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# Dependence of hydrocarbon sigma CC bond strength on bond angles: the concepts of "inverted", "direct" and "superdirect" bonds. 

Rubén Laplaza, ${ }^{[b]}$ Julia Contreras-Garcia ${ }^{[c]}$, Franck Fuster ${ }^{[c]}$, François Volatron ${ }^{[c]}$, and Patrick Chaquin*[a]


#### Abstract

The bond energy ( BE ) of CC in $\mathrm{CH}_{3}-\mathrm{CH}_{3}$ with respect to geometry frozen fragments follows a sigmoidal increase as a function of the $\theta=$ HCC pyramidalization angle. Using dynamic orbital forces as a $B E$ index, the same behaviour as a function of a unique $<\theta>$ parameter, mean angle of the substituents, is found for 24 single CC bonds in various hydrocarbons. Thus the $<\theta>$ parameter appears as a straightforward and robust index of the geometrical constraints which can either strengthen or weaken a bond. This way, CC sigma bonds can be easily classified into weak "inverted" bonds for $<\theta><90^{\circ}$ (eg. in [111]propellane and bicyclobutane), "direct" (or "normal") bonds for $90^{\circ}$ $\ll \theta><120^{\circ}$ (eg. ethane), and strong "superdirect" bonds for $<\theta \gg 120^{\circ}$ (eg. in tetrahedryltetrahedrane and butadiyne).


Keywords: Chemical bonding, Inverted bonds, superdirect bonds, orbital forces, hydrocarbons

## Introduction

In a recent publication, we revisited the properties of the so-called "inverted bond" in [1.1.1]propellane (Figure 1)[1]. Let us recall that inverted bonds result from the overlap of s+p hybrids by their smaller lobe (Figure 1), by contrast to "normal" or "direct" bonds in which overlap occurs between their bigger lobes. The energy of the central CC bond of

[^0]propellane was evaluated [2] to ca. $60 \mathrm{kcal} / \mathrm{mol}$ and this unexpected high value was the subject of many works [3]. Its origin was attributed either to a strong $\sigma$ bond of "charge shift" nature [3b] or to $\pi$-type three-electron two centers ensured by the $\mathrm{CH}_{2}$ bridges [3c].

In ref [1], we used $\mathrm{C}_{2} \mathrm{H}_{6}$ models to mimic in silico the CC bond inversion by decreasing the $\theta=$ HCC angle from its optimized value, close to $111^{\circ}$, down to $70^{\circ}$. The CC dissociation energy, computed with respect to geometry frozen $\mathrm{CH}_{3}$ moieties, was found to decrease rapidly and by extrapolation should tend to zero for $\mathrm{HCC}=60^{\circ}$. The use Dynamic Orbital Forces (DOF) as indices of bond strengths confirmed this result: the intrinsic $\sigma$ bond energy in propellane should be near zero, and thus the CC bonding is essentially $\pi$ in nature. In a response by Braïda et al. [4], this result was contested, arguing that, due to its charge shift nature, the bond strength in propellane could not be evaluated using DOFs.


Figure 1. "Inverted", "direct" and "superdirect" bonds according to the $\theta$ angle of substituents. [1.1.1]Propellane, ethane and tetrahedryl-tetrahedrane exemplify these three types of bonds respectively.

By contrast, in some C-C bonds, the substituent angles are significantly greater than their value in ethane, with an associated increase of the bond energy. Though the unsubstituted molecule is unstable [5], tetrahedryl-tetraedrane (Figure 1) is the limiting example of such a situation, with substituent angles close to $145^{\circ}$ and a central bond remarkably strong (136 $\mathrm{kcal} / \mathrm{mol}$ ) and short ( $1.426 \AA$ ) [ 6 ]. We propose the term "superdirect" for such bonds. Thus, as displayed in Figure 1, sigma bonds can be classified into "inverted", "direct" and "superdirect" according to the value of the $\theta$ pyramidalization angle.

In the present work, our aim is to study the dependence of $\sigma$ CC bond strength of hydrocarbons on the bond angles of its substituents. In a first step $\mathrm{C}_{2} \mathrm{H}_{6}$ and related models will offer an in silico overview of this relation. Then, we will show that that the $\sigma$ CC bond strength in any hydrocarbon can be characterized by a unique angle parameter leading to the concepts of "inverted", "direct" and "superdirect" bonds. For this purpose, bond strengths were compared using the Dynamic Orbital Forces (DOF) as indices of intrinsic bond energy and as a tool of $\sigma / \pi$ partition in a panel of 35 bonds in 28 molecules.

## Computational Details

Optimized geometries and bonding energies (BE) with respect to geometry frozen fragments have been calculated at the $\operatorname{CCSD}(\mathrm{T}) / \mathrm{cc}-\mathrm{pVQZ}$ level for $\mathrm{C}_{2} \mathrm{H}_{6}$ and $\mathrm{CH}_{3}-\mathrm{H}$ models, and at the MP2/cc-pVTZ level for $\mathrm{Si}_{2} \mathrm{H}_{6}, \mathrm{Ge}_{2} \mathrm{H}_{6}$ and $\mathrm{N}_{2} \mathrm{H}_{4}$. The geometry of 28 hydrocarbon molecules was also optimized at the MP2/cc-pVTZ level (see supplementary data). The derivatives of the canonical molecular orbitals were calculated, with the same basis set as geometry optimization, by a finite difference of bond lengths of $0.002 \AA$ to $0.004 \AA$ according to the case, thanks to a home-made script (available upon request). The Gaussian09 program was used throughout this work [7].

## Results and discussion

## 1. In silico $\mathrm{C}_{2} \mathrm{H}_{6}$ and related models

### 1.1. Influence of HCC angles on CC bond energy in $\mathrm{C}_{2} \mathrm{H}_{6}$

In the $\mathrm{C}_{2} \mathrm{H}_{6}$ model, all six $\theta=\mathrm{HCC}$ angles are frozen from $70^{\circ}$ to $145^{\circ}$. After optimization of the remaining geometrical parameters, the C-C bond energy (BE) with respect to geometry frozen $\mathrm{CH}_{3}$ moieties has been computed at the $\operatorname{CCSD}(\mathrm{T}) / c \mathrm{c}-\mathrm{pVQZ}$ level. In this model (Table 1 and Figure 2), BE decreases rapidly when $\theta$ decreases from the optimized geometry to yield an inverted bond. It increases significantly when $\theta$ increases to yield a superdirect bond. The direct/superdirect limit has been taken somewhat arbitrarily for $\theta=120^{\circ}$.

Table 1. The $\mathrm{C}_{2} \mathrm{H}_{6}$ model. Geometrical parameters $\mathrm{R}(\AA$ ) and bonding energy BE ( $\mathrm{kcal} / \mathrm{mol}$, with respect to two $\mathrm{CH}_{3}$ at frozen geometry) as function of $\theta(C C S D(T) / c c-p v Q Z)$. The results for $\theta \leq 111.2^{\circ}$ are taken from ref. 1.

|  |  | $\mathrm{C}_{2} \mathrm{H}_{6}$ |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :---: | :--- | :--- | :--- | :--- | :--- |
| $\theta$ | $145^{\circ}$ | $140^{\circ}$ | $130^{\circ}$ | $120^{\circ}$ | opt $\left(111.2^{\circ}\right)$ | $100^{\circ}$ | $95^{\circ}$ | $90^{\circ}$ | $80^{\circ}$ | $70^{\circ}$ |
| $\mathrm{R}(\mathrm{CC})$ | 1.411 | 1.422 | 1.448 | 1.483 | 1.527 | 1.628 | 1.708 | 1.830 | 2.231 | 2.9 |
| $\mathrm{R}(\mathrm{CH})$ | 1.18 | 1.135 | 1.111 | 1.097 | 1.091 | 1.085 | 1.082 | 1.079 | 1.079 | 1.089 |
| BE | 154.2 | 152.8 | 145.0 | 131.6 | 114.1 | 81.6 | 63.3 | 44.5 | 15.4 | 5.6 |



Figure 2. CC bond energy $(\mathrm{BE})$ in $\mathrm{C}_{2} \mathrm{H}_{6}$ with respect to geometry frozen $\mathrm{CH}_{3}$ fragments as a function of $\theta=$ HCC angles $\left(\theta=111.2^{\circ}\right.$ optimized value); CCSD $(T) / c c-p v Q Z$.

### 1.2. Qualitative interpretation

The overall sigmoidal shape of $B E$ curve as a function of $\theta$ can be interpreted qualitatively by an evaluation of the overlap of both $\mathrm{s}+\mathrm{p}$ hybrids, $h_{1}$ and $h_{2}$ (Figure 3).


Figure 3. Overlap in direct and inverted bonding.

The hybrids $h_{1}$ and $h_{2}$ are written as:

$$
\begin{aligned}
& h_{1}=\alpha s_{1}+\beta p_{1} \\
& h_{2}=\alpha s_{2}+\beta p_{2}
\end{aligned}
$$

with $\alpha^{2}+\beta^{2}=1$. Setting $\beta>0$ :

$$
\begin{aligned}
& \alpha<0 \text { for } \theta<90^{\circ} \\
& \alpha=0 \text { for } \theta=90^{\circ} \\
& \alpha>0 \text { for } \theta>90^{\circ}
\end{aligned}
$$

The theoretical limits of $\theta$ are $0^{\circ}$, with $\alpha=-\beta=-1 / \sqrt{ } 2$ and $180^{\circ}$, with $\alpha=\beta=1 / \sqrt{ } 2$. The corresponding hybridization states can be referred to as $\mathrm{sp}^{-1}$ and sp respectively. Between these limits, the following hybridization states are encountered: $\mathrm{sp}^{-2}(\alpha=-1 / \sqrt{ } 3)$, $\mathrm{sp}^{-3}(\alpha=-$ $1 / 2), s^{0} p(\alpha=0), s^{3}(\alpha=1 / 2), \operatorname{sp}^{2}(\alpha=1 / \sqrt{ } 3)$. The following values of $\alpha$ for $\mathrm{CH}_{3}$ are obtained with the minimal basis STO-3G for $\mathrm{CH}_{3}$ and various $\theta$ (Table 2). For $\theta=120^{\circ}$, the calculated s participation to the hybrid is found 0.6 , close to $1 / 2$ which is the theoretical value for $\mathrm{sp}^{2}$. This angle value can be taken as the (arbitrary) limit between "direct" and "superdirect" bonds.

Table 2. Coefficient $\alpha$ of the s AO in the $\mathrm{CH}_{3}$ SOMO hybrid as a function of $\theta$ angle (see Figure 3).

| $\boldsymbol{\theta}$ | $\mathbf{6 0}$ | $\mathbf{7 0}$ | $\mathbf{8 0}^{\boldsymbol{\circ}}$ | $\mathbf{9 0}^{\boldsymbol{\circ}}$ | $\mathbf{1 0 0}^{\boldsymbol{\circ}}$ | $\mathbf{1 1 0 ^ { \circ }}$ | $\mathbf{1 2 0}^{\boldsymbol{\circ}}$ | $\mathbf{1 3 0}^{\boldsymbol{\circ}}$ | $\mathbf{1 4 0}^{\boldsymbol{\circ}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\alpha$ | -0.601 | -0.483 | -0.294 | 0.000 | 0.294 | 0.483 | 0.601 | 0.693 | 0.786 |

The overlap $S$ of $h_{1}$ and $h_{2}$ is given by:
$S=\left\langle\alpha s_{1}+\beta p_{1} \mid \alpha s_{2}+\beta p_{2}\right\rangle=\alpha^{2}\left\langle s_{1} \mid s_{2}\right\rangle+\beta^{2}\left\langle p_{1} \mid p_{2}\right\rangle+2 \alpha \beta\left\langle s_{1} \mid p_{2}\right\rangle$
In a first step, the overlaps $S_{\text {eq }}$ of $s+p$ hybrids of $\mathrm{CH}_{3}$ have been computed at the CC equilibrium distances in the $\mathrm{C}_{2} \mathrm{H}_{6}$ model for each $\theta$ value (red curve in Figure 4a). Then, in order to emphasize the effect of hybridization alone, the overlap $\mathrm{S}_{0}$ has been determined for a constant CC distance of $1.5 \AA$. Note that, in this case, to a first approximation, the three atomic overlaps in Eq. 1 are close to 0.3:
$S_{0} \approx 0.3\left(\alpha^{2}+\beta^{2}+2 \alpha \beta\right)=0.3(1+2 \alpha \beta)$
The corresponding values are reported in Figure 4a (black curve). Both $\mathrm{S}_{0}$ and $\mathrm{S}_{\text {eq }}$ as a function of $\theta$ have a sigmoidal shape similar to the bonding energy in Figure 2. The two curves are nearly coincident for $\theta<110^{\circ}$ indicating the prominent role of the hybridization in
this region. Moreover, the bonding energy appears closely connected to both $S_{\text {eq }}$ and $S_{0}$ (Figure 4 (b)), with, again a quasi-superimposition in the corresponding region.


