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M. Vals, A. Spiga, F. Forget, E. Millour, L. Montabone, et al.. Study of gravity waves distribution and propagation in the thermosphere of Mars based on MGS, ODY, MRO and MAVEN density measurements. Planetary and Space Science, 2019, 178, pp.104708. 10.1016/j.pss.2019.104708 . hal-02967848

HAL Id: hal-02967848 https://hal.sorbonne-universite.fr/hal-02967848v1

Submitted on 15 Oct 2020 $\,$

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Study of gravity waves distribution and propagation in the thermosphere of Mars based on MGS, ODY, MRO and MAVEN density measurements

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9	Key Points:
10	• Gravity wave activity causes density perturbations in the Martian thermosphere.
11	• MAVEN found a correlation between gravity wave activity and inverse background
12	temperature.
13	• Lower-altitude aerobraking measurements do not show this correlation, except for
14	Mars Odyssey.
15	Aerobraking data and climate models suggest instead wave activity correlated with
16	static stability.
17	• No such correlation in low latitudes points to a mix of saturation, critical levels and

¹⁸ Sources.

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19 Abstract

20	By measuring the regular oscillations of the density of CO_2 in the upper atmosphere (be-
21	tween 120 and 190 km), the mass spectrometer MAVEN/NGIMS (Atmosphere and Volatile
22	EvolutioN/Neutral Gas Ion Mass Spectrometer) reveals the local impact of gravity waves.
23	This yields precious information on the activity of gravity waves and the atmospheric condi-
24	tions in which they propagate and break. The intensity of gravity waves measured by MAVEN
25	in the upper atmosphere has been shown to be dictated by saturation processes in isothermal
26	conditions. As a result, gravity waves activity is correlated to the evolution of the inverse of
27	the background temperature. Previous data gathered at lower altitudes (~95 to ~150 km)
28	during aerobraking by the accelerometers on board MGS (Mars Global Surveyor), ODY
29	(Mars Odyssey) and MRO (Mars Reconnaissance Orbiter) are analyzed in the light of those
30	recent findings with MAVEN. The anti-correlation between GW-induced density perturba-
31	tions and background temperature is plausibly found in the ODY data acquired in the polar
32	regions, but not in the MGS and MRO data. MRO data in polar regions exhibit a correlation
33	between the density perturbations and the Brunt-Väisälä frequency (or, equivalently, static
34	stability), obtained from Global Climate Modeling compiled in the Mars Climate Database.
35	At lower altitude levels (between 100 and 120 km), although wave saturation might still be
36	dominant, isothermal conditions are no longer verified. In this case, theory predicts that the
37	intensity of gravity waves is no more correlated to background temperature, but to static sta-
38	bility. At other latitudes in the three aerobraking datasets, the GW-induced relative density
39	perturbations are correlated with neither inverse temperature nor static stability; in this par-
40	ticular case, this means that the observed activity of gravity waves is not only controlled by
41	saturation, but also by the effects of gravity-wave sources and wind filtering through critical
42	levels. This result highlights the exceptional nature of MAVEN/NGIMS observations which
43	combine both isothermal and saturated conditions contrary to aerobraking measurements.

44 **1 Introduction**

Gravity waves propagate as perturbations of the stratified atmospheric fluid [*Gossard and Hooke*, 1975], with the buoyancy force being the restoring mechanism giving rise to the waves [cf *Fritts and Alexander*, 2003; *Alexander et al.*, 2010, for a review]. While being essentially regional-scale phenomena, gravity waves can be responsible for significant dynamical and thermal forcing of the global atmospheric state, as they transfer their momentum and

-2-

energy upon their saturation and breaking in the upper atmosphere [*Lindzen*, 1981; *Palmer et al.*, 1986; *McFarlane*, 1987].

