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Statistical approaches to assimilate ASCAT soil moisture information: Part I Methodologies and first assessment

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Land surfaces are characterised by strong heterogeneities of soil texture, orography, land cover, soil moisture, snow and other variables. These are very challenging to represent accurately in radiative transfer models which have a limited reliability over land, especially for observations such as given. This has resulted in difficulties for assimilation of land surface related satellite observations in numerical weather prediction models. Simple statistical relationships between the satellite observations and surface variables have therefore been considered in the last 20 years. In this study, we propose to compare two such approaches: the CDF-matching (used as a normalisation and an inversion technique) and the Neural Network (NN) methods. The CDF-matching finds a simple mono-variate relationship at the local scale and is very dependent on the LSM on which it is calibrated. NNs are global multivariate models able to exploit auxiliary information and the synergy of multiple instruments, but the solution is global and no local characteristics are constraining the solution. One of these two methods can be better suited, depending on the application, in particular the simplicity of the satellite/variable relationship. We illustrate here these concepts using the ASCAT (Advanced SCATerometer) observations for the SM retrieval in an assimilation context. The two approaches are compared and combined. We also compare the more traditional inversion scheme and the forward modelling that could be attractive for assimilation purposes. It is shown that in the context of SCAT, the inversion approach seems better suited than the forward modelling. It is also shown that it is possible to combine the global model obtained using the NN and the localised information of the LSM offered by the CDF-matching.

Key Words: Assimilation; remote sensing; soil moisture; neural network; CDF-matching; ASCAT.

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1. Introduction

Satellite observations are an important source of information for assimilation into Numerical Weather Prediction (NWP) models (????). Two different approaches to the assimilation of satellite observations can be considered: the assimilation of the raw radiances R or the assimilation of the retrieved products P . The assimilation process weights the different sources of information (i.e. satellite and model) based on their respective uncertainties (?). An uncertainty estimate for the satellite information is therefore necessary on R or P .

Forward model - Since reliable uncertainties on retrieved products are difficult to obtain (i.e. they are state-dependent and sensitive to several factors), the assimilation of raw radiances R instead of retrieved products P has been preferred in the past. The assimilation of R is possible only when the Radiative Transfer (RT) to simulate R is reliable enough. For instance, this has been the case for atmospheric applications, e.g. sounding of temperature and humidity atmospheric profiles. For many years the assimilation of radiances was restricted to clear skies, with careful screening for cloud and precipitation. However, a number of NWP centres have recently made significant progress in assimilating radiances in the presence of cloud and precipitation. This was made possible in part by improvements to scattering parameterisations in the RT models (?). The RT calculations are less accurate for surface simulations because required auxiliary parameters (soil texture, surface emissivities, vegetation state, *etc.*) are often difficult to obtain and have large uncertainties at the global scale. Furthermore, it is often assumed that observation errors can be represented by the sum of (1) a constant instrument error, and (2) a constant RT error, whatever the surface or atmospheric conditions. This simple assumption is satisfactory in many cases, but it can also be misleading since instrument and RT errors might be state-dependent (?) and very difficult to model (e.g., (?) for an investigation of more realistic assumptions for cloudy situations with microwave observations).

Inverse model - Since RT simulations at the surface are difficult, the assimilation of retrieved products P is a viable alternative to direct assimilation of raw radiances R . For instance, the assimilation of retrieved SM from satellite observations can be more useful (?) than the assimilation of the raw satellite data R . This has been shown for instance for SMOS (Soil Moisture and Ocean Salinity) observations (?). The assimilation of retrieved products P requires some estimation of the uncertainties, but they are often considered to be constant. In fact, estimating retrieval uncertainties is a difficult task but it should be noted that *a priori* errors (i.e., the error of the *a priori* information before the satellite observations are used in the assimilation) need to be characterised too, and this was not an easy task for the NWP community: uncertainty estimates were global at first, then latitudinally-dependent, and they became state-dependent (see for instance (?)) and this is still a subject of research. Such an effort can be performed too for retrieval errors. For instance, when retrieved by a classical optimal interpolation technique, a state-dependent error is provided by the theory (?). The same process can be performed with any statistical inversion scheme, including for the NN retrievals (?).

One important aspect of assimilation is that assimilated data need to be coherent enough with the numerical model. Otherwise, jumps will be generated in the time series of the model variables, with values alternating between the satellite observations and the model climatology. Therefore, an often adopted strategy is to bias-correct the satellite observations using globally available predictors, in order to better match the model at the pixel level. One example for atmospheric variables is variational bias-correction (?). Another form of bias-correction often used for surface applications is the CDF-matching (Cumulative Distribution Function) (????). With this approach, the CDF of the assimilated satellite information is first transformed towards the CDF of the corresponding variable in the model (both CDFs are assumed to be Gaussian), before the assimilation is done. This means that averages, ranges of values, and even physical units of the variable are harmonised. This process has some advantages and some drawbacks, which will be discussed below. The relationship between observation (backscatter) and variable (soil moisture) is not simple. However, thanks to many simplifications

and assumptions leading to a pixel by pixel temporal change detection retrieval for ASCAT, the relationship between satellite derived soil moisture and model soil moisture is represented by a simple relationship. The CDF-matching represents a simple scaling between the satellite measurement and the variable to retrieve, enabling it to be used as a local retrieval scheme (?).

NN are statistical models that allow for a link to be built between satellite observations and the geophysical variables to retrieve (???). They have mostly been used as a retrieval tool, in inversion mode. They can also be used as forward models to simulate satellite observations (?). This approach hasn't been used as frequently, in part because RT can be very complex and necessitates many inputs which are not always available. NN are designed to represent relatively simple, statistical relationships at the global scale, and very important physical dependencies might not be attainable only from a data-driven approach. A compromise could be found in the form of an hybrid model where inputs of the NN are chosen to simplify the forward model (as in the RTTOV model (???)) and physical relationships could be coded in the NN, the training would then estimate the appropriate coefficients of such relationships. Furthermore, the use of a NN direct model in an assimilation scheme would mean that errors are present in the forward (the NN) and the inverse mode (inside the assimilation), where a NN retrieval scheme would include only inversion errors.

Therefore, several strategies can be used to exploit satellite observations into land surface models. In this paper, two questions will be addressed in the context of the ASCAT observations: (1) should we develop an inverse (for the assimilation of retrieved products P) or a forward (for the assimilation of raw observations R) statistical model? (2) What is the best matching/inversion technique, NN or CDF-matching? While these approaches can be implemented separately, their combination will also be considered. The NN can bring its global perspective and its exploitation of auxiliary/ancillary information, while the CDF-matching can help improve the local matching of the satellite information with the LSM if this is required to facilitate the assimilation.

The ASCAT (Advanced SCATerometer) instrument (?) is an active microwave scatterometer acting in the C-band (5.3 GHz). The instrument is flown aboard the MetOp satellites with a revisit time of 1-2 days. It provides a backscatter value at a 25 km spatial resolution. The ASCAT soil penetration depth is typically around 1-2 cm, but can be significantly larger for very dry soils (?). A global dataset of surface SM has been built from ASCAT backscatter observations using the change detection technique (?). The EUMETSAT Satellite Applications Facility for Hydrology (H SAF) has adopted this approach for the development and production of level 2 ASCAT-derived surface SM products. The 25 km sampling H SAF product (??) is assimilated operationally in the UK Met Office and the ECMWF forecasting systems (????), and it is used for research developments in other NWP centres (?), but prior to assimilation the SM is bias-corrected via the CDF matching technique. The same ASCAT backscatter observations will be considered here for the retrieval of surface SM, but instead using the NN approach. In the past, ASCAT observations have been combined *a posteriori* with passive microwave observations (?) or combined as inputs to a retrieval process, e.g. (?). It is foreseen that the techniques presented in this paper could be extended to passive microwave observations such as those derived from the SMOS mission (??).