Figure 4. (a) Variation of overlap $S$ with $\theta$ in $\mathrm{C}_{2} \mathrm{H}_{6}$ model: $\mathrm{S}_{\text {eq }}$ at equilibrium $\mathrm{R}(\mathrm{CC})$ distance (red curve); $\mathrm{S}_{0}$ for a CC constant distance of $1.5 \AA$ (black curve). (b) Variation of CC bond energy BE as a function of $\mathrm{S}_{\text {eq }}$ (red curve) and $\mathrm{S}_{0}$ (black curve).

Finally, this model emphasizes the role on BE of the overlap of the two $s+p$ hybrids which increases with $\theta$, together with $\alpha$, algebraic participation of the sAO to these hybrids.

### 1.3. Related models: $\mathrm{Si}_{2} \mathrm{H}_{6}, \mathrm{Ge}_{2} \mathrm{H}_{6}, \mathrm{~N}_{2} \mathrm{H}_{4}$ and $\mathrm{CH}_{4}$

Though we are mainly interested in CC bonds in this work, we examined some models involving other bonds to compare their behaviour when similar angle constraints are imposed.

Two heavier systems, $\mathrm{Si}_{2} \mathrm{H}_{6}$ and $\mathrm{Ge}_{2} \mathrm{H}_{6}$, have been studied at the MP2/cc-pVTZ level following the approach of the $\mathrm{C}_{2} \mathrm{H}_{6}$ model. Figures $5(\mathrm{a})$ and $5(\mathrm{~b})$ display the variation of BE as a function of the $\theta$ angles $\mathrm{H}-\mathrm{Si}-\mathrm{Si}$ and $\mathrm{H}-\mathrm{Ge}-\mathrm{Ge}$ respectively. The two curves are very similar. They have also the same general shape as for $\mathrm{C}_{2} \mathrm{H}_{6}$, with a weaker $B E$ increase in the superdirect region $\left(\theta>120^{\circ}\right)$. It appears that the decrease of the ns-np gap in these both species, with respect to $\mathrm{C}_{2} \mathrm{H}_{6}$, is only of minor consequence as compared to the angle variation.


Figure 5. Central bond energies (BE) of $\mathrm{Si}_{2} \mathrm{H}_{6}(\mathrm{a})$ and $\mathrm{Ge}_{2} \mathrm{H}_{6}$ (b) with respect to geometry frozen $\mathrm{AH}_{3}$ fragments as functions of $\theta$ angles $\mathrm{H}-\mathrm{Si}-\mathrm{Si}$ and $\mathrm{H}-\mathrm{Ge}-\mathrm{Ge}$ respectively (MP2/cc-pVTZ).

The BE of the NN bond of $\mathrm{NH}_{2}-\mathrm{NH}_{2}$ in $\mathrm{D}_{2 \text { d }}$ symmetry was also studied as a function of $\theta=$ HNN angles. The dissociation energy was computed with respect to geometry frozen $\mathrm{NH}_{2}$ fragments in their ${ }^{2} \mathrm{~A}_{1}$ state. It should be noted that $\mathrm{N}-\mathrm{N}$ bond breaking results in the formation of two $\mathrm{NH}_{2}$ radicals possessing a lone pair in a $2 p \mathrm{AO}$ and a semi occupied $\mathrm{s}+\mathrm{p}$ hybrid. In its optimized geometry, this state is ca. $34 \mathrm{kcal} / \mathrm{mol}$ above the ${ }^{2} \mathrm{~B}_{1}$ ground state [8]. Thus the value of BE in geometry optimized $\mathrm{N}_{2} \mathrm{H}_{4}$ lies at $68 \mathrm{kcal} / \mathrm{mol}$ above the NN dissociation energy into $2 \mathrm{NH}_{2}$ in their ground state.


Figure 6. $\mathrm{N}-\mathrm{N}$ bond energy (BE) in $\mathrm{N}_{2} \mathrm{H}_{4}\left(\mathrm{D}_{2 \mathrm{~d}}\right)$ with respect to geometry frozen $\mathrm{NH}_{2}$ fragments as a function of $\theta=\mathrm{H}-\mathrm{N}-\mathrm{N}$ angles (MP2/cc-PVTZ).

Finally, we studied the energy of one $\mathrm{C}-\mathrm{H}$ bond in $\mathrm{CH}_{4}$ as a function of the $\theta$ pyramidalization angle of the $\mathrm{CH}_{3}$ moiety. Results in Table 3 and Figure 6 are similar to the preceding ones. Nevertheless, because we deal here with the deformation of only one $\mathrm{CH}_{3}$ group, yielding either "semi-inverted" or "semi-superdirect" bonds, the relative variation of BE is smaller than in the case of $\mathrm{C}_{2} \mathrm{H}_{6}$ (cf. Figure 2). Note that the influence of bond angles on bond lengths has already been studied in $\mathrm{CH}_{4}$ and related species [9].

Table 3. $\mathrm{H}_{3} \mathrm{C}-\mathrm{H}$. Geometrical parameters $\mathrm{R}(\AA)$ and bond energy BE of CH ( $\mathrm{kcal} / \mathrm{mol}$, with respect to H and $\mathrm{CH}_{3}$ at frozen geometry) as function of $\theta$; opt $=109.5^{\circ}$; CH 1 refers to H in $\mathrm{CH}_{3}$ group; CCSD(T)/ccpVQZ level of calculation.

|  | $\mathrm{H} \mathrm{C}-\mathrm{H}$ |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\theta$ | $140^{\circ}$ | $130^{\circ}$ | $120^{\circ}$ | opt | $100^{\circ}$ | $90^{\circ}$ | $80^{\circ}$ | $70^{\circ}$ | $60^{\circ}$ |
| $\mathrm{R}(\mathrm{CH})$ | 1.063 | 1.068 | 1.076 | 1.087 | 1.105 | 1.132 | 1.174 | 1.229 | 1.290 |
| $\mathrm{R}(\mathrm{CH} 1)$ | 1.134 | 1.108 | 1.095 | 1.087 | 1.085 | 1.084 | 0.876 | 1.003 | 1.130 |
| BE | 138.4 | 134.1 | 127.7 | 119.4 | 107.5 | 90.6 | 70.8 | 54.1 | 44.9 |



Figure 7. CH bond energy (BE) in $\mathrm{H}_{3} \mathrm{C}-\mathrm{H}$ (red bond) with respect to H and geometry frozen $\mathrm{CH}_{3}$ fragments as a function of $\theta=\mathrm{HCH}$ angle ( $\operatorname{CCSD}(\mathrm{T}) / c c-p v Q Z)$.

All studied models agree with the fact that the bond energy is strongly dependent on the substituent angles: it decreases rapidly with the inverted character of the bond and increases with its superdirect character. These phenomena follow the same variation as $\mathrm{C}_{2} \mathrm{H}_{6}$ in section 1.1 which suggest that they can be interpreted similarly by of the hybridization of the s+p AOs overlapping in the bond formation, controlled by these angles. Specifically, BE increases with the $s$ (algebraic) coefficient in the $s+p$ hybrids. This result is well-known for "direct" C-H bonds with aliphatic ( $\mathrm{sp}^{3}$ ), ethylenic ( $\mathrm{sp}^{2}$ ) and acetylenic ( sp ) carbons as well as
in direct C-C bonds [10], for example regarding the strong central bond of tetrahedryltetraedrane [6b,11]. Nevertheless, the final optimized CC distance involves other parameters as evidenced by energy decomposition analysis [12]. Moreover, it was shown in a recent work that the contraction of CC bonds along a series $C\left(s p^{3}\right)-C\left(s p^{3}\right), C\left(s p^{3}\right)-C\left(s p^{2}\right)$ and $C\left(s p^{3}\right)-$ $C(s p)$ does not originate from an increase in the $s$ character of the second atom, but in a decrease of the steric (Fermi) repulsion between substituents of both carbons [13]. Indeed, in the $A H_{n}-A H_{n}$ models of the preceding study, we observe that direct bonds shorten as $\theta$ increases, together with H...H distances resulting in weaker Fermi repulsion. The situation is less clear for inverted bonds. As an example, in $\mathrm{C}_{2} \mathrm{H}_{6}$, for $\theta=90^{\circ} \mathrm{R}(\mathrm{CC})=1.830 \AA$ with $\mathrm{H} . . . \mathrm{H}=$ 2.12 Å. For $\theta=80^{\circ}$ the $H \ldots$... distance increases very weakly ( $2.14 \AA$ ), resulting in a negligible decrease in Fermi repulsion, while $R(C C)$ significantly increases by $0.4 \AA(2.231 \AA)$. It suggests that the bond length could be controlled by hybridization in inverted bonds.

## 2. Inverted, direct, and superdirect bonds: generalization for sigma CC bonds in hydrocarbons

### 2.1. Mean angle $<\theta>$ of substitution

The preceding models preserve a symmetry axis along the bond under scrutiny with equal pyramidalization angles of H substituents on each heavy atom. We will now extend the inverted/direct/superdirect character to any CC $\sigma$ bond in hydrocarbons, be it formally a single bond or a $\sigma$ bond in a formally multiple bond. For this purpose, we define a < $\theta$ > parameter as simply the mean value of the angles of the six substituents on both carbon atoms; the $\pi$ bonds are treated as $\sigma$ ones in these calculations. Two examples are given in Figure 8.


Figure 8. Calculation of the $\langle\theta>$ angle for the red bond in cyclopropane and cyclobutene.

In cyclopropane, the red bond has 4 H at $118^{\circ}$ and two C at $60^{\circ}$, yielding $\langle\theta\rangle \approx 99^{\circ}$. In cyclobutene, the red bond is considered as having 2 C at $94^{\circ}, 1 \mathrm{H}$ at $132^{\circ}, 1 \mathrm{C}$ at $84^{\circ}$ and 2 H at $116 .^{\circ}$ yielding $\langle\theta\rangle=106^{\circ}$. This way, the central $\mathrm{C}-\mathrm{C}$ bond in butadiyne $\mathrm{HC} \equiv \mathrm{C}-\mathrm{C} \equiv \mathrm{CH}$ has the $\langle\theta\rangle$ theoretical maximum value of $180^{\circ}$. In formally multiple bonds, the $\langle\theta\rangle$ angle is determined in a similar way. For example, in acetylene $\mathrm{H}-\mathrm{C} \equiv \mathrm{C}-\mathrm{H}$, the $\sigma$ CC bond in considered as having 4 C at $0^{\circ}$ and 2 H at $180^{\circ}$, yielding $\langle\theta\rangle=60^{\circ}$.