Gravity waves are ubiquitous in the Martian atmosphere and were actually one of the 52 first atmospheric phenomenon to be witnessed by orbiting spacecraft [Briggs and Leovy, 53 1974]. As is the case on Earth [O'sullivan and Dunkerton, 1995; Vincent and Alexander, 54 2000; Plougonven et al., 2003; Spiga et al., 2008], those waves may be triggered in the Mar-55 tian lower atmosphere by different sources: topography [Pickersgill and Hunt, 1979, 1981], 56 convection [Spiga et al., 2013; Imamura et al., 2016], or jet-streams and fronts in ageostrophic 57 evolution. Amongst all those sources, only the impact of the topographic source on the global 58 circulation is accounted for in all Martian Global Climate Models [GCM, e.g. Barnes, 1990; 59 Collins et al., 1997; Forget et al., 1999; Hartogh et al., 2005], although the exploration of the 60 impact of an additional non-orographic source is a topic of current active research [Medvedev 61 et al., 2015; Gilli et al., 2018]. 62

The upward propagation of gravity waves from their tropospheric sources to the up-63 per atmosphere leads to large departures of density, temperature and winds in the thermo-64 sphere, owing to the exponential increase of gravity wave amplitude with height [Fritts and 65 Alexander, 2003; Parish et al., 2009]. Measurements of CO2 density through accelerome-66 ters, gathered during the aerobraking of Mars Global Surveyor (MGS), Mars Odyssey (ODY) 67 and Mars Reconnaissance Orbiter (MRO) observed the sustained gravity wave activity in 68 the Martian thermosphere between 90 and 130 km [Fritts et al., 2006; Creasey et al., 2006; 69 Tolson et al., 2007b]. Those measurements also demonstrated the large variability of the 70 gravity-wave amplitudes with season, local time, latitude and longitude. 71

The Mars Atmosphere and Volatile Evolution (MAVEN) mission to Mars [*Jakosky et al.*, 2015], operating since 2014, is dedicated to studying the upper atmosphere of Mars and, as such, is a unique opportunity to broaden the knowledge of gravity wave activity on Mars. The mass spectrometer NGIMS (Neutral Gas Ion Mass Spectrometer) on board MAVEN [*Mahaffy et al.*, 2015] recently delivered new and more accurate measurements of density fluctuations at upper altitudes between 120 and 300 km, identified as typical gravity-wave signatures [*Yiğit et al.*, 2015; *England et al.*, 2017].

Based on those MAVEN/NGIMS measurements, *Terada et al.* [2017] observed that
 gravity-wave amplitudes derived from Ar density with wavelengths between ~100 and ~500 km
 near the exobase in the Martian thermosphere are anti-correlated with the background tem-

-3-

perature. The authors demonstrated this anti-correlation by considering gravity waves saturation caused by convective instability in the upper thermosphere. These observations were further discussed in a recent study focusing on Ar density between 120 and 200 km by *Siddle et al.* [2019], who observed that gravity waves amplitudes also increase with increasing solar zenith angle.

The goal of this paper is to build on those recent findings by MAVEN and to expand 87 this analysis by comparing all available aerobraking data from other orbiting spacecraft. In 88 particular, we explore the saturation conditions of gravity waves in a lower part of the ther-89 mosphere (between 90 and 130 km) than the one observed by MAVEN (between 120 and 90 300 km). Thus, we obtain a broader dataset of the variability of gravity wave activity with 91 altitude, latitude and season. This allows us to compare the available measurements with di-92 agnostics obtained by GCM through the Mars Climate Database [MCD Lewis et al., 1999; 93 Forget et al., 1999; Millour et al., 2015] 94

This paper is organized as follows. In section 2, we provide information on the datasets. Section 3 features a discussion of the MAVEN/NGIMS measurements, while section 4 features a comparative discussion of the aerobraking datasets. We conclude in section 5.

2 Data and Method

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2.1 Datasets used in this study

During aerobraking operations in the Martian thermosphere, the accelerometers of MGS, ODY and MRO [*Lyons et al.*, 1999; *Smith and Bell*, 2005; *Tolson et al.*, 2008] acquired data during 850 passes for MRO (since September 1997, Martian Year [MY] 23) [*Keating et al.*, 2002], 320 passes for ODY (since October 2001, MY 25) [*Tolson et al.*, 2007a], and 430 passes for MGS (from April to August 2006, MY 28) [*Tolson*, 2007], covering latitude ranges from 60°N to 90°S for MGS, 30°N to 90°N for ODY, and 0° to 90°S for MRO. Periapsis altitudes varied from about 95 km to 150 km (see Figures 1 and 2).

