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## The case for considering polarization in the interpretation of electrical and electromagnetic measurements in the 3 kHz to 3 MHz frequency range

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1 **The case for considering polarization in the interpretation of electrical and**  
2 **electromagnetic measurements in the 3 kHz to 3 MHz frequency range.**

3

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9

10 **Abstract**

11 Usually, *in-situ* electrical polarisation measurements (in geophysical prospection  
12 referred to as Induced Polarization (IP), or Spectral Induced Polarization (SIP)) have been  
13 carried out at frequencies below 1 kHz. These techniques have been used mainly for mining  
14 exploration, followed by a larger panel of environmental applications. However, in this ultra  
15 and extremely low frequency domain, the duration of each individual measurement is long:  
16 typically several tens of minutes for a single full SIP spectrum down to the mHz range. This  
17 restriction makes it unrealistic to implement high-density measurement mapping campaigns  
18 over large areas, which would otherwise be possible at higher frequencies. In the intermediate  
19 frequency range [3 kHz – 3 MHz], laboratory studies of soil and rock samples have shown  
20 that they can be strongly polarized notably in the presence of clays, and this property has been  
21 confirmed by several *in-situ* mapping experiments using electromagnetic induction (EMI) in  
22 the time and frequency domains (FDEM and TDEM), as well as by the electrostatic method  
23 (often named Capacitive Coupled Resistivity or CCR). The present paper recalls these results

24 in an effort to promote polarisation measurements at intermediate frequencies, and to  
25 emphasize the importance of measuring this phenomenon.

26

27 **Key words:** electrical polarisation, permittivity, [3 kHz – 3 MHz] frequency range

28

## 29 **1.-Introduction**

30 For more than a century, electrical resistivity/conductivity has played a crucial role in  
31 near-surface geophysics (Jakosky 1940), for both large surface mapping and localised  
32 tomographic/sounding studies based on the measurement of this property. Reference books  
33 dealing with the electrical and electromagnetic methods themselves (Keller & Frischknecht  
34 1966, Nabighian ed. 1988 and 1991) and describing different fields of application have  
35 contributed to the development of their physical and theoretical foundations and provided  
36 numerous practical examples (Scollar et al. 1990, Rubin & Hubbard 2005, Sharma 2008,  
37 Dentith & Mudge 2015). Since the seminal work of Archie (1942), considerable research has  
38 been devoted to the analysis of several specific parameters - porosity, clay content, water  
39 saturation, water mineralization, etc... - affecting the electrical resistivity (e.g. Glover 2015).  
40 Various applications, ranging from mining exploration to precision farming can benefit from  
41 airborne and ground surveys of this property, over large surface areas. Extensive review  
42 papers can be found in the literature, as for example by Pellerin (2002) or Doolittle & Brevik  
43 (2014) in the case of near-surface applications. However, as the use of induction  
44 electromagnetic methods is commonly limited to electrical resistivity alone, they do not  
45 provide a full description of the electrical response of near surface rocks and soils. The  
46 determination of their polarisation properties can also be considered, as one cannot *a priori*  
47 exclude unknown but possibly valuable information.

48           Polarisation phenomena were observed very early, in both surface and logging  
49 measurements, and Schlumberger (1920) coined the term ‘polarisation provoquée’  
50 (“provoked polarisation” in English) which was later (with a possible confusion with the  
51 electromagnetic induction) changed in English to ‘induced polarisation’ (IP). During the 50’s  
52 the IP method was applied in time domain measurements (Bleil 1953), and encountered  
53 considerable success in ground prospecting campaigns applied to mining, as it was able to  
54 reveal disseminated mineralization (mainly semiconductor sulphides, e.g. Pelton et al.  
55 (1978)). However, even in the absence of minerals, researchers became aware of the role  
56 played by clay in IP, including mixtures of clay and coarser particles (Vaquier et al. 1957,  
57 Okay et al. 2014). Over the last thirty years, significant developments were achieved on the  
58 role of the clay and of the fluid characteristics on the IP signal in the context of groundwater  
59 and environmental studies (e.g. Luo and Zhang 1998, Kemna et al. 2012, Binley et al. 2015).  
60 Various laboratory studies and field exploration campaigns have been reported, and  
61 theoretical models have been proposed. The latter, in particular, established links between  
62 electrical polarisation and hydraulic properties (Börner et al. 1996, Revil & Florsch 2010,  
63 Fiandaca et al. 2019). Field measurements were performed mostly in the time domain, by  
64 measuring the voltage decay after cut-off, over a period ranging from one second to several  
65 minutes. However, frequency domain measurements made it possible to gain a better  
66 understanding of the frequency dependence of IP (the spectral IP, SIP). Regular workshops  
67 allowed the IP community to report on-going research, to publish in special issues, of which  
68 the most recent were edited by Camerlynck, Chauris, Mainault and Schmutz (2015 and 2016),  
69 Fiandaca, Flores Orozco and Hördt (2017) and by Ntarlagiannis, Wu and Ustra (2019).

70           IP requires significantly long measurement periods: most frequency domain laboratory  
71 studies are carried out over the [1 mHz -1 kHz] frequency range, field measurements last for  
72 several minutes per point if such low frequencies are included. This requirement limits

73 complete field studies of IP to fixed point measurements, compatible with 1D soundings.  
74 Current electrical resistivity tomography (ERT) acquisition devices used for IP limit the  
75 practical frequency range above 1 Hz and below 100 Hz, , but as the number of periods  
76 necessary for a good staking controls in the field the progression speed of towed instruments,  
77 such frequencies do not match with rapid motion. In order to overcome this limitation, shorter  
78 measurement times and higher frequency ranges are needed. Adding higher frequencies to  
79 classical IP field investigations will also give access to potential new information  
80 (identification of relaxation phenomena with shorter time constant for example) and to a  
81 better characterisation of known IP phenomena.

82 There also exists specific *in-situ* difficulties associated with galvanic IP  
83 measurements: ground dependent EM coupling between cables or electrode polarisation  
84 (Bhattacharyya and Morrison 1963, Pelton et al. 1978, Kelter et al. 2018). In the [3 kHz – 3  
85 Hz] frequency range these specific difficulties can be overcome by using other measurement  
86 principles: magnetic sensors (coils) (Simon et al. 2019) and capacitive poles (Grard and  
87 Tabbagh 1991). If one uses metallic electrodes (or liquid electrodes) inserted in the ground  
88 one has both a capacitance and a resistance thus a phase shift and significant risk of phase  
89 rotation if one of the two characteristics changes, while if one only uses capacitances there is  
90 no phase shift and the only difficulty is linked with the relative magnitude of the capacitance  
91 at the poles and at the feeding wire (but the leaks are proportional to the capacitances and a  
92 model can be performed), poles are only required to present significantly higher capacities  
93 than feeding wires

94 The range of permittivity and conductivity values relevant to Ground Penetrating  
95 Radars (GPR) and Time Domain Reflectometry (TDR) applications, have been well  
96 documented at frequencies above 30 MHz, and electrical polarisation is usually interpreted in  
97 terms of the orientation of polar water molecules. However, little is known between SIP and

98 GPR frequency ranges. At frequencies in the [3 kHz – 3 MHz] interval, which includes VLF  
99 (Very Low Frequency), LF (Low Frequency) and MF (Medium Frequency) measurements, a  
100 small number of field observations and tests have been carried out, using three different  
101 techniques: Time-Domain Electromagnetics (TDEM), Frequency-Domain Electromagnetic  
102 induction (FDEM), and the electrostatic method (Capacitive Coupled Resistivity, CCR).  
103 However, with all these techniques the measured responses are usually dominated by the  
104 electrical conductivity and the polarisation part is most often neglected. Nevertheless a larger  
105 number of both laboratory and field experiments are needed to evaluate the validity of this  
106 choice. An accurate evaluation the influence of electrical polarisation would permit a better  
107 understanding of its magnitude in various field contexts.