### 2.2. Dynamic orbital forces as index of intrinsic bond energy and tool for $\sigma / \pi$ partition

For the study of the relation between $\sigma$ bond strength and $\langle\theta>$ in real systems, 35 CC bonds of various $\langle\theta\rangle$ were considered in a panel of 28 molecules (Tables 4 and 5). In many of these cases, the BE of C-C bonds can no longer be computed in the same way as in the first section, namely by dissociation of two geometry frozen fragments. Thus we will use the dynamic orbital forces (DOF)[14] as indices of bond energies.

According to Koopman's theorem, the derivative of the $i^{\text {th }}$ canonical MO energy $\varepsilon_{i}$ with respect to a bond length ( $\mathrm{R}(\mathrm{CC}$ ) in the case of a CC bond) is:

$$
\begin{equation*}
\frac{d \varepsilon_{i}}{d R(C C)}=\frac{d E^{0}}{d R(C C)}-\frac{d E_{i}^{+}}{d R(C C)} \tag{3}
\end{equation*}
$$

where $E_{0}$ is the energy of the neutral species and $E_{i}^{+}$the energy of the ion resulting from the loss of one electron in the $i^{\text {th }}$ MO. This relation is exact if the MOs are the same for the neutral and cationic species (frozen MO approximation). If the geometry of the neutral species is optimized, $\mathrm{dE}^{\circ} / \mathrm{dR}(\mathrm{CC})=0$ and the DOF is thus the opposite of the force exerted along $R(C C)$ upon diabatic ionization. It has already been used as a measure of the bonding/antibonding character of the MO with respect to this bond [15]. Also it has been shown that a MO of positive DOF has a positive contribution to the dissociation energy and vice-versa [16]. Thus one can assume that the sum $\Sigma_{\text {tot }}$ of these derivatives over valence MOs occupied by $n_{i}$ electrons :

$$
\Sigma_{t o t}=\sum_{i}^{o c c} n_{i} \frac{d \varepsilon_{i}}{d R(C C)}
$$

is an index of bond strength. This idea has been successfully developed [1, 17, 18], especially in the case of CC bond in hydrocarbons $[1,18]$. Also, this quantity can be decomposed into $\sigma$ ( $\Sigma_{\sigma}$ ) and $\pi\left(\Sigma_{\pi}\right)$ components allowing to compare these both contributions:
$\Sigma_{t o t}=\sum_{i}^{o c c} n_{i} \frac{d \varepsilon_{i}}{d R(C C)}=\sum_{j}^{\sigma o c c} n_{j} \frac{d \varepsilon_{j}}{d R(C C)}+\sum_{k}^{\pi o c c} n_{k} \frac{d \varepsilon_{k}}{d R(C C)}=\Sigma_{\sigma}+\Sigma_{\pi}$

However $\Sigma_{\text {tot }}$ is an intrinsic quantity of the system, whereas the bond energy dissociation with respect to geometry frozen fragments (BE) considered in section 1 involves the electronic relaxation of fragments and thus some reorganization energy. This tends to lower BE with respect to the intrinsic bond energy, but this difference should be small if the two following conditions are fulfilled: (i) the bond is symmetrically or nearly symmetrically substituted, resulting in a negligible electron transfer by bond dissociation and (ii) no significant stabilization of the radicals obtained occurs by conjugation or hyperconjugation. In Figure 9, we report BE as a function of $\Sigma_{\text {tot }}$ for the $\mathrm{C}_{2} \mathrm{H}_{6}$ model and various CC bonds (taken from ref. 18). We observe an excellent linear correlation ( $R^{2}=0.98$ ) of $B E$ of CC bonds and $\Sigma_{\text {tot }}$ in the series $\mathrm{C}_{2} \mathrm{H}_{2}, \mathrm{C}_{2} \mathrm{H}_{4}, \mathrm{C}_{6} \mathrm{H}_{6}, \mathrm{C}_{2} \mathrm{H}_{6}$ and $\mathrm{C}_{3} \mathrm{H}_{6}$ (black line in Figure 9). Regarding the $\mathrm{C}_{2} \mathrm{H}_{6}$ model with various $\theta$ values (red curve in Figure 9), the curve is strictly superimposed to the preceding black line for $\Sigma_{\text {tot }}>0.4$. For smaller $\Sigma_{\text {tot }}$ values, the slope decreases and BE tends to zero for $\Sigma_{\text {tot }} \approx 0$.


Figure 9. Bond energy ( $\mathrm{kcal} / \mathrm{mol}$ ) with respect to geometry frozen fragments (MP2/cc-pVTZ) as a function of $\Sigma_{\text {tot }}$ (a.u.).

This way, $\Sigma_{\text {tot, }}$, though computed from H-F level MOs, is found to be correlated to CC bond strength. This result is empirical, but further supported by a large amount of evidence regarding bond energies. Indeed, a very good correlation ( $R^{2}=0.97$ ) is found with respect to BE values calculated at the DFT $\omega$ B97XD/aug-qzvp level for bonds 1, 12, 19, 27, 26, 29, 34 of Tables 4 and 5 [19]. Moreover, $\Sigma_{\text {tot }}$ can be compared with intrinsic bond energies computed from AIM critical point properties and bond paths (using, of course, correlated electron densities) [20]: a good linear correlation is again obtained ( $\mathrm{R}^{2}=0.96$ ) with the set of bonds $\mathbf{1}$, 4, 8, 9, 12, 13, 18, 19, 26, 29, 30, 33, 34 of Tables 4 and 5 (see Supplementary data Fig. 1). Clearly, the fact that electron correlation is not included in $\Sigma_{\text {tot }}$ can be questionable. Nevertheless, KS MOs obey eq. 3 only approximately, with discrepancies depending on the nature of the functional [21]. Moreover, a lower correlation of the CC BEs of the five molecules of Fig. 9 is observed with $\Sigma_{\text {tot }}$ from KS MOs of various functionals: $\mathrm{R}^{2}=0.92$ (B2PLYP), 0.92 (CAM-B3PLYP), 0.74 (B3LYP) respectively, vs. 0.98 (H-F). Thus, as far as the molecule is satisfactorily described at the H-F level, we can consider $\Sigma_{\text {tot }}$ as a straightforward empirical index allowing the comparison of the CC intrinsic bond strengths in hydrocarbons, with a decomposition into $\Sigma_{\sigma}$ and $\Sigma_{\pi}$ reflecting their relative $\sigma$ and $\pi$ components.


Figure 10. Bonds (red bold) and molecules of Table 4.

### 2.3. Sigma CC bond energy and mean angle of substitution $<\theta\rangle$

### 2.3.1. Formally single bonds

In Table 4, we report the values of $\Sigma_{\text {tot }}, \Sigma_{\sigma}$ and $\Sigma_{\pi}$ in a panel of formally single 24 C-C bonds, displayed in Figure 10, by order of decreasing values of $\langle\theta\rangle$ from $180^{\circ}$ to $60^{\circ}$. The concept of directedness/invertedness concerns $\sigma$ bonds, and thus we will be interested mainly in the $\Sigma_{\sigma}$ component, though $\Sigma_{\text {tot }}$ and $\Sigma_{\pi}$ could also offer useful information.

Table 4. Values of $\Sigma_{\text {tot }}, \Sigma_{\sigma}, \Sigma_{\pi}$ (a.u.); \% of $\Sigma_{\pi}$ in $\Sigma_{\text {tot }}$, equilibrium bond length $R(C C)(A ̊)$ and the corresponding values of $\langle\theta\rangle\left({ }^{\circ}\right)$ for formally single C-C bonds (TET = tetrahedryl; BCP = bicyclopentyl; CUB = cubyl, see also Figure 10).

| Label | Molecule | $\boldsymbol{\Sigma}_{\text {tot }}$ | $\Sigma_{\boldsymbol{\sigma}}$ | $\boldsymbol{\Sigma}_{\boldsymbol{\pi}}$ | \% $\pi$ | R(CC) | < $\boldsymbol{\theta}$ > |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\mathrm{HC} \equiv \mathrm{C}-\mathrm{C} \equiv \mathrm{CH}$ | 0.513 | 0.450 | 0.064 | 12.4 | 1.369 | 180 |
| 2 | TET-C $=$ CH | 0.527 | 0.437 | 0.090 | 17.1 | 1.394 | 163 |
| 3 | TET-TET | 0.468 | 0.447 | 0.021 | 4.5 | 1.419 | 145 |
| 4 | $\mathrm{CH}_{3}-\mathrm{C} \equiv \mathrm{CH}$ | 0.458 | 0.415 | 0.042 | 9.1 | 1.458 | 145 |
| 5 | TET-CH3 | 0.495 | 0.442 | 0.053 | 10.1 | 1.476 | 128 |
| 6 | BCP-BCP | 0.489 | 0.434 | 0.055 | 11.3 | 1.477 | 127 |
| 7 | CUB-CUB | 0.478 | 0.420 | 0.058 | 12.1 | 1.465 | 125 |
| 8 | $\mathrm{CH}_{2}=\mathrm{CH}-\mathrm{CH}=\mathrm{CH}_{2}$ | 0.478 | 0.433 | 0.045 | 9.4 | 1.453 | 121 |
| 9 | $\mathrm{CH}_{3}-\mathrm{CH}=\mathrm{CH}_{2}$ | 0.418 | 0.399 | 0.019 | 4.5 | 1.505 | 116 |
| 10 | $\mathrm{Ph}-\mathrm{CH}_{3}$ | 0.415 | 0.397 | 0.019 | 4.6 | 1.503 | 115 |
| 11 | $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{C}-\mathrm{C}\left(\mathrm{CH}_{3}\right)_{3}$ | 0.439 | 0.392 | 0.048 | 10.8 | 1.565 | 111 |
| 12 | $\mathrm{CH}_{3}-\mathrm{CH}_{3}$ | 0.413 | 0.392 | 0.021 | 4.9 | 1.527 | 111 |
| 13 | cyclohexane | 0.445 | $0.425^{\text {a }}$ | $0.02^{\text {a }}$ | $4.5{ }^{\text {a }}$ | 1.565 | 110 |
| 14 | methenecyclopropane (3-4) | 0.414 | 0.397 | 0.017 | 4.1 | 1.464 | 109 |
| 15 | cyclopentane | 0.420 | 0.403 | $0.017^{\text {b }}$ | 4.3 | 1.526 | 108 |
| 16 | cyclobutene (2-3) | 0.445 | 0.400 | 0.045 | 10.1 | 1.537 | 106 |
| 17 | cyclobutene (3-4) | 0.404 | 0.396 | 0.008 | 2.0 | 1.565 | 105 |
| 18 | cyclobutane | 0.408 | 0.401 | $0.007^{\text {b }}$ | 1.7 | 1.546 | 105 |
| 19 | cyclopropane | 0.364 | 0.368 | -0.004 | -1.1 | 1.504 | 99 |
| 20 | methenecyclopropane (1-2) | 0.333 | 0.333 | 0.000 | 0.0 | 1.539 | 97 |
| 21 | cyclopropene | 0.281 | 0.283 | -0.002 | -2.0 | 1.508 | 88 |
| 22 | tetrahedrane | 0.353 | 0.278 | 0.075 | 21.2 | 1.478 | 88 |
| 23 | bicyclobutane | 0.360 | 0.215 | 0.146 | 39.7 | 1.500 | 82 |
| 24 | [1.1.1]Propellane | 0.275 | -0.029 | 0.304 | 110.5 | 1.596 | 60 |

[^1]Molecules 1-8 can be considered as having a superdirect bond, with $\Sigma_{\sigma}$ ranging from 0.415 up to 0.450 a.u. for butadiyne 1, which has the maximum theoretical value of $\langle\theta\rangle\left(180^{\circ}\right)$. For the direct bonds $\mathbf{9 - 1 8}\left(116^{\circ} \ll \theta><105^{\circ}\right), \Sigma_{\sigma}$ is generally close to 0.4 a.u. Ethane $\mathbf{1 2}$ can be taken as the prototype of "standard" direct CC bond with $\Sigma_{\sigma}=0.392$ a.u. Bonds 19 and 20, are formally direct ( $<\theta>=99^{\circ}$ and $97^{\circ}$ respectively) but have significantly lower $\Sigma_{\sigma}(0.368$ and 0.333 a.u. respectively) according to ring strain. Molecules 21-24 possess inverted bonds and $\Sigma_{\sigma}$ less than 0.283 a.u., corresponding to strong strains, down to a slightly negative value in propellane 24 (-0.029 a.u. with $\langle\theta\rangle=60^{\circ}$ ).