Section 2 gives the historical background of neural networks for satellite remote sensing. Section 3 introduces the datasets used in this study. In Section 4, the NN and CDF-matching are presented, including new CDF-matching approaches; and the diagnostics used in this study are proposed in the context of the assimilation framework. Experiments based on SM retrieval from ASCAT data are presented in Section 5. Finally, Section 6 concludes this study and provides some practical perspectives.

2. Neural network for satellite remote sensing

Neural Networks (NN) have been widely used in the field of satellite remote sensing, for more than 20 years, for the atmosphere (??), or the land (?) and ocean (?) surfaces. Two key limitations have driven the need to develop NN approaches: Firstly that no physical RT model is accurate enough for surface applications, and secondly, that no empirical SM database is large or representative enough to calibrate a statistical retrieval scheme. Therefore, ? proposed a NN approach based on four innovations:

- (1) *Use a NN for the retrieval of SM* - Although NN methods were not easily accepted initially, because they were considered as “black-box” approaches, their relevance to better understand physical problems is now widely acknowledged. NNs can extract in a synthetic way physical relationships buried in a large database. Hence, NN methods for satellite retrievals has grown tremendously in popularity in the past decade (??), with also recent enthusiasm on big data such as deep learning (?) and convolutional neural networks (?).
- (2) *Train this NN using model SM outputs* - The use of model SM to train the NN was strongly rejected in the early days of NN developments. It was thought at that time that a NN trained in this way would then only reproduce the spatial and temporal behaviour of the model, and consequently would be useless. This is wrong because the NN is trained at the pixel and instantaneous scales, with no information on location or time. Spatial or temporal patterns from the model are not imposed on the NN: Once trained, the NN temporal and spatial dynamics is driven by its inputs (i.e., the satellite observations) and not by the model. The NN can even be trained with an imperfect database provided that this database includes the general sensitivities required for the retrieval. The machine learning approach will find these general sensitivities and will remove any spurious behaviour not coherent with the input data. During the learning phase, the NN will not take into account these errors if they are not coherent with the satellite observations. ? illustrates this principle and show how to use it to identify suspect regions in the model SM, and ? checks how a synthetic error can be corrected by the NN. Therefore, an imperfect dataset can be used to calibrate a NN retrieval scheme. There are still controversial aspects regarding model-trained NN retrievals. For example, a NN retrieval was trained using SMOS SM retrievals performed using a physical inversion scheme (?) instead of using the SM model outputs, with the aim of speeding up the physical inversion scheme. This is a valid approach, since the NN is designed to reproduce the physical inversion scheme and it might correct some of its errors. However, the training using LSM SM outputs will continue to be preferable because they often provide better SM estimates at the global scale than the dedicated satellite datasets. Furthermore, there is no “incestuous” process prohibiting the use of a model-trained NN in the assimilation. The NN is trained using model data, just as the CDF-matching is calibrated using model outputs. Either way, this should not invalidate the assimilation of the retrieved SM observations.
- (3) *Facilitate the exploitation of SM satellite information by assimilating the NN-retrieved SM instead of using a “physical” forward model* - The assimilation community generally prefers to assimilate raw satellite observations instead of retrieved products. One of the reasons is that it is necessary to specify uncertainties of the data assimilated into the model. It is considered that errors on the satellite observations are easier to quantify than errors in retrieved products. However, errors in satellite observations are not trivial, they must include instrument errors (often considered constant in the microwave) but also RT errors and other errors of representation which are much more complex (??). Furthermore, “physical” forward models largely rely on empirical parametrizations that would be more accurate if they were based on NN approaches rather than simple linear regressions. For observations related to the atmosphere, RT errors are easier to specify (at least in clear sky), but when dealing with surface parameters, RT errors are large, highly state-dependent, and difficult to estimate (?). A characterisation of retrieved parameters is comparatively not so difficult because they are statistical in nature. LSM assimilation of retrieved surface products instead of the raw observations has now started (?) and it is a good alternative to direct assimilation of the radiances while no reliable-enough RT model is available.
- (4) *Use the synergy of multiple observations, in particular the passive and active microwave observations* - The use of multiple satellite data to perform a retrieval was not common practice in the past, and it is still not widespread for several reasons. For instance, assimilation centres prefer to use the observations of satellites in an independent way, for commodity and practical issues. Project management in space agencies is also a limitation for the use of several instruments. The European Space Agency (ESA) has recently implemented the approach where two independent datasets of SM are merged *a posteriori* for the ESA

CCI soil moisture (?) from passive and active microwave observations. Using the multi-instrument/multi-wavelength synergy by combining *a priori* the observations in the retrieval should, however, be more optimal than the *a posteriori* merging of retrieved products (?). In fact, NN are very good tools to exploit the synergy of several instruments, in particular for SM (?). Combining passive and active microwave observations is now in evidence (e.g. (?)).

These four propositions in ? are still valid because the difficulties listed then (i.e., lack of a reliable RT model or large-scale empirical SM database) have not yet been solved. The NN approach is now being accepted and developed in agencies such as CNES (Centre National d'Etudes Spatiales), ESA (European Space Agency), NASA (National Aeronautics and Space Administration) or ECMWF (European Centre for Medium-Range Weather Forecasts).

Note that neural network and physical inversion scheme should not be opposed and could be combined. For instance, a retrieval scheme needs to be available soon enough after the launch of a new satellite. So a physical iterative inversion scheme might be necessary, or a radiative transfer model should be used to build a synthetic database to train a neural network inversion. After the acquisition of about one year of data, real observations should be enough to train a NN model.

3. Datasets

In this paper we use ASCAT level 2 data and the latest ECMWF reanalysis ERA5 data of soil temperature, leaf area index, SM, and two-meter air temperature diurnal cycle amplitude (?). The study period is spanning several years, from 1 January 2016 to 31 December 2019. Both ERA5 and ASCAT observations are projected into a common 0.25°-resolution grid.

3.1. ERA5 database

3.1.1. Soil Temperature (ST)

ST is provided by ERA5 in four vertical levels: 0-7cm; 7-28cm; 28-100cm; and 100-289cm. We will use the value of the upper layer to be more closely linked to the SM remotely-sensed by the ASCAT measurements. Fig. 1 shows an example of a ERA5 ST layer 1 map for June 11th 2016. Only some ascending and descending orbits are represented due to the coincidence with all the data sources. It can be seen that ST can facilitate the identification of surface types (vegetated areas, arid regions, latitudinal location, *etc.*) so it can potentially provide information on the presence of water in the soil.

3.1.2. Leaf Area Index (LAI)

Vegetation information has an impact of the backscatter coefficient of the ASCAT measurements. So it is important to consider it especially at the global scale, but also at the local level when vegetation has a seasonality (?). Several variables describing vegetation could be considered such as the LAI or the Normalised Difference Vegetation Index (NDVI). The LAI is privileged here because it is more easily expressed in the model. Satellite datasets could be used here to document the vegetation (e.g. (???)), as ancillary information. Since the objective is in this study to exploit the ASCAT SM information in the ECMWF LSM assimilation scheme, the ERA5 LAI is chosen. An example of ERA5 LAI is also presented in Fig. 1.

3.1.3. Amplitude of the diurnal cycle of surface temperature ΔT

As shown in ?, the amplitude of the diurnal cycle of temperature is strongly related to the SM and hence, can be used to quantify the presence of water in the soil. The higher the SM is, the higher the thermal inertia becomes, implying a lower ΔT . See Fig. 1 for an example of ERA5 ΔT on June 11th 2016.