108         At the macroscopic scale, electrical polarisation corresponds to a situation in which the  
109 barycentre of the positive charges does not coincide with the barycentre of the negative  
110 charges. At the microscopic pore/grain scales, different processes with different relaxation  
111 geometric scales and time constants limit the free displacement of electric charges. Although  
112 their detailed classification (Kemna et al. 2012) could be questioned, one can cite: electrode  
113 polarisation, membrane polarisation (Marshall and Madden 1959), electrochemical  
114 polarisation, interfacial polarisation/diffuse layer polarisation (Revil 2013), and Maxwell-  
115 Wagner polarisation (Chen and Or 2006). Depending on the frequency and temperature  
116 ranges involved, all of these processes can contribute to the magnitude of the polarisation and  
117 can add together so that it could be difficult to single one out and a regular decrease with  
118 frequency can be often observed. It must also be underlined that anisotropy in the shape of the  
119 polarized volume plays a major part in the magnitude of their moment (Tabbagh et al. 2009).

120         In a first step towards the assessment of polarisation in the [3 kHz – 3 MHz] frequency  
121 range and in view of a better interpretation of EMI or CCR surveys, the present paper

122 provides an overview of published experimental results, at both field and laboratory scales,  
123 and in both time and frequency domains.

124 Part of these experimental results were collected during the course of laboratory SIP  
125 experiments, at frequencies of 10 kHz or higher. The considered published results serve as a  
126 basis to illustrate the global magnitude of polarisation and conductivity values without being  
127 able to identify the different polarisation processes. In an effort to focus this study on  
128 common rocks and soils, we do not consider measurements carried out on media containing  
129 electronic conductor/semiconductor minerals (oxides, sulphides, metallic particles or  
130 graphite).

131

## 132 **2.-How should the electrical polarisation be expressed?**

133 In the Maxwell-Ampère equation, the electrical polarisation is represented by the  
134 displacement currents. In the frequency domain this can be written:

$$135 \quad \text{curl } H = (\sigma_0 + i\omega\varepsilon)E \quad (1),$$

136 where  $E$  is the electric field,  $H$  is the magnetic field,  $\sigma_0$  is the direct current electrical  
137 conductivity,  $\omega$  is the angular frequency ( $\omega = 2\pi f$ ),  $i = \sqrt{-1}$ , and  $\varepsilon$  is the dielectric  
138 permittivity. Although this last property describes the dielectric behaviour, in order to take the  
139 dielectric losses into account it must be considered complex quantity:  $\varepsilon = \varepsilon' - i\varepsilon''$ . Here, the  
140 imaginary term has the same phase as the motion of free carriers (direct current conductivity,  
141  $\sigma_0$ ), from which it cannot be experimentally distinguished. The measured conductivity thus  
142 corresponds to:  $\sigma' = \sigma_0 + \omega\varepsilon''$ , which leads to the Maxwell-Ampère equation being written as:

$$143 \quad \text{curl } H = (\sigma_0 + \omega\varepsilon'' + i\omega\varepsilon')E = (\sigma' + i\omega\varepsilon')E \quad (2)$$

144 These properties can be also expressed in the form of a complex conductivity ( $\sigma' +$   
 145  $i\sigma''$ ) or a complex resistivity ( $\rho' - i\rho''$ ), leading to the following correspondences:  $\sigma' = \sigma_0 +$   
 146  $\omega\varepsilon''$  and  $\sigma'' = \omega\varepsilon'$ .

147 In several publications authors usually refer to a formula derived from the Cole-Cole  
 148 (1941) model to describe polarisation phenomena (e.g. Pelton et al. 1978):

$$149 \quad \rho(\omega) = \rho_0 \left[ 1 - m \left( 1 - \frac{1}{1 + (i\omega\tau)^c} \right) \right] \quad (3)$$

150 where  $\rho_0$  is the direct current resistivity,  $m$  is the chargeability and  $c$  expresses the  
 151 enlargement of the relaxation constant ( $\tau$ ) distribution. Note that Eq. (3) is an empirical  
 152 representation of the polarization mechanisms occurring in geological media, but other  
 153 empirical models exist, among which multiple or generalized Cole-Cole (see Ghorbani et al.  
 154 2009), or constant phase angle model (see for instance Dias (2000) for an extended model  
 155 collection).

156 In the following text, in an effort to homogenise and clarify the representation of  
 157 polarisation and in agreement with other researcher approaches (Knight and Endres (2005),  
 158 Revil (2013), Loewer et al. (2017)), we regroup all the different polarization mechanisms that  
 159 can contribute and we express the electrical polarisation in terms of a real effective parameter,  
 160 the relative permittivity  $\varepsilon_r$ , defined by  $\varepsilon' = \varepsilon_0 \varepsilon_r$  ( $\varepsilon_0$  being the permittivity in vacuum,  $\varepsilon_0 = 8.854 \times$   
 161  $10^{-12} \text{ Fm}^{-1}$ ). Consequently, when considering the published results expressed by the imaginary  
 162 part of the conductivity we introduce  $\varepsilon_r = \frac{\sigma''(\omega)}{\omega\varepsilon_0}$ , and when they are expressed by equation

163 (3) we identify  $\rho(\omega)$  with  $\frac{1}{\sigma' + i\omega\varepsilon_0\varepsilon_r}$ . In the following text this relative effective

164 permittivity is for sake of simplicity denominated permittivity, we also use the term imaginary  
 165 part of the permittivity for  $\varepsilon''/\varepsilon_0$ .



166

### 167 **3. Looking first at simple experimental cases**

168 As introductory illustrations of both the magnitude and the frequency dependence of  
169 the permittivity we present in Figure 1a and b the experimental results obtained in laboratory  
170 for one soil sample and one rock sample in the [100 Hz – 10 MHz] range using a capacitive  
171 cell and a vector multi-meter (PSM 1735, NumetricQ, Ltd). The cell dimensions are, Figure  
172 1c, 19 x 160 x 160 mm<sup>3</sup>.

