-size and carrying capacity in a log space</td>
<td>-0.75</td>
<td>L^{-2}L^{-1}</td>
<td>Brown et al 2004</td>
</tr>
<tr>
<td>$b_K$</td>
<td>Intercept of the relationship between body-size and carrying capacity in a log space</td>
<td>10</td>
<td>L^{-2}</td>
<td>Log number of individuals per area</td>
</tr>
<tr>
<td>$I$</td>
<td>Disturbance intensity</td>
<td>0.8</td>
<td>$\phi$</td>
<td>Proportion of punctual abundance reduction</td>
</tr>
<tr>
<td>$T$</td>
<td>Disturbance period</td>
<td>3</td>
<td>T</td>
<td>Time between two disturbances</td>
</tr>
<tr>
<td>dev_I</td>
<td>Deviation from mean intensity defining the interval of the uniform distribution from which variable intensities are drawn</td>
<td>0, 10, 20, 25</td>
<td>%</td>
<td>Percentage</td>
</tr>
<tr>
<td>dev_T</td>
<td>Deviation from mean period defining the interval of the uniform distribution from which variable periods are drawn</td>
<td>0, 25, 50, 100</td>
<td>%</td>
<td>Percentage</td>
</tr>
<tr>
<td>$t_{max}$</td>
<td>Maximum time of the simulations</td>
<td>10,000</td>
<td>T</td>
<td></td>
</tr>
<tr>
<td>$h$</td>
<td>Time step</td>
<td>0.01</td>
<td>T</td>
<td></td>
</tr>
<tr>
<td>$rep$</td>
<td>Number of replicate disturbance sequences</td>
<td>100</td>
<td>$\phi$</td>
<td></td>
</tr>
</tbody>
</table>

Dimensions L and T mean length and time, respectively.
Note: Lower disturbance intensities ($I \in \{0.3,0.5,0.6\}$) and longer periods ($T \in \{5,10,50\}$) have been explored, resulting in lower effects of variability than those shown in Fig. S8
Table S6: Predator-prey model parameters for the simulations showed in Figs. S9-S11.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
<th>Values</th>
<th>Dimension</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>$M$</td>
<td>Prey body-size</td>
<td>10, 30, 100, 300, 1000, 3000, 10000</td>
<td>L</td>
<td></td>
</tr>
<tr>
<td>$a_r$</td>
<td>Slope of the relationship between body-size and growth rate in a log space</td>
<td>-0.25</td>
<td>T$^{-1}$L$^{-1}$</td>
<td>Brown et al 2004</td>
</tr>
<tr>
<td>$b_r$</td>
<td>Intercept of the relationship between body-size and growth rate in a log space</td>
<td>0.4</td>
<td>T$^{-1}$</td>
<td></td>
</tr>
<tr>
<td>$K$</td>
<td>Prey carrying capacity</td>
<td>5000</td>
<td>L$^{-2}$</td>
<td>number of individuals per area</td>
</tr>
<tr>
<td>$a$</td>
<td>Predator attack rate</td>
<td>0.01</td>
<td>T$^{-1}$/L$^{-2}$</td>
<td>attacks per predator (given their abundance per area) and per unit of time</td>
</tr>
<tr>
<td>$m$</td>
<td>Predator mortality rate</td>
<td>0.1</td>
<td>T$^{-1}$</td>
<td>Proportion of predator death per unit of time</td>
</tr>
<tr>
<td>$\epsilon$</td>
<td>Predator conversion efficiency</td>
<td>0.1</td>
<td>$\varnothing$</td>
<td>Proportion of prey caught converted into predator</td>
</tr>
<tr>
<td>$I$</td>
<td>Disturbance intensity (in %)</td>
<td>0, 10, 20, 30, 40, 50, 60, 70, 80, 90, 95</td>
<td>$\varnothing$</td>
<td>Percentage of punctual abundance reduction</td>
</tr>
<tr>
<td>$T$</td>
<td>Disturbance period</td>
<td>0, 2, 3, 4, 5, 8, 10, 20, 100</td>
<td>T</td>
<td>Time between two disturbances</td>
</tr>
</tbody>
</table>

Dimensions L and T mean length and time, respectively.
Table S7: Species information. Species names, taxonomic group, average length (µm), carrying capacity $K$ (individuals/ µl), growth rate $r$ (1/day) and trophic status (bacterivores, autotroph, predators). Species’ traits (mean ± SD) are from Carrara et al. (2012), Haddad et al. (2008) and lab measurements.