In addition to those aerobraking datasets, the CO₂ density variations from 3124 orbits are available from MAVEN/NGIMS mass spectrometer data reported in the NASA Planetary Data System from October 2014 (MY32) to February 2017 (MY33) [*Benna and Lyness*, 2014]. Considering the NGIMS settings were changed to a new operating mode starting from February 2015, as mentioned in *England et al.* [2017] and *Terada et al.* [2017], we chose to focus on datasets from February 2015 to February 2017. The instrument is still in

-4-

- operation at the time of writing and the present study can be complemented in the future
- by an analysis of the interannual variability. The MAVEN observations cover (high periap-
- sis) altitude ranges between ~120 km and ~190 km, and have large latitudinal coverage, as
- shown in Figure 1 and Figure 2.



Figure 1. Vertical (km) and seasonal (Solar Longitude in degrees) coverage of Mars Global Surveyor
 (MGS), Mars Odyssey (ODY), Mars Reconnaissance Orbiter (MRO) and MAVEN (MVN) spacecrafts, each
 dot corresponds to the periapsis location of one orbit

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2.2 Computing the amplitude of gravity wave perturbations

Along each orbit trajectory, we extract the longitudes, latitudes, solar longitudes (L_s , 124 which is the position of the planet on its orbit, defined as an angle from a reference posi-125 tion, corresponding by convention to the northern spring equinox), local times, altitudes, 126 CO_2 density measurements, as well as the elapsed time from the periapsis. The geodesic 127 distance from the periapsis is calculated from the latitude and longitude displacements. A 128 relative density perturbation $\delta \rho_r$ is obtained by subtracting the mean density ρ_m [considered 129 here to be a 40-second rolling averaged density, as in Tolson et al., 1999, 2005, 2007b, 2008; 130 *Creasey et al.*, 2006] from the instantaneous density ρ_i , and by normalizing with the mean 131 density 132

$$\delta\rho_r = \frac{\rho_i - \rho_m}{\rho_m} \tag{1}$$



Figure 2. Latitudinal (degrees) and seasonal (Solar Longitude in degrees) coverage of Mars Global Surveyor (MGS), Mars Odyssey (ODY), Mars Reconnaissance Orbiter (MRO) and MAVEN (MVN) spacecrafts, each dot corresponds to the periapsis location of one orbit

Typical examples of orbit trajectory, absolute and relative density variations, obtained for the MGS orbit 1046 and for the MAVEN orbit 3641 are shown in Figure 3. Considering the relative density perturbations, rather than the absolute value, enables a direct diagnostic of the effect of gravity waves, with the underlying assumption that the 40-second average provides an acceptable estimate of the "background" atmospheric state upon which the gravity waves propagate.

In order to quantify the amplitude (i.e. the intensity) of the observed gravity waves on a single orbit, and to assess the spatial and seasonal variability of the gravity wave activity, we calculate for each orbit the Root Mean Square (RMS) of the fluctuations of relative densities $\delta \rho_r$ along the trajectory.

Figure 4 (MAVEN/NGIMS data) and Figure 5 (aerobraking data) show the seasonal variations of the GW activity as quantified by this RMS quantity, i.e. the RMS as a function of the L_s , all other parameters (longitudes, latitudes, local times, altitudes) confounded. A distinctive pattern of amplitude fluctuations with season is found in the MAVEN data in Figure 4, in agreement with the tendencies discussed in *Terada et al.* [2017].



Figure 3. Left: example of orbit 1046 from MGS, Right: example of orbit 3641 from MAVEN. From Left to Right: orbit's trajectory characterized by the displacement in altitude along the distance from periapsis in km; Density variations in kg km⁻³ in function of the distance from periapsis in km ; Relative density variation in function of the distance from periapsis in km.

2.3 Temperature estimates

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The background temperature *T* is estimated at each point of each orbit with the ideal gas law and the hydrostatic equilibrium, as a function of the mean density of CO₂ ρ and the



Figure 4. Seasonal variability of GWs amplitudes measured by MAVEN/NGIMS. Each point corresponds to the RMS of the relative densities calculated over each orbit. In this figure the RMS has been calculated on the points around the periapsis, where the trajectory is close to be horizontal, at distances from the periapsis comprised between -700 and 700 km. This restriction reduces the altitude range to around 15 km above the periapsis. Data gathered from Martian Year (MY) 32 are in red, and data from MY33 in blue.

165 altitude z as follows:

$$\int \frac{\partial \rho}{\rho} = -\frac{g}{R_{CO_2}T} \int \partial z \tag{2}$$

with g the gravitational acceleration and R_{CO_2} the ideal gas constant of CO₂.

