

Water Table and Permeability Estimation From Multi-Channel Seismoelectric Spectral Ratios

Kaiyan Hu, Hengxin Ren, Qinghua Huang, Ling Zeng, Karl E Butler, Damien Jougnot, Niklas Linde, Klaus Holliger

► To cite this version:

Kaiyan Hu, Hengxin Ren, Qinghua Huang, Ling Zeng, Karl E Butler, et al.. Water Table and Permeability Estimation From Multi-Channel Seismoelectric Spectral Ratios. Journal of Geophysical Research: Solid Earth, 2023, 128 (5), pp.436-447. 10.1029/2022JB025505. hal-04186355

HAL Id: hal-04186355 https://hal.sorbonne-universite.fr/hal-04186355v1

Submitted on 26 Aug 2023 $\,$

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

1	Water Table and Permeability Estimation from Multi-Channel Seismoelectric
2	Spectral Ratios
3	Kaiyan Hu ^{1,2,4} , Hengxin Ren ^{3,4*} , Qinghua Huang ^{1*} , Ling Zeng ⁴ , Karl E. Butler ⁵ ,
4	Damien Jougnot ⁶ , Niklas Linde ⁷ , Klaus Holliger ⁷
5 6	¹ Department of Geophysics, School of Earth and Space Sciences, Peking University, Beijing 100871, China.
7	² Shenzhen Institute, Peking University, Shenzhen 518057, China.
8 9	³ Guangdong Provincial Key Laboratory of Geophysical High-resolution Imaging Technology, Southern University of Science and Technology, Shenzhen 518055, China.
10 11	⁴ Department of Earth and Space Sciences, Southern University of Science and Technology, Shenzhen 518055, China.
12 13	⁵ Department of Earth Sciences, University of New Brunswick, P.O. Box 4400, Fredericton, New Brunswick E3B 5A3, Canada.
14	⁶ Sorbonne Université, CNRS, EPHE, UMR 7619 METIS, Paris F-75005, France.
15	⁷ Institute of Earth Sciences, University of Lausanne, CH-1015 Lausanne, Switzerland.
16	
17 18	Corresponding author: Qinghua Huang (huangq@pku.edu.cn); Hengxin Ren (<u>renhx@sustech.edu.cn</u>)
19	
20	Key Points:
21 22	• Multi-channel seismoelectric spectral ratios are sensitive to the water table depth and the permeabilities of shallow layers
23	• Broad learning neural network is introduced to perform the inversion efficiently
24 25	• This study allows us to monitor the water table depth from the ground surface for an otherwise pre-defined model
26	
27	Manuscript published in Journal of Geophysical Research: Solid Earth
28 29 30 31 32	Hu, K., Ren, H., Huang, Q., Zeng, L., Butler, K. E., Jougnot, D., Linde, N., Holliger, K. (2023) Water Table and Permeability Estimation from Multi-Channel Seismoelectric Spectral Ratios, Journal of Geophysical Research: Solid Earth, 128(5), e2022JB025505, <u>doi:10.1029/2022JB025505</u> .

33 Abstract

Recent developments in predicting and interpreting seismoelectric signals suggest a great potential 34 for studying near-surface hydrogeological properties, particularly in the vadose zone. Previous 35 studies have revealed that the seismoelectric spectral ratios obtained from earthquake-triggered 36 seismoelectric data contain valuable hydrogeological information concerning porous media (e.g., 37 permeability, porosity, fluid viscosity, and salinity). This study introduces Multi-Channel 38 SeismoElectric Spectral Ratios (MC-SESRs) by considering an active seismic source acting on the 39 40 ground surface. The frequency- and saturation-dependent excess charge density is adopted to calculate the cross-coupling coefficients. Applying a supervised learning task based on a flat neural 41 network, the so-called "broad learning" model, to map and extract the features of MC-SESRs data, 42 we seek to determine the permeability and the water table depth. Our results indicate that (1) MC-43 44 SESRs are sensitive to the water table depth and permeability; (2) using more traces of SESRs data 45 for inversion can increase accuracy; (3) the changing water table can be rapidly determined by the MC-SESRs by resorting to the broad learning inverse model, and it can attain an excellent accuracy 46 47 while disturbed by data noise and misspecified model parameters (e.g., porosity and permeability) with errors of up to 20%. The proposed MC-SESRs inversion has potential applications for non-48 49 invasive monitoring in shallow porous media (e.g., frost thawing and geothermal upwelling).

50 Plain Language Summary

A seismic source acting on the ground or occurring in porous materials containing water will 51 generate seismic and electromagnetic field waves. The spectral ratios between the electric field 52 and the seismic field are defined as SeismoElectric Spectral Ratios (SESRs), which are sensitive 53 to physical properties' contrasts at layer boundaries (e.g., water table and hydrogeological and/or 54 lithological layer boundaries). Applying SESRs to reconstruct hydrogeological parameters 55 eliminates the need to know the seismic source function, which greatly facilitates quantitative 56 interpretation. However, SESRs are often acquired by natural earthquakes in previous studies. It 57 58 limits interpreting SESRs to one-trace data. This study uses an active seismic source to obtain the Multi-Channel SESRs (MC-SESRs). We conduct several experiments on synthetic MC-SESRs 59 data by using a neural network to obtain water table depths and permeabilities for a layered Earth 60 model. Our results show that the trained neural network can instantly predict the time-variant water 61 62 table depths accurately. This study indicates that the quantitative interpretation of MC-SESRs data allows for effective and rapid characterization of near-surface hydrogeological properties and also
 provide a possible approach for the non-invasive monitoring of hydrogeological variations in
 shallow porous media by using controllable source.

66

Keywords Hydrogeophysics; Seismoelectric coupling; Vadose zone; Water table monitoring;
 Seismoelectric spectral ratios; Broad learning

69 **1. Introduction**

In porous media, the surface of the solid grains (e.g., silicate minerals) is typically 70 negatively charged due to fluid-mineral interactions (Glover & Jackson, 2010; Hunter, 1981; Revil 71 et al., 2015). Considering the electrical double layer (EDL) model at the microscopic scale (1 - 10 72 nm) (Figure 1a), a portion of the counterions (cations for negatively charged mineral surfaces) 73 coats the interface between the mineral surface and pore fluid forming the Stern layer while the 74 remaining excess charges are distributed in the diffuse Gouy-Chapman layer (Glover & Jackson, 75 2010; Revil & Jardani, 2013). There is a shear plane in the diffuse Gouy-Chapman layer, beyond 76 which the pore fluid and ions can move relative to the solid frame. As shown in Figure 1b, the 77 78 electrical potential at the shear plane is defined as the Zeta potential (Hunter, 1981; Jougnot et al., 2020). The Zeta potential is commonly used to estimate the electrokinetic coupling coefficient, 79 which characterizes the relationship between electrical and hydraulic potential differences 80 associated with fluid flow within a porous medium (Hunter, 1981). Note that all acronyms used in 81 this paper are listed in Table A1 of Appendix A. 82

Relative motions occur during the passage of seismic wavefields. Due to the electrokinetic 83 effect, this process may generate streaming currents and natural electric fields (Pride, 1994; Revil 84 85 et al., 2015; Revil & Linde, 2006). This process is commonly called seismoelectric (SE) 86 conversion. The SE signals contain valuable information concerning the physical properties of both the pore fluid and the solid skeleton. The SE method can be used to determine 87 hydrogeological properties provided the data measured on the ground surface or in boreholes are 88 properly interpreted (Revil et al., 2012). During the past two decades, the SE method has seen 89 90 significant development through (1) theoretical studies (e.g., Huang, 2002; Jougnot & Solazzi, 2021; Monachesi et al., 2018; Solazzi et al., 2022; Thanh et al., 2022), (2) numerical modeling 91 approaches (e.g., Garambois & Dietrich, 2002; Grobbe & Slob, 2016; Haines & Pride, 2006; Hu 92