<table>
<thead>
<tr>
<th>Species</th>
<th>Taxonomic group</th>
<th>Length (µm)</th>
<th>K (ind/ml)</th>
<th>$r$ (1/d)</th>
<th>Feeding type</th>
</tr>
</thead>
<tbody>
<tr>
<td>Blepharisma sp.,</td>
<td>Ciliate</td>
<td>471.3 ± 57.1</td>
<td>59.5 ± 4.7</td>
<td>0.67 ± 0.07</td>
<td>Bact/predator</td>
</tr>
<tr>
<td>Cephalodella sp.</td>
<td>Rotifer</td>
<td>112.7 ± 11.2</td>
<td>902.8 ± 121.8</td>
<td>0.67 ± 0.11</td>
<td>Bact</td>
</tr>
<tr>
<td>Chilomonas sp.,</td>
<td>Flagellate</td>
<td>23.3 ± 3.7</td>
<td>1572 ± 278.3</td>
<td>0.98 ± 0.13</td>
<td>Bact</td>
</tr>
<tr>
<td>Chlorogonium eucihlorum</td>
<td>Flagellate</td>
<td>30</td>
<td>-</td>
<td>-</td>
<td>Bact/autotroph</td>
</tr>
<tr>
<td>Colpidium sp.,</td>
<td>Ciliate</td>
<td>81 ± 7.8</td>
<td>1379 ± 76.6</td>
<td>1.5 ± 0.08</td>
<td>Bact</td>
</tr>
<tr>
<td>Cyclidium sp.</td>
<td>Ciliate</td>
<td>20</td>
<td>4038</td>
<td>1.51</td>
<td>Bact</td>
</tr>
<tr>
<td>Euglena gracilis</td>
<td>Flagellate</td>
<td>36.7 ± 6.4</td>
<td>84 578</td>
<td>0.87</td>
<td>Bact/autotroph</td>
</tr>
<tr>
<td>Euplotes aediculatus</td>
<td>Ciliate</td>
<td>85.4 ± 8.6</td>
<td>359</td>
<td>0.43</td>
<td>Bact/autotroph</td>
</tr>
<tr>
<td>Loxocephalus sp.</td>
<td>Ciliate</td>
<td>140</td>
<td>-</td>
<td>-</td>
<td>Bact</td>
</tr>
<tr>
<td>Paramecium aurelia</td>
<td>Ciliate</td>
<td>111.6 ± 15.1</td>
<td>111.1 ± 2.6</td>
<td>0.86 ± 0.02</td>
<td>Bact</td>
</tr>
<tr>
<td>Paramecium caudatum</td>
<td>Ciliate</td>
<td>250</td>
<td>-</td>
<td>-</td>
<td>Bact</td>
</tr>
<tr>
<td>Spirostomum sp.</td>
<td>Ciliate</td>
<td>843.8 ± 149.7</td>
<td>13.6 ± 4.2</td>
<td>0.57 ± 0.15</td>
<td>Bact/predator</td>
</tr>
<tr>
<td>Tetrahymena sp.</td>
<td>Ciliate</td>
<td>26.7 ± 4.8</td>
<td>2997 ± 196</td>
<td>2.24 ± 0.15</td>
<td>Bact</td>
</tr>
</tbody>
</table>
6. Supplementary Figures