Figure 1. June 11th 2016, maps of auxiliary information from ERA5. From top to bottom: Soil Temperature at layer 1 (ST 1), Leaf Area Index (LAI), and amplitude of diurnal cycle of Temperature (ΔT).

3.1.4. Soil Moisture

SM is provided in ERA5 for several layers: levels 1 (0-7 cm); 2 (7-28 cm); 3 (28-100 cm); and 4 (100-289 cm). In the following, we will focus in the layer 1 since this is the level that ASCAT observations are most sensitive to. SM is provided as volumetric soil moisture in m^3/m^3 . Since SM is the objective in this study, this will be a strategic variable for the calibration of the retrieval schemes and for the evaluation of the SM information content. Fig. 2(top/left) represents an example of SM provided by ERA5, expressed in m^3/m^3 , for June 11th 2016.

3.2. ASCAT information

ASCAT is a C-band (5.255 GHz) scatterometer using vertically polarised antennas (?). Ground echoes are received by the instrument and, after de-chirping, the backscattered signal is spectrally analysed and detected. On board ASCAT, two sets of three antennas measure the resultant electromagnetic backscatter, in two 500 km wide swaths, on each side of the satellite ground track. ASCAT instruments are onboard the Metop-A (launched on October 19th 2006), Metop-B (launched on 17th September 2012), and Metop-C (launched on November 7th 2018) satellites. The Metop series is constituted of polar orbiting meteorological satellites that form the space segment component of the EUMETSAT Polar System. Metop satellites are in a lower polar orbit, at an altitude of 817 km, to provide observations of the global atmosphere, oceans and continents.

ASCAT has been designed primarily to measure wind speed and direction over the oceans. However, ASCAT has also proved to be very useful for the retrieval of several other geophysical variables. In fact, the backscattering coefficient σ , measured with scatterometers, is dependent on the dielectric properties of the soil surface layer, surface roughness, and vegetation. In particular,

Figure 2. June 11th 2016. Left: from top to bottom, SM from ERA5, retrieval from ASCAT retrieval, CDF-matching of ASCAT σ_{40} (Experiment 1), NN retrieval (Experiment 2), and NN+CDF retrieval (Experiment 3). Right: from top to bottom, σ_{40} from ASCAT, from NN direct model (Experiment 4) σ_{40} , and NN+CDF direct model (Experiment 5)

177 increasing the fraction of water contained in soil increases the dielectric properties thus ASCAT measurements can be used to retrieve
 178 SM. With the rapid global coverage, day or night and all-weather operation, ASCAT offers a unique tool for long-term climate studies.

179 One huge advantage of active measurements (compared to passive microwave observations) is their spatial resolution, suitable for
 180 agricultural or small-scale hydrology applications e.g., (?). The major issue when using this type of data is the contaminating effect of
 181 other parameters such as vegetation or roughness. For instance, Woodhouse and Hoekman (??) estimated SM with an inversion method

that incorporates both a model and *a priori* quantitative information, at the global scale. However, modelling such complex signals are very difficult so another strategy has been introduced to derive a SM index at the pixel level to produce a global SM database (??). This localisation of the retrieval allows for the suppression of the spatial variabilities in the contaminating effect.

The local incidence angle of the ASCAT measurements varies. In order to obtain a dataset in which the samples are comparable to each other, a linear regression has been performed to express the measured backscatter as a function of the incidence angle for each pixel. This regression function was then used to interpolate the measurements to a common incidence angle of 40° in a manner similar to the one proposed by ?, reducing the influence of the vegetation cover on the signal. This harmonisation of the ASCAT measurements are done in a very simple way (i.e. linear regression) and when using these transformed backscatters, the underlying hypothesis is that vegetation has no impact or remains constant along the time, which is not always satisfied. The transformed ASCAT data will be denoted by σ_{40} (?) in the following sections of this paper. Fig. 2(top/right) represents an example of σ_{40} for June 11th 2016.

This σ_{40} has been used to retrieve soil moisture. ? define a Soil Wetness Index (SWI) between 0 and 100 by normalising observations of σ_{40} using their minimal and maximal values (estimated over a long time series): a linear transformation is used to set the historical extremes of $f(p)$ to 0 and 100. This type of approach is performed on a pixel-by-pixel basis since a dedicated retrieval is defined for each location. The SWI needs to be transformed into a SM using a reference, for instance from the ECMWF model: The $SWI = 0$ is associated to SM_{min} and $SWI=100$ is associated to SM_{max} , both SM values provided by the model. So in fact, the retrieval is calibrated on the model, at a pixel scale. The quality of the retrieval is based on several aspects: for instance, a long time series of observations is needed to capture the extremes and a good estimation of SM should be provided by the reference model.

3.3. Preliminary analysis

A preliminary analysis of the ERA5 and ASCAT data is conducted at global scale, for the period 2016-2019, to assess their large-scale spatial and temporal variabilities. All the collocated samples of the database are gathered, whatever the location and the time, and then statistics can be performed to analyse the links among the variables. Fig. 3 represents the correlation matrix between the variables

Figure 3. Correlation matrix between the variables present in the database, at the global scale, and for multiple years (January 2016 to December 2019).

gathered in the database, at the global scale and for several years. The bottom row represents the correlations of the other variables with the ERA SM, so it provides an indication of the SM information that can be obtained from the ASCAT and the auxiliary variables. The σ_{40} backscatter from ASCAT is correlated at the 0.61 level with SM. ERA5 ST 1 is only negatively correlated at -0.31. The LAI vegetation variable is highly correlated with SM (0.64). The amplitude of the diurnal cycle of temperature, at the -0.59 level, is also a very good information for the SM. These numbers are coherent with the results in ? and ?.

Since these correlations integrate all the locations, for all the seasons, this is only a very general measure. Correlations could be obtained at the pixel scale, sometimes with higher correlations. It would be misleading to directly compare the correlations in Fig. 3 and temporal correlations at the pixel level because these two correlations measure different relationships. The correlations of Fig. 3 integrate the changes in σ_{40} that are related to other factors than the SM such as for instance the vegetation or the roughness of local conditions. The ASCAT σ_{40} is as sensitive to vegetation than to SM, meaning that if used at the global scale, both SM and vegetation information need to be delineated. These contaminating factors reduce the σ_{40} -to-SM link at the global scale. This is why when considering global relationships, it is necessary to use auxiliary (i.e. from ERA5) and even ancillary (i.e. independent from ERA5) information. Therefore, a choice needs to be made between global and local relationships, or a way to combine both approaches is necessary if we want to improve both aspects.

4. Methodology for the exploitation of soil moisture information

CDF-matching is a pixel-based and simple model used to rescale satellite data towards the model, prior to assimilation. Several CDF-matching approaches will be presented here, including new ones. CDF-matching can also be used as a retrieval scheme, for simple cases like the retrieval of SM using scatterometer data. On the other side, NNs aim at a more complex, multi-parameter global relationship between the satellite observations and the SM. These two approaches have not the same objective but they share several features. Their similarities/differences and advantages/drawbacks will be discussed and compared. The possibility of combining them will also be presented.

4.1. CDF-matching

CDF-matching is a general and simple idea where the CDF of one variable p is transformed using a function f to mimic that of another variable t . However, this can be done in various ways, and for multiple objectives.