- ¹⁶⁷ We split the orbit in three parts.
- The middle leg is the part of the orbit track close to the periapsis, where the displacement is almost horizontal, the density almost constant, and, consequently, where the temperature can no longer be deduced from equation 2. We arbitrarily define this middle leg as containing the points for which the ratio between the mean density and the maximal density is greater than 10%.
 The is lease black are servered to the period all the fearly the server is a local data.
- 2. The inbound leg corresponds to the points located "before" the perapsis not included
 in the middle leg.
- 3. The outbound leg refers to the points located "after" the periapsis not included in the
 middle leg.



Figure 5. Seasonal variability of GWs amplitudes measured by aerobraking instruments MGS, ODY and MRO. Each point corresponds to the RMS of the relative densities calculated over each orbit. In this figure the RMS has been calculated on the points around the periapsis, where the trajectory is close to be horizontal, at distances from the periapsis comprised between -400 and 400 km. Beyond these distances the aerobraking data become very noisy. This restriction reduces the altitude range to around 10 km above the periapsis.

Thus the middle leg of the measurements is excluded from the comparative analysis, and we only keep the inbound and outbound profiles for all aerobrakings and MAVEN/NGIMS measurements.

We found that in the inbound and outbound legs, the temperature profiles follow a sim-180 ilar vertical gradient. We thus study the variability of temperature from one orbit to another 181 with a single representative value for both the inbound and outbound legs, chosen as the aver-182 age value on each leg. Those temperatures estimated from aerobraking and MAVEN/NGIMS 183 measurements are compared in Figure 6 and Figure 7 with the temperature in the Mars Cli-184 mate Database [built from Global Climate Model (GCM) simulations Millour et al., 2015] 185 for the same spatio-temporal coordinates (L_s , longitude, latitude, altitude, local time). Only 186 the comparisons of temperatures measured on outbound legs versus temperature modeled in 187 the MCD are displayed for the sake of brevity; the analysis for inbound legs is similar. The 188 MCD temperatures are systematically lower than those observed by MAVEN and aerobrak-189 ing, and there is also much more variability in the observation data points; however, the over-190 all seasonal variability is well reproduced, except the $L_s = 290^\circ$ maximum observed by ODY. 191



Figure 6. Mean background temperature estimated over the outbound leg and calculated from the CO₂ density observations (blue dots) and estimated with the MCD (red dots) as a function of Solar Longitude; from the upper to the lower : MGS, ODY and MRO

This gives us confidence that using a value of background temperature averaged over the in bound and outbound legs is suitable to carry out an analysis of the seasonal (climatological)
 trends.

3 Vertical Propagation of Gravity Waves: analysis of the MAVEN observations in the thermosphere

In the absence of additional wave sources and dissipation processes [e.g., radiative damping *Eckermann et al.*, 2011], the amplitude of gravity waves is expected to grow exponentially with altitude as the atmospheric density decreases. Conversely, the amplitudes of gravity waves appear to anti-correlate with altitude, according to the altitudes of the MAVEN measurements shown in Figure 1 and the amplitudes $\delta\rho$ of the perturbations shown in Fig-

-10-



Figure 7. Mean background temperature estimated over the outbound leg and calculated from the CO₂
 density observations of NGIMS instrument (blue dots) and estimated with the MCD (red dots) as a function of
 Solar Longitude

ure 4. In other words, in the MAVEN observations, gravity-wave amplitude seems to corre-208 late with density, as opposed to an anti-correlation expected if the amplification of gravity-209 wave amplitude with altitude (and reduced density) was the only controlling factor. This is 210 confirmed by considering the seasonal variations of density perturbations $\delta \rho$ at a constant 211 pressure level, e.g. at pressures $4 \times 10^{-8} < P < 6 \times 10^{-8}$ Pa (corresponding to altitudes 212 between ~160 and ~240 km) in Figure 8. The observed variability in gravity-wave amplitude 213 must be controlled by either the sources of those waves and/or the impact of saturation and 214 critical levels. 215

In the MAVEN measurements, gravity wave activity in the thermosphere is randomly distributed with longitude and latitude (figures not shown). No correlation appears to exist between this gravity wave activity and either the position of topographical highs and lows (mountains and craters), or the position of mesospheric jet-streams. This suggests that the regional distribution of the intensity of gravity waves is more controlled by propagation effects [e.g., filtering by saturation or critical levels, *Fritts and Alexander*, 2003] than by the distribution of the sources triggering those waves.