Figure S1: Critical generation time required for long-term population persistence under different disturbance regimes (equation (2)). Disturbance period is on the x-axis and the lines depict different disturbance intensities (percentage of abundance reduction). As an example, the grey point shows that if a population experiences a recurrent disturbance killing 20% of the population every 30 time units, it has to have a generation time (time needed to double the population) of less than 134 time units to persist.
Figure S2: Effect of disturbance frequency on community size-structure and total biomass for different disturbance intensities: a-b) \( I = 10\% \) c-d) \( I = 30\% \), e-f) \( I = 50\% \), g-h) \( I = 70\% \). See Fig. 5 for \( I = 90\% \). Statistics of the Welch two-sample t-tests for the effect of disturbance regimes on total biomass compared to controls: b) \( I = 10\% \): \( f_{0.08}: t = 3.95, p\text{-value} = 0.004, f_{0.11}: t = -0.62, p\text{-value} = 0.56, f_{0.16}: t = 4.15, p\text{-value} = 0.002, f_{0.33}: t = 0.75, p\text{-value} = 0.48 \). d) \( I = 30\% \): \( f_{0.08}: t = 0.24, p\text{-value} = 0.82, f_{0.11}: t = 1.22, p\text{-value} = 0.26, f_{0.16}: t = 1.7, p\text{-value} = 0.29, f_{0.33}: t = 0.5, p\text{-value} = 0.63 \). f) \( I = 50\% \): \( f_{0.08}: t = 3.74, p\text{-value} = 0.005, f_{0.11}: t = -0.17, p\text{-value} = 0.87, f_{0.16}: t = 1.26, p\text{-value} = 0.26, f_{0.33}: t = 6.15, p\text{-value} < 0.001 \). h) \( I = 70\% \): \( f_{0.08}: t = 3.82, p\text{-value} = 0.004, f_{0.11}: t = 0.12, p\text{-value} = 0.91, f_{0.16}: t = 1.5, p\text{-value} = 0.18, f_{0.33}: t = 12.7, p\text{-value} < 0.001 \). See Table S3 for the significance of each treatment on the size-classes of the community size-structure.
Figure S3: Experimental results: effect of disturbance intensity on community size-structure and total biomass for different disturbance frequencies: a-b) $f = 0.08$, c-d) $f = 0.11$, e-f) $f = 0.16$. See Fig. 5 for $f = 0.33$. Statistics of the Welch two-sample t-tests for the effect of disturbance regimes on total biomass compared to controls: b) $f = 0.08$: $I_{10\%}$: $t = 4$, p-value = 0.004, $I_{30\%}$: $t = 0.2$, p-value = 0.81, $I_{50\%}$: $t = 3.7$, p-value = 0.004, $I_{70\%}$: $t = 3.8$, p-value = 0.004, $I_{90\%}$: $t = 8$, p-value < 0.001. d) $f = 0.11$: $I_{10\%}$: $t = -0.6$, p-value = 0.56, $I_{30\%}$: $t = 1.2$, p-value = 0.25, $I_{50\%}$: $t = -0.17$, p-value = 0.87, $I_{70\%}$: $t = 0.12$, p-value = 0.9, $I_{90\%}$: $t = 8.5$, p-value < 0.001. f) $f = 0.16$: $I_{10\%}$: $t = 4.1$, p-value = 0.001, $I_{30\%}$: $t = 1.17$, p-value = 0.29, $I_{50\%}$: $t = 1.26$, p-value = 0.25, $I_{70\%}$: $t = 1.5$, p-value = 0.18, $I_{90\%}$: $t = 13.2$, p-value < 0.001. See Table S3 for the significance of each treatment on the size-classes of the community size-structure.
Figure S4: Comparison between experimental results and model predictions for different disturbance intensities: a-c) $I = 10\%$, d-f) $I = 30\%$, g-i) $I = 50\%$, j-l) $I = 70\%$. a, d, g, j) Predicted effect of disturbance frequency on the community size-structure of experimental communities. b, e, h, k) Observed effect of disturbance frequency on the community size-structure of experimental communities (similar to Fig. 4a). c, f, i, l) Difference between observed and predicted mean abundance for each size-class.
**Figure S5:** Comparison between experimental results and model predictions for different disturbance frequencies: a-c) $f = 0.33$, d-f) $f = 0.16$, g-i) $f = 0.11$, j-l) $f = 0.08$. a, d, g, j) Predicted effect of disturbance intensity on the community size-structure of experimental communities. b, e, h, k) Observed effect of disturbance intensity on the community size-structure of experimental communities (similar to Fig. 4a). c, f, i, l) Difference between observed and predicted mean abundance for each size-class.
Figure S6: Effect of intensity and period variability on size-abundance pyramids.
Community size-structure at dynamical steady state with no disturbance (dotted lines) or disturbances of period 3 (f=0.33) and intensity 80% of abundance reduction, either regular (black lines) or variable (red lines). Red lines give the 95% confidence intervals from one hundred disturbance sequences affecting the same 1000 co-occurring species community during about 10,000-time units. For each disturbance, period and intensity are randomly drawn from uniform distributions in intervals 3±X% and 0.8±Y%, respectively, with X ∈ {0, 25, 50, 100} and Y ∈ {0, 10, 20, 25}. Effects decrease for lower intensities and longer periods (not shown).
Figure S7: Size-structure response to varying slopes and intercepts of the allometric relationship between population growth rate, \( r \), and body-size, \( M \) (equation (12)).