& Gao et al., 2011; Jougnot et al., 2013; Ren et al., 2016a, b; Zheng et al., 2021), (3) physical 93 laboratory experiments (e.g., Bordes et al., 2015; Devis et al., 2018; Wang et al., 2020; Zhu & 94 Toksöz, 2013), and (4) field measurements (e.g., Butler et al., 2018; Dupuis & Butler, 2006; 95 Garambois & Dietrich, 2001; Rabbel et al., 2020; Thompson & Gist, 1993). As the understanding 96 of SE signals grows, this method is of increasing interest to researchers in near-surface geophysics 97 (e.g., Grobbe et al., 2020). The electromagnetic (EM) wave fields originating from seismic 98 excitations are regarded as a superposition of three types of patterns (Figure 1c): (1) localized SE 99 field waves accompanying seismic waves in porous media, which are also commonly referred to 100 as coseismic electric field waves (Bordes et al., 2015; Jougnot et al., 2013; Pride & Garambois, 101 2002); (2) radiation waves induced on interfaces or directly converted from a seismic source 102 (Dupuis et al., 2007; Haartsen & Pride, 1997; Garambois & Dietrich, 2002; Pride & Haartsen, 103 1996) and (3) evanescent waves generated on interfaces if the seismic incident angle is larger than 104 the critical angle (Butler et al., 2018; Dzieran et al., 2019; Ren et al., 2016a; Yuan et al., 2021; 105 Zheng et al., 2021). The generation of interfacial radiation and evanescent SE waves results from 106 property contrasts at an interface (Garambois & Dietrich, 2002; Ren et al. 2016a, b). Interfacial 107 radiation SE waves and evanescent SE waves offer a way to examine permeability or porosity 108 contrasts (Dzieran et al., 2019, 2020), parameters determining the soil moisture characteristic 109 (Zyserman et al., 2017), strong saturation contrasts such as the water table (Bordes et al., 2015; 110 Warden et al., 2013), and other parameters (e.g., Archie's parameters, density, bulk, and shear 111 112 modulus).



113

Figure 1. Schematic illustration of the generation of electromagnetic waves by seismoelectric conversion. (a) and (b) Electrical double layer and the corresponding electrical potential distribution. (c) Generation of localized, interfacial radiated, and evanescent electromagnetic wavefields due to an active seismic source.

Based on numerical simulation studies, Ren et al. (2016b) put forward the idea that 118 evanescent SE waves could be the main contribution to EM signals observed during earthquakes. 119 This idea was later adopted by Dzieran et al. (2019) to investigate earthquake-triggered SE signals 120 121 in data from Northern Chile. They show that the SeismoElectric Spectral Ratios (SESRs), defined as the ratios between the absolute values of the electric field and the seismic acceleration in the 122 frequency domain, have a site-specific frequency dependence with a decreasing amplitude with 123 increasing frequency. Dzieran et al. (2019) explain this trend by the fact that the amplitudes of 124 125 evanescent SE waves decay approximately with $\exp(-\omega p\Delta z)$, where ω is the angular frequency, p is the EM wave slowness, and Δz is the separation in depth between the receiver and the interface 126 127 (Ren et al. 2018). Dzieran et al. (2019, 2020) successfully apply the SESRs to interpret shallow layered porous media's porosity and fluid salinity. However, Dzieran et al. (2020) state that the 128

SESRs are less sensitive to permeability variations. Inspired by Dzieran et al. (2019, 2020), this
 study extends the applications of SESRs data in several ways.

First, we change the strategy of calculating the SE coupling coefficient. Dzieran et al. 131 (2019, 2020) calculate the electrokinetic coupling coefficient defined by Pride (1994), accounting 132 for the Zeta potential. Instead, we rely on the effective excess charge density to calculate the 133 electrokinetic coupling coefficient (e.g., Revil & Mahardika, 2013; Revil et al., 2015). Both in 134 saturated and partially-saturated conditions, the effective excess charge density is highly correlated 135 136 with permeability (Guarracino & Jougnot, 2018; Jougnot et al., 2020; Soldi et al., 2019). At low 137 frequencies, the ratio of the effective excess charge density at partial water saturation to the excess charge density at full saturation is proportional to the reciprocal of water saturation under the 138 assumption of a thick EDL model (Linde et al., 2007a; Revil et al., 2007). To account for frequency 139 140 dependence, we adopt an approximate empirical formulation by using the relaxation time to relate 141 the quasi-static to dynamic electrokinetic coupling coefficient proposed by Revil & Mahardika (2013), which has been tested by experimental measurements and other approaches (Jougnot & 142 143 Solazzi, 2021).

144 Second, we consider the case of having both the seismic source and sensors located near 145 the ground surface, which is very common in active-source SE field measurements (e.g., Butler et al., 1996, 2018; Dupuis et al., 2007; Garambois & Dietrich, 2001; Mikhailov et al., 1997; 146 Thompson & Gist, 1993). Three-dimensional SE forward modeling algorithms using the 147 reflectivity method (e.g., Garambois & Dietrich, 2002; Grobbe & Slob, 2016; Haartsen & Pride, 148 149 1997; Ren et al., 2007, 2010) to calculate full waveform simulations for layered media suffer from highly time-consuming computations when the source and receivers both lie very close to surface. 150 As the computation of full waveforms relies on numerical integration in the wavenumber domain, 151 the integrand oscillates strongly with the wavenumber when the depth difference between the 152 source and the receiver is small, which may cause a slow convergence. Zheng et al. (2021) solved 153 this convergence problem by adopting the peak-trough averaging method (Zhang et al., 2001, 154 2003), which selects peak and trough values in a stably oscillating sequence to apply the repeated 155 average method (Dahlquist & Björck, 1974). Hence it offers an accurate and efficient tool for 156 active-source SE forward modeling. This allows us to deal with any source-receiver geometries, 157 particularly ground-based seismic sources. The Amplitude Variation versus Offset (AVO) method 158 159 based on multi-channel observation has been widely applied in oil and gas exploration (Rutherford

& Williams, 1989). Multi-channel measurements can also be implemented in SE field experiments 160 for stratified sediments. For example, Butler et al. (2018) presented that the multi-channel high-161 resolution EM field data, illustrating multiple modes of SE signals, providing information on 162 subsurface porous materials complementary to that provided by multi-channel seismic reflection 163 data. Moreover, Rabbel et al. (2020) document the potential of using the interfacial SE responses 164 to map the water table by comparing the multi-channel SE measurements with other geophysical 165 measurements, such as ground-penetrating radar and traditional seismic recordings. Inspired by 166 AVO and SESRs, we propose a Multi-Channel SESRs (MC-SESRs) method that, in addition to 167 frequency variations, makes use of the variations of SESRs with respect to the source-receiver 168 offsets. Thus, we can use more spatial information of SESRs data in the inversions and obtain an 169 improved reconstruction accuracy. 170

171 Third, the SESRs are determined by different parameters in different complicated non-172 linear ways. For example, the water table variations affect the water saturation distribution, which determines the effective permeability (e.g., Mualem, 1976; van Genuchten, 1980), the permittivity 173 174 (e.g., Linde et al., 2006), the electrical conductivity, the electrokinetic coupling coefficient (e.g., Warden et al., 2013; Revil & Mahardika, 2013; Zyserman et al., 2017), the bulk density, the elastic 175 moduli, the seismic velocity (e.g., Mao et al., 2022; Solazzi et al., 2021) and so on. Dzieran et al. 176 (2019) mentioned that inverse modeling of SESRs may need a more advanced approach compared 177 to the conventional linearized inversion algorithm used in their work. Machine learning, which is 178 179 enjoying increasing interest in geophysics, may offer a corresponding option.