Figure 8. Upper: Vertical (km) and seasonal (Solar Longitude in degrees) coverage of MAVEN (MVN) spacecraft, each dot corresponds to the periapsis location of one orbit. Down: Seasonal variability of GWs amplitudes measured by MAVEN/NGIMS at a constant pressure level P such as $4 \times 10^{-8} < P < 6 \times 10^{-8}$ Pa. Each point corresponds to the RMS of the relative densities calculated over each orbit. Data gathered from Martian Year (MY) 32 are in red, and data from MY33 in blue.

The background horizontal wind plays a particularly crucial role in impacting the conditions for the upward propagation of gravity waves emitted in the troposphere. A critical level occurs when and where the background horizontal wind velocity \bar{u} almost equals the gravity wave phase speed *c* [first Eliassen-Palm theorem, *Lindzen*, 1981]. A gravity wave that reaches a critical level can no longer propagate towards the thermosphere: hence hor izontal circulations may filter out gravity waves emitted in the troposphere from the meso sphere and the thermosphere.

Considering, for the sake of simplicity, a gravity-wave phase speed c = 0 (typical of 235 orographic gravity waves), we explored the regional and seasonal variability of background 236 horizontal winds \bar{u} simulated in the MCD from the troposphere to the lower mesosphere 237 (since no measurements of such winds are available). We found no correlation between this 238 variability, and the regional and seasonal variability of the gravity wave amplitudes observed 239 by MAVEN (not shown). While the modeled winds have not been validated and may differ 240 from reality, there is no reason to explain the variability of the observed gravity wave ampli-241 tudes solely with the occurrence of critical levels. 242

It follows from the above discussions that the most likely possibility to explain the observed variability of gravity wave amplitude in the MAVEN observations is the breaking/saturation due to convective instability. This shall lead to, according to *Terada et al.* [2017], the gravity wave amplitudes to be inversely proportional to the background temperature. Let us propose an alternate, yet equivalent, derivation of the theoretical arguments in *Terada et al.* [2017] that we will use in section 4.

The saturation of a gravity wave occurs as soon as it encounters convective instability [*Lindzen*, 1981; *Hauchecorne et al.*, 1987; *Terada et al.*, 2017]. Local mixing occurs as the gravity wave breaks, inducing an adiabatic (neutral) temperature lapse rate. We consider the case of a medium-frequency gravity wave $f \ll \omega \ll N$, where f, ω and N are respectively the Coriolis, the gravity-wave and the Brunt-Väisälä frequencies, with N such that

$$N^2 = \frac{g}{T} \left[\frac{\partial T}{\partial z} + \frac{g}{C_p} \right]$$

assuming the short-wavelength approximation $2 H k_z \gg 1$, where k_z is the vertical wave number. Which are reasonable assumptions for most gravity waves observed in planetary upper atmospheres [*Fritts and Alexander*, 2003]. In those conditions, according to *Hauchecorne et al.* [1987], the saturated conditions lead to

$$k_z \theta'_s = \frac{N^2 \bar{\theta}}{g} \implies \frac{\theta'_s}{\theta} = \frac{N^2}{gk_z}$$
 (3)

where θ'_s is the amplitude of the wave at saturation (expressed in perturbations of potential temperature), $\bar{\theta}$ the background potential temperature and *g* the acceleration of gravity. Besides, the linearized fluid equations applied to the propagation of gravity waves [*Fritts and*

Alexander, 2003] lead to:

$$\frac{\theta'}{\bar{\theta}} = \frac{1}{c_s^2} \frac{P'}{\bar{\rho}} - \frac{\rho'}{\bar{\rho}} \tag{4}$$

- where ρ is the density, P' and ρ' the pressure and density perturbations, and c_s the sound
- speed. We can neglect the compressibility term related to the background density gradient,
- which is equivalent to filter out acoustic gravity waves $(c_s \rightarrow \infty)$. This entails:

$$\left|\frac{\rho'}{\bar{\rho}}\right| = \left|\frac{\theta'}{\bar{\theta}}\right| \tag{5}$$