173 The soil is a clay loam coming from the A horizon of the ‘Jardin du Roy’ in Paris.  
174 This material is indeed complex, where beside mineral grains exist a lot of biological active  
175 and residual elements but the presence of a soil layer is usual in geophysical surveys. It has a  
176 high porosity,  $n=0.481$  (bulk density 1.34 g.cm<sup>-3</sup>). When dried, at 105°C for 24 hours, the real  
177 part of the permittivity equals 3 over the whole frequency range in agreement with the Topp  
178 et al. (1980) equation. In that soil sample the drying has eliminated all the polarisation  
179 mechanisms except the atomic polarisation of solid grains. The presented measurements have  
180 been achieved at a high volumetric water content:  $\theta=0.446$  (quasi saturation). One can  
181 observe (Figure 1a) that the imaginary part is linearly decreasing with frequency, the slope  
182 corresponding to a DC conductivity of 21.6 mS.m<sup>-1</sup> thus to 46  $\Omega$ .m (thin line). The real part  
183 has very high values in low frequency as it starts from  $9 \times 10^5$  at 100 Hz, and reaches 4 000 at  
184 3 kHz. Its linear decrease fits with a Jonscher’s exponent of -1.45 (Jonscher 1977). Such a  
185 regularity in the decrease corresponds to a large distribution of relaxation times. Higher  
186 frequency values agrees relatively well with the Topp et al. formula: for  $\theta=0.446$ ,  $\epsilon_r=29$ . The  
187 curves corresponding to the modelling expression,

$$188 \quad \epsilon_r = (9 \cdot 10^5 (\omega/\omega_0)^{-1.45} + 29 - i 0.0216/(\omega\epsilon_0)) \quad (4),$$

189 are drawn by a thin continuous lines in the Figure 1a,  $\omega_0$  being the angular frequency  
190 corresponding to 100 Hz.

191 The rock sample is a Lutetian limestone extracted from the Saint Pierre Aigle quarry  
192 (Aisne, France). It contains calcite, 85% in weight, sand 10% and a few percent of  
193 phyllosilicates (clay). The open porosity  $n$  equals 0.18. The results presented in Figure 1b are  
194 measured when the sample is dry,  $\theta=0.017$ , and the conductivity is too low to be measurable.  
195 In addition to the high frequency permittivity behaviour, one can observe a unique relaxation  
196 process which fits the following expression (thin lines in Figure 1b),

$$197 \quad \varepsilon(\omega) = \frac{\Delta\varepsilon}{1+(i\omega\tau)^c} + \varepsilon_h' - i\varepsilon_h'' \quad (5),$$

198 where  $\Delta\varepsilon = 28$ , the real part of the high frequency permittivity  $\varepsilon_h' = 4.5$ , its imaginary part  
199 equals  $\varepsilon_h'' = 0.5$ ,  $c = 0.65$  and  $\tau = 1.75 \mu\text{s}$ .

200 In this second sample, the behaviour of the permittivity is very different in amplitude  
201 and in frequency dependence from that of the moist soil, but even this dry rock sample has a  
202 real part of the permittivity staying above 30 between 100 Hz and 10 kHz, significantly  
203 higher than 4.5 at high frequencies.

204

## 205 **4.-Published effective permittivity values in laboratory**

### 206 **4.1 Experiments covering the [3 kHz – 3 MHz] frequency range**

207 In order to understand in-field observations made at ground surface or by means of  
208 well logging, and to assess the different hypotheses that can be proposed to interpret the data,  
209 various laboratory studies have been carried out on both natural and synthetic samples.  
210 Unfortunately, there are more published results derived from laboratory studies than from  
211 field campaigns. Several studies have covered a wide frequency range, and the results of some

212 are given in Table 1. It can be observed that clayey formations have permittivity values above  
213 hundred or thousand between 10 and 100 kHz.

#### 214 **4.2 Values determined at 10 kHz by SIP experiments**

215 SIP gave rise to a large number of laboratory studies, designed to assess the roles  
216 played by minerals, their grain size distribution, as well as their fluid nature and content.  
217 Several different models have also been tested in the context of these studies, some of which  
218 were carried out at frequencies of several tenths of a kilohertz, allowing the permittivity to be  
219 determined at 10 kHz (Table 2). Again values of permittivity above 1000 are reported for  
220 clayey formations.

221

### 222 **5.-Published *in-Situ* data**

#### 223 **5.1 Electrostatic measurements (CCR)**

224 This method can be seen as a generalization of the DC resistivity, where the injection  
225 electrodes are replaced by an open capacitor and the voltage electrodes by another open  
226 capacitor (Grard and Tabbagh 1991, Tabbagh et al. 1993, Kuras et al. 2006). To reduce the  
227 pole impedances, the transmitted frequency(ies) must in practice be larger than or equal to 10  
228 kHz. By adopting 100 kHz as the upper frequency limit imposed by the induction effect  
229 (Benderitter et al. 1994, Tabbagh and Panissod 2000), an adequate depth of investigation is  
230 achieved for most engineering and environmental applications.

231 Table 3 summarises the ranges of resistivity and permittivity obtained following the  
232 acquisition of profile or map data series.

#### 233 **5.2 Electromagnetic frequency domain measurements**

234 Is it possible to measure IP using an inductive system, which would pave the way to  
235 direct and large ground and airborne applications? This old question (Hohmann et al. 1970)  
236 led to a series of studies that concluded negatively, although these were carried out using  
237 simulations and experiments limited to 1.5 kHz for transmitter coil - receiver coil instrument  
238 configurations. More recently, some *in situ* experiments have been performed at higher  
239 frequencies, using both helicopter-borne and ground-based devices (Table 4) and the coil-coil  
240 configuration gave reliable results even at medium frequencies (Kessouri et al. 2016). For  
241 FDEM measurements using uniform primary fields, radio-magnetotellurics (RMT) or wave-  
242 tilt measurements, the influence of the electrical polarisation has been considered in theory  
243 (Grossley 1981) with permittivity values as high as 200 (Sinha et al 1977) but unfortunately  
244 the published experiments are limited to very high resistive areas (permafrost and/or  
245 crystalline basement) where the permittivity remains below 10 (Kalscheuer et al. 2008).

### 246 **5.3 TDEM measurements**

247 In principle, TDEM measurements (Nabighian and Macnae 1988) correspond to an  
248 extended frequency range, and, as the cut-off time can be as short as 4  $\mu$ s (Thiesson et al.  
249 2007, Auken et al. 2019), the frequency range considered in the present review corresponds to  
250 the early time-domain samples but IP effects can also be observed at late times. The presence  
251 of electrical polarisation is observed as an unexpected cancellation of monotonicity in the  
252 decrease of the step and impulse responses by reference to what would be expected with the  
253 same transmitter/receiver configuration when only conductivity and magnetic viscosity are  
254 considered. This phenomenon has been observed since the 70's (Lee 1975), and can only be  
255 explained by electrical polarisation (Weidelt 1982). In some cases, the authors were able to  
256 check these observations by direct current IP measurements and/or by Cole-Cole modelling.