We thus observe (Figure 11) a general increase of $\Sigma_{\sigma}$ with $\langle\theta\rangle$, following the same sigmoidal shape as observed for the models of sections 1 and 3 . As a landmark, we report on the same figure the variation of $\Sigma_{\sigma}$ for the $\mathrm{C}_{2} \mathrm{H}_{6}$ model (red curve), showing that the behaviour of real bonds is quite similar to that of this $\mathrm{C}_{2} \mathrm{H}_{6}$ model.


Figure 11. $\Sigma_{\sigma}$ (a.u.) values for bonds in molecules 1-22 with respect to the mean substituent angle $<\theta>\left({ }^{\circ}\right)$. The red curve corresponds to $\mathrm{C}_{2} \mathrm{H}_{6}$ model.

The value of $\Sigma_{\text {tot }}$ in tetramethylbutane 11 (0.439 a.u.) suggests that its intrinsic bond energy is greater than that of ethane $\mathbf{1 2}$ ( 0.413 a.u.) though its experimental dissociation energy is significantly smaller ( $78.6 \mathrm{kcal} / \mathrm{mol}$ vs. $90.2 \mathrm{kcal} / \mathrm{mol}$ ) [22]. Nevertheless, the BE of both
species with respect to geometry frozen fragments (MP2/cc-PVTZ) are found nearly equal ( $113.0 \mathrm{kcal} / \mathrm{mol}$ for 11 and 113.9 for $\mathbf{1 2}$ ). Moreover, the electronic relaxation in $\mathrm{Me}_{3} \mathrm{C}$ - radical involves a significant stabilization by hyperconjugation, which leads to an underestimation of the calculated BE of $\mathbf{1 2}$ with respect to the actual intrinsic bond strength.

The $\pi$ participation to $\Sigma_{\text {tot }}$, corresponding to the total bond strength, is generally no more than ca. $10 \%$ in all superdirect or direct bonds. In can be noted that the high BE in butadiyne 1 as compared to that of ethane 12 is due to $\sigma$ strengthening ( $\Delta \Sigma_{\sigma}=0.058$ a.u.) more than to conjugation ( $\Delta \Sigma_{\pi}=0.043$ a.u.). The same remark holds for butadiene 8 , whose corresponding values are $\Delta \Sigma_{\sigma}=0.041$ a.u. and $\Delta \Sigma_{\pi}=0.024$ a.u. Also, it has been proposed that the strong bond of $\mathbf{3}$ originates equally both from its high s character and from hyperconjugation [23 ]; but in the present work the hyperconjugation term appears weak, with only $4.5 \%$ contribution of $\pi \mathrm{MOs}$ to $\Sigma_{\text {tot. }}$. This is further supported by the $12 \%$ of $\pi$ energy that was determined from Energy Decomposition Analysis [6b].

In the series of cyclanes, we observe a regular decrease of $\Sigma_{\text {tot, }}$ as the ring strain increases: cyclohexane 13 ( 0.445 a.u.), cyclopentane 15 ( 0.420 a.u.), cyclobutane 18 ( 0.408 a.u.) and cyclopropane 19 ( 0.368 a.u.). Because their rings are non-planar (except cyclopropane 19), the $\pi$ MOs have been identified visually for 15 and 18 . For cyclohexane 13 the $\sigma / \pi$ partition becomes problematic because most of the MOs have both types of participation; we assumed that $\Sigma_{\pi}$ is close to the value observed for ethane. Under these conditions, a decrease of $\Sigma_{\sigma}$ is also observed along the series together with $\langle\theta\rangle$. The slightly negative $\pi$ participation in $\mathbf{1 9}$ and $\mathbf{2 1}$ can be due to their quasi-eclipsed conformation, this participation being nearly zero in eclipsed ethane. Furthermore, it is well known that cyclobutane 18 and cyclopropane 19 have very close strain energies, $26.5 \mathrm{kcal} / \mathrm{mol}$ and $27.5 \mathrm{kcal} / \mathrm{mol}$ respectively [24], though the three-membered cycle could appears as much more strained. Taking into account that these energies involve all the bonds, it has been suggested that three weaker CC bonds in cyclopropane are compensated by six stronger CH bonds [25]. Indeed, $\left\langle\theta>(\mathrm{CH})=109.5^{\circ}\right.$ for 18 and $116.3^{\circ}$ for 19: thus the CH bonds in cyclopropane are found to have some superdirect character. Moreover, from Table 3, the C-H BE increase can be evaluated to ca. $6.9 \mathrm{kcal} / \mathrm{mol}$, close to previous determinations ( $8.6-8.8 \mathrm{kcal} / \mathrm{mol}$ ) [26].


Figure 12. Various $\Sigma$ values (a.u.) for CC bonds in ethane and a series of three-membered cyclic molecules (red bond).

The series of three-membered ring species $\mathbf{1 9}, \mathbf{2 2}, 23$ and $\mathbf{2 4}$, compared to ethane $\mathbf{1 2}$ (Figure 12), is of a particular interest. The CC bond undergoes a progressive inversion with < $\theta$ > decreasing from $111.2^{\circ}$ (direct bond in 12) to $60^{\circ}$ (inverted bond in propellane 24). $\Sigma_{\sigma}$ decreases monotonously from 0.392 a .u. in ethane down to $-0.029 \mathrm{a} . \mathrm{u}$. in propellane. But at the same time, this decrease is compensated to a large extent by an increase of $\Sigma_{\pi}$ for $\mathbf{2 2}, \mathbf{2 3}$ and 24. As a matter of fact, the presence of two CH bridges in $\mathbf{2 2}$, two and three $\mathrm{CH}_{2}$ bridges in $\mathbf{2 3}$ and $\mathbf{2 4}$ respectively, allows the formation of three-center two-electron bonds of $\pi$ character. The relative contributions of MOs to $\sigma$ and $\pi$ bonding have been detailed in ref. [1] in the case of propellane 24. The " $\mathrm{CH}_{2}$ bridge" MOs of bicyclobutane $\mathbf{2 3}$ are displayed in Figure 13, together with their respective DOF. They are characterized, according to their $\pi$ nature, by a nodal plane containing the central bond and are of $a_{2}$ and $b_{2}$ symmetry within the $\mathrm{C}_{2 v}$ group. One of these MOs (14) is found antibonding (DOF = -0.069 a.u.) while the other three are bonding. It is worthy to insist on the fact that, on the basis of the evolution of the $\Sigma$ and $<\theta>$ values, the central bond of propellane $\mathbf{2 4}$ behaves as expected in this series and does not appear as a particular case, in spite of its "charge shift" character within VB method [3b].


Figure 13. Bridge bond MOs, and corresponding DOF (a.u.) of bicyclobutane 23.

The variation of $R(C C)$ as a function of $\langle\theta>$ deserves a comment. Bonds 1-13 have generally a weak $\pi$ participation and they are not subject to cycle constraints. Their lengths thus result from a free interplay of their strength (essentially controlled by their s component) and the Fermi repulsion of their substituents: both these parameters tend to shorten the CC bond as $\langle\theta\rangle$ increases, as observed in Figure 14 (blue squares). These bonds have the same characteristics as the CC bond in the $\mathrm{C}_{2} \mathrm{H}_{6}$ model which behaves similarly (red curve). By contrast, bonds $\mathbf{1 4 - 2 4}$ are subject to cycle constraints and $\pi$ component of various importance, and their bond lengths (cyan circles) diverge from those of the $\mathrm{C}_{2} \mathrm{H}_{6}$ model.


Figure 14. Bond lengths ( $A$ ) vs. mean angle $\langle\theta\rangle$; bonds 1-12 (blue squares); bonds 12-24 (cyan circles); $\mathrm{C}_{2} \mathrm{H}_{6}$ model (red curve).

### 2.3.2. Sigma bonds in formally multiple bonds

From a panel of 11 formally multiple bonds, displayed in Figure 15, we report in Table 5 the values of $\Sigma_{\text {tot }}, \Sigma_{\sigma}, \Sigma_{\pi}$ (a.u.) and the mean angle $\langle\theta>$ calculated for their $\sigma$ component. For benzene $\mathbf{2 4},\left\langle\theta>=100^{\circ}\right.$ is the mean of the two values of Kékulé structures.

The $\Sigma_{\text {tot }}$ values range from 0.479 a.u. to 0.579 a.u. for double bonds, from 0.577 a.u. to 0.616 a.u. for triple bonds and is 0.480 a.u. for the "half double bond" of benzene. As expected, $\Sigma_{\text {tot }}$ is slightly smaller in the conjugated $\mathbf{3 0}$ and $\mathbf{3 3}$ than in the corresponding non conjugated 29 and 34.

Table 5. Values of $\Sigma_{\text {tot, }} \Sigma_{\sigma}, \Sigma_{\pi}$ (a.u.) for CC bonds in multiple bonds and the corresponding values of $\langle\theta\rangle\left({ }^{\circ}\right)$ for their $\sigma$ bond $\left(=\mathrm{C}_{3} \mathrm{H}_{4}\right.$ : cyclopropylidene, cf. Fig. 15).

| label | Molecule | $\boldsymbol{\Sigma}_{\text {tot }}$ | $\boldsymbol{\Sigma}_{\boldsymbol{\sigma}}$ | $\boldsymbol{\Sigma}_{\boldsymbol{\pi}}$ | $\% \boldsymbol{\pi}$ | $\mathbf{R}(\mathbf{C C})$ | $<\boldsymbol{\theta}>$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{2 5}$ | $\mathrm{H}_{2} \mathrm{C}=\mathrm{C}=\mathrm{CH}_{2}$ | 0.516 | 0.315 | 0.201 | 39.0 | 1.308 | 100 |
| $\mathbf{2 6}$ | $\mathrm{C}_{6} \mathrm{H}_{6}$ | 0.480 | 0.342 | 0.139 | 29.9 | 1.394 | $100^{\mathrm{a}}$ |
| $\mathbf{2 7}$ | $\mathrm{H}_{4} \mathrm{C}_{3}=\mathrm{C}_{3} \mathrm{H}_{4}$ | 0.537 | 0.354 | 0.183 | 34.0 | 1.316 | 97 |
| $\mathbf{2 8}$ | $\mathrm{CH}_{2}=\mathrm{C}_{3} \mathrm{H}_{4}$ | 0.479 | 0.283 | 0.196 | 40.9 | 1.323 | 90 |
| $\mathbf{2 9}$ | $\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}_{2}$ | 0.521 | 0.267 | 0.254 | 48.8 | 1.332 | 81 |
| $\mathbf{3 0}$ | $\mathrm{CH}_{2}=\mathrm{CH}-\mathrm{CH}=\mathrm{CH}_{2}$ | 0.488 | 0.256 | 0.232 | 52.6 | 1.340 | 80 |
| $\mathbf{3 1}$ | cyclobutene | 0.519 | 0.283 | 0.236 | 45.5 | 1.350 | 77 |
| $\mathbf{3 2}$ | cyclopropene | 0.579 | 0.277 | 0.304 | 52.5 | 1.300 | 71.5 |
| $\mathbf{3 3}$ | $\mathrm{HC} \equiv \mathrm{C}-\mathrm{C} \equiv \mathrm{CH}$ | 0.577 | 0.159 | 0.418 | 72.4 | 1.219 | 60 |
| $\mathbf{3 4}$ | $\mathrm{HC} \equiv \mathrm{CH}$ | 0.616 | 0.145 | 0.471 | 76.5 | 1.211 | 60 |
| $\mathbf{3 5}$ | cyclopentyne | 0.524 | 0.087 | 0.437 | 83 | 1.245 | 40 |

[^2]

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34


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Figure 15. Bonds (red bold) and molecules of Table 5.