4.1.1. Methodology

Several versions of the transformation f can be used for the CDF-matching:

Gaussian matching - The first approach is the classical CDF-matching technique used in NWP centres such as at ECMWF. The objective is to transform p (satellite observation) so that the CDF of $f(p)$ is similar to the CDF of t , under the Gaussian hypothesis. In this case, prediction p and target t are of similar nature (e.g. SM information). Let μ_p and σ_p be the mean and standard deviation of p ; and μ_t and σ_t be the mean and standard deviation of the target t . If the p and t distributions are Gaussian, the objective is to get the mean and standard deviation of $f(p)$ closer to those of t . The linear transformation f is then chosen following:

$$f(p) = A + B \cdot p, \text{ with } \begin{cases} B = \frac{\sigma_t}{\sigma_p} \\ A = \mu_t - B \cdot \mu_p \end{cases} \quad (1)$$

This transformation f offers a perfect bias-correction and normalisation of p towards t , but the CDFs will agree only if the PDFs of p and t are Gaussian. This means that the CDF-matching will not be optimal if, for instance, there are more extremes than with a Gaussian distribution (i.e. positive kurtosis), or if the distributions are not symmetric (positive or negative skewness) which is often the case with variables ranging between fixed thresholds such as with $0 \leq \text{SM} \leq 1$. Linear functions do not improve correlation, so $\text{COR}(p,t) = \text{COR}(f(p),t)$. Actually, the relationship in Eq. (1) is performed at ECMWF at the monthly scale (with a 3-months moving window): This can then improve the correlation at the seasonal scale: $\text{COR}(p,t) \leq \text{COR}(f(p),t)$.

241 *Binning approach* - Another method focuses on an empirical representation of the CDF rather than on the Gaussian assumption
 242 used in the first approach. A binning is first performed (e.g. regular or by quantile) on both t and p variables. The transformation f
 243 is then represented by the association of each ordered bin: e.g. each data in the first quantile of p is associated to the average of the
 244 first quantile of t . This approach should preserve better the extreme values of t and this technique can handle non-symmetric PDFs
 245 because no assumption is made on the distributions of p or t . The obtained transformation $f(p)$ provides discretised values, but the
 246 discretisation resolution depends only on the chosen binning; and continuous functions (splines, polynomial) can be used to link the
 247 bins if continuity is an issue.

248 *Function approximation* - A function approximation can be used to obtain a relationships f from p to t . What is new in this approach
 249 is that the observed sample-to-sample link between p and t in the reference dataset is actually used, contrarily to the first two CDF-
 250 matching approaches that work independently on the p and t spaces to estimates the CDFs. This link can be interesting to exploit: It
 251 will be seen in the following that this is what the NN methodology does, as any machine learning technique. Another advantage is
 252 that a continuous transformation is obtained, and it is possible to control the complexity of f based on physical constraints (monotonic
 253 function or not, smoothness of the physical link, *etc.*). As for any function approximation, it is not entirely sure that extreme events
 254 can be well preserved/represented, this needs to be checked for each particular case. Non-symmetric and non-Gaussian distributions
 255 can be processed if f is chosen to be non-linear. Since this method is richer (i.e. more freedom in the choice and complexity of the
 256 transformation f), this method is more complex to control and subject to instabilities, but constraints can be used to stabilise it.

Approach	Method	Matching object	Database	Auxil. info.	Link x/y ?	Extremes	Linearity	Improv. corr.?
CDF-matching	Gaussian match	CDF mean & std	Pixel	No	No	Not really	Yes ⁽¹⁾	No ⁽¹⁾
	Binning	Empirical CDF			No	Yes	No	Yes
	Fct. approx.	Linear relationship			Yes	Not particularly	Yes	No
		Nonlinear relation.			Yes	Depend	No	Yes
Neural Network	MLP	Multivar. relation.	Global	Yes	Yes	Not particularly	No	Yes

Table 1. Feature comparison of the CDF-matching and NN approaches for function $x \rightarrow y$. The sign ⁽¹⁾ means “except if seasonal”.

257 Table 1 compares several features of these three CDF-matching approaches. One way to chose the right technique is to monitor the
 258 scatterplot between p and t . The symmetry of the PDFs, proportion of extreme cases, or the non-linearity of the relationship between
 259 the two variables should determine which method to use. Practical tests should also be performed to analyse the spatial pattern of the
 260 diagnostics. The transformation f can be linear or non-linear. A linear transformation can be good enough if the p -to- t link is simple
 261 enough at the pixel scale. In the case of a linear f , the correlation is not changed ($\text{Cor}(p,t) = \text{Cor}(f(p), t)$). If the scatter plots between p
 262 and t are complex, a nonlinear f can be chosen, and this can potentially improve the correlation: $\text{Cor}(p, t) \leq \text{Cor}(f(p), t)$.

263 The CDF-matching works at the pixel level to exploit mainly the temporal information of the satellite observation. This means that
 264 spatial patterns in the satellite observations can be transformed toward the LSM. The objective here is to use the dynamics of the
 265 satellite observation, and less its spatial pattern.

266 4.1.2. Rescaling tool

267 Let p be a prediction (e.g. a satellite SM retrieval) and t be the corresponding target retrieval (e.g. the reference SM). A “rescaling”
 268 technique intends to find a transformation $f(\cdot)$ of the satellite estimates so that $f(p)$ is “closer” to the model variable t . For instance,
 269 the goal is to perform a bias-correction and/or transform the range of variability. The most widely used rescaling technique in the
 270 context of assimilation is the CDF-matching. This method is often used *prior* to the assimilation of the satellite information into LSMs.
 271 The general objective is to find a transformation f so that the $\text{CDF}(f(p))$ is similar to $\text{CDF}(t)$. This transformation is done at the
 272 pixel level. The fact that averages and ranges of values are put in agreement facilitates the assimilation of $f(p)$ by avoiding jumps in
 273 the model variables. In general, the CDF-matching does not change the ordering of the satellite data at the pixel scale, but only their

274 dynamics. This is true if the CDF-matching transformation is strictly increasing which is the case in general. At ECMWF, the CDF
 275 matching performed using a different transformation for each month so the annual ordering could potentially be changed in this case.
 276 But the idea behind the CDF matching is really to not changed the ordering of states locally at the pixel level. Temporal correlations
 277 can actually be changed after the CDF-matching, but mostly if we use a nonlinear transformation. However, it is important to note that
 278 the spatial pattern of the satellite information can be transformed, towards the spatial pattern of the model, because spatial ordering of
 279 the satellite data is not preserved. This can truly distort the spatial information from the satellite towards the patterns of the model.

Figure 4. CDF-matching examples over two pixels for SM (two top lines), and σ_{40} (two bottom lines). From left to right: (1) The scatter plot of the NN estimate versus the target data; (2) Same but with a linear regression and 3^{rd} -order polynomial fits; (3) Scatterplots of the targets with respect to the satellite observation (NN estimate, and CDF-matched with linear and polynomial fit); (4) The PDFs of the NN estimate and the corresponding CDF-matching; (5) The time series of the target, NN estimate, and CDF-matching (3^{rd} -order polynomial fit).

280 Fig. 4 illustrates the CDF-matching for two SM examples and two σ_{40} examples. The first column represents the scatter plots
 281 between the estimate p (x-axis) and the target data t (y-axis). The agreement between the σ_{40} is not exceptional for these two locations
 282 (correlations of 0.53 and 0.62) probably because other surface parameters such as vegetation impact the backscatter. Correlations for
 283 the SM is higher (0.73 and 0.71). The goal of a CDF matching should be to transform the x-axis so that the scatter plot becomes as
 284 close as possible to the diagonal line. This figure illustrates the CDF-matching by function approximation: in the second column, linear
 285 and 3^{rd} -order polynomial fits are used to find the optimal link between p and t . When applied to the estimate p , these fits f transform it
 286 towards the target t : in the third column, the original scatter plot in blue is translated toward the diagonal line for both CDF-matchings.
 287 As a consequence, the PDFs get closer (from blue to green) to the reference PDF (in red), in the fourth column, although the matching
 288 is not perfect as the quality of the original scatter plots determines the quality of the fitting that can be obtained by the CDF-matching
 289 procedure.