257 The corresponding permittivity values, listed in Table 5 below, are estimated from the  
258 following equation:  $\varepsilon_r = \frac{1}{\omega\varepsilon_0} \text{Im}\left(\frac{1}{\rho(\omega)}\right)$ .

259

## 260 **6- General appraisal: amplitude of the polarisation response and relation with** 261 **conductivity**

262 An overview of the permittivity and resistivity variations is synthetized in Figure 2.  
263 Although these results do not give an exhaustive list of the experimental studies reported in  
264 the literature, they are sufficient to establish what the electrical polarisation looks like in the  
265 [3 kHz – 3 MHz] frequency range.

266 (1) The magnitude of the electrical polarisation expressed in  $\varepsilon_r$  can exceed  
267 10 000. It is certainly higher than that observed in the range of frequencies  
268 used for GPR/TDR, as summarized by the Topp et al. (1980) cubic  
269 formula;

270 (2) It can be seen that there is consistency between laboratory (Tables 1 and 2)  
271 and field measurements (Tables 3, 4 and 5).

272 (3) Below approximately 300  $\Omega\cdot\text{m}$  (above 3.3  $\text{S}\cdot\text{m}^{-1}$ ), the permittivity looks  
273 inversely correlated with resistivity. It exhibits a high variability at least as  
274 strong as that of the resistivity. Figure 2 illustrates this anti-correlation.  
275 However points are not grouped along a straight or curved line, but  
276 scattered. Consequently a significant part of information existing in  
277 permittivity is independent on that existing in resistivity.

278 (4) As expected, the existence of several relaxation mechanisms with gradually  
279 increasing time constants corresponds to a decrease of the polarisation with  
280 frequency.

281 (5) In all tabulated results, clay content and ionic strength contribute  
282 dominantly to polarisation.

283 Figure 3 plots the product  $\varepsilon_0 \varepsilon_r \omega$  as a function of  $\sigma$ , derived from laboratory samples. It  
284 can be seen that the samples can be divided into two distinct groups, depending on the  
285 presence (higher conductivity) or absence (lower conductivity) of clay. In the first group,  
286 most of the data points lay between the lines indicating a contribution of 0.1 and 0.01 of the  
287 permittivity relatively to the conductivity. This shows that although conductivity dominates  
288 the response, the permittivity responses should also be taken into account. In the second  
289 group, the permittivity responses clearly dominate the results. It is thus always necessary to  
290 consider both responses.

291 Tables 1 to 5 reveal that, when the measured resistivity is high, its decrease as a  
292 function of frequency due to the presence of dielectric losses,  $\omega \varepsilon''$ , is more easily observable.  
293 In cases where the dielectric losses contribution is significant, it would be useful to compare  
294 these frequency-dependent measurements with the direct current resistivity, in the field as  
295 well as in the laboratory.

## 296 **7 Implications for field measurements**

297 It is clear that any processing of field data should consider the polarisation processes  
298 independently from the usual conduction processes in the [3 kHz – 3 MHz] frequency range  
299 where short measurement durations open the way to high density surveys. In this range the  
300 different electrical methods can be split in in three groups: the coil – coil EMI methods, the  
301 EMI methods using distant sources, and the electrostatic method (CCR). In the first group, for  
302 lower frequencies, measurement interpretation may be even more complicated by the  
303 influence of the magnetic properties. Thus, two situations can be considered: in the first, the  
304 method is not sensitive to magnetic properties, which may intervene in the second situation.

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### ***7.1 In absence of magnetic property influences***

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In the first situation, given that the Maxwell-Ampère equation states that the conduction the displacement currents are 90 degree's out-of-phase from the conduction ones, the measurement of both in-phase and out-of-phase components (by reference to the primary source signal) is necessary and sufficient to determine the apparent resistivity and the apparent permittivity. Recent electronics devices can easily perform the separation between in-phase and out-of-phase components. The calculation of apparent properties can be done by inversion (Kessouri et al. 2016), by lookup tables (Huang and Fraser 2002) or master curves. Using an inversion procedure is of common use with the electrostatic method (Souffaché et al. 2010, Przyklenk et al. 2016) and with coil –coil FDEM instruments where the frequency is sufficiently high and/or the coil separation sufficiently large (Simon et al. 2019). However, in Magnetotellurics (or Radio MT in the considered range) the influence of the permittivity modifies both the amplitude of the wave impedance and the phase lag between the electric and magnetic fields. Consequently both amplitude and phase sounding curves are distorted and a precise interpretation would be impossible in absence of a phase reference locked on the source of the primary field.

322

### ***7.2 In presence of magnetic property influences***

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For small FDEM or TDEM instruments setup, the magnetic properties may have a strong influence. For FDEM, to the best of our knowledge for ground measurements if the magnetic susceptibility do not exceed  $10^{-3}$  SI, the rule of thumb criterion  $(f L) > 10^6 \text{ Hz.m}$  is relevant ( $L$  being the separation between coils) for neglecting the magnetic susceptibility response. If not, several possibilities exist:

328 (1) in FDEM determine the magnetic susceptibility by moving the frequency at the  
329 lower possible values (for example for a metric inter-coil spacing instrument use a frequency  
330 around 10 kHz), where the rule of thumb criterion  $(fL) < 3 \cdot 10^4 \text{ Hz} \cdot \text{m}$  is relevant to neglect the  
331 permittivity response, and in TDEM determine the magnetic viscosity by the late time  
332 response.

333 (2) in FDEM set the height of the instrument in HCP (horizontal coplanar) coil  
334 configuration in such way that the magnetic response is negligible as it is known that the  
335 magnetic susceptibility response crosses 0 if the instrument altitude equals  $0.38L$  (for example  
336 if  $L=3.66$  m the instrument can be held at a height of 1.4 m)

337 (3) in FDEM use both HCP and VCP (vertical coplanar) configurations because in the  
338 HCP the permittivity in-phase response opposes the magnetic susceptibility while in the VCP  
339 it adds (Benech et al. 2016). In all cases, instruments must be carefully calibrated (Thiesson et  
340 al. 2014).

341 The same ideas of combining coil separation and clearance can be applied in TDEM  
342 (Finco 2019).

343

## 344 **8- Conclusion**

345 We present the results of varied laboratory and field experiments conducted over  
346 different material for different objectives. A very brief review of our scope and objectives is  
347 in order here.

348 First, since the magnitude of the permittivity response can be significant (and in some  
349 case dominant), exploration geophysicists should not neglect  $\epsilon\omega$  in favour of  $\sigma$ , when  
350 implementing EM inductive (both frequency and time domain) and electrostatic exploration  
351 methods. In other words, (i) even if present practices are limited to conductivity, taking into



352 account the permittivity will allow a better determination of the conductivity itself which is  
353 imperative when simultaneously interpreting different type of conductivity measurement  
354 techniques and (ii) there is no reason to *a priori* exclude information.