The $\langle\theta\rangle$ values corresponding to the $\sigma$ part of the double and triple bonds are greater than $90^{\circ}$ only in $\mathbf{2 5}, \mathbf{2 6}$ and 27 . Indeed, their $\Sigma_{\sigma}$ values are smaller than that of cyclopropane 19 (0.372 a.u.). The $\sigma$ participation to $\Sigma_{\text {tot }}$ is generally close to $50 \%$ in standard alkenes and no more than ca. $25 \%$ in alkynes, which has been already noted [16]. Their variations as a function of $\langle\theta\rangle$ are shown in Figure 16 with the same scale as in Figure 11 for the sake of comparison. Like in formally single bonds, $\Sigma_{\sigma}$ tends to decrease with $\langle\theta\rangle$, but significantly more slowly. From these results, the $\sigma$ bond in multiple bonds can be generally considered as formally inverted.


Figure 16 . Values of $\Sigma_{\sigma}$ (a.u.) for the $\sigma$ bond in the formally multiple bond compounds 22-33 (cyan diamonds). The red curve corresponds to the $\mathrm{C}_{2} \mathrm{H}_{6}$ model for comparison.

The series 27, $\mathbf{2 8}$ and 29 is illustrative of the influence of bond angles on $\sigma$ bonds in double bonds (Table 5). The presence of two and one cyclopropenyl fragments in 27 and 28 respectively tends to increase $\langle\theta\rangle$ and $\Sigma_{\sigma}$, with respect to 29 . The same evolution is observed from cyclobutene $\mathbf{3 1}$ to cyclopropene 32.

The $\sigma$ bonds of alkynes possess formally four C substituents at $0^{\circ}$ and thus have a maximum $\langle\theta\rangle$ value of $60^{\circ}$. Because cyclopropyne and cyclobutyne are unstable, cyclopentyne 35 appears to possess a $\sigma$ bond with the smallest possible $\langle\theta\rangle$ value ( $40^{\circ}$ ) and thus the weakest $\Sigma_{\sigma}$ (0.087 a.u.) among all multiple bonds considered. In turn, the small $\langle\theta>$ value for $\sigma$ in triple bonds entails for $\langle\theta\rangle(\mathrm{CH})$ its maximum theoretical value of $180^{\circ}$ in 33 and 34 , in agreement with high CH bond dissociation in acetylene and hydrogen cyanide.

## Conclusion

The bonding energy BE of the CC bond in the $\mathrm{CH}_{3}-\mathrm{CH}_{3}$ model is strongly dependant of the $\theta=\mathrm{HCC}$ angles, exhibiting a sigmoidal variation. Starting from $\theta$ equilibrium value, BE decreases rapidly when $\theta$ decreases to yield "inverted bonds" $\left(\theta<90^{\circ}\right)$ and tends to zero for $\theta=60^{\circ}-70^{\circ}$. On the contrary, $B E$ increases when $\theta$ increases above its equilibrium value. We propose the term "superdirect" for the latter type of bonds. Within MO framework, this general behaviour is closely related to the $s$ participation in the $s+p$ hybrid AOs involved in the CC bond.

These results are generalized to any CC sigma bond in hydrocarbons using the sum of dynamic orbital forces (DOF) as index of intrinsic bond energy. The strength of $\sigma$ bonds is essentially controlled by a unique $\langle\theta>$ parameter, mean value of its substituent angles. In formally single CC bonds, this strength increases according to a sigmoidal variation as function of $\langle\theta\rangle$ (from a panel of 24 bonds in 22 molecules). The difference of $\langle\theta\rangle$ from the standard value of ca. $110^{\circ}$ appears as a crude, but straightforward and robust, index of the strain exerted on a $\sigma$ bond. For $\left\langle\theta><110^{\circ}\right.$ values, this strain is "negative" which weakens
the bond as its "inverted" character increases; for $\left\langle\theta \gg 110^{\circ}\right.$ this strain is "positive", resulting in a strengthening of the bond as its "superdirect" character increases.

As a matter of fact, the weakest sigma bonds are encountered in tetraedrane $\left(\langle\theta\rangle=88^{\circ}\right)$, bicyclobutane $\left(\langle\theta\rangle=82^{\circ}\right)$, vanishing in propellane $\left(\langle\theta\rangle=60^{\circ}\right)$. At the opposite, the strongest $\sigma$ CC bonds are found in butadiyne ( $\langle\theta\rangle=180^{\circ}$ ) and bonds having tetrahedryl and/or ethynyl substituent(s) (< $\left\langle\gg 120^{\circ}\right.$ ). It also accounts for the strain energy of cyclanes.

We also considered $\sigma$ bonds in formally multiple bonds, with a panel of 11 molecules. These systems correspond to small $\langle\theta\rangle$ values and $\sigma$ bonds significantly weaker than in standard single bonds. This way, $\sigma$ bonds in multiple bonds can be considered as formally inverted in most of cases.
[1 ]R. Laplaza, J. Contreras-Garcia, F. Fuster, F. Volatron, P. Chaquin, Chem. Eur. J. 2020, 26, 6839-6845.
[2] a) K. B. Wiberg, F. H. Walker, J. Am. Ckem. Soc. 1982, 104, 5239-5240; b) D. Feller, E. R. Davidson, J. Am. Chem. Soc. 1987, 109, 4133-4139; c) J. E. Jackson, L. C. Allen, J. Am. Chem. Soc 1984, 106, 591-599.
[3] a) T. Kar, K. Jug, Chem. Phys. Lett. 1996, 256, 201-206; b) W. Wu, J. Gu, J. Song, S. Shaik, P. C. Hiberty Angew. Chem. 2009, 121, 1435 -1438; c) M. D. Newton, J. M. Schulman, J. Am. Chem. Soc. 1972, 94, 773-778; d) W. Stohrer, R. Hoffmann, J. Am. Chem. Soc. 1972, 94, 779-786; e) E. Honegger, H. Huber, E. Heilbronner, J. Am. Chem. Soc. 1985, 107, 7172-7174; f) O. Schafer, M. Allan, G. Szeimies, M. Sanktjohansert, J. Am. Chem. Soc. 1992,114,8180-8186; g) M. Messerschmidt, S. Scheins, L. Grubert, M.I Pätzel, G. Szeimies, C. Paulmann, P. Luger, Angew. Chem. Int. Ed. 2005, 44, 3925 -3928.
[4] B. Braïda, S. Shaik, W. Wu, P. C. Hiberty, Chem. Eur. J. 2020, 26, 5935-6939.
[5] S. Kozuch, Org. Lett. 2014, 16, 4102-4105.
[6] a) I. Fernandez, G. Frenking, Chem. Eur. J. 2006, 12, 3617 - 3629; b) G. Gayatri, Y. Soujanya, I. Fernández, G. Frenking, G. Narahari Sastry, J. Phys. Chem. A 2008, 112, 12919-12924. c) Y. Mo, Org. Lett. 2006, 8(3), 535538.
[7] Gaussian 09, Revision A.01, M. J. Frisch, G. W. Trucks, H. B. Schlegel, G. E. Scuseria, M. A. Robb, J. R. Cheeseman, G. Scalmani, V. Barone, B. Mennucci, G. A. Petersson, H. Nakatsuji, M. Caricato, X. Li, H. P. Hratchian, A. F. Izmaylov, J. Bloino, G. Zheng, J. L. Sonnenberg, M. Hada, M. Ehara, K. Toyota, R. Fukuda, J. Hasegawa, M. Ishida, T. Nakajima, Y. Honda, O. Kitao, H. Nakai, T. Vreven, J. A. Montgomery, Jr., J. E. Peralta, F. Ogliaro, M. Bearpark, J. J. Heyd, E. Brothers, K. N. Kudin, V. N. Staroverov, R. Kobayashi, J. Normand, K. Raghavachari, A. Rendell, J. C. Burant, S. S. Iyengar, J. Tomasi, M. Cossi, N. Rega, J. M. Millam, M. Klene, J. E. Knox, J. B. Cross, V. Bakken, C. Adamo, J. Jaramillo, R. Gomperts, R. E. Stratmann, O. Yazyev, A. J. Austin, R. Cammi, C. Pomelli, J. W. Ochterski, R. L. Martin, K. Morokuma, V. G. Zakrzewski, G. A. Voth, P. Salvador, J. J. Dannenberg, S. Dapprich, A. D. Daniels, Ö. Farkas, J. B. Foresman, J. V. Ortiz, J. Cioslowski, D. J. Fox, Gaussian, Inc., Wallingford CT, 2009
[8] Y. Yamaguchi, B. C. Hoffman, J. C. Stephens, H. F. Schaefer, J. Phys. Chem. A 1999, 103, 38, 7701-7708
[9] W. A. Shirley, R. Hoffmann, V. S. Mastryukov, J. Phys. Chem. 1995, 99, 4025.
[10] a) H. A. Bent, J. Chem. Educ. 1960, 37 (12), 616-624; b) M. J. S. Dewar, H. N. Schmeising, Tetrahedron 1959, 5, 166-178; c) R. A. Alden, J. Kraut, T. G. Traylor, J. Am. Chem. Soc. 1968, 90, 74-82; d) S. Osawa, M. Sakai, E. Osawa, J. Phys. Chem. A 1997, 101, 1378-1383. e) M. G. Brown Trans. Faraday Soc., 1959, 55, 694-700. f) D.
A. Root, C. R. Landis, T. Cleveland, J. Am. Chem. Soc. 1993, 115, 4201-4209
[11] M. Tanaka, A. Sekiguchi, Angew. Chem., Int. Ed. 2005, 44, 5821-5823
[12] a) A. Krapp, F. M. Bickelhaupt, G. Frenking, Chem. Eur. J. 2006, 12, 9196-9216.
[13] P. Vermeeren, W-J. van Zeist, T. A. Hamlin, C. Fonseca Guerra, F. M. Bickelhaupt, Chem. Eur. J. 2021 doi.org/10.1002/chem. 202004653
[14] F.W. Averill, G. S Painter, Phys. Rev. B 1986, 34(4) 2088-2095
[15] a) F.M.Bickelhaupt, J. K. Nagle, W.L. Klemm, J. Phys. Chem. A 2008, 112, 2437-2446; b) P. J. Robinson, A.N. Alexandrova, J. Phys. Chem. A 2015, 119, 12862-12867. c) P. Chaquin, Y. Canac , C. Lepetit, D. Zargarian, R. Chauvin, Int. J. Quant. Chem. 2016, 116, 1285-1295; d) P. Chaquin, F. Fuster, F. Volatron, Int. J. Quant. Chem 2018, 118, 25658-25659
[16] T. Tal, J. Katriel, Theoret. Chim. Acta 1977, 46, 173-181
[17] a) Y. Yamaguchi, R.B. Remington, J.F. Gaw, H. F. Schaefer III, G. Frenking, Chem. Phys. 1994, 180, 55-70; b) Y. Yamaguchi, R.B. Remington, J.F. Gaw, H. F. Schaefer III, G. Frenking, J. Chem. Phys. 1993, 98 (11), 8749-8760; c) Yamaguchi, B. J. DeLeeuw, C. A. Richards, Jr., H. F. Schaefer III, G. Frenking. J. Am. Chem. Soc. 1994, 116, 11922-11930.
[18] F. Fuster, P. Chaquin, Int. J. Quant. Chem. 2019,119 (20), e25996
[19] R. Laplaza, V. Polo, J. Contreras-Garcia, J. Phys. Chem. A 2020, 124, 176-184
[20] a) K. Exner, P.v. R. Schleyer, J. Phys. Chem. A 2001, 105, 3407-3416; b) S. Grimme, J. Am. Chem. Soc. 1996, 118, 1529-1534
[21] R. Laplaza, C. Cardenas, P. Chaquin, J. Contreras-Garcia, P. W. Ayers, J. Comp. Chem. 2020, 42 (5), 334-343
[22] J. Blanksby, G. B. Ellison, Acc. Chem. Res. 2003, 36, 4, 255-263
[23] Y. Mo, Org. Lett. 2006, 8(3), 535-538.
[24] a) K. W. Wiberg, Angew. Chem. Int. Ed. Eng. 1986, 25, 312-322; b) K. W. Wiberg, R.A. Fenoglio, J. Am. Chem. Soc. 1968, 90, 3395-3397.
[25] D.Cremer, J. Gauss, J. Am. Chem. Soc. 1986, 108, 7467-7477
[26] a) R. D. Bach, O. Dimitrenko, J. Org. Chem. 2002, 67, 3884-3896; b) R. D. Bach, O. Dimitrenko, J. Am. Chem. Soc. 2004 126, 4444-4452.