180 In this study, we rely on the broad learning (BL) model to invert hydrological parameters using MC-SESRs data. The BL system proposed by Chen and Liu (2017) is a flat neural network 181 with a single lateral layer neural network, in contrast to deep structured neural networks. It is 182 developed from the Random Vector Functional Link Neural Network (RVFLNN) (Pao et al., 1994) 183 to apply an enhancement layer to link the input and output. Broadly expanding the enhancement 184 nodes may enhance the capacity to approach non-linear problems. It only needs to learn the matrix 185 weights of the link between the enhancement layer and output. Other matrix weights are randomly 186 generated. Thus, the RVFLNN is a flat net without hidden layers, which avoids overtraining the 187 neural network with many adjustable hyperparameters (Pao et al., 1994). Correspondingly, the BL 188 structure improves the RVFLNN by adding a mapping feature layer to replace the original input 189 190 based on the sparse autoencoder. Hence the BL structure first captures the features of input data in the mapping feature layer. Since the BL network structure is fixed, its main advantage is that it
avoids elusive complicated deep architectures and iterative training processes (Gong et al., 2022).
Its efficient capacities for processing noisy time series and text classifications have been verified
(Chen & Liu, 2017; Du et al., 2020; Feng et al., 2019; Gong et al., 2022).

Most recently, Yang et al. (2022, 2023) applied the BL neural network to Rayleigh wave 195 inversion. Considering a 1-D Earth model, Yang et al. (2022) examined the thickness and shear-196 wave velocity ranges of each layer by the well-trained BL neural network. Then they used the 197 198 optimal ranges as the search space of a Bayesian approach to complement the parameter optimization. Their results indicated that this two-stage approach can provide more accurate shear-199 wave velocity models than without using a priori search space estimated by a BL model. Yang et 200 al. (2023) also verified that using the BL approach to Rayleigh wave inversion may achieve a 201 202 comparable accuracy but consume less training time than deep convolutional neural networks. In 203 this study, we aim to determine hydrogeological parameters (water table depth and shallow layer permeabilities) under partially-saturated conditions by MC-SESRs data. For a specific investigated 204 205 area whose layered structure had been determined, the well-trained BL model can, if fed with MC-SESR data, estimate the water table depth and update the permeability in the shallow layer in a 206 quasi-instantaneous manner. Due to its high training efficiency, BL can easily be retrained to 207 optimize the network when more MC-SESRs data is obtained. This study may provide a new 208 209 monitoring strategy for obtaining the water table depths using the time-lapse MC-SESRs data. It 210 also has the potential application in long-term observations for assessing groundwater storage and monitoring volcanic activities. 211

This paper is structured as follows. Section 2 describes the basic SE coupling equations, numerical simulation of the SE data, and our inversion framework. Section 3 focuses on analyzing the sensitivity of permeability and depth of water table (dwt) to MC-SESRs. Section 4 tests the performance of the BL neural network and presents the inversion results. Section 5 discusses the inversion results, and we provide conclusions in Section 6.

217 2. Methodology

218 **2.1. Cross-coupling equations**

For fluid-saturated isotropic porous media, the cross-coupled constitutive transport equations, including macroscopic Ohm's and Darcy's Law, can be expressed in the frequency domain through the following governing equations (Pride, 1994; Pride & Haartsen, 1996; Revil & Mahardika, 2013):

$$\mathbf{J} = \sigma^*(\omega)\mathbf{E} + L^*(\omega)(-\boldsymbol{\nabla}p_{\rm f} + \omega^2\rho_{\rm f}\mathbf{u}_{\rm s}), \tag{1}$$

$$-i\omega\mathbf{w} = L^*(\omega)\mathbf{E} + \frac{k^*(\omega)}{\eta_{\mathbf{w}}}(-\nabla p_{\mathbf{f}} + \omega^2 \rho_{\mathbf{f}} \mathbf{u}_{\mathbf{s}}),$$
(2)

$$-p_{\rm f} = C\nabla \cdot \mathbf{u}_{\rm s} + M\nabla \cdot \mathbf{w},\tag{3}$$

$$\mathbf{T} = \left[\left(K_{\rm G} - \frac{2}{3} G \right) \nabla \cdot \mathbf{u}_{\rm s} + C \nabla \cdot \mathbf{w} \right] \mathbf{I} + G (\nabla \mathbf{u}_{\rm s} + \nabla \mathbf{u}_{\rm s}^{\rm T}), \tag{4}$$

$$-\rho_b \omega^2 \mathbf{u}_{\rm s} - \rho_{\rm f} \omega^2 \,\mathbf{w} = \left(K_G + \frac{4}{3}G\right) \nabla (\nabla \cdot \mathbf{u}_{\rm s}) - G \nabla \times \nabla \times \mathbf{u}_{\rm s} + C \nabla (\nabla \cdot \mathbf{w}) + \mathbf{F}, \quad (5)$$

where Equations 1-2 describe the electrokinetic cross-coupling relationship between the electric 223 field **E** (V/m) and the volume-averaged fluid filtration displacement **w** (m) = $\phi(\mathbf{u}_{\rm f} - \mathbf{u}_{\rm s})$, which 224 is defined by the porosity ϕ (m³/m³) and the volume-averaged fluid and solid displacements (\mathbf{u}_{f} 225 and \mathbf{u}_{s}). The subscripts 'f' and 's' designate fluid and solid properties, respectively. We consider 226 a time-harmonic disturbance varying as $e^{-i\omega t}$ with $i = \sqrt{-1}$ the imaginary unit, $\omega = 2\pi f$ the 227 angular frequency in rad/s, and f (Hz) the frequency. The superscript '*' indicates that a property 228 is frequency-dependent and hence complex. $k^*(\omega)$ thus denotes the frequency-dependent 229 permeability (m²). Permeability reflects the ability of porous media to allow fluid to flow through 230 the pores. Equations 3 and 4 describe the poroelastic relations (Biot, 1956, 1962a, b) with I 231 denoting the identity matrix. The parameters C (Pa) and M (Pa) are associated with the elastic 232 moduli (Pride, 1994). $K_{\rm G}$ (Pa) and G (Pa) denote the undrained bulk modulus and shear modulus 233 of the solid skeleton. ρ_b (kg/m³) and **F** (N) in Equation 5 are the mass density of the porous 234

material and the body force applied on the bulk material, respectively. All parameters and theirunits used in this study are listed in Table A2 of Appendix A.

Due to harmonic variations of the bulk-stress tensor **T** (N/m²) and the pore fluid pressure $p_{\rm f}$ 237 238 (Pa), the flow changes from the viscous laminar regime to the inertial laminar regime beyond the critical or transition frequency (Revil & Mahardika, 2013; Solazzi et al., 2020, 2022). The 239 permeability becomes frequency-dependent and complex-valued beyond the critical frequency, 240 and its absolute value decreases with increasing frequency (Solazzi et al., 2020). η_w denotes the 241 dynamic viscosity of pore water $(1.002 \times 10^{-3} \text{Pa} \cdot \text{s})$. The macroscopic electrical current density I 242 (A/m²) is the superposition of the conduction current density $\sigma^*(\omega)\mathbf{E}$ and the streaming current 243 density \mathbf{J}_{ek}^* written by: 244

$$\mathbf{J}_{\mathbf{e}\mathbf{k}}^* = L^*(\omega)(-\nabla p_{\mathbf{f}} + \omega^2 \rho_{\mathbf{f}} \mathbf{u}_{\mathbf{s}}),\tag{6}$$

in which $\sigma^*(\omega)$, and $\rho_f = (1 - S_w)\rho_a + \rho_w$ denote the complex electrical conductivity (S/m) and 245 the fluid density (kg/m³), respectively. S_w , $\rho_a = 1.21$ (kg/m³) and $\rho_w = 1000$ (kg/m³) are the 246 water saturation, the density of the air and pore water. Note that we consider pore water as a dilute 247 solution with low salinities (commonly around 0.002 mol/L) and, hence, the solute density is 248 neglected. For highly saline solutions (e.g., seawater, contaminated water), the mass density of the 249 solute would need to be included. Unless mentioned otherwise, the parameters used in this paper 250 251 refer to standard ambient conditions (1 atm and 20 °C). The presence of harmonic electric fields usually makes the electrical conductivity of porous materials vary with frequency due to 252 polarization effects of electrically conductive mineral grains, interfacial electrochemistry, or 253 colloidal chemistry (Revil, 2013). The effective electrical conductivity in the frequency domain 254 can be expressed by (Revil et al., 2015): 255

$$\sigma^*(\omega, S_{\rm w}) = F^{-1} S_{\rm w}^n \sigma_{\rm w} + \sigma_{\rm sur} + i \big(\sigma_{\rm quad} - \omega \varepsilon_0 \kappa \big). \tag{7}$$