290 The last column in Fig. 4 represents the time series of the target, original and CDF-matched variables. The blue time series
 291 (prediction) is well translated in green to the black one (target). The linear fitting does not impact the dynamics of the variable, the

non-linear fitting can potentially change part of this dynamic. This can be seen on the correlations before and after the CDF-matching, given for the four samples of Fig. 4 in Table 2. As expected, the non-seasonal linear CDF-matching has no impact on the correlation, it is just a rescaling technique, like the Gaussian CDF-matching approach. The non-linear CDF-matching on the contrary can increase the correlation, as expected.

Variable	COR(p,t)	COR(Lin(p), t)	COR($(P_3(p),t)$)
SM	0.729	0.729	0.763
SM	0.709	0.709	0.752
σ_{40}	0.533	0.533	0.580
σ_{40}	0.619	0.619	0.648

Table 2. The correlations before and after the CDF-matching (linear and 3rd-order polynomial fits) for the four samples of Fig. 4.

The CDF-matching by function approximation could be criticised because it can significantly change the satellite observations towards the target. It was commented earlier that this was a criticism for NNs trained on model data. However, the CDF-matching is a simple, mono-variate function, often monotonic (i.e. mostly an increasing function for CDF-matching). The CDF-matching does not change the nature of the satellite observations, except in the case of a negative correlation between p and t : with the Gaussian and binning techniques, the sign of the correlation cannot be changed, but the function approximation approach can invert the correlation sign by using a decreasing function f . However, if the two variables p and t (supposed to represent the same variable for a CDF-matching) are negatively correlated in some locations, it means that the satellite retrieval p is of very poor quality and should not be CDF-matched for assimilation.

CDF-matching is generally done at the pixel level to exploit the temporal information of the satellite data. Actually, the CDF-matching could also be done by gathering all the data for all the pixels, so that the CDF-matching is performed on both the temporal and the spatial variations. This would mean that the overall CDFs of the two datasets would be put in agreement (e.g. same global mean, same extremes) but this would not modify the spatial pattern of the satellite observations towards the model. In this way, the CDF-matching retrieval scheme could be more directly compared to the NN retrieval that will be presented in the following section.

4.1.3. Retrieval scheme

? define a Soil Wetness Index (SWI) between 0 and 100 by normalising observations of σ_{40} using their minimal and maximal values (estimated over a long time series): a linear transformation is used to set the historical extremes of $f(p)$ to 0 and 100. The rescaling by extreme values is not based on the full CDF information so the $CDF(f(p))$ can differ from $CDF(t)$. In order to be exploitable for assimilation, this index is then generally CDF-matched to the model SM so that the SWI are not between 0 and 100 but rather between the minimal and maximal value of t (in each pixel). A direct and unique rescaling by extreme can be done directly on the σ_{40} to the minimal and maximal values of m . These two approaches are mathematically equivalent and the simpler approach should be preferred.

When the σ_{40} /SM relationship is simple enough, the CDF-matching can even be used as a simple retrieval scheme. When using such an approach, the underlying hypothesis is that the ASCAT backscatter σ_{40} might be related to the SM and other parameters; but when considered locally in one pixel, the σ_{40} is only dependent on the SM (the other variables do not vary). In this way, the link between the satellite observation σ_{40} and the variable SM becomes simple enough to be represented by a mono-variate relationship. This might be true for variables constant in time such as soil texture, but it is not valid everywhere for variables such as vegetation*. So this approach can appear simplistic, but it might be adequate in some locations, and it is at the basis of the retrieval schemes developed for ASCAT retrieval of SM.

*Remember that the ASCAT backscatter is estimated at 40° incidence angle because it is less sensitive to vegetation in this case, but this is not a perfect approximation of course

The retrieval here is based on a target t variable from the model. If a global dataset of real observations is available, the retrieval could be calibrated on it. But the training using a model reference is an interesting approach potentially helping the assimilation, as long as the temporal variability of the satellite observation is preserved in the $f(p)$. The retrieval is performed at the same time as the CDF-matching is done.

As for the CDF-matching, the function approximation can use a decreasing or increasing function f to change the sign of the correlation. Again, if the correlation between p and t has not always the same sign at the global scale, a problem in p is probable. For instance, it can mean that an auxiliary information is truly necessary to describe a more complex link between the two variables, and some additional work would be required so that the correlations have the same sign in all locations.

4.2. Neural Networks

4.2.1. Model

Among the NN techniques that can be used to perform satellite remote sensing, the MLP (Multi-Layered Perceptron) (?) is certainly the most widely used. We will use this model but other neural architectures could be chosen instead, such as deep learning networks. A MLP is a non-linear mapping model: Given an input X , it provides an output Y in a non-linear way. The neurons are organised in successive layers. Each layer in the NN is composed of individual neurons. A neuron performs first a weighted average of its inputs from the previous layer. The so-called synaptic weights are associated to each connection between two neurons. Every neuron has a connection with all the neurons of the previous layer for a fully connected network. Once this weighted average is done, a non-linear sigmoid function g is applied, the Tanh function is used here. The final output of a neuron i is then given by:

$$y_i = g \left(\sum_{j=1}^N w_{ji} x_j \right) \quad (2)$$

where $(x_j; j = 1, \dots, N)$ are the N inputs of neuron i , and w_{ji} is the synaptic weight between neuron j and i (?). The MLP model is defined by the number of input neurons (i.e., the size of the inputs), the number of outputs, and the number of neurons in the hidden layers that control the complexity of the model. A study has to be conducted to define the optimal number of hidden layer(s) and the number of neurons in the hidden layer(s). A balance needs to be found: Too many free parameters in the model can result in over-learning (over-parameterisation) leading to degraded generalisation properties. On the contrary, too few free parameters will yield under-parameterisation and bias errors in the model. Provided that enough samples are available to train the NN, any continuous relationship, as complex as it is, can be represented by a MLP (?). Furthermore, in ?, a theorem shows that a two hidden layer NN is able to represent any discontinuous function which can be an important feature for inverse problems.

The estimation of the optimal parameters of the NN is performed during the training stage. For that purpose, a loss function is first defined (the least-squares is used here as done usually). Then, a gradient descent algorithm allows to find optimal parameters so that the NN estimates are as close as possible to the actual outputs provided in the learning database.

4.2.2. NN database

Once the NN architecture is defined, a training dataset including input/output couples is required to determine the weights W in the model. A quality criterion is defined to specify how well the NN reproduces this training dataset (e.g. least squares). An optimisation algorithm improves this quality criterion (by reducing the errors) in order to find the optimal parameters W . The optimisation algorithm is the back-propagation algorithm from (?). It is a stochastic gradient descent that has been optimised to the hierarchical structure of the NN to speed up the learning stage.

Learning databases to train NN are generally built in two ways. First, a collection of states (e.g. SM plus other variables) are used as inputs for a RT model to obtain associated simulated satellite observations (e.g. σ_{40}). We call this approach “physical” as it uses a physical model to construct the database. As mentioned earlier, such forward RT models for surface properties are not yet fully satisfactory. Second, a collection of true satellite observations is put in coincidence with a large and representative collection of true SM *in situ* measurements. Again, this approach is not possible in our case because such collection of SM measurements is not available.