Supplementary data
$\mathrm{Si}_{2} \mathrm{H}_{6}$ and $\mathrm{Ge}_{2} \mathrm{H}_{6}$ model. Geometrical parameters $\mathrm{R}(\mathrm{A})$ and bonding energy BE (kcal/mol with respect to two $\mathrm{AH}_{3}$ in frozen geometry) as functions of $\theta$; opt $=110.4^{\circ}\left(\mathrm{Si}_{2} \mathrm{H}_{6}\right)$; opt $=110.4^{\circ}\left(\mathrm{Ge}_{2} \mathrm{H}_{6}\right)$; MP2/ccpVTZ level of calculation.

|  | $\mathrm{Si}_{2} \mathrm{H}_{6}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :---: | :--- | :--- | :--- | :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\theta$ | $140^{\circ}$ | $130^{\circ}$ | $120^{\circ}$ | opt | $100^{\circ}$ | $90^{\circ}$ | $80^{\circ}$ | $70^{\circ}$ | $60^{\circ}$ |  |  |  |  |  |  |  |
| $\mathrm{R}(\mathrm{SiSi})$ | 2.242 | 2.289 | 2.321 | 2.351 | 2.394 | 2.492 | 2.726 | 3.038 | 3.287 |  |  |  |  |  |  |  |
| $\mathrm{R}(\mathrm{SiH})$ | 1.517 | 1.497 | 1.486 | 1.481 | 1.477 | 1.471 | 1.469 | 1.483 | 1.501 |  |  |  |  |  |  |  |
| BE | 83.9 | 81.8 | 80.2 | 76.8 | 68.8 | 45.6 | 15.3 | 1.1 | -0.4 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  | $\mathrm{Ge}_{2} \mathrm{H}_{6}$ |  |  |  |  |  |
| $\theta$ | $140^{\circ}$ | $130^{\circ}$ | $120^{\circ}$ | opt | $100^{\circ}$ | $90^{\circ}$ | $80^{\circ}$ | $70^{\circ}$ | $60^{\circ}$ |  |  |  |  |  |  |  |
| $\mathrm{R}(\mathrm{GeGe})$ | 2.271 | 2.316 | 2.357 | 2.398 | 2.458 | 2.568 | 2.800 | 3.068 | 3.281 |  |  |  |  |  |  |  |
| $\mathrm{R}(\mathrm{GeH})$ | 1.554 | 1.536 | 1.525 | 1.518 | 1.513 | 1.505 | 1.505 | 1.523 | 1.546 |  |  |  |  |  |  |  |
| BE | 83.8 | 81.3 | 79.0 | 74.5 | 65.1 | 44.1 | 17.7 | 6.0 | 5.7 |  |  |  |  |  |  |  |

$\mathrm{N}_{2} \mathrm{H}_{4}$ in $\mathrm{D}_{2 d}$ symmetry. Geometrical parameters $\mathrm{R}(\mathrm{A})$ and bonding energy BE (kcal/mol with respect to two $\mathrm{NH}_{2}$ in frozen geometry) as functions of $\theta$; opt $=119.9^{\circ}$; $\mathrm{MP2} / \mathrm{cc}-\mathrm{pvTZ}$ level of calculation.

|  |  | $\mathrm{N}_{2} \mathrm{H}_{4} \mathrm{D}_{2 \mathrm{~d}}$ |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :---: | :---: | :---: |
| $\theta$ | $150^{\circ}$ | $130^{\circ}$ | opt | $110^{\circ}$ | $100^{\circ}$ | $90^{\circ}$ | $80^{\circ}$ | $70^{\circ}$ | $60^{\circ}$ |  |  |  |
| $\mathrm{R}(\mathrm{NN})$ | 1.299 | 1.326 | 1.363 | 1.420 | 1.507 | 1.647 | 1.852 | 2.054 | 2.196 |  |  |  |
| $\mathrm{R}(\mathrm{NH})$ | 1.039 | 1.008 | 1.000 | 0.995 | 0.993 | 0.992 | 0.997 | 1.008 | 1.024 |  |  |  |
| $B E$ | 166.7 | 156.63 | 141.0 | 119.0 | 91.0 | 58.6 | 31.0 | 16.3 | 11.2 |  |  |  |

Optimized geometries of molecules studied (MP2/cc-pvtz level)

## Butadiyne

$\qquad$

| 1 | 6 | 0 | 0.000000 | 0.000000 | 0.684335 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 2 | 6 | 0 | 0.000000 | 0.000000 | -0.684335 |
| 3 | 6 | 0 | 0.000000 | 0.000000 | 1.903689 |
| 4 | 6 | 0 | 0.000000 | 0.000000 | -1.903689 |
| 5 | 1 | 0 | 0.000000 | 0.000000 | 2.965786 |
| 6 | 1 | 0 | 0.000000 | 0.000000 | -2.965786 |

Tetrahedrylacetylene

| ----------------------------------------------------------- |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 6 | 0 | 0.000000 | 0.000000 | 1.365443 |
| 2 | 6 | 0 | 0.000000 | 0.000000 | -0.028739 |
| 3 | 6 | 0 | 0.000000 | 0.852836 | -1.245152 |
| 4 | 6 | 0 | 0.738578 | -0.426418 | -1.245152 |
| 5 | 6 | 0 | -0.738578 | -0.426418 | -1.245152 |
| 6 | 1 | 0 | 0.000000 | 1.865724 | -1.584871 |
| 7 | 1 | 0 | 1.615765 | -0.932862 | -1.584871 |
| 8 | 1 | 0 | -1.615765 | -0.932862 | -1.584871 |
| 9 | 6 | 0 | 0.000000 | 0.000000 | 2.583686 |
| 10 | 1 | 0 | 0.000000 | 0.000000 | 3.645005 |

## Tetrahedryl-tetrahedrane

| 1 | 6 | 0 | 0.000000 | 0.000000 | 0.709477 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 6 | 0 | -0.000000 | -0.000000 | -0.709477 |
| 3 | 6 | 0 | 0.740741 | 0.427667 | -1.919852 |
| 4 | 6 | 0 | -0.000000 | -0.855335 | -1.919852 |
| 5 | 6 | 0 | -0.740741 | 0.427667 | -1.919852 |
| 6 | 6 | 0 | 0.000000 | 0.855335 | 1.919852 |
| 7 | 6 | 0 | 0.740741 | -0.427667 | 1.919852 |
| 8 | 6 | 0 | -0.740741 | -0.427667 | 1.919852 |
| 9 | 1 | 0 | 1.610621 | 0.929892 | -2.283026 |
| 10 | 1 | 0 | -0.000000 | -1.859785 | -2.283026 |
| 11 | 1 | 0 | -1.610621 | 0.929892 | -2.283026 |
| 12 | 1 | 0 | 0.000000 | 1.859785 | 2.283026 |
| 13 | 1 | 0 | 1.610621 | -0.929892 | 2.283026 |
| 14 | 1 | 0 | -1.610621 | -0.929892 | 2.283026 |

## Propyne

| 1 | 6 | 0 | 0.000000 | 0.000000 | -1.243796 |
| ---: | ---: | ---: | ---: | ---: | ---: |
| 2 | 6 | 0 | 0.000000 | 0.000000 | 0.214652 |
| 3 | 1 | 0 | 0.000000 | 1.017866 | -1.628225 |
| 4 | 1 | 0 | 0.881498 | -0.508933 | -1.628225 |
| 5 | 1 | 0 | -0.881498 | -0.508933 | -1.628225 |
| 6 | 6 | 0 | 0.000000 | 0.000000 | 1.428404 |
| 7 | 1 | 0 | 0.000000 | 0.000000 | 2.489115 |

Methyl-tetrahedrane

| 1 | 6 | 0 | 0.000000 | 0.000000 | 1.809723 |
| :---: | :---: | :---: | ---: | ---: | ---: |
| 2 | 6 | 0 | 0.000000 | 0.000000 | 0.333615 |
| 3 | 6 | 0 | 0.000000 | 0.855953 | -0.872305 |
| 4 | 6 | 0 | 0.741277 | -0.427977 | -0.872305 |
| 5 | 6 | 0 | -0.741277 | -0.427977 | -0.872305 |
| 6 | 1 | 0 | 0.000000 | 1.855820 | -1.246812 |
| 7 | 1 | 0 | 1.607187 | -0.927910 | -1.246812 |
| 8 | 1 | 0 | -1.607187 | -0.927910 | -1.246812 |
| 9 | 1 | 0 | 0.000000 | -1.019353 | 2.193965 |
| 10 | 1 | 0 | -0.882786 | 0.509677 | 2.193965 |
| 11 | 1 | 0 | 0.882786 | 0.509677 | 2.193965 |

## Cubyl-cubane

| 1 | 6 | 0 | 0.000000 | 0.000000 | 0.000000 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 6 | 0 | 0.000000 | 0.000000 | 1.571683 |
| 3 | 6 | 0 | 1.564587 | 0.000000 | 1.563699 |
| 4 | 6 | 0 | 1.571620 | -0.001858 | -0.000904 |
| 5 | 6 | 0 | 1.561805 | -1.566438 | -0.003751 |
| 6 | 6 | 0 | -0.002810 | -1.571615 | -0.000960 |
| 7 | 6 | 0 | -0.004724 | -1.564601 | 1.563656 |
| 8 | 6 | 0 | 1.560369 | -1.565085 | 1.561350 |
| 9 | 1 | 0 | 2.187615 | -2.194280 | 2.189101 |
| 10 | 1 | 0 | 2.195543 | 0.623338 | 2.193543 |
| 11 | 1 | 0 | -0.629997 | -2.193672 | 2.193462 |
| 12 | 1 | 0 | -0.632916 | 0.634845 | 2.189688 |
| 13 | 1 | 0 | 2.190536 | -2.196997 | -0.628610 |
| 14 | 1 | 0 | 2.190007 | 0.631496 | -0.634941 |
| 15 | 1 | 0 | -0.637966 | -2.188119 | -0.635030 |
| 16 | 6 | 0 | -0.844965 | 0.847669 | -0.845468 |
| 17 | 6 | 0 | -0.842083 | 2.419360 | -0.844281 |
| 18 | 6 | 0 | -0.844927 | 0.847986 | -2.417124 |
| 19 | 6 | 0 | -2.416665 | 0.849702 | -0.844613 |
| 20 | 6 | 0 | -2.409524 | 0.848079 | -2.409221 |
| 21 | 6 | 0 | -0.840115 | 2.412553 | -2.408885 |
| 22 | 6 | 0 | -2.406693 | 2.414307 | -0.841568 |
| 23 | 6 | 0 | -2.405207 | 2.413162 | -2.406665 |
| 24 | 1 | 0 | -0.212059 | 0.213260 | -3.035289 |
| 25 | 1 | 0 | -3.035161 | 0.216330 | -0.210713 |
| 26 | 1 | 0 | -3.032426 | 3.042491 | -3.034294 |
| 27 | 1 | 0 | -3.035379 | 3.044850 | -0.216659 |
| 28 | 1 | 0 | -0.214832 | 3.041733 | -3.038567 |
| 29 | 1 | 0 | -0.206921 | 3.035715 | -0.210086 |
| 30 | 1 | 0 | -3.040474 | 0.224921 | -3.039236 |