355         Second, the measurement and in-field mapping of permittivity may open opportunities  
356 for the exploration of a broad range of new types of geophysical information. In the  
357 considered frequency range, both conductivity and permittivity depend on the total amount of  
358 mobile ions, conductivity corresponding to free motion and permittivity to constrained  
359 motions limited by what may oppose to the ion displacements: pore size and throat  
360 configuration, disposition, shapes and types of clay platelets, etc...

361

362 **References**

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512



513 **Figure captions**

514 Figure 1: Example of frequency variation of the permittivity of (a) a clay loam soil (A  
515 horizon) sample, (b) the Saint Pierre Aigle limestone: (bold continuous line for the real part,  
516 bold dashed line for the imaginary part). The corresponding models (respectively expression  
517 (4) and (5)) are in thin continuous lines, (c) capacitive cell and PSM vector multi-meter.

518 Fig 2: Relationship between the relative permittivity and the conductivity (in  $\text{Sm}^{-1}$ )/resistivity  
519 (in  $\Omega\cdot\text{m}$ ). For the different tables (left) and for the different frequencies (right).

520 Fig 3: Laboratory results: comparison between  $\varepsilon_0\varepsilon_r\omega$  (in  $\text{S m}^{-1}$ ) and  $\sigma$  (in  $\text{Sm}^{-1}$ ) values

521

522 **Table captions**

523 Table 1: Permittivity values in laboratory experiments covering the [3 kHz – 3 MHz] range.  
524 (Notations:  $a$  is the side of a square cell,  $e$  is the thickness of disk, cylindrical or square cells  
525 and  $d$  is the diameter of cylindrical or disk cell).

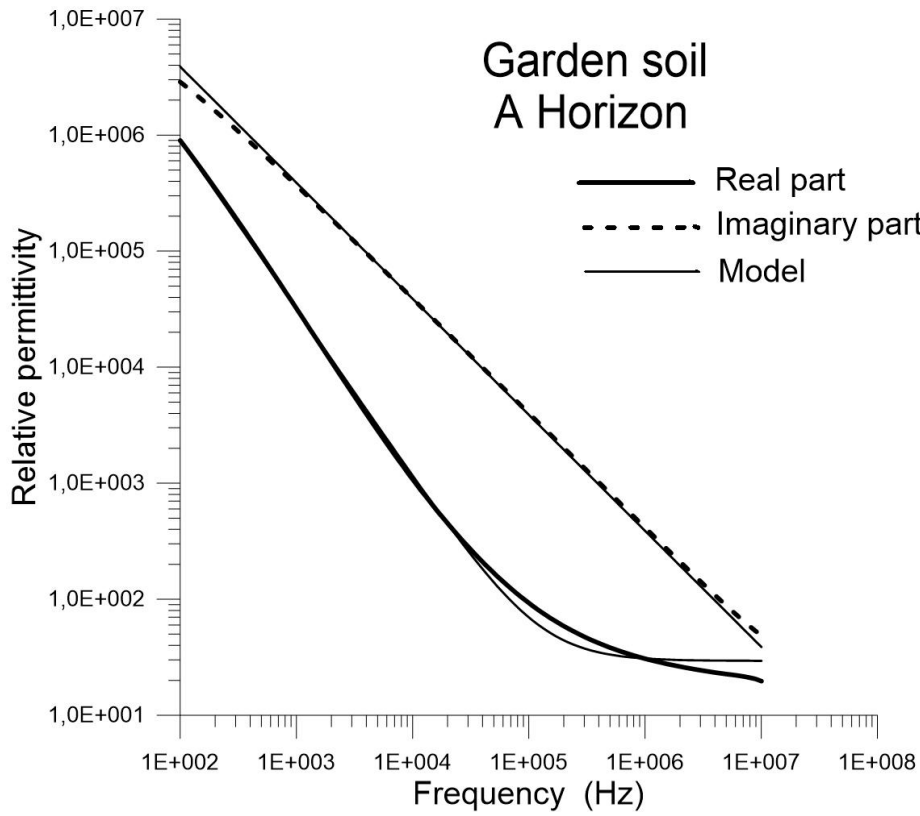
526 Table 2: Permittivity values delivered at 10 kHz by laboratory SIP experiments. (Notations:  $e$   
527 is the thickness of disk or cylindrical cells and  $d$  is the diameter of cylindrical or disk cell).

528 Table 3: Permittivity values obtained by *in-situ* electrostatic measurements.

529 Table 4: Permittivity values obtained by *in situ* frequency domain measurements.

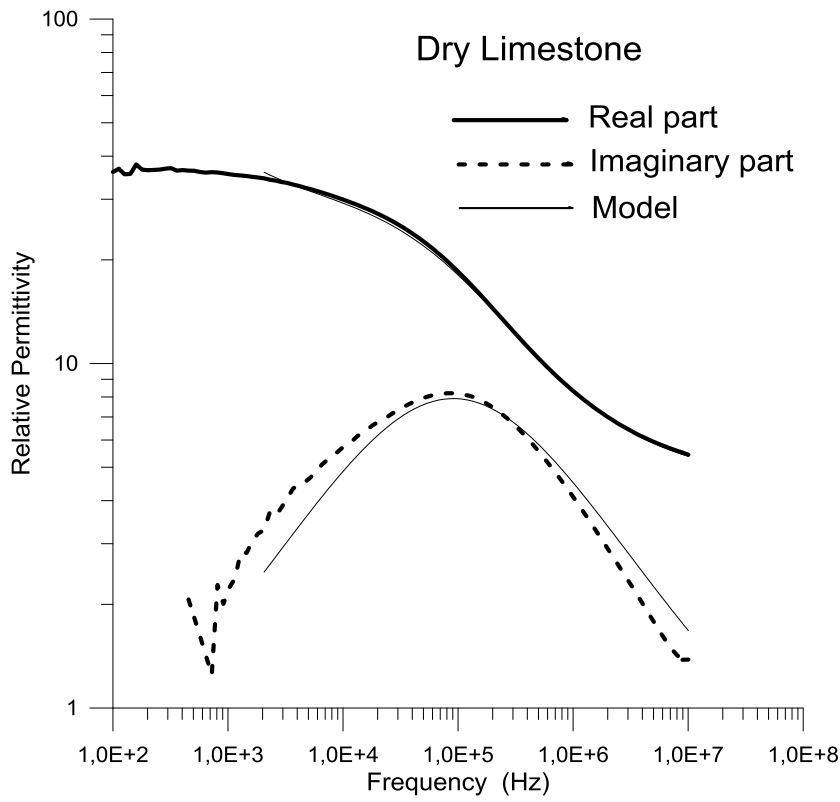
530 Table 5: Permittivity values obtained by *in situ* TDEM measurements.