It was proposed in ? to use real satellite observations (σ_{40}) with SM from a reanalysis (such as SM from ERA5). Over the whole database constructed to define the NN, representing more than 1 million points, 60% are kept for the learning, 20% for the testing, and 20% for the validation. These three datasets have been selected randomly. Since the number of samples in each one is very large, their statistical characteristics are similar. (1) The training of the NN is performed on the learning database. (2) The testing database is used in parallel to the training process: at each learning step, the learning database is used to improve the parameters of the NN model. The testing database is not directly used to change the NN parameters, but it is used in each step of the learning to monitor the results of the NN in an independent database. This allows measuring the generalisation capacity of the NN, i.e., its ability to perform retrievals on new data. During the learning, the generalisation errors are monitored and the learning is stopped when, after a decrease, they start to increase. This procedure avoids the over-training of the NN, i.e., the problem in which an algorithm performs very well on its learning data set but poorly on new data. (3) The testing database is used several times, first to measure the generalisation capacities of the NN on each step of the learning process, second for all the tested NN configurations. As a consequence, the whole NN selection process could “learn” the testing database (i.e., be biased toward it) and the evaluation of the generalisation errors could become misleading. To avoid this problem, another independent database is used: The validation database. It is only used to estimate the retrieval errors on an independent data, once the learning is complete, and once the model is chosen.

There are several advantages of the NN training of SM-retrieval based on reanalysis data. For instance, the obtained SM is “compatible” with the SM of the reanalysis model: the overall histogram of SM at the global scale should be relatively close to that of the model. This means that definition of SM and its units are compatible. Contrarily to the CDF-matching done at the pixel-level, this is only true at the global scale. It means that systematic biases can be present regionally: (1) The satellite observations might not have enough information to change their estimate at the regional scale and the model has more information. In this case, some auxiliary information could be added to the NN retrieval to compensate for this. (2) The model can also be wrong, and the retrieval which is based on the observation does not agree with it. What is important is that the NN retrieval of SM should be based on the satellite information, because this is what we want to exploit in the assimilation.

Another advantage of learning on reanalysis data concerns the use of multiple instruments. Instruments can be different at the same time (like passive and active microwave observations), or they can be similar ones but consecutive in a long time-record. Having a same reference (i.e. the reanalysis) to train each retrieval is a true advantage for their inter-calibration.

4.3. *Quality criteria*

We want to compare several technical configurations using CDF-matching or NN to extract SM information from the ASCAT instrument. Some diagnostics are therefore needed to measure the quality of the proposed solutions. It is not easy to compare agreements in the satellite observation space (p) and on the model variable space (t). The following quality criteria measure some type of coherency between the satellite observations and the model. This is required to assimilate the satellite observations into the model. However, the objective cannot be to get too close to the model, otherwise there would be no additional information in the satellite observations. We will comment, in the discussion, on the spatial and temporal information included in the satellite observations and how they are preserved by the different approaches.

Three types of metrics will be considered in the following:

- The temporal correlation between the satellite observation and the model SM, on each pixel. This measure indicates if the dynamics in the satellite observation is coherent enough with the ERA5 data. As mentioned in the introduction, the dynamics of satellite observations are the most important feature for assimilation so some calibration techniques are often used in NWP centres to suppress differences in absolute values but preserving the dynamical behaviour.
- The range of variability of the satellite observations compared to the model will also be assessed. The minimal, maximal and range of values will be compared between the model and the satellite observations, to make sure that variables are actually similar (several units can be considered for measuring SM), and that they comparable extreme distributions. Regression model predictions are always inside the range of variability of the dataset used to train them.
- Bias and standard deviation errors will also be measured between the model and the satellite observations. These diagnostics indicate differences between the two estimates not in relative terms (like the correlation) but in terms of absolute values.

Each time, the same sample dataset will be used for the satellite observations and the model so that if one data is missing for one, it will not be taken for the other. In this way, statistics can reliably be compared to each other.

NN are un-biased estimator model. This means that the average of the estimations is equal to the average of the targets present in the learning database, so there should be no biases between the target (model) and the estimated (NN) estimates. But this is true only at the global scale, when mixing all pixels and all time steps. Local biases can be encountered regionally due to very particular conditions and/or missing auxiliary information. CDF-matching, by definition, do not have biases at the pixel level because the calibration has been done pixel by pixel for that purpose.

As any other statistical models, NN will always tend to dampen the range of variability of the target dataset (model). This is due to the fact, again, that some information on extreme cases is missing so the statistical model provides “averaged” values for these extremes. The CDF-matching technique, in opposition, is by definition following the range of variability of the target dataset (model), minimal and maximal values will be respected, as long as the training dataset for the CDF-matching is large enough to include these extremes. However, it does not mean that extremes will be well retrieved, as extremes on both datasets (objective and estimation) can occur in totally different times of the dataset record.

Again, if the target (model) is wrong, it does not mean that the NN will reproduce these errors. In fact, the NN model tries to obtain global physical relationships that link the inputs and the output, at the pixel scale. This means that no spatial or temporal error structures of the model would be reproduced by the NN because it actually has no information about the localisation of each pixel. The NN can be trained using the ERA5 model but if ERA5 is wrong, it will correct it because after the training stage, the spatial and temporal variability in the NN outputs are only driven by the observations, not the model. If a regional incoherency is present in the model, the NN would try to correct this incoherency between the regional and the global scales.

It is clear that each diagnostic provides different information on the similarities of the datasets (range of values), on the statistics (bias and STD errors) and on the agreement (correlation) between the datasets. Table 1, indicates the methods that can improve the correlation or not, or those that represent better the extremes.

5. Experiments and results

In this paper, five experiments will be conducted. Three of them (Exp. 1, 2, 3) are designed to perform a retrieval, i.e. estimate SM based on the satellite information; and two (Exp. 4, 5) aim at representing a forward model, from the SM to the satellite observation (see Table 3). These inverse and forward models are investigated to help making the decision between the assimilation of retrieved SMs or direct observations σ_{40} . Experiments use the CDF-matching approach (Exp. 1), the NN method (Exp. 2, 4), or a combination of them (Exp. 3, 5). The scheme in Fig. 5 illustrates how these five experiments try to relate the two spaces: satellite observations and SM.

Mode	Experiment number	Inputs	Model	Learning outputs	Inputs to assimilation
Inverse	1	ASCAT σ_{40}	CDF-Matching	ERA5 SM	SM
	2	ASCAT σ_{40} +ST1+LAI+ ΔT	NN		
	3	ASCAT σ_{40} +ST1+LAI+ ΔT	NN+CDF		
Forward	4	ERA5 SM +ST1+LAI+ ΔT	NN	ASCAT σ_{40}	σ_{40}
	5	ERA5 SM +ST1+LAI+ ΔT	NN+CDF		

Table 3. Description of Experiments 1, 2, 3, 4, and 5. SM is soil moisture.

Figure 5. Scheme representing the five strategies (in green) to exploit the ASCAT information for SM. The green arrows represent the experiments with the input and output variables that are used in each model. Experiments 1, 2, and 3 use ASCAT data to estimate a SM compatible with ERA5, and experiments 4 and 5 intend to build a forward model using input ERA5 data to estimate a backscatter σ_{40} compatible with ASCAT.

In the following, the computational coast will not be mentioned as both the CDF-matching and NN are very fast and negligible for any NWP center. The NN method is slightly faster than the CDF-matching, but the CDF-matching speed depends on the used approach (Gaussian matching, binning approach, function approximation), see Section 4.1.1.

5.1. Retrieval schemes

Experiment 1 uses the retrieval scheme based on the CDF-matching technique (section 4.1.3). The CDF-matching here is not only a rescaling but an inversion process. This approach intends to find a direct and simple relationship (i.e. third-order polynomial function) between the ASCAT σ_{40} and the ERA5 SM. Only the ASCAT backscatter is used as an input here, but the inversion is performed at the pixel level to compensate for this lower information content compared to other retrieval schemes. Fig. 2(left column, third row) represents the SM retrieved using this scheme: the general spatial pattern is quite well represented by the CDF-matching retrieval when compared to the ERA5 SM.