Bicyclopentyl-bicyclopentane

| 1 | 6 | 0 | 0.000000 | 0.000000 | 0.000000 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 6 | 0 | 0.000000 | 0.000000 | 1.476529 |
| 3 | 6 | 0 | 1.235875 | 0.000000 | -0.945198 |
| 4 | 6 | 0 | -0.617937 | 1.070299 | -0.945198 |
| 5 | 6 | 0 | -0.617937 | -1.070299 | -0.945198 |
| 6 | 6 | 0 | 0.617937 | 1.070299 | 2.421727 |
| 7 | 6 | 0 | 0.617937 | -1.070299 | 2.421727 |
| 8 | 6 | 0 | -1.235875 | 0.000000 | 2.421727 |
| 9 | 1 | 0 | 1.841954 | 0.905975 | -0.940633 |
| 10 | 1 | 0 | 1.841954 | -0.905975 | -0.940633 |
| 11 | 1 | 0 | -0.136379 | 2.048166 | -0.940633 |
| 12 | 1 | 0 | -1.705574 | 1.142191 | -0.940633 |
| 13 | 1 | 0 | -1.705574 | -1.142191 | -0.940633 |
| 14 | 1 | 0 | -0.136379 | -2.048166 | -0.940633 |
| 15 | 1 | 0 | 0.136379 | 2.048166 | 2.417163 |
| 16 | 1 | 0 | 1.705574 | 1.142191 | 2.417163 |
| 17 | 1 | 0 | 1.705574 | -1.142191 | 2.417163 |
| 18 | 1 | 0 | 0.136379 | -2.048166 | 2.417163 |
| 19 | 1 | 0 | -1.841954 | 0.905975 | 2.417163 |
| 20 | 1 | 0 | -1.841954 | -0.905975 | 2.417163 |
| 21 | 6 | 0 | 0.000017 | 0.000017 | -1.878476 |
| 22 | 6 | 0 | -0.000011 | -0.000020 | 3.355005 |
| 23 | 1 | 0 | -0.000025 | -0.000043 | 4.442214 |
| 24 | 1 | 0 | 0.000033 | 0.000038 | -2.965685 |

## Butadiene

| 1 | 6 | 0 | -0.329758 | 0.647521 | -0.000000 |
| :---: | :---: | :---: | ---: | ---: | ---: |
| 2 | 6 | 0 | 0.329758 | -0.647521 | -0.000000 |
| 3 | 6 | 0 | 0.329758 | 1.814118 | -0.000000 |
| 4 | 6 | 0 | -0.329758 | -1.814118 | -0.000000 |
| 5 | 1 | 0 | -1.414227 | 0.645163 | -0.000000 |
| 6 | 1 | 0 | 1.414227 | -0.645163 | 0.000000 |
| 7 | 1 | 0 | -0.194087 | 2.758274 | -0.000000 |
| 8 | 1 | 0 | 0.194087 | -2.758274 | -0.000000 |
| 9 | 1 | 0 | 1.411329 | 1.839762 | -0.000000 |
| 10 | 1 | 0 | -1.411329 | -1.839762 | -0.000000 |

## Propene

| 1 | 6 | 0 | -1.232913 | -0.158738 | 0.000026 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 2 | 1 | 0 | -2.015649 | 0.595245 | -0.000171 |
| 3 | 1 | 0 | -1.377883 | -0.786249 | 0.878373 |
| 4 | 1 | 0 | -1.377606 | -0.785975 | -0.878623 |
| 5 | 6 | 0 | 0.136158 | 0.466050 | 0.000056 |
| 6 | 6 | 0 | 1.275252 | -0.228612 | -0.000008 |
| 7 | 1 | 0 | 0.192737 | 1.547745 | 0.000065 |
| 8 | 1 | 0 | 2.234189 | 0.268016 | -0.000137 |
| 9 | 1 | 0 | 1.273235 | -1.310985 | 0.000047 |

Toluene

| 1 | 6 | 0 | -2.415144 | -0.002270 | 0.000033 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 1 | 0 | -2.809508 | -1.016360 | 0.000061 |
| 3 | 1 | 0 | -2.804712 | 0.511247 | 0.878884 |
| 4 | 6 | 0 | -0.912107 | -0.006142 | -0.000063 |
| 5 | 1 | 0 | -2.805010 | 0.511537 | -0.878477 |
| 6 | 6 | 0 | -0.199887 | 1.197282 | -0.000047 |
| 7 | 6 | 0 | 1.192018 | 1.206440 | 0.000005 |
| 8 | 6 | 0 | 1.898648 | 0.004672 | 0.000043 |
| 9 | 6 | 0 | 1.202335 | -1.200913 | 0.000010 |
| 10 | 6 | 0 | -0.191752 | -1.201943 | -0.000057 |
| 11 | 1 | 0 | -0.742565 | 2.134899 | -0.000057 |
| 12 | 1 | 0 | 1.724139 | 2.148118 | 0.000019 |
| 13 | 1 | 0 | 2.979900 | 0.009033 | 0.000096 |
| 14 | 1 | 0 | 1.741288 | -2.138667 | 0.000022 |
| 15 | 1 | 0 | -0.728201 | -2.142563 | -0.000091 |


| 1 | 6 | 0 | 0.000000 | 0.000000 | 0.782528 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 6 | 0 | 0.000000 | 0.000000 | -0.782528 |
| 3 | 6 | 0 | -1.418321 | 0.164956 | 1.337132 |
| 4 | 6 | 0 | 0.566304 | -1.310780 | 1.337132 |
| 5 | 6 | 0 | 0.852017 | 1.145824 | 1.337132 |
| 6 | 6 | 0 | -0.852017 | 1.145824 | -1.337132 |
| 7 | 6 | 0 | 1.418321 | 0.164956 | -1.337132 |
| 8 | 6 | 0 | -0.566304 | -1.310780 | -1.337132 |
| 9 | 1 | 0 | 1.815450 | 1.159684 | -1.139447 |
| 10 | 1 | 0 | -0.562430 | 2.110427 | -0.920393 |
| 11 | 1 | 0 | 2.108898 | -0.568135 | -0.920393 |
| 12 | 1 | 0 | 1.403062 | 0.025100 | -2.419069 |
| 13 | 1 | 0 | -0.723268 | 1.202537 | -2.419069 |
| 14 | 1 | 0 | -1.912041 | 0.992384 | -1.139447 |
| 15 | 1 | 0 | -0.679794 | -1.227637 | -2.419069 |
| 16 | 1 | 0 | 0.096591 | -2.152068 | -1.139447 |
| 17 | 1 | 0 | -1.546468 | -1.542292 | -0.920393 |
| 18 | 1 | 0 | 0.723268 | 1.202537 | 2.419069 |
| 19 | 1 | 0 | 1.912041 | 0.992384 | 1.139447 |
| 20 | 1 | 0 | 0.562430 | 2.110427 | 0.920393 |
| 21 | 1 | 0 | -2.108898 | -0.568135 | 0.920393 |
| 22 | 1 | 0 | -1.403062 | 0.025100 | 2.419069 |
| 23 | 1 | 0 | -1.815450 | 1.159684 | 1.139447 |
| 24 | 1 | 0 | -0.096591 | -2.152068 | 1.139447 |
| 25 | 1 | 0 | 1.546468 | -1.542292 | 0.920393 |
| 26 | 1 | 0 | 0.679794 | -1.227637 | 2.419069 |

Cyclohexane

| 1 | 6 | 0 | 1.135709 | 0.904931 | 0.234992 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 6 | 0 | 1.351539 | -0.531060 | -0.235023 |
| 3 | 6 | 0 | 0.215871 | -1.435970 | 0.235046 |
| 4 | 6 | 0 | -1.135653 | -0.904953 | -0.235030 |
| 5 | 6 | 0 | -1.351569 | 0.531021 | 0.235001 |
| 6 | 6 | 0 | -0.215902 | 1.435983 | -0.234971 |
| 7 | 1 | 0 | 2.310794 | -0.907935 | 0.122777 |
| 8 | 1 | 0 | 1.391821 | -0.546973 | -1.328254 |
| 9 | 1 | 0 | 0.222265 | -1.478672 | 1.328277 |
| 10 | 1 | 0 | 0.369094 | -2.455198 | -0.122635 |
| 11 | 1 | 0 | -1.169452 | -0.931908 | -1.328262 |
| 12 | 1 | 0 | -1.941698 | -1.547264 | 0.122692 |
| 13 | 1 | 0 | -2.310748 | 0.907970 | -0.122915 |
| 14 | 1 | 0 | -1.392020 | 0.546846 | 1.328230 |
| 15 | 1 | 0 | -0.369039 | 2.455110 | 0.123009 |
| 16 | 1 | 0 | -0.222352 | 1.479022 | -1.328207 |
| 17 | 1 | 0 | 1.169764 | 0.932036 | 1.328225 |
| 18 | 1 | 0 | 1.941597 | 1.547257 | -0.123020 |

## Methylenecyclopropane

| 1 | 6 | 0 | 0.000000 | 0.000000 | 1.637560 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 6 | 0 | 0.000000 | 0.000000 | 0.314826 |
| 3 | 6 | 0 | -0.000000 | 0.769522 | -0.930967 |
| 4 | 6 | 0 | -0.000000 | -0.769522 | -0.930967 |
| 5 | 1 | 0 | -0.000000 | 0.927484 | 2.192993 |
| 6 | 1 | 0 | -0.000000 | -0.927484 | 2.192993 |
| 7 | 1 | 0 | -0.912752 | 1.264168 | -1.232173 |
| 8 | 1 | 0 | 0.912752 | 1.264168 | -1.232173 |
| 9 | 1 | 0 | 0.912752 | -1.264168 | -1.232173 |
| 10 | 1 | 0 | -0.912752 | -1.264168 | -1.232173 |

## Cyclopentane

| 1 | 6 | 0 | 0.775713 | -1.027363 | -0.072565 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 6 | 0 | 1.199241 | 0.416969 | 0.216013 |
| 3 | 6 | 0 | 0.000454 | 1.232464 | -0.280599 |
| 4 | 6 | 0 | -1.198909 | 0.417850 | 0.216070 |
| 5 | 6 | 0 | -0.776509 | -1.026785 | -0.072642 |
| 6 | 1 | 0 | 1.316189 | 0.572102 | 1.289968 |
| 7 | 1 | 0 | 2.137055 | 0.689412 | -0.264202 |
| 8 | 1 | 0 | 0.000449 | 1.253947 | -1.373199 |
| 9 | 1 | 0 | 0.000822 | 2.262668 | 0.073374 |
| 10 | 1 | 0 | -2.136629 | 0.691169 | -0.263845 |
| 11 | 1 | 0 | -1.315456 | 0.572858 | 1.290087 |
| 12 | 1 | 0 | -1.147928 | -1.333823 | -1.049694 |
| 13 | 1 | 0 | -1.185977 | -1.725700 | 0.654397 |
| 14 | 1 | 0 | 1.147130 | -1.335104 | -1.049397 |
| 15 | 1 | 0 | 1.184406 | -1.726337 | 0.654847 |