Therein, *n* denotes the saturation exponent and $F = \phi^{-m}$ is the electrical formation factor in Archie's first and second laws with cementation exponent *m* (Archie, 1942). $\varepsilon_0 = 8.85418 \times 10^{-12}$ F/m is the vacuum permittivity. κ denotes the static effective dielectric constant, which is the function of the water saturation: (Linde et al., 2006):

$$\kappa(S_{\rm w}) = \frac{(F-1)\kappa_{\rm s} + S_{\rm w}{}^n \kappa_{\rm w} + (1-S_{\rm w}{}^n)\kappa_{\rm a}}{F}.$$
(8)

The range of the dielectric constant for most rock-forming minerals is 4-6 and is commonly 260 assumed to be $\kappa_s = 4$ for dry sand grains in near-surface measurements (e.g., Fitterman, 2015; 261 Knight & Endres, 2005). $\kappa_w = 80.1$ and $\kappa_a = 1$ represent the dielectric constants of the pore 262 water and the air, respectively. Based on a volume-averaging method, Equation 8 is derived from 263 a two-phase model (i.e. pore fluid and solid grains) by Pride (1994), accounting for the effective 264 pore fluid formed by water and air and combining Archie's first and second laws (Linde et al., 265 2006). This equation assumes that the two fluid phases in the pore space are immiscible. The 266 physical relationship (Equation 8) has been previously used to simulate seismoelectric signals 267 (e.g., Rosas-Carbajal et al., 2020). The surface electrical conductivity σ_{sur} and the quadrature 268 electrical conductivity σ_{quad} in Equation 7 are related to the fraction and mobility of counterions 269 in the diffuse layer and in the Stern layer, respectively (Revil, 2013; Revil et al., 2015). Both 270 conductivities are functions of water saturation. More details of these coefficients calculated by 271 272 material properties and saturation levels, can be found in Table A3 of Appendix A.

Based on the EDL model (Figure 1a), Equations 1 and 2 express that the poromechanical 273 influence contributes to the streaming source current, and the electric field contributes to the pore-274 fluid flow under the electroosmosis effect (Revil & Mahardika, 2013). The critical dynamic 275 parameter $L^*(\omega)$ reflects the cross-coupling relationship. Due to the significance of frequency-276 dependent cross-coupling coefficient $L^*(\omega)$ in transport equations, its calculation has attracted 277 considerable attention in the recent decade (Jougnot & Solazzi, 2021; Jouniaux & Zyserman, 2016; 278 279 Soldi et al., 2020; Thanh et al., 2022; Warden et al., 2013). A popular approach is using the Zeta potential to describe the cross-coupling coefficient (Dukhin & Derjaguin, 1974; Pride, 1994; 280 Warden et al., 2013; Zyserman et al., 2017). An alternative is to use the movable (effective) excess 281 charge density \hat{Q}_{v}^{*} (C/m³) and permeability to directly relate the relative flow to streaming current 282 generation (Revil & Linde, 2006). The cross-coupling coefficient calculated by both approaches 283 284 explains some experimental measurements (Bordes et al., 2015; Revil & Mahardika, 2013; Zhu & Toksöz, 2013). In terms of partially-saturated conditions considering only water and air in the pore 285

space, the latter approach conveniently relates $L^*(\omega)$ to the effective permeability and \hat{Q}_v^* as functions of the water saturation by (Revil & Mahardika, 2013; Soldi et al., 2020):

$$L^*(\omega, S_{\mathrm{w}}) = \frac{k^*(\omega, S_{\mathrm{w}})\hat{Q}_{\mathrm{v}}^*(\omega, S_{\mathrm{w}})}{\eta_{\mathrm{w}}}.$$
⁽⁹⁾

The frequency-dependent (dynamic) characteristics of permeability and effective excess charge density are approximately described by the relaxation time or the angular transition frequency ω_t (rad/s), which determines the transition from the viscous (low frequency) to inertial laminar flow (high frequency) (Revil & Mahardika, 2013). $\omega_t(S_w)$ is expressed as a function of water saturation by Revil and Mahardika (2013) and Solazzi et al. (2020):

$$\omega_{\rm t} = \frac{\eta_{\rm w} \phi S_{\rm w}}{\rho_{\rm w} k_0(S_{\rm w}) \tau_{\rm w}(S_{\rm w})},\tag{10}$$

where τ_w denotes the tortuosity related to the topology of the pore space. The saturation-dependent 293 tortuosity is equivalent to $\phi FS_w^{(1-n)}$ based on Archie's law (e.g., Niu & Zhang, 2019; Jougnot et 294 al., 2018; Revil et al., 2007; Revil & Jougnot, 2008). Since $n \ge 1$ $(1 - n \le 0)$, the tortuosity 295 increases with the decrease of water saturation (e.g., Ghanbarian et al., 2013; Jougnot et al., 2018), 296 while the transition frequency increases with the decrease of water saturation. Here, $k_0(S_w)$ 297 denotes the quasi-static ($\omega = 0$) effective permeability as a function of saturation. When the 298 frequency-dependent effective permeability and excess charge density are considered, Equation 9 299 is written by (Revil & Mahardika, 2013): 300

$$L^*(\omega, S_w) = \frac{k_0(S_w)\widehat{Q}_{v,0}(S_w)}{\eta_w \sqrt{1 - \frac{i\omega}{\omega_t}}}.$$
(11)

There are two main approaches to describe this effective excess charge density $\hat{Q}_{v,0}$: either by volume-averaging (Linde et al., 2007a) or flux-averaging (Jougnot et al., 2012). In this work, the excess charge density at a saturated state is estimated from permeability using (Jardani et al., 2007):

$$\log 10(\hat{Q}_{v,0}^{\text{sat}}) = -0.82\log 10(k_0^{\text{sat}}) - 9.23.$$
(12)

The superscript 'sat' denotes a fully saturated condition. This empirical relationship has been applied to various samples ranging from different salinities and lithologies even if it did not consider the effect of salinities of pore water on the excess charge density (Jardani et al., 2007; Jougnot et al., 2015).

Another empirical relationship between the voltage coupling coefficient under saturated conditions C_0^{sat} (mV/m) and the electrical conductivity of pore water σ_w (S/m) is expressed as (Linde et al., 2007b):

$$\log(|C_0^{\text{sat}}|) = -0.895 - 1.319 \log(\sigma_w) - 0.1227 [\log(\sigma_w)]^2,$$
(13)

312 where σ_w is estimated by the salinity C_w (mol/L) (Sen & Goode, 1992):

$$\sigma_{\rm w} = (5.6 + 0.27T - 1.5 \times 10^{-4} T^2) C_{\rm w} - \frac{(2.36 + 0.099T) C_{\rm w}^{\frac{3}{2}}}{1 + 0.214 C_{\rm w}},$$
(14)

where *T* is the temperature in Celsius (°C). Thus, the voltage coupling coefficient C_0^{sat} varies with pore water salinity. Compared with laboratory and field measurements, Equation 13 works well in a range of $10^{-2} - 10^{0.5}$ S/m for σ_w , which covers typical pore water environments (Linde et al., 2007b, Jougnot et al., 2015; Hu et al., 2020). By changing the unit of C_0^{sat} to V/m, it can be transformed from the static coupling coefficient L_0^{sat} (A/m²) by:

$$C_0^{\text{sat}} = -\frac{L_0^{\text{sat}}}{\sigma_0}.$$
 (15)

Further, C_0^{sat} can be used to express the $\hat{Q}_{v,0}^{\text{sat}}$ with:

$$\widehat{Q}_{\mathbf{v},\mathbf{0}}^{\mathrm{sat}} = -\frac{c_0^{\mathrm{sat}}\sigma_0\eta_W}{k_0^{\mathrm{sat}}}.$$
(16)

We may use Equation 12 to estimate $\hat{Q}_{v,0}^{sat}$ under a known k_0^{sat} or we may derive $\hat{Q}_{v,0}^{sat}$ by Equations 13-16 using the salinity of pore water (Jougnot et al., 2015). Otherwise, C_0^{sat} can be obtained by measuring the voltage differences and hydraulic pressure differences of samples to calculate values of $\hat{Q}_{v,0}^{sat}$ by Equation 16.