Experiment 2 uses the NN approach presented in section 4.2. This is the NN solution introduced in ?, used later on in ?? and ?. The inputs for the retrieval are the ASCAT real observations σ_{40} plus the ERA auxiliary information (ST1, LAI and ΔT). The NN uses four

inputs, ten neurons in the hidden layer, and one output coding the SM. Fig. 2 (left column, fourth row) represents a daily retrieval. The spatial pattern is very close to that of the ERA5 SM (top row). It can be noted that compared to the CDF-matching retrieval of Exp. 1, the extreme positive values (larger SM) are less well retrieved by the NN. This is to be expected because the NN uses a compromise between all the pixels at the global scale, and this means that extremes are reduced. Additional information would be required in order to better characterise these extremes everywhere.

This is exactly the objective of *Experiment 3* that combines the NN of Section 4.2 and the CDF-matching of section 4.1.2. As in Exp. 1, the extreme values are a better fit to ERA5 SM.

Fig. 6 represents on the left the correlations between the target (ERA5 SM for Exp. 1, 2, 3) and the estimation. For SM, the Exp. 1 CDF-matching of the σ_{40} appears to have overall the best correlations except in some regions (Europe, Northern part of South America, Eastern USA, mountains (Himalaya and the Andes) and part of the Sahara desert) where Exp. 3 can have higher correlations. Bias errors are equal to zero for the Exp. 1 and 3 that use CDF-matching. This is logical and we see that the purely NN retrieval of Exp. 2 that intends to find a global relationship has some limited regional biases, as mentioned in Section 4.2. The third column in Fig. 6 represents the Standard Deviation (STD) of the errors. It is noticeable that Exp. 2 and 3 have almost the same STD errors (only the regional bias errors are corrected by the CDF-matching). The regions where Exp. 3 seems better than Exp. 1 are the same as for the correlation. The fact that the global NN performs better in these regions means that the auxiliary information (ST1, LAI and ΔT) is important for the SM retrieval and that σ_{40} alone is missing this information.

Fig. 7 (third row) shows that the NN approach is able to extract information from the ASCAT observations and the auxiliary information to fairly well reproduce the extremes of the ERA5 SM. The fourth row shows that combining the NN and CDF-matching approaches enables the extremes of the ERA5 SM to be better captured. Using one or the other really depends on what we want to achieve with the retrievals. In the context of weather forecasting in NWP, the CDF-matching is desirable to facilitate the assimilation.

Annex 7 provides some statistics about minimal, maximal and range of variability for these three experiments.

5.2. Forward modeling

Physical (?) and empirical (?) RT forward models are available, but their accuracy is not entirely satisfactory yet and simulations still have significant errors compared to real observations, challenging the strategy of assimilating raw observations such as the ASCAT σ_{40} . One reason is that input parameters are not available at the global scale. Furthermore, processes are so complex that it is difficult to characterise them at the global scale. This explains why assimilation of retrieved SM has gained interest (?). Is the NN ability to capture simple but general relationships at the global scale good enough to simulate with enough accuracy the ASCAT backscatter σ_{40} ?

Forward RT modelling using NN has been tried (e.g., ?) but this approach has been rarely used in the past compared to the inversion. One explanation is that physical models are available in many applications. This is true for atmospheric variables for which RT models are more reliable, but less true for surface variables. In addition, it is generally admitted that numerous input parameters are necessary to simulate the satellite observations and some are very difficult to obtain at the global scale. Since the SM/ σ_{40} relationship is simple in the retrieval model, especially when localised at the pixel scale, it is worth investigating if a simple NN forward model could be constructed.

The two NN forward modelling schemes (experiments 4 and 5) are presented in Fig. 5 and Table 3). In order to simulate correctly ASCAT σ_{40} , several input parameters are required. Surface SM is of course the variable that we are interested in, but vegetation (LAI) is a variable highly impacting the ASCAT backscatter so it needs to be included. Soil Temperature (ST) and the amplitude of the diurnal cycle of temperature are also added. In addition to the NN model, experiment 5 also includes a CDF-matching.

Figure 6. Correlations (left), bias (center) and STD (right) errors at the global scale, from top to bottom for Exp. 1, 2, 3, 4 and 5.

Fig. 4 represents on the left the correlations between the target ASCAT σ_{40} and the estimation (Exp. 4 and 5). The overall structure is similar to the correlations in the SM space (Exps. 1, 2 and 3). However, the magnitude of the correlations are however lower. Some spatial features are noticeable such as a strong dipole in South America or negative correlations over the Sahara. As expected, the NN retrieval can be regionally biased (in the Sahara and middle East) but this problem is solved when adding the CDF-matching. The standard deviation is, however, not impacted by the CDF-matching.

Finally, when comparing to the error structures and correlation levels, the retrieval of the SM seems more reliable than the simulation of the forward model. To obtain better results, additional input information would probably be required, potentially all the geophysical parameters impacting the backscatter. However some of these parameters (structure of the vegetation, soil texture, etc.) can be very difficult to obtain at the global scale with enough accuracy. Note that the assimilation of the outputs of such forward models would require a transformation of these σ_{40} into the model state variable (i.e., SM), through the Jacobians of the RT, and this would add up even more errors. In addition, in the current methodology the observations are interpolated to model grid point locations which may favour the inverse methods. For conventional forward models the model values are usually interpolated to the observation locations before running the forward model. It would be interesting to investigate whether the interpolation method makes a difference to the performance of the forward NN model. This will be the subject of a future study.

Figure 7. Minimum (left), maximum (center), and range (right) for SM. From top to bottom for ERA5, Exp. 1, 2 and 3.

5.3. Comparison of the CDF-matching techniques

In Section 4.1.1, several approaches were presented to perform CDF-matching. Fig. 8 represents the distributions of the correlations between the CDF-matching of ASCAT σ_{40} and ERA5 SM (TOP), the CDF-matching of the NN SM-retrieval and ERA5 SM (MIDDLE), and the CDF-matching of the NN-estimation backscatter and the ASCAT σ_{40} (BOTTOM). Three CDF-matching methods are compared, the Gaussian, binning and function approximation (i.e. third-order polynomial) approaches and the averaged correlations are provided. The Gaussian CDF-matching does not improve the correlation of the original data because it is a linear method. The binning and function approximation use a non-linear function so they can increase the correlation. The highest improvement is given when using the function approximation (averaged correlations from 0.53 to 0.65, from 0.57 to 0.61 and from 0.43 to 0.54). This improvement comes from the fact that negative correlations (present in some locations, see Fig. 6) can be transformed into positive ones using a negative function. As a consequence, no negative correlations can be seen for the function approximation.

5.4. Combining algorithms

A priori screening of the assimilated satellite data is already in place at ECMWF. Therefore, a dedicated screening could be developed specifically for retrieval SM. It is proposed here to combine Exps. 1 and 3 by defining in which pixels one is better than the other one. To illustrate the potential of this approach for the assimilation, Fig. 9 represents in the first maps the correlations of pixels where Exp. 1 is better, the second map when the Exp. 3 is better, and the second map when both are combined. It can be seen that this combination could be highly beneficial, in particular in half of South Africa, most of Europe, large regions over North America and South-East Asia. Implementation of such strategy should not be difficult, less for instance than the inclusion of a RT model in the assimilation system.

Figure 8. Distributions of the correlations between: the CDF-matching of ASCAT σ_{40} and ERA5 SM (TOP), the CDF-matching of the NN SM-retrieval and ERA5 SM (MIDDLE), and the CDF-matching of the NN-estimation backscatter and the ASCAT σ_{40} (BOTTOM). The CDF-matching is performed using the three approaches: Gaussian transformation, binning, and function approximation. The mean correlation is provided in the legend for each experiment.