- ²⁶⁵ Combining equations 3 and 5, we obtain the equation expressing the relative density pertur-
- ²⁶⁶ bations by gravity waves:

$$\delta \rho = \frac{|\rho'|}{\bar{\rho}} = \frac{N^2}{k_z g} \tag{6}$$

which corresponds to the observed diagnostic described in equation 1. Isothermal background profiles $T = T_0$ are often observed in the Martian thermosphere, where EUV heating is offset by molecular conduction [*Bougher et al.*, 1990]. In the specific case of isothermal profiles, N^2 can be reduced to:

$$N^{2} = \frac{g}{\bar{\theta}} \frac{\mathrm{d}\bar{\theta}}{\mathrm{d}z} = \frac{g^{2}}{C_{p}T_{0}}$$
(7)

which yields the "inverse temperature" dependency [*Terada et al.*, 2017] in the case of isothermal profiles at saturation:

$$\delta \rho = \frac{|\rho'|}{\bar{\rho}} = \frac{g}{k_z C_p} \frac{1}{T_0}$$
(8)

MAVEN data are acquired high in the Martian thermosphere (above 150 km) even 273 for deep dip acquisitions: hence the temperature profiles retrieved by MAVEN are approx-274 imately isothermal [England et al., 2017; Terada et al., 2017]. The temperature profiles mod-275 eled and compiled in the MCD also indicate widespread isothermal profiles at the altitudes 276 probed by MAVEN. Comparing Figures 4 and 9 confirms qualitatively equation 8, i.e. the 277 correlation between the amplitude of gravity wave perturbations and the inverse background 278 temperature. Quantitatively, in the case of the inbound leg of each orbit, a correlation coeffi-279 cient $R \simeq 0.70$ between the average of the relative density and the calculated temperature is 280 found (see Figure 10). Our analysis of the MAVEN is thus compliant with the one conducted 281 by Terada et al. [2017], and we now turn to the analysis of aerobraking data in the lower ther-282 mosphere. 283



Figure 9. Seasonal variability of the background temperature estimated from MAVEN/NGIMS density measurements (ideal gas law and hydrostatic equilibrium). Each point corresponds to the inverse of the mean background temperature calculated over the outbound leg of each orbit. Data gathered from Martian Year (MY) 32 are in red, and data from MY33 in blue.



Figure 10. Correlation between the average of the absolute relative density and the average of the background temperature calculated for MAVEN/NGIMS data over the inbound leg of each orbit. Temperature is obtained from the density observations by means of the ideal gas law and the hydrostatic equilibrium

4 Gravity Waves in the Lower Thermosphere: Aerobraking Data

292 4.1 Analysis

Aerobraking data have been studied in the past to observe the activity of gravity waves in the lower thermosphere, either to discuss the variability of potential sources [*Creasey et al.*, 2006] or to assess wave filtering by zonal jets and how large-amplitude GWs could penetrate to high altitudes [*Fritts et al.*, 2006]. Here we assess if the "inverse temperature" correlation inferred from the MAVEN/NGIMS data [*Terada et al.*, 2017, and section 3 of this paper] can be extended to those lower-thermosphere aerobraking observations obtained by the three accelerometers of MGS, ODY and MRO.

In the aerobraking observations, as is emphasized by Tolson et al. [2005] and Tolson 300 et al. [2008], the intensity of density perturbations are systematically lower when the space-301 craft enters the polar vortex (e.g. MRO during the southern hemisphere winter and ODY dur-302 ing the northern hemisphere winter). Figure 11 shows two examples: ODY orbit 155, which 303 goes through the northern hemisphere winter vortex at $Ls = 298.30^{\circ}$ and latitude 82.43°N, 304 and MRO orbit 250, going through the southern hemisphere winter vortex at $Ls = 90.01^{\circ}$ 305 and latitude=69.50°S. These variations of density perturbations within the same orbital track 306 could be explained by the anti-correlation between temperature and gravity wave activity ex-307 plained above [an explanation that was not provided in *Tolson et al.*, 2008]. Polar warming 308 at thermospheric altitudes [first observed by ODY during aerobraking, *Keating et al.*, 2003] 309 results from the adiabatic heating generated by the subsidence of air over the winter pole pro-310 duced by strong interhemispheric transport [González-Galindo et al., 2009]. The entry of 311 the spacecraft inside the polar vortex is then expected to be associated with an increase of 312 temperature, leading to a decrease of gravity wave activity according to equation 8. 313

In Figures 12 and 13, the observed RMS of the relative density variations is compared to the inverse of the background temperature, calculated for each orbit of each instrument over the outbound leg (for the sake of brevity, similar results over the inbound leg are not shown). Latitudinal and seasonal variability are displayed respectively in Figures 12 and 13.