For partially saturated conditions, we applied the volume-averaging method to scale $\hat{Q}_{v,0}$ by the effective saturation $S_e = \frac{S_w - S_{wr}}{1 - S_{wr}}$ (Linde et al., 2007a; Revil & Cerepi, 2004; Revil et al., 2007):

$$\hat{Q}_{v,0}(S_w) = \frac{\hat{Q}_{v,0}^{\text{sat}}}{S_e},$$
(17)

where S_{wr} (unitless) denotes the residual (irreducible) water saturation. Alternative formulations have been derived to explicitly describe the dynamic process of $\hat{Q}_{v,0}$ varying with water saturation based on the characteristic pore-size distribution (Jackson, 2010; Jougnot et al., 2012; Soldi et al., 2020; Solazzi et al., 2022). Furthermore, the frequency-dependent effective excess charge density is calculated by applying a scaling factor $\sqrt{1 - \frac{i\omega}{\omega_t}}$ (Revil & Mahardika, 2013), which also has been further developed by Jougnot and Solazzi (2021) and Thanh et al. (2022).

331 Apart from the effective permeability and excess charge density, other effective parameters (e.g., the electrical conductivity σ^* , the mass density of fluid ρ_f) in Equations 1 and 2 strongly 332 depends on the water saturation as well. Besides, the two fluid phases in the pore space affect the 333 mechanical properties (e.g., the effective bulk moduli) that need to be considered in 334 hydromechanical modeling of the volumetric strain of porous media and the infiltration 335 displacement (Equations 3-5). This indicates that seismic signals could respond to variations in 336 water saturation. We summarize the frequency-dependent (dynamic) and saturation-dependent 337 parameters in Table A3 of Appendix A. More details with regard to the parameters mentioned 338 above as well as the derived equations can be found in Revil & Mahardika (2013). 339

340

2.2. Multi-Channel SeismoElectric Spectral Ratios (MC-SESRs)

For isotropic layered media, as the SE field and the seismic particle acceleration field are triggered by the same seismic source, the seismic source function can be canceled when we calculate the ratios of SE fields to the seismic acceleration fields in the frequency domain (Dzieran et al., 2019). Therefore, the SESRs can be represented by the ratio of their Green's functions $GE(\omega)$ and $Ga(\omega)$, which is expressed as (Dzieran et al., 2019):

$$SESR(\omega) = \frac{E(\omega)}{a(\omega)} = \frac{GE(\omega)}{Ga(\omega)},$$
(18)

where $\mathbf{E}(\omega)$ denotes the SE field spectra. $\mathbf{a}(\omega)$ denotes the seismic ground acceleration field spectra, which also can be replaced by the components of seismic ground velocity spectra with $i\omega \mathbf{v}(\omega)$ or displacement spectra with $-\omega^2 \mathbf{u}(\omega)$. The SESR indicates the ratio of Green's functions, which contains the information of stratified porous media. The modulus of SESRs varies with position, or offset from the seismic source, represented by:

MC-SESR
$$(\omega, x_i) = \frac{|E_{x,i}(\omega)|}{|a_{x,i}(\omega)|}, i = 1, 2, ..., B$$
 (19)

where *i* denotes the measured points and *B* is the total number of measured points. Here, $E_{x,i}$ and a_{x,i} denotes the horizontal electric field and seismic ground acceleration in the frequency domain at point *i*.

354

2.3. Inversion framework

Deterministic inverse modeling (e.g., Gauss-Newton, Conjugate Gradient, Levenberg-355 Marquardt) algorithms need to construct an objective function, including the data misfit and a 356 regularization term. The latter depends on prior and empirical information. In weakly non-linear 357 problems, the iterative adjustment of model parameters using gradient-based information enables 358 a minimum objective function to be attained. However, it is time-consuming when we deal with 359 high-dimension parameter estimation, and these parameters affect the SESRs in a non-linear way. 360 Furthermore, such deterministic inversions might fail to recover the true model, although the 361 modeling data well match the observed data (Wu et al., 2021). 362

In this study, we aim to reconstruct the permeability and water table depth using the nearsurface MC-SESRs data. As the water table is affected by land-management practices, precipitation, evapotranspiration, and other environmental changes, its depth may change with time. Machine learning techniques may allow us to efficiently monitor the dynamic water table. A

large number of samples are employed to train a neural network, which can construct the mapping 367 process between the input data (MC-SESRs) and the output data (water table depth and 368 permeability). Once the neural network is well trained, we can adapt it to a specific region to 369 monitor variations of its water table and permeability efficiently. Deep-structured neural networks 370 have been employed in solving geophysical inverse problems (e.g., Laloy et al., 2021; Wu et al., 371 2021), which are alternatives for the SESRs inversion. But the many hidden layers included in 372 such networks produce a large quantity of hyperparameters, which need large data sets and many 373 training epochs to be estimated. Complicated deep architectures empower the neural network to 374 project a more complex relationship between the input and output layers. However, the computing 375 time is increased due to the iterations of training epochs, and overtrained networks could result. 376 Chen and Liu (2017) propose a broad learning (BL) neural network that adopts a flat architecture 377 without a complex multilayer structure. Its network structure does not change within the training 378 process (Figure 2). It avoids adjusting elusive hyperparameters in the network, and its design 379 largely decreases the training time compared with deep networks. Broadly expanding the mapping 380 layer enhances the capacity of the neural network to approach complicated projecting 381 relationships. More important, the broadly expanding structure can be used for incremental 382 learning without retraining the network when additional data are available in input data (Chen & 383 Liu, 2017). Compared with the performance of deep structured neural networks (e.g., deep 384 convolutional neural networks, deep Boltzmann machines, and deep belief networks) on MNIST 385 and NORB data sets, Chen and Liu (2017) demonstrated that the BL system can ensure a 386 comparable classification accuracy while vastly reducing the training time. Recently, the BL 387 approach has been applied to effectively and efficiently process classification and regression 388 problems (Gong et al., 2022). Therefore, the BL approach is considered here to perform water 389 390 table depth and permeability inversions using MC-SESRs data.