Cyclobutene

| 1 | 6 | 0 | -0.909002 | 0.604983 | 0.002790 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 6 | 0 | -0.496336 | -0.884221 | -0.021184 |
| 3 | 6 | 0 | 0.988341 | -0.455433 | 0.000554 |
| 4 | 6 | 0 | 0.599137 | 0.837360 | 0.021080 |
| 5 | 1 | 0 | -1.425772 | 0.508830 | 0.955495 |
| 6 | 1 | 0 | -0.810247 | -1.499500 | 0.819550 |
| 7 | 1 | 0 | -0.666874 | -1.450130 | -0.934753 |
| 8 | 1 | 0 | -1.352216 | 1.011522 | -0.903980 |
| 9 | 1 | 0 | 1.963360 | -0.924442 | 0.000822 |
| 10 | 1 | 0 | 1.198911 | 1.737583 | 0.043429 |

Cyclobutane

| ------------------------------------------------------------------0. |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 6 | 0 | 0.757332 | -0.757538 | -0.152879 |
| 2 | 6 | 0 | 0.757531 | 0.757298 | 0.152889 |
| 3 | 6 | 0 | -0.757304 | 0.757526 | -0.152888 |
| 4 | 6 | 0 | -0.757559 | -0.757311 | 0.152878 |
| 5 | 1 | 0 | 0.934441 | -0.934560 | -1.212866 |
| 6 | 1 | 0 | -1.406096 | -1.405694 | -0.431553 |
| 7 | 1 | 0 | -0.934720 | -0.934278 | 1.212866 |
| 8 | 1 | 0 | 1.405673 | -1.406115 | 0.431555 |
| 9 | 1 | 0 | -1.405671 | 1.406100 | 0.431531 |
| 10 | 1 | 0 | 0.934686 | 0.934371 | 1.212858 |
| 11 | 1 | 0 | 1.406090 | 1.405678 | -0.431534 |
| 12 | 1 | 0 | -0.934402 | 0.934651 | -1.212858 |

## Cyclopropane

| 1 | 6 | 0 | 0.522701 | 0.522701 | 0.522701 |
| :--- | :--- | :--- | ---: | ---: | ---: |
| 2 | 6 | 0 | -0.522701 | -0.522701 | 0.522701 |
| 3 | 6 | 0 | -0.522701 | 0.522701 | -0.522701 |
| 4 | 6 | 0 | 0.522701 | -0.522701 | -0.522701 |
| 5 | 1 | 0 | -1.138859 | -1.138859 | 1.138859 |
| 6 | 1 | 0 | 1.138859 | -1.138859 | -1.138859 |
| 7 | 1 | 0 | 1.138859 | 1.138859 | 1.138859 |
| 8 | 1 | 0 | -1.138859 | 1.138859 | -1.138859 |

## Cyclopropene

| 1 | 6 | 0 | 0.000000 | -0.000000 | 0.861579 |
| ---: | ---: | ---: | ---: | ---: | ---: |
| 2 | 6 | 0 | -0.000000 | 0.649373 | -0.499546 |
| 3 | 6 | 0 | -0.000000 | -0.649373 | -0.499546 |
| 4 | 1 | 0 | -0.000000 | 1.578880 | -1.035900 |
| 5 | 1 | 0 | -0.000000 | -1.578880 | -1.035900 |
| 6 | 1 | 0 | -0.912333 | 0.000000 | 1.448438 |
| 7 | 1 | 0 | 0.912333 | -0.000000 | 1.448438 |

## Tetrahedrane

| 1 | 6 | 0 | 0.522701 | 0.522701 | 0.522701 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 2 | 6 | 0 | -0.522701 | -0.522701 | 0.522701 |
| 3 | 6 | 0 | -0.522701 | 0.522701 | -0.522701 |
| 4 | 6 | 0 | 0.522701 | -0.522701 | -0.522701 |
| 5 | 1 | 0 | -1.138859 | -1.138859 | 1.138859 |
| 6 | 1 | 0 | 1.138859 | -1.138859 | -1.138859 |
| 7 | 1 | 0 | 1.138859 | 1.138859 | 1.138859 |
| 8 | 1 | 0 | -1.138859 | 1.138859 | -1.138859 |

## Bicyclobutane

| 1 | 6 | 0 | 0.750113 | -0.000000 | -0.313997 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 6 | 0 | -0.750113 | 0.000000 | -0.313997 |
| 3 | 6 | 0 | -0.000000 | 1.130771 | 0.312484 |
| 4 | 6 | 0 | -0.000000 | -1.130771 | 0.312484 |
| 5 | 1 | 0 | -0.000000 | 1.214060 | 1.395784 |
| 6 | 1 | 0 | 0.000000 | 2.073678 | -0.219140 |
| 7 | 1 | 0 | -0.000000 | -1.214060 | 1.395784 |
| 8 | 1 | 0 | -0.000000 | -2.073678 | -0.219140 |
| 9 | 1 | 0 | 1.401767 | -0.000000 | -1.167567 |
| 10 | 1 | 0 | -1.401767 | 0.000000 | -1.167567 |

## [1.1.1] Propellane

| ------------------------------------------------------------- |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 6 | 0 | 0.000000 |  |  |
| 2 | 6 | 0 | 0.000000 | 1.2900000 | 0.797800 |
| 3 | 6 | 0 | 0.000000 | 0.000000 | 0.00000 |
| 4 | 6 | 0 | -1.117692 | -0.645300 | 0.000000 |
| 5 | 6 | 0 | 1.117692 | -0.645300 | 0.000000 |
| 6 | 1 | 0 | 0.917248 | 1.864705 | 0.000000 |
| 7 | 1 | 0 | -0.917248 | 1.864705 | -0.000000 |
| 8 | 1 | 0 | -1.156257 | -1.726713 | 0.000000 |
| 9 | 1 | 0 | -2.073506 | -0.137992 | 0.000000 |
| 10 | 1 | 0 | 2.073506 | -0.137992 | -0.000000 |
| 11 | 1 | 0 | 1.156257 | -1.726713 | 0.00000 |

Allene

| 1 | 6 | 0 | 0.000000 | -0.000000 | 0.861579 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 2 | 6 | 0 | -0.000000 | 0.649373 | -0.499546 |
| 3 | 6 | 0 | -0.000000 | -0.649373 | -0.499546 |
| 4 | 1 | 0 | -0.000000 | 1.578880 | -1.035900 |
| 5 | 1 | 0 | -0.000000 | -1.578880 | -1.035900 |
| 6 | 1 | 0 | -0.912333 | 0.000000 | 1.448438 |
| 7 | 1 | 0 | 0.912333 | -0.000000 | 1.448438 |

Benzene

| -------------------------------------------------------------- |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 6 | 0 | 0.000000 | 1.393655 | 0.000000 |
| 2 | 6 | 0 | 1.206941 | 0.696827 | 0.000000 |
| 3 | 6 | 0 | 1.206941 | -0.696827 | 0.000000 |
| 4 | 6 | 0 | -0.000000 | -1.393655 | -0.000000 |
| 5 | 6 | 0 | -1.206941 | -0.696827 | 0.000000 |
| 6 | 6 | 0 | -1.206941 | 0.696827 | 0.000000 |
| 7 | 1 | 0 | 0.000000 | -2.475102 | -0.000000 |
| 8 | 1 | 0 | 2.143501 | -1.237551 | -0.000000 |
| 9 | 1 | 0 | -2.143501 | -1.237551 | -0.000000 |
| 10 | 1 | 0 | 2.143501 | 1.237551 | -0.000000 |
| 11 | 1 | 0 | -2.143501 | 1.237551 | -0.000000 |
| 12 | 1 | 0 | 0.000000 | 2.475102 | 0.000000 |

Cyclopropenylcyclopropane

| 1 | 6 | 0 | 0.000000 | 0.000000 | -0.658092 |
| :--- | :--- | :--- | ---: | ---: | ---: |
| 2 | 6 | 0 | -0.000000 | 0.000000 | 0.658122 |
| 3 | 6 | 0 | -0.000000 | 0.823752 | 1.846708 |
| 4 | 6 | 0 | -0.000000 | -0.823752 | 1.846708 |
| 5 | 1 | 0 | 0.921944 | 1.143333 | 2.307577 |
| 6 | 1 | 0 | -0.921944 | 1.143333 | 2.307577 |
| 7 | 1 | 0 | -0.921944 | -1.143333 | 2.307577 |
| 8 | 1 | 0 | 0.921944 | -1.143333 | 2.307577 |
| 9 | 6 | 0 | 0.000000 | -0.823752 | -1.846678 |
| 10 | 6 | 0 | 0.000000 | 0.823752 | -1.846678 |
| 11 | 1 | 0 | -0.921944 | -1.143097 | -2.307711 |
| 12 | 1 | 0 | 0.921944 | -1.143097 | -2.307711 |
| 13 | 1 | 0 | 0.921944 | 1.143097 | -2.307711 |
| 14 | 1 | 0 | -0.921944 | 1.143097 | -2.307711 |

Ethylene

| 1 | 6 | 0 | 0.000000 | 0.000000 | 0.666024 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 6 | 0 | 0.000000 | 0.000000 | -0.666024 |
| 3 | 1 | 0 | 0.000000 | 0.922818 | 1.227906 |
| 4 | 1 | 0 | -0.000000 | -0.922818 | 1.227906 |
| 5 | 1 | 0 | -0.000000 | -0.922818 | -1.227906 |
| 6 | 1 | 0 | 0.000000 | 0.922818 | -1.227906 |

Acetylene

| 1 | 6 | 0 | 0.000000 | 0.000000 | 0.605689 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 6 | 0 | 0.000000 | 0.000000 | -0.605689 |
| 3 | 1 | 0 | 0.000000 | 0.000000 | -1.667231 |
| 4 | 1 | 0 | -0.000000 | 0.000000 | 1.667231 |

Cyclopentyne

| -------------------------------------------------------------1.0 |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 6 | 0 | 1.159043 | 0.622398 | 0.000000 |
| 2 | 6 | 0 | -0.185533 | 1.278265 | 0.000000 |
| 3 | 6 | 0 | -1.124324 | 0.000015 | 0.000000 |
| 4 | 6 | 0 | -0.185533 | -1.278236 | 0.000000 |
| 5 | 6 | 0 | 1.159043 | -0.622369 | 0.000000 |
| 6 | 1 | 0 | -0.346237 | 1.900966 | 0.878197 |
| 7 | 1 | 0 | -0.346237 | 1.900966 | -0.878197 |
| 8 | 1 | 0 | -0.346237 | -1.900936 | -0.878197 |
| 9 | 1 | 0 | -0.346237 | -1.900936 | 0.878197 |
| 10 | 1 | 0 | -1.775609 | -0.000249 | -0.873575 |
| 11 | 1 | 0 | -1.775609 | -0.000249 | 0.873575 |



Fig. 1. Correlation between BE (from AIM data, ref 20) and $\Sigma_{\text {tot }}$


[^0]:    ${ }^{[a]}$ Pr. P. Chaquin
    Laboratoire de Chimie Théorique (LCT)
    Sorbonne Université, CNRS, F-75005 Paris
    E-mail : chaquin@lct.jussieu.fr
    ${ }^{[b]}$ Dr. R. Laplaza
    Laboratoire de Chimie Théorique (LCT)
    Sorbonne Université, CNRS, F-75005 Paris
    Departamento de Química Física
    Universidad de Zaragoza
    50009 Zaragoza, Spain
    [c] Dr. J. Contreras-Garcia, Dr. F. Fuster, Dr. F. Volatron
    Laboratoire de Chimie Théorique (LCT)
    Sorbonne Université, CNRS, F-75005 Paris

[^1]:    ${ }^{\text {a }}$ Estimated on the basis of the same $\Sigma_{\pi}=0.02$ a.u. as 12 . ${ }^{\mathrm{b}}$ The $\pi \mathrm{MOs}$ have been visually identified, which can lead to some uncertainty.

[^2]:    ${ }^{\text {a }}$ Mean value of the two Kékulé structures.