The amplitude of gravity waves present similar features with the inverse of temperature in the MGS observations, with an amplitude increase at latitudes 60°S, 50°N and particularly at 20°S, where inverse temperature is higher in Figure 12, corresponding to $L_s \sim 70^\circ$ in Figure 13. The anti-correlation seems easier to identify in ODY data, in particular at polar latitudes

-16-



Figure 11. Examples of orbit 155 of ODY and orbit 250 of MRO. Density variations in kg km⁻³ in function of the distance from periapsis in km

324	around $80^\circ\text{N},$ where a clear decrease of GWs amplitude is correlated with the polar warming
325	(see previous paragraph). Conversely, no obvious correlation between density perturbations
326	and inverse temperature is found in the MRO aerobraking data: there is an increase in grav-
327	ity waves activity from latitude -90° to -70°, while the tendency for inverse temperature is
328	unclear, corresponding to $L_s \sim 35^\circ$ in Figure 13. Furthermore, the gravity waves activity de-
329	creases at $L_s \sim 95^\circ$, corresponding to a latitude of -20° , whereas it is not the case for inverse
330	temperature. Correlations have been calculated for the three instruments between the grav-
331	ity waves amplitude and inverse temperature as done for MAVEN in Figure 10, but for all of
332	them the correlation coefficient R remains below 0.5. The largest correlation coefficient is
333	obtained for ODY ($R = 0.48$), whereas it is around 0.2 for the two other datasets.

4.2 Discussion

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The correlation between density perturbations, caused by gravity waves, and the in-342 verse background temperature, suggested by equation 8, appears to be observed by MAVEN/NGIMS. 343 A similar correlation, albeit less clear-cut than with the MAVEN/NGIMS dataset, is also 344 noticed during ODY aerobraking phases at high latitudes. This correlation seems to be ob-345 served at certain locations for MGS, as seen in the previous section, and also in particular 346 cases for MRO, as seen in the previous section for the orbits located in the polar warming. 347 However, for those two spacecrafts, the correlation is not clear at all in the global analysis of 348 the complete datasets. 349



Figure 12. From the upper to the lower: MGS, ODY, MRO. From the left to the right: RMS of the relative density calculated over the outbound leg according to the latitude of the orbit's periapsis, inverse of the mean background temperature calculated from the observations over the outbound leg according to the latitude of the orbit's periapsis

The aerobraking density measurements correspond to periapsis conditions at lower altitudes than the MAVEN/NGIMS measurements (cf. Figure 1). There, the assumption of isothermal profiles could not be valid. Indeed, in Figure 14 we compare the temperature gradients calculated with the MCD for the three aerobraking missions along with MAVEN/NGIMS. The Figure shows that MAVEN/NGIMS data mainly correspond to isothermal profiles, whereas the three other instruments present larger temperature gradients. Yet, equation 8 is only effective in isothermal conditions. As a matter of fact, we observe in the ODY data that a po-

-18-



Figure 13. From the upper to the lower: MGS, ODY, MRO. From the left to the right: RMS of the relative density calculated over the outbound leg according to L_s , inverse of the mean background temperature calculated from the observations over the outbound leg according to L_s

tential correlation between gravity wave activity and inverse temperature only appears where 357 the temperature gradient is the lowest, at higher latitudes. This is also possibly the case for 358 MGS at the points located around latitudes -60° and -20°. However, MRO, which presents 359 the lowest temperature gradient, presents no clear correlation with the inverse temperature. 360 There could be an explanation for the temperature gradient being lower for ODY and MRO, 361 despite the fact they are lower in altitude: at polar latitudes, the polar warming shifts the 362 threshold for isothermal conditions to lower altitudes in the mesosphere. Furthermore, when 363 the temperature gradient is significant, the more general equation 6 shall prevail instead of 364

-19-



Figure 14. Upper: Absolute value of the mean temperature gradient along the latitude calculated with the MCD over the outbound leg of each orbit of the different aerobraking instruments and MAVEN/NGIMS. Down: Absolute value of the mean temperature gradient along the L_s calculated with the MCD over the outbound leg of each orbit of the different aerobraking instruments and MAVEN/NGIMS.

equation 8, which means that the amplitude of gravity waves is proportional to the static stability N^2 rather than the inverse background temperature.