As a supervised machine learning task, we need to generate a large number of training samples. We assume the number of samples is *N* for training the network and the number of inverted layers of permeability is *L*. If there are *A* frequencies and *B* measured points (traces) in Equation 19, the input matrix **X** is MC-SESRs data (Figure 2a). The output matrix **Y** is made up of *N* depths of the water table written by a vector $\mathbf{dwt}_{N\times 1}$ and $N \times L$ permeability matrix written by $\mathbf{K}_{N\times L}$ (Figure 2c). Using the neural-network architecture of the BL model (Chen & Liu, 2017), we first need to extract the features of MC-SESRs data as the input layer (Figure 2b):

$$\mathbf{F}_i = \varphi_i(\mathbf{X}\mathbf{W}_i + \boldsymbol{\beta}_i), \, i = 1, 2, \dots, Q$$
(20)

where \mathbf{F}_i denotes the *i*th mapped feature matrix. \mathbf{W}_i and $\boldsymbol{\beta}_i$ denote the random weighting matrix 398 and bias term, which are initially generated by standard uniform distributions in a range of [-1,1]. 399 Assuming $A \times B = C$, the sizes of matrices of \mathbf{W}_i and $\boldsymbol{\beta}_i$ are $C \times P$ and $N \times P$, respectively. As 400 shown in Figure 2b, P is the number of feature nodes in each mapping feature group i. Q is the 401 number of mapping features. The function φ_i maps the sum of matrices **XW**_i + β_i to [-1,1] by 402 normalizing the minimum and maximum value each row (1, 2, ..., N). The sparse autoencoder is 403 employed to shrink the input data and extract its mapping features by adapting W_i (Chen & Liu, 404 2017). As shown in Equation 20, this feature extracting step of the input data can be replaced by 405 other extracting approaches from popular artificial neural networks (e.g., deep convolutional 406 neural networks) (Gong et al., 2022). 407

408 The features of input data extracted by mapping feature groups $\mathbf{F}^Q = [\mathbf{F}_1, \mathbf{F}_2, ..., \mathbf{F}_Q]$ are 409 broadly expanded by *M* enhancement nodes with:

$$\mathbf{E}_{j} = \xi_{j}([\mathbf{F}_{1}, \mathbf{F}_{2}, \dots, \mathbf{F}_{Q}]\mathbf{W}_{ej} + \boldsymbol{\beta}_{ej}), j = 1, 2, \dots, M$$
(21)

where \mathbf{E}_j denotes the matrix of *j*th enhancement node. \mathbf{W}_{ej} and $\boldsymbol{\beta}_{ej}$ are randomly generated similar to Equation 20. In this study, we used the hyperbolic tangent sigmoid transfer function as the non-linear activation function $\xi_j(\cdot)$. Each enhancement node is integrated to an enhancement layer with $\mathbf{E}^M = [\mathbf{E}_1, \mathbf{E}_2, ..., \mathbf{E}_M]$.

The output-layer hydrogeological parameters $\mathbf{Y} = [\mathbf{dwt}, \mathbf{K}]$ and the last layer integrated by input features and the enhancement layer are connected by a weighting matrix \mathbf{W}^{M} :

$$\mathbf{Y} = \begin{bmatrix} \mathbf{F}_1, \mathbf{F}_2, \dots, \mathbf{F}_Q | \mathbf{E}_1, \mathbf{E}_2, \dots, \mathbf{E}_M \end{bmatrix} \mathbf{W}^M,$$
(22)

Therefore, the training process only needs to estimate the connected-link matrix \mathbf{W}^{M} through solving the pseudoinverse matrix $[\mathbf{F}^{Q}|\mathbf{E}^{M}]^{+}$:

$$\mathbf{W}^M = [\mathbf{F}^Q | \mathbf{E}^M]^+ \mathbf{Y}.$$
 (23)

Following Chen and Liu (2017), the ridge regression approximation is employed to optimize \mathbf{W}^{M} by fulfilling:

arg min:
$$\|[\mathbf{F}^{Q}|\mathbf{E}^{M}]\mathbf{W}^{M} - \mathbf{Y}\|_{2}^{2} + \lambda \|\mathbf{W}^{M}\|_{2}^{2},$$
 (24)

where λ denotes a tradeoff regularization factor and $\|[\mathbf{F}^Q]\mathbf{E}^M]\mathbf{W}^M - \mathbf{Y}\|_2^2$ is the error term of the 420 training set. Except for the connected matrix \mathbf{W}^{M} , the remaining weight matrices in the network 421 are randomly generated. Consequently, we can use the well-trained network with the optimal 422 connected weights \mathbf{W}^{M} to invert MC-SESRs data. For example, if we acquired more MC-SESRs 423 424 data, we just need to replace Input **X** with the new (untrained) data in Equation 20. By following similar computations to the training process by Equations 20-22, we then extract the mapping 425 features of the inversion data and use an activation function to learn these features in the 426 enhancement layer. Thus, we obtain the newly mapped feature matrices and enhancement matrices. 427 Multiplied with the weight matrix derived from the training process (Equations 23 and 24), we can 428 obtain the estimated water table depth and permeability (Equation 22). 429



430

431 **Figure 2.** Broad learning (BL) procedure including (a) the input (MC-SESRs data) layer, (b) the

mapping feature layer and the enhancement layer, and (c) the output (permeability with watertable) layer employed in this study.

434 **3. Sensitivity Analysis**

3.1. Basic test model

We first design a basic test model (Figure 3). It consists of five horizontal layers of porous 436 materials. It is assumed that the shallow two layers (layers 1-2) are mainly made up of loamy 437 438 sands, and the deeper two-layer soils (layers 3-4) with lower permeabilities considered as silty sands. The bottom layer 5 is assumed as a known layer with lower permeability (0.01 D), porosity 439 (0.05), and electrical conductivity (16 μ S/cm). These hydrogeological parameters are chosen 440 based on Carsel and Parrish (1988). The initial water table is set at 3 m, implying that the 441 shallowest layer is partially saturated (Figure 3a). The Richards' equation (Richards, 1931) is used 442 to solve the hydraulic problem in the vadose zone. The Mualem-van Genuchten (MVG) empirical 443 model (Mualem, 1976; van Genuchten, 1980) is used to estimate the relationship between the 444 water saturation and the effective permeability with the pore pressure. Based on the MVG model 445 by introducing the soil-water characteristic parameters α_{VG} (m⁻¹), n_{VG} and $m_{VG} = 1 - 1/n_{VG}$, the 446 effective water saturation S_e and the static permeability k_0 at partially saturated conditions are 447 expressed by: 448

$$S_{\rm e} = \frac{1}{\left[1 + (\alpha_{VG}|H_{\rm p}|)^{n_{VG}}\right]^{m_{VG}}},\tag{25}$$

$$k_{0} = k_{0}^{\text{sat}} S_{e}^{\frac{1}{2}} \left[1 - \left(1 - S_{e}^{\frac{1}{m_{\text{VG}}}} \right)^{m_{\text{VG}}} \right]^{2}.$$
 (26)

Here, we assume that the absolute pressure head $|H_p|$ (m) in the vadose zone is equal to the vertical 449 distance between its elevation and the position of the water table (Zyserman et al., 2017). The 450 effective electrical conductivity is calculated by Equation 7, whose formulas and the used 451 parameters are given in Table A3 of Appendix A and Table S1 of the Supporting Information). 452 The water saturation, the effective permeability, and the effective electrical conductivity of the top 453 four layers are presented in Figures 3b-d under the assumption that the pore water salinity is 454 homogeneous at 2×10^{-3} mol/L at 293.15 K, respectively. Note that the effect of the salinity at 455 this level on the fluid mass density is negligible. In contrast, the mass density of the fluid solute 456 should be considered in a highly saline environment (e.g., Hu et al., 2023). The specific parameters 457 of each layered material are given in Table 1, whose descriptions can be found in Table A2 of 458 459 Appendix A.