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532

533 Figure 1a



534

535 Figure 1b

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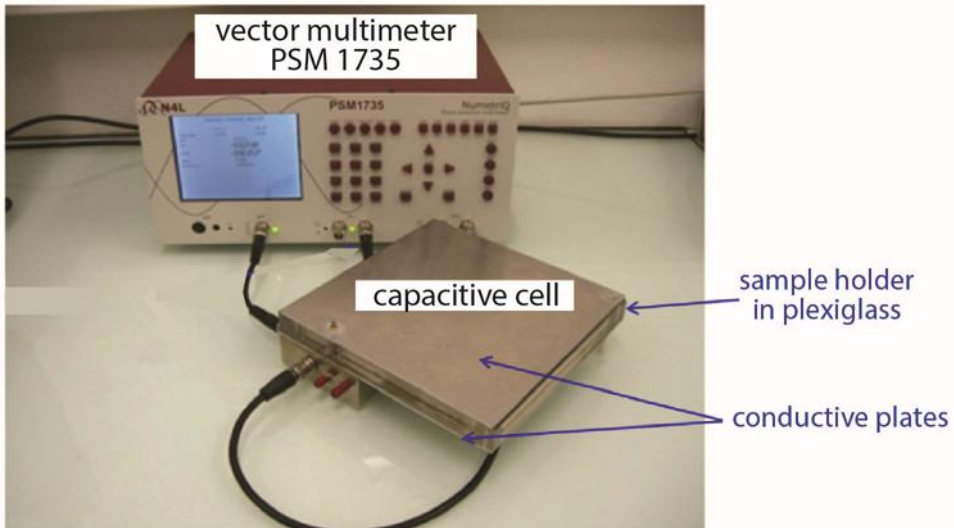


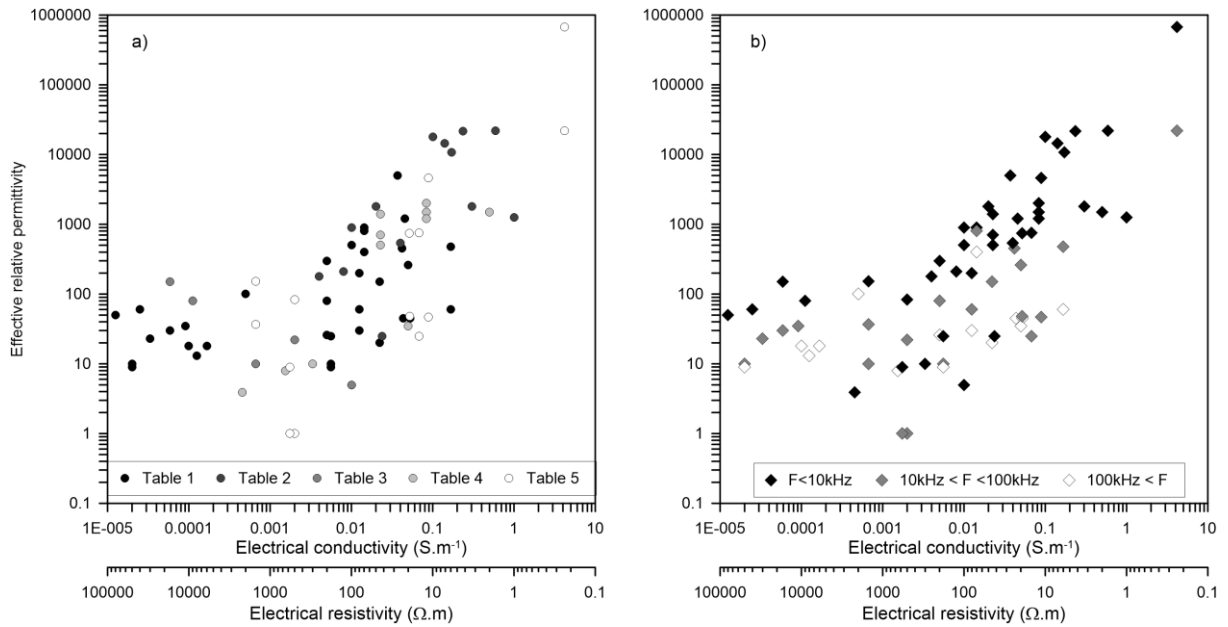
Figure 1c

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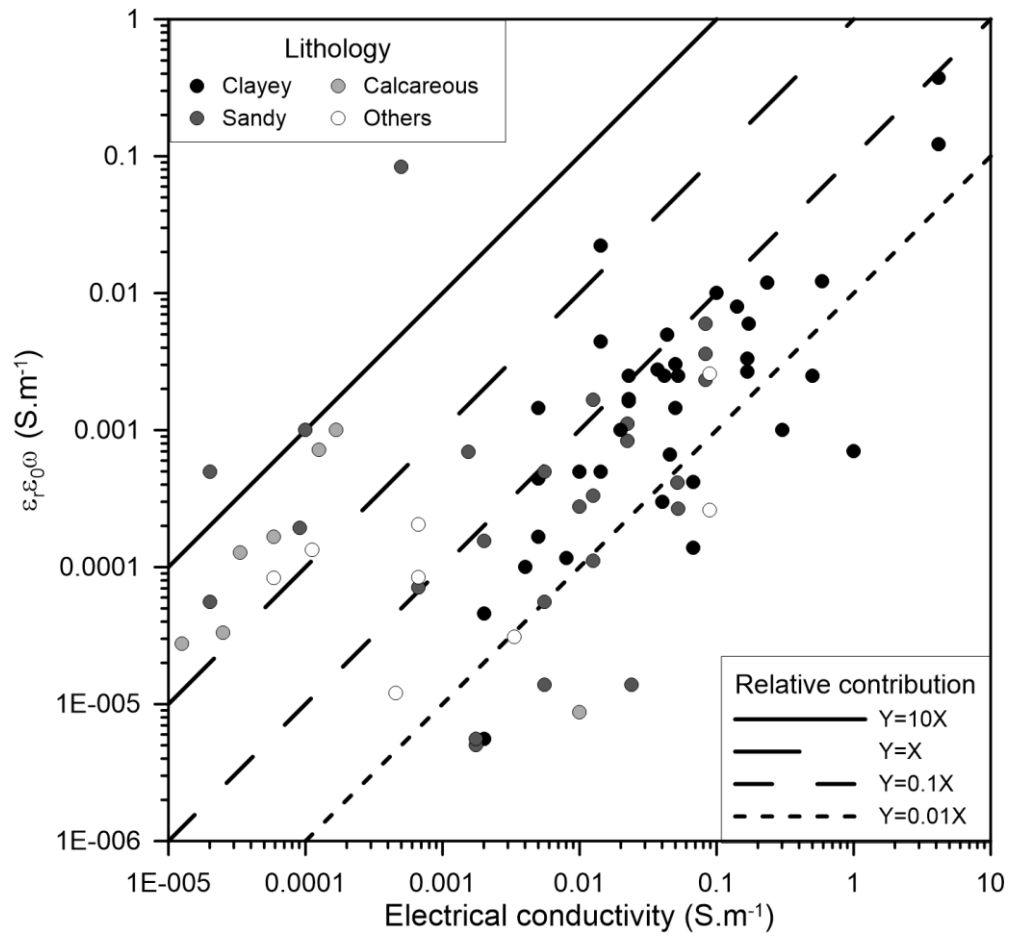
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541