a–c) Variation of the slope of the relationship, \( a_r \) (different greys), with the intercept sets to \( b_r = 0.4 \).

d–f) Variation of the intercept of the relationship, \( b_r \) (different greens), with the slope sets to \( a_r = -0.25 \).

a,d) No disturbances.

b–e) Small disturbance regime with intensity \( I = 30\% \) and frequency \( f = 0.05 \) (in the same time units than growth rates).

c–f) Stronger disturbance regime with intensity \( I = 50\% \) and frequency \( f = 0.2 \). Dotted lines in middle and right panels show the size-structure without disturbance (left panels) for comparison. Results are obtained from equation (5).
Figure S8: Size-structure response to varying slope and intercept of the allometric relationship between population carrying capacity, $K$, and body-size, $M$ (equation (13)). a–c) Variation of the slope of the relationship, $a_K$ (different greys), with the intercept sets to $b_K = 10$. d–f) Variation of the intercept of the relationship, $b_K$ (different greens), with the slopes sets to $b_K = -0.75$. a,d) No disturbances. b,e) Moderate disturbance regime with intensity $I = 40\%$ and frequency $f = 0.1$ (in the same time units than growth rates). c,f) Stronger disturbance regime with intensity $I = 70\%$ and frequency $f = 0.25$. Dotted lines in panels b, c, e, and f show the size-structure without disturbance (left panels) for comparison. Results are obtained from equation (5).
Figure S9: Equilibria for varying disturbance frequency, intensity, and prey size.
Mean abundances at dynamical equilibrium of a Lotka-Volterra predator-prey model submitted to recurrent disturbances of increasing frequencies (x-axis) and intensities (% of punctual abundance reduction in rows), and for different prey sizes (columns). Prey growth rate, $r$, depends on the body-size, $M$: $r = e^{-0.25 \times \ln(M) + 0.5}$. Other parameters are set to: $K = 5000$, $\varepsilon = 0.1$, $a = 0.01$, and $m = 0.1$ (see Table S6). Black circles denote cases without disturbances.
Figure S10: Equilibria for varying disturbance intensity, frequency and prey sizes.
Mean abundances at dynamical equilibrium of a Lotka-Volterra predator-prey model submitted to recurrent disturbances of increasing intensities (x-axis; % of punctual abundance reduction), and frequencies (rows), and for different prey sizes (columns). Prey growth rate, \( r \), depends on the body-size, \( M \): \( r = e^{-0.25 \times \ln(M) + 0.5} \). Other parameters are set to: \( K = 5000 \), \( \varepsilon = 0.1 \), \( a = 0.01 \), and \( m = 0.1 \) (see Table S6). Black circles denote cases without disturbances.
Figure S11: Equilibria for varying prey sizes and disturbance regimes.
Mean abundances at dynamical equilibrium of a Lotka-Volterra predator-prey model submitted to recurrent disturbances, with increasing prey sizes (x-axis) and for different disturbance intensities (columns; % of punctual abundance reduction) and frequencies (rows). Prey growth rate, $r$, depends on the body-size, $M$: $r = e^{-0.25 \times ln(M) + 0.5}$. Other parameters are set to: $K = 5000$, $\varepsilon = 0.1$, $a = 0.01$, and $m = 0.1$ (see Table S6). Black circles denote cases without disturbances.
7. Supplementary References