Figure 3. Basic test model and its observations. (a) Geometry, (b) water saturation, (c) effective
permeability, and (d) effective electrical conductivity in the top four layers

460

There is a vertical force point source at the ground marked with a red square in Figure 3a. We assume that the seismic source function $f_s(t)$ (N) presents as a Ricker wavelet with a peak frequency f_p of 20 Hz:

$$f_{\rm s}(t) = -2.506 \times 10^5 \left[1 - 2(\pi f_{\rm p})^2 \left(t - \frac{2}{f_{\rm p}} \right)^2 \right] \exp[-(\pi f_{\rm p})^2 (t - \frac{2}{f_{\rm p}})^2].$$
(27)

The spectrum of this zero-phase wavelet is in a range of ~ 70 Hz. This wavelet and its frequency 466 band are usually considered in seismoelectric simulations (e.g., Jardani et al., 2010). Equation 27 467 is applied to calculate the body force of Equation 5 in forward modeling. Receivers are installed 468 at 0.1 m below the ground surface. The offset ranges from 5 - 105 m with 101 horizontal 469 acceleration sensors and 101 horizontal point dipoles. The offset represents the distance between 470 the source and each accelerometer or central point of each dipole. The interval of two adjacent 471 receivers is 1 m (Figure 3a). Please note that the seismic particle velocity $\mathbf{v}(\omega)$ obtained by 472 geophones could also be used to calculate SESRs by transforming $\mathbf{a}(\omega)$ to $i\omega \mathbf{v}(\omega)$. As mentioned 473 in Section 2.2, measuring SESRs does not require knowledge of the seismic source function, so 474

we would not need to know the amplitude of the seismic source. Additionally, the SE responses are proportional to the amplitude of seismic sources, either for explosive sources or weight drops, demonstrated in the field tests (Butler et al., 1999). Therefore, according to the specific prospecting conditions, this seismic source function can be replaced with other source functions. However, the seismic strength and waveform used here are adopted to illustrate that the predicted electric fields are expected to be measurable for a reasonable seismic source.

Based on Section 2.1, with the dynamic and saturation-dependent parameters chosen, 481 especially the cross-coupling coefficient $L^*(\omega, S_w)$ in Equation 11, the peak-trough averaging 482 approach based on Luco-Apsel-Chen Generalized Reflection and Transmission Method (LAC 483 GRTM) (Zheng et al., 2021) is applied to obtain the frequency solution of the governing equations. 484 The wave-field components are derived from the numerical integral over the wavenumber domain. 485 The integrand includes the Bessel function and exponential terms of fast and slow P, S, and EM 486 waves. Compared with the seismic wavelength, the relatively small source-receiver vertical 487 differences make integrands more intensively oscillate. Therefore, this situation may cause a slow 488 convergence computationally (Zheng et al., 2021). The peak-trough averaging approach uses a 489 certain wavenumber interval in a stably oscillating range to determine peaks and troughs of 490 integrands and subsequently apply the repeat average method to efficiently compute the numerical 491 integration (Dahlquist & Björck, 1974). Thus, it allows us to consider more flexible source-492 receiver geometries. All used dynamic and saturation-dependent parameters and corresponding 493 formulations are given in Table A3 of Appendix A, and we summarize a flow chart of the model 494 generation in Figure 4. We assume that the data recorded from 0 to 0.5 s is digitized by 4096 495 samples with a sample interval of 0.1221 ms. After the full-waveform computation of this model, 496 we display the horizontal components of seismic ground acceleration and SE wave fields (Figure 497 5). Since a zero-phase wavelet was applied to simulate the seismic source (Equation 27), a time 498 delay is shown in the waveforms (Figure 5). In addition, due to a low saturation ($S_w = 0.12$) 499 occurring on the near-surface (~0.3 m), the corresponding S-wave velocity is 1242.5 m/s. The 500 surface waves can have a high apparent velocity to present in longer source-receiver offsets than 501 the offset range shown in Figure 5. In this case, the maximum absolute horizontal electric field is 502 26.27 μ V/m. Although the electric-field signals are vulnerable to noise, the environmental noise 503 504 level can be managed to below the order of 0.1 μ V/m (see Butler et al., 2007; Dupuis et al., 2007;

505 Thompson & Gist, 1993). The near-surface electric field of this case is, hence, sufficient to be 506 observed.



508 **Figure 4.** Framework of MC-SESRs generation





Figure 5. Horizontal components of wave fields under the basic test model (a) seismic ground
acceleration and (b) seismoelectric wave fields

The horizontal components of seismic ground acceleration and SE wave fields recorded in the time domain are subsequently transformed into the frequency domain. Then the MC-SESRs over the full 0.5s time window are calculated by Equation 19. Here, we take the frequency in the

range of 2-72 Hz. The MC-SESRs' contour map of this numerical model is shown in Figure 6a. 515 The SESRs with greater strength are mainly distributed in a short-offset range (10 - 40 m) and a 516 low-frequency range (~ 10 Hz). Since the SESR concept under the assumption of the localized 517 (coseismic) SE field waves are linear with the ground acceleration, the frequency-dependent 518 behaviors depend on the evanescent and radiated SE field waves (Dizeran et al., 2019). The 519 generation of the radiated SE field waves is commonly regarded as caused by the seismic waves 520 nearly vertically arriving at interfaces and the ground surface. Although the radiated EM waves 521 generated by the direct SE conversions at the source also depend on the frequency, their strength 522 is weak. The subsurface properties' variations barely affect the component of MC-SESRs 523 originating from the direct SE conversions. 524



Once the seismic incident angle is larger than the critical angle θ_c :

$$\theta_{\rm c} = \arcsin\left(\frac{V_{\rm sei}}{V_{\rm EM}}\right),$$
(28)

where V_{sei} (m/s) and V_{EM} (m/s) denote the seismic wave velocity and EM wave velocity, 526 respectively, the SE conversion leads to the generation of evanescent SE waves. Actually, θ_{c} 527 approaches zero due to $V_{\rm EM} \gg V_{\rm sei}$. The existence of physical properties' contrasts causes the 528 interfacial SE responses, mainly containing evanescent SE field waves. The superposition of 529 different modes of SE conversions makes the spectral ratios between the SE responses and the 530 ground acceleration are of frequency dependence. Thus, the SESR modulus decreasing with the 531 increasing frequency mainly attributes to the evanescent SE waves, which approximately decay 532 with a factor $\exp(-\omega p\Delta z)$ (Ren et al., 2018). The horizontal EM wave slowness p relies on the 533 incident angle of the seismic waves arriving at the interface and inducing the localized SE waves. 534 The spatial variations of SESRs presumably are complicated due to the presence of a vadose zone. 535 The multi-channel SE field waves combined with the ground acceleration field waves are sensitive 536 to water table variations (e.g., Rabbel et al., 2020). Using MC-SESRs facilitates the inversion of 537 hydrogeological parameters due to without reconstructing the seismic source function. Selecting 538 SESRs from near- and far-offset receivers, we show the SESRs varying over frequency for three 539 receivers with different offsets of 5 m, 30 m, and 50 m, respectively. As shown in Figures 6b-d, 540 the SESRs at different offsets have a similar frequency dependence. The SESR generally increases 541 as the frequency decreases, and their log-scale variations show an approximately linear correlation 542

in the low-frequency domain (\sim 10 Hz), and it oscillates at higher frequencies. Notably, the oscillating signatures are more notable in the far-offset range (Figures 6c-d). These oscillatory characteristics may originate from the electric field induced by the guided *P*-wave traveling in the upper two layers.



547

Figure 6. The MC-SESRs of the basic test model with (a) the contour map of MC-SESRs in
logarithmic scale showing variations both with frequency and offsets. Sample SESR curves as a
function of frequency at different offsets: (b) 5 m, (c) 30 m and (d) 50 m.