Figure 9. Illustration of the combination of SM retrievals. Top: correlation between retrieved and ERA4 SMs on pixels where Exp. 1 is better; Middle: Same for Exp. 3; Bottom: combination of these pixels.

6. Conclusion and perspectives

This study is intended to inform long-term strategies for the assimilation of satellite-derived observations of surface variables into LSMs using the ASCAT derived soil moisture estimates and ERA5 data. Some general approaches have been proposed that could be used to other satellite observations, other NWP frameworks, and other geo-physical variables.

The first aspect discussed in this paper concerns the CDF-matching techniques. In addition to the classical Gaussian approach commonly used in NWP centres, we proposed two new methods: the binning and the function approximation. These three techniques share some features and each has its own advantages and drawbacks, with different levels of agreement with the target model reference. Among the characteristics that are interesting to consider is the ability of the CDF-matching to increase correlation with the target provided by non-linear approaches. The choice of the CDF-matching should really be dependent on the considered application. However, it would be interesting to test new CDF-matching techniques in an assimilation framework to fully understand their potential.

The limitations of RT models have inhibited the direct assimilation of satellite observations sensitive to surface variables such as SM. Global statistical relationships have been proposed in the past to overcome this difficulty (?). In this paper, the NN and CDF-matching methods have been reviewed and conceptually compared. We have shown that CDF-matching can be used as a local retrieval scheme. Assimilation performs a weighting of the information from the satellite and the state of the LSM, based on their respective accuracies. The CDF-matching approach is a mono-variate model highly calibrated towards the LSM, in contrast to the NN which is a multivariate global model. Both methods have pros and cons: The CDF-matching uses the dynamical information of the satellite observations, but any spatial information is lost. The NN intends to obtain physical relationships at the global scale, which is a more ambitious task. The NN is less calibrated towards the model, as it can correct the LSM dynamical behaviour and spatial patterns. The optimal choice between these two methods is truly dependent on some aspects of the application: quality of the satellite observation, simplicity of the satellite/variable physical relationship, availability of auxiliary information, or desire to exploit the synergy of multiple instruments.

For the retrieval of SM from the ASCAT backscatter, the CDF-matching appears to perform well. This comes from the fact that the ASCAT backscatter σ_{40} dynamics are mainly dependent on the local SM conditions and less on the other factors (vegetation, surface roughness, etc.). The relationship between σ_{40} and SM is simple enough that CDF-matching is a good strategy. This would probably not be the case for passive microwave observations for instance because the relationship would be more complex and dependent on other factors (?).

NN and CDF-matching are not dependent on each other: NN do not necessitate CDF-matching because their SM agrees better with the model, and CDF-matching does not require the NN modelling. However, we have shown that NN and CDF-matching can actually be combined, which is an advantage if multi-instrument data needs to be combined.

Using a NN for the forward RT model does not perform as well as for the inverse model in this study. This may seem surprising because in an inverse problem such as remote sensing, forward models are mathematically well-posed but the inverse model can become ill-posed (in terms of existence, uniqueness and stability of the solution). However, the inverse problem here (this might be different for another application) is simple as only local and statistical relationships are sufficient. The forward model requires complex deterministic relationships, using several auxiliary variables, which are not easy to obtain at the global scale. Furthermore, in the forward modelling for LSM assimilation strategy, knowledge of the observation errors is required (instrument plus NN forward modelling errors), and the inversion still needs to be performed in the assimilation (related to the inversion of the Jacobian matrix in the assimilation formula, see ?) so that observation variables are transformed into model variables such as SM. This “inversion” also comes with uncertainties. We hypothesise that adding instrument, forward and inversion errors might be less optimal than inverting directly the satellite data into SM and assimilating it. This would be different if the forward model was very reliable, like in atmospheric applications. This needs, however, to be explored with assimilation experiments.

Perspectives for this work are numerous. The first step will be to perform some SM retrieval validation using *in situ* measurements. Some additional diagnostics (e.g. first guess departures) will also be analysed to better characterise the potential of these approaches in the context of variational assimilation. This will be done in the Part II companion paper.

The next step will be to integrate these developments and to conduct data assimilation experiments to evaluate the impact on NWP forecasts. The results from an assimilation experiment do not always determine whether one retrieval scheme is better than another,

as assimilation systems might need further developments to fully take advantage of some additional information. Indeed, it is often difficult to obtain a positive forecasting impact when assimilating very new satellite observations as numerous adjustments are required to optimally exploit the new information. However, the inverse and forward approaches could be tested in exactly the same conditions (screening, amount of information) so the comparison should really indicate which method seems more promising. Furthermore, it is envisaged that the NN approach will be employed by the EUMETSAT Satellite Applications Facility for Hydrology (H SAF). It would complement the change detection approach that is currently used in the ASCAT surface SM derivation (??). Furthermore, high quality global H-SAF root-zone SM products are generated by assimilating the ASCAT surface SM into an LSM ???. Complementary root-zone SM products are planned at 10 km resolution, which will benefit from assimilating NN based ASCAT surface SM. As already mentioned, the ASCAT data have been pre-processed using a linear regression to estimate the backscatter at a 40° incidence angle. This was done because it was shown that impact of vegetation is less important at this angle but this is only partially true. If the vegetation was also retrieved at the same time, it might be possible to avoid such a pre-processing step and invert more or less directly the ASCAT backscatter at its original incidence angle.

The NN forward model would greatly benefit from the collaboration with RT experts in several ways. For instance, all the information used by such physical models could be used as inputs to the NN, however NN expertise is always required to really exploit, in an optimal way, this information. As mentioned previously, using an approximate forward model and then assimilating the satellite observations directly (requiring some kind of “inversion” in the assimilation formalism through the inversion of the RT Jacobians matrices), adds up two uncertainties; where the statistical inversion produces output data that is already in model space. These aspects need additional analysis.

NN are perfect tools to exploit the synergy of multiple instruments with multi-wavelengths (????). Combining passive and active microwave observations for SM retrieval is now in evidence, see e.g. ? or ?. The fact that the retrievals can be done using the same methodology is a tremendous advantage, and it was shown that the *a priori* combination of information for the retrieval is more advantageous than the *a posteriori* combination of individual retrievals. Attempts should then be made to combine ASCAT and SMOS data in the framework presented here. SMOS NN retrievals are already quite mature (?) so this could be an interesting extension to the work presented here.

Finally, these assimilation ideas could be exploited for other surface variables than soil moisture. For instance, statistical retrievals of land surface temperatures and surface emissivities have been proposed in ? in the microwaves and in ? in the infrared, and a similar approach was proposed too for the surface fluxes ?. Since vegetation also impacts the satellite observations ?, it would be beneficial to retrieve this quantity too, simultaneously.

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590 7. Annexe

591 Similarly to Fig. 7, the minimum (left), maximum (center), and range (right) for σ_{40} is provided in Fig. 10, from top to bottom for
 592 ASCAT, Exp. 4 and 5. Range and correlations statistics are also provided for SM and σ_{40} for the 5 experiments over: Europe (Fig. 11),
 593 USA (Fig. 12), Australia (Fig. 13), South America (Fig. 14), Africa (Fig. 15) and Asia (Fig. 16).

Figure 10. Minimum (left), maximum (center), and range (right) for σ_{40} . From top to bottom for ASCAT, Exp. 4 and 5.

Figure 11. Statistics Europe

Figure 12. Statistics USA

Figure 13. Statistics Australia

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Figure 14. Statistics South America

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