542 Figure. 2



543

544 Figure. 3

545

Reference	Sample size and cell	Sample characteristics	Frequency	Electrical resistivity	Relative permittivity
Scott et al. 1967, J.G.R., 72, 5101-5115.	Cylindrical capacitance cell d=2.54 cm e=2.54 cm 2 electrodes	Mancos shale (3.8% volume water content)	10 kHz	200 Ω.m	300.
			100 kHz	200 Ω.m	80.
			1 MHz	200 Ω.m	26.
Kenyon 1984 Journal of applied Physics, 55 ,3153-3159	Coaxial cell	Whitestone calcite saturated with 1.07Ω.m NaCl solution	1 MHz	18 Ω.m	800
Knight & Nur 1987, Geophysics 52(2), 644-654.	Disk-shaped capacitance cell d=5.1 cm e=0.5 cm 2 electrodes	CH66-79 Berea sandstone, Sw=0.36 deionized water	100 kHz	11,000 Ω.m	35.
			1 MHz	10,000 Ω.m	18.
		St Peter's sandstone Sw=0.36 deionized water	100 kHz	50,000 Ω.m	10.
			1 MHz	50,000 Ω.m	9.
Garrouch & Sarma 1994, Geophysics 59(6) 909-917.	Disk-shaped capacitance cell e=3 to 10 mm 2 and 4 electrodes	102 shaly sand brine saturated (8%)	10 kHz	27 Ω.m	5,000.
			100 kHz	24 Ω.m	450.
			2 MHz	23 Ω.m	45.
		144 sandy clay brine, saturated (8%)	10 kHz	Not given	15,000.
			100 kHz		500.
			2 MHz		100.
Tabbagh 1994, Archaeometry, 36, 159-170.	Square capacitance cell a=190 mm e=19 mm 2 electrodes	Sandy clay loam, saturated 43 %	10 kHz	70 Ω.m	900.
			100 kHz	70 Ω.m	800.
			1 MHz	70 Ω.m	400.
		Volcanic sand, saturated 43.6 %	10 kHz	Not given	50.
			100 kHz		25.
			1 MHz		15.
		Porous limestone, saturated 16.5%	10 kHz	Not given	40.
			100 kHz		35.
			1 MHz		25.
Lesme & Frye 2001, J.G.R., 106-B3, 4079-4090	Disk-shaped capacitance cell 2 electrodes	Berea sandstone (68% quartz), saturated (0.01M NaCl)	10 kHz	80 Ω.m	200.
			100 kHz	80 Ω.m	60.
			1 MHz	80 Ω.m	30.
Sternberg & Levitskaya 2001. Radio Science 36(4), 709-719.	Coaxial cell	Avra valley sandy silt with clay, water content 10.6%	10 kHz	22 Ω.m	1,200.
			100 kHz	20 Ω.m	260.
			1 MHz	19 Ω.m	45.
		Brookhaven sandy soil, water content 9.75 %	10 kHz	180 Ω.m	25.
			100 kHz	180 Ω.m	10.
			1 MHz	180 Ω.m	9.
Oh & al. 2007, Environ. Geol. 51, 821-833	Disk-shaped capacitance cell d= 70 mm e=2 mm 2 electrodes	Sandy soil, water content 23%	100 kHz	45 Ω.m	150.
			1 MHz	45 Ω.m	20.
		Sandy soil with 10% bentonite, water content 23%	100 kHz	6 Ω.m	480.
1 MHz	6 Ω.m	60.			
Wagner et al. 2011 IEEE Geoscience & Remote Sensing 49-7,	Coaxial cell d=7 and 16 mm length 100mm	Silty clay loam (Unstrut river, Germany) Porosity 0.43, Water content 0.38	10 kHz	9 Ω.m	5,000
			100 kHz	8.5 Ω.m	410
			1 MHz	8 Ω.m	295
Abou El-Anwar & Gomaa, 2013, Geophys. Prospect., 61, 630-644.	Cylindrical, 2 electrodes	sandy lime-mudstone/dolostone	10 kHz	40,000 Ω.m	60.
			100 kHz	17,000 Ω.m	30.
			1 MHz	6,000 Ω.m	18.
		sandy dolomitic bioclastic wackestone-mudstone	10 kHz	80,000 Ω.m	50.
			100 kHz	30,000 Ω.m	23.
1 MHz	8,000 Ω.m	13.			

546 Table 1

Reference	Sample size and cell	Sample characteristics	Electrical resistivity	Relative permittivity 10 kHz
Börner et al. 1993, Geophys. Prosp. 41, 83-98.	Cylindrical d=20mm e=30mm 4 electrodes	KT2 Clay	1 $\Omega$ .m	1,260.
		E14 shaly sandstone ( $\sigma_w=0.01$ S/m)	250 $\Omega$ .m	180.
		E6 shaly sandstone ( $\sigma_w= 0.002$ S/m)	125 $\Omega$ .m	210.
		BEN bentonite with brine ( $\sigma_w=1$ S/m)	1.7 $\Omega$ .m	22,000.
		KAO kaolinite with brine ( $\sigma_w=1$ S/m)	10 $\Omega$ .m	18,000.
Breede et al. 2012, Near Surface Geophysics, 10, 479-489	Cylindrical d=8 cm e=10 cm 4 electrodes	Sand/Clay (5%) mixture saturated	100 $\Omega$ .m	900.
		Sand/Clay (20 %) mixture saturated	50 $\Omega$ .m	1,800.
Okay et al. 2014, Geophysics, 79(6), E353-E375.	Cylindrical d=20 cm e=10 cm 4 electrodes in square array	Saturated, kaolinite with 20% sand $\sigma_w=0.02$ S/m	25 $\Omega$ .m	540.
		Saturated smectite with 20% sand $\sigma_w=0.02$ S/m	3.3 $\Omega$ .m	1,800.
Kremer et al. 2016, Geophys. J. Inter. 207, 1303 – 1312.	Cylindrical e=40 cm d=30 cm Rectangular 4 electrode array over a section	Saturated silica sand $\sigma_w=15$ mS/m	Not given	234
		Saturated silica sand $\sigma_w=100$ mS/m	Not given	1,440.
		Saturated carbonated sand $\sigma_w=15$ mS/m	Not given	180.
		Saturated carbonated sand $\sigma_w=100$ mS/m	Not given	1,260.
Loewer et al; Geophysical Journal International 210, 1360-1373	Cylindrical cell length 70 mm d=20mm 4 electrodes array	Soil A: moist silty clay water content 0.358	12,6 $\Omega$ .m	1,000
		Soil B laterite water content 0.303	100 $\Omega$ .m	630
		Soil C humus water content 0.368	63 $\Omega$ .m	200
		Obersulzbacher sanstone Formation factor 34 Archie exponent 2.19	100 $\Omega$ .m	400
Revil et al. 2017, Water Ressources Research, 53, WR020655	Disk shaped d=7. cm e=2.5 cm 4 electrodes in Wenner array	Peat (AC_0580585123), $\sigma_w=0.031$ S/m	4.26 $\Omega$ .m	21,600.
		Clay (CW_0580586130), $\sigma_w=0.031$ S/m	7.1 $\Omega$ .m	14,400.
		Sandy Clay (AR_1126238AA) $\sigma_w=0.031$ S/m	5.85 $\Omega$ .m	10,800.
Revil et al. 2018 Geophysics, 83(2), E55-E74	Cylindrical 4 electrodes	Low porosity sandstone (Eocene deltaic formation) $\sigma_w=0.11$ S/m	42 $\Omega$ .m	25.