The possible correlation with static stability N^2 can be tested with the MCD in the conditions that were met by the aerobraking measurements. Figure 15 displays the comparison between the RMS of the relative density acquired at the different aerobraking orbits and the



Figure 15. From the upper to the lower: MGS, ODY, MRO. Left : RMS of the relative density calculated over the outbound leg of each orbit of aerobraking data according to the latitude of the orbit's periapsis ; Right : Mean static stability N^2 calculated over the outbound leg of each orbit of aerobraking data according to the latitude of the orbit's periapsis, N^2 has been calculated by means of the Mars Climate Database (MCD) at the different orbital characteristics and with the corresponding dedicated MCD dust scenarios of Mars Year (MY) 25 (MCD detailed document, *Montabone et al.* [2015])

- static stability calculated from the MCD (for the corresponding orbital spatio-temporal co-
- ordinates). We observe the same peak of gravity waves activity and static stability for MGS
- $_{376}$ at latitude -20° and in the North pole, but not for the other latitudes. A good correlation be-
- tween the GWs activity and the static stability, as with the inverse temperature, can be found
- for ODY. Regarding MRO, the static stability N^2 correlates well to the observed amplitude of
- gravity waves in high-latitude regions (latitudes above -50° S), but such a correlation is not
- ³⁸⁰ found at lower latitudes.

There might be multiple reasons for aerobraking measurements not following equa-387 tion 6 in the low and mid latitudes. Firstly, while no correlation was found with potential 388 sources of gravity wave, it is still possible that outside the polar regions, propagation effects 389 would compete with the regional variability of gravity-wave sources. Secondly, following 390 a similar argument, the filtering by critical levels was ruled out for a lack of clear tendency, 391 but might be of peculiar importance for specific regions [see Spiga et al., 2012]. Thirdly, 392 the regional variability of vertical wavelength k_z , a parameter found in equations 6 and 8, in 303 principle could impact density perturbations [Smith et al., 1987], which then would be less 394 clearly correlated to static stability N^2 . 395

5 Conclusion

We have studied the seasonal and regional variability of density perturbations, putatively caused by the propagation of gravity waves in the thermosphere, in different sets of data issued from the aerobraking phases of MGS, ODY and MRO (accelerometers) and the observations of the NGIMS instrument on board MAVEN. The modeling compiled in the Mars Climate Database has been used to complement background atmospheric conditions obtained by observations. Our conclusions are as follows:

- The correlation found in the MAVEN observations by *Terada et al.* [2017] between
 the inverse background temperature and the density perturbations reasonably extends
 to the ODY aerobraking measurements, but not to the MGS and MRO aerobraking
 measurements. This result emphasizes the exceptional nature of MAVEN datasets,
 which combine both isothermal and saturated conditions (equation 8). The seasonal
 variability of inverse background temperature measured by MAVEN is reproduced in
 the Mars Climate Database.
- 2. In comparison to MAVEN/NGIMS measurements, MGS, ODY and MRO aerobrak-410 ing data cover a lower layer in the thermosphere, where the Mars Climate Database 411 predicts non-isothermal conditions. In these conditions, and under the hypothesis of 412 saturation, a correlation between the gravity waves perturbation with the static stabil-413 ity is expected (equation 6). A correlation of density perturbations monitored both 414 by ODY and MRO during aerobraking in polar regions with static stability N^2 is ob-415 served and indicates that wave saturation might be still dominant, but the isothermal 416 conditions are no longer verified (equation 6). 417

-22-

- The spatial variability of gravity-wave-induced density perturbations are difficult to
 explain for the global MGS dataset and in lower latitudes for ODY and MRO aero braking, where no clear correlation with neither inverse temperature nor static sta bility is found. The effects of gravity-wave sources, or wind filtering effects through
 critical levels, were ruled out as explanations for most of the measured variability, yet
 might play a stronger role in the low-to-mid latitudes.
- Future studies will employ measurements during the aerobraking phase of the ExoMars Trace Gas Orbiter, as well as new measurements by MAVEN, to confirm the conclusions drawn in this study and the existing literature. Broadening the knowledge of gravity wave activity in the mesosphere and thermosphere is crucial to understand the large-scale heat and momentum budget of this part of the Martian atmosphere.

429 Acknowledgments

- 430 The authors acknowledge Centre National d'Études Spatiale (CNES) and European Space
- Agency (ESA) for financial support. We thank two reviewers for thorough and constructive
- 432 comments that helped us to improve this paper.

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