548 Table 2

549

550

Reference	Array configuration	Soil or rock context	Frequency	Electrical resistivity range	Relative permittivity range
Grard & Tabbagh 1991, J.G.R., 96-B3, 4117-4123.	1m x 1.17m rectangular array	Quaternary alluvial sand	128 kHz	500 – 2500 $\Omega$ .m	22. – 60.
Tabbagh et al. 1993, Geophysical Prospecting, 41, 579-597.	1m x 1.17m rectangular array	Sandy soil above rhyolite	128 kHz	1500 – 7000 $\Omega$ .m	10. – 200.
Przyklenk et al. 2016 Geoph. J. Int., 206 1352-1365.	Wenner arrays a=1m, 1.5m, 2m	Ice over Triassic limestone in a tunnel	10 kHz	17000 $\Omega$ .m	150
			30 kHz	9000 $\Omega$ .m	80
Souffaché et al. 2016, Archaeometry, 58-5, 705-721.	0.15m x 0.27m rectangular array	Lutetian calcareous stone in monuments	31.25 kHz	100 – 30000 $\Omega$ .m	5 - 10000

551 Table 3

552

Reference	Instrument & coil configuration	Soil or geological context	Frequency	Electrical resistivity range	Relative permittivity range
Huang & Fraser 2001, Geophysics, 66(1) 148-157	Helicopter borne Dighem HCP L=6.3 m	Crystalline basement in northern Canada	56 kHz	300 - 120,000 $\Omega$ .m	10 - 80.
Huang & Fraser 2002, Geophysics, 67(3) 727-738	Helicopter borne Dighem HCP L=6.3 m	At the center of a shallow lake in Northern Canada	56 kHz	2,800 $\Omega$ .m	65
Hodge, 2004, SEG 74th (abstracts), 660-663.	Helicopter born Dighem HCP L=6.3 m	Slave geological province, northern Canada	56 kHz	2,200 – 24,000 $\Omega$ .m	3.9 - 17.2
Kalscheuer et al. 2008 Geophysical J. int.,175, 486-514	Tensor RMT	Ävrö Island (Sweden) Granite	14 – 226 kHz	Granite median value 50,000 $\Omega$ .m	6
Benech et al. 2016 Near Surface Geophysics 14(4) 337-344.	CMD HCP and VCP L=1.28m & 0.71m	Salted clayey soil over a marl weathered substratum	30 kHz	2 - 15 $\Omega$ .m	1,500 – 30,000
Simon et al. 2019 Near Surface Geophysics 17, 27-41	GEM-2 HCP L=1.66m	Archaeological site bordering the shore line, Loam	21.03 kHz	12 - 80 $\Omega$ .m	2,000 – 4,300
			43.35 kHz	12 - 80 $\Omega$ .m	1,500 – 4,000
			89.43 kHz	12 - 80 $\Omega$ .m	1,200 – 2,200
Simon et al. 2019 Near Surface Geophysics 17, 27-41	GEM-2 HCP L=1.66m	Archaeological site Loam	21.03 kHz	44 - 700 $\Omega$ .m	1,400 – 2,600
			43.35 kHz	44 - 700 $\Omega$ .m	700 - 1300
			89.43 kHz	44 - 700 $\Omega$ .m	500 - 900
Kessouri et al. 2016 Geophysics 81(1) E1-E16	CE 120 prototype PERP L=1.2m	Clay loam	1.56 MHz	20 - 60 $\Omega$ .m	35 - 110
Kessouri et al. 2016 Geophysics 81(1) E1-E16	CE 120 prototype PERP L=1.2m	Sandy alluvial	1.56 MHz	650 – 10,000 $\Omega$ .m	8 - 18

553 Table 4

554

Reference	TDEM instrument	Local Geology	Cole-Cole interpreted parameters	$\epsilon_r$ 10 kHz	$\epsilon_r$ 100 kHz
Walker & Kojikawasaki, 1988, <i>Geoexploration</i> , 25, 245-254	EM37 400m x 400m central-loop	Permafrost, clay and/or gas hydrates	1000 m first layer $\rho_0=1000 \Omega.m$ , $m=0.5$ , $\tau=0.00069s$ , $c=1$ .	83.	1.
Flis et al. 1989, <i>Geophysics</i> , 54(4), 514-523	Early time SIROTEM 100m x 100m coincident loop	pelite/sandstone	layer 1 (15m thick): $\rho_0=22 \Omega.m$ , $m=0.13$ , $\tau=0.01s$ , $c=0.25$ layer 2: $\rho_0=600\Omega.m$ , $m=0.05$ , $\tau=0.01s$ , $c=0.25$	747.  9.	48.  1.
Descloitres et al. 2000, <i>J. App. Geo.</i> , 45 1-18 ;	PROTEM 47 100m x 100m Receivers at several offsets	Caldera of Fogo Volcano	60 m first layer $\rho_0=10000 \Omega.m$ , $m=0.85$ , $\tau=0.00002s$ , $c=0.8$	153.	37.
Hallbauer-Zadorozhnaya & Bessonov, 2002, <i>EJEEG</i> , 7, 239-264	KARIER 5m x 5m coincident loop	Hydrocarbon contaminated quaternary sand above Albian clay	20 m first layer $\rho_0=15 \Omega.m$ , $m=0.25$ , $\tau=0.00018s$ , $c=1$ .	4,626.	47.
Antonov & Shein 2008, <i>Russian geology and geophysics</i> , 49, 790-802	100m x 100m Coincident loop	Clay quarry overlain by quaternary alluvium	Second layer between 4 and 48m, $\rho_0=16 \Omega.m$ , $m=0.073$ , $\tau=0.00076s$ , $c=0.53$	755.	25.
Hallbauer-Zadorozhnaya et al. 2016, <i>J. App. Geo.</i> , 133, 16-24.	Zerotem 50m x 50m central loop	Marine clay	Fourth layer below 59 m $\rho_0=0.5 \Omega.m$ , $m=0.25$ , $\tau=0.0035s$ , $c=1$ .	7,275.	73.
Finco et al. 2018, <i>Hydrological Processes</i> , 32, 3954-3965	TEM-FAST 25m x 25m coincident loop	Sebkha Kelbia salted wetland	2 m first layer $\rho_0=1.5 \Omega.m$ , $m=0.84$ , $\tau=0.01s$ , $c=0.955$	83,300.	926..

555 Table 5

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