551

552 **Table 1**

553 Parameters of the basic test model

Property	Units	Layer 1	Layer 2	Layer 3	Layer 4	Layer 5
Thickness	m	6	9	5	15	Inf.
φ	m ³ /m ³	0.41	0.43	0.46	0.38	0.05
$\alpha_{ m VG}$	m ⁻¹	12.4	-	-	-	-
n _{VG}	-	1.89	-	-	-	-
S _{wr}	-	0.1585	-	-	-	-
$ ho_{ m s}$	kg/m ³	2650	2650	2650	2650	2700
$ ho_{ m w}$	kg/m ³			1000	·	
$ ho_{\mathrm{a}}$	kg/m ³	1.21	-	-	-	-
$ ho_{ m b}^{ m sat}$	kg/m ³	1973.5	1940.5	1891	2023	2615
C _w	mol/L			2× 10 ⁻³		
$\sigma_0^{ m sat}$	S/m	0.0073	0.0077	0.0083	0.0067	0.0016
$\eta_{ m w}$	Pa·s			1×10 ⁻³	!	
η_{a}	Pa·s	1.8× 10 ⁻⁵	-	-	-	-
Т	K		·	293.15		

ĸs	-	4					
κ _w	-	80.1					
ĸa	-		1				
т	-	1.35					
n	-	1.85					
Ks	GPa	35	35	35	35	36	
G	GPa	2.49	2.49	14.08	14.08	15	
K _{fr}	GPa	2.84	2.84	14.4	14.4	20	
K _w	GPa	2.25					
K _a	Ра	1.43× 10 ⁵	-	-	_	_	

554

3.2. Analysis of permeability

First, we test the sensitivity of SESRs with respect to permeability. The considered typical ranges in the critical zone refer to Carsel and Parrish (1988). The saturated permeability k_j^{sat} of the top four layers (j = 1,2,3,4) in the basic test model is 5.67, 8.51, 1.42, and 4.26 D, respectively (Figure 3c). By changing the saturated permeability of shallow layers (j = 1,2,3,4) \pm 50%, we calculated the absolute MC-SESRs difference concerning the original model by:

$$\Delta \text{SESR}(\omega, x_i, j) = \left| \text{SESR}(\omega, x_i)^{k_j^{\text{sat}} + 50\%} - \text{SESR}(\omega, x_i)^{k_j^{\text{sat}} - 50\%} \right|, \tag{29}$$

where the horizontal offset x_i ranges from 5 to 105 m with the number of receivers i =561 1,2, ..., 101. The short-offset (~20 m) SESRs have more changes when the permeability of shallow 562 layers has been changed than the permeability of deep layers has been changed (Figure 7). Their 563 maximum absolute differences with changing the saturated permeability of each layer decrease in 564 depth, which is 0.0877, 0.0636, 0.0377, and 0.0069 (Figures 7c, 7e, 7h, and 7l), respectively. The 565 MC-SESRs mainly change in near-offset traces ($x_i < 45$ m) and low frequencies (f < 10 Hz). The 566 absolute differences of SESRs are less when the permeability in the lower zone changes (Figure 567 71), whose maximum absolute difference of SESRs is an order of magnitude smaller than for layers 568 1 and 2. As shown in Figure 7, by changing the permeability of different layers, the absolute 569 differences of SESRs produce different variations either in frequency or laterally. 570



Figure 7. The MC-SESRs in logarithmic scale with respect to (a-d-g-j) 50% decrease and (b-e-hk) 50% increase the basic test model of (a-c) layer 1, (d-f) layer 2, (g-i) layer 3, and (j-l) layer 4. (c-f-i-l) The absolute MC-SESRs difference in logarithmic scale of the corresponding layers calculated by Equation 29.

571

To test the behaviors of SE wave-fields by changing the permeability of each layer, we 576 compare the differences between the original waveforms with the changed waveforms in Figure 8. 577 As shown in Figures 8e-h, the variations of SE wave fields are largest when the permeability of 578 layer 2 changes (Figures 8b and 8f). Layer 2 is saturated and provided with the highest saturated 579 permeability in the basic test model. Interestingly, the differences by changing the permeability of 580 layer 1 (Figure 8e) show a very different trend within 0.06 - 0.14 s in contrast with other layers 581 (Figures 8f-h). Layer 1 is a partially saturated zone, which produces a different behavior on 582 waveforms compared with other layers. 583



584

Figure 8. (a-d) Horizontal components of SE wave fields for the basic test model (black solid lines) and for cases of 50% increase (red lines) and decrease (blue lines) in the permeability of layers 1-4 respectively. (e-h) Differences between SE wave fields obtained for cased of 50% increased (red lines)/decreased (blues lines) permeability in layers 1-4 respectively compared to those obtained for the original model, at three particular offsets, whose amplitudes are amplified by a factor of 8 compared to those in (a-d).

3.3. Analysis of water table

Second, we test how the different depths of the water table or partially-saturated conditions 592 influence the distributions of MC-SESRs. Accounting for a static partially-saturated state, the VG 593 model is used to determine the water saturation (van Genuchten, 1980). The water table of the 594 basic test model is assumed to vary seasonally in a year. In this case, we assume the rainy season 595 is from September to November with higher water levels, and the period of March to May is the 596 dry season with lower water levels (Figure 9a). Correspondingly, the water saturation and the 597 effective permeability at the shallow layer change with the water table (Figures 9b-c). As the used 598 parameter α_{VG} (12.4 m⁻¹) of the VG model is large, the permeability is rather low at low 599 saturations. Note that the contour map of permeabilities shown in Figure 9c is an interpolation 600

result in the time and space domain. Permeabilities below the water level in each layer are different constants, as the basic test model presented in Figure 2c. The SESRs with the short (5 m), medium (30 m), and long (50 m) source-receiver offset are collected to show their responses to the variations of the water table (Figures 9d-f). The absolute ratios increase in the rainy season with higher water levels and decrease in the dry season with lower water levels.

Furthermore, the strength of SESRs in the high-frequency domain is increased when the 606 water table is in the shallow zone (e.g., September-November). The amplitudes of evanescent SE 607 signals decay exponentially with the normal direction of the interfaces (Ren et al., 2016b; Ren et 608 al., 2018). This implies that deep water tables cause weaker SE signals than shallow water tables. 609 610 This characteristic is also embodied in the SESRs data obtained at the source-receiver offset of 30 m (Figure 9e). Nevertheless, the sensitivity of the SESRs obtained at a more extended offset (50 611 612 m) responding to the dynamic water table depth is considerably weakened (Figure 9f). This test implies we may use the time-lapse MC-SESRs data in short source-receiver traces to monitor the 613 water table depth variations. 614



Figure 9. The modeling results with the water table vary over time. (a) The depth of the water table, (b) the time-lapse variations of the water saturation with depth, (c) the effective permeability, and the SESRs in logarithmic scale collected at a source-receiver distance of (d) 5 m, (e) 30 m and (f) 50 m.

615

620 4. Inversion Results

Employing synthetic seismic and SE data generated for the basic test model introduced in 621 Section 3.1, we carry out a three-step strategy to perform MC-SESRs inversion. We assume that 622 the depth and properties of the bottom layer 5, and all other layer depths and properties except for 623 the water table depth and the permeabilities of layers 1-4 are known. The prior information could 624 have been determined by drilling and other geophysical methods (e.g., Dzieran et al, 2019). This 625 could represent a scenario where there was interest to monitor temporal changes in depth to the 626 627 water table and to determine permeabilities of the near surface layers (to 35 m depth) for hydrogeological applications. 628

To begin, we generated random samples by drawing permeabilities for each of layers 1 - 4 629 from predefined reasonable ranges, and drawing a water table depth in layer 1 randomly from the 630 range of 1 - 5 m. We account for the ranges of hydraulic conductivity K_i^{sat} of layers 1-2, referring 631 to materials consisting of loamy sands. Layers 3-4 with a lower range of the soil permeabilities are 632 considered to contain more silty sands (Carsel & Parrish, 1988). The hydraulic conductivity of 633 layers 1-2 ranges from 3 to 35 cm/h and layers 3-4 ranges from 0.02 to 15 cm/h, which can be 634 transformed to the ranges of permeability k_j^{sat} by is equal to $\frac{K_j^{\text{sat}}\eta_w}{\rho_w g}$, where g (m/s²) denotes the 635 gravitational acceleration (9.81 m/s^2). Following the flowchart of the model generation (Figure 636 4), we calculated MC-SESRS of 7000 random samples. Therefore, the first step is to obtain the 637 7000 input-output pairs. 638

639

4.1. Performance of the BL neural network

In the second step, we randomly selected 5000 from the 7000 input-output pairs for training 640 the BL neural network (Figure 2). In addition, 1500 randomly generated samples were split into 641 the original validation dataset (500 samples) and the original testing dataset (1000 samples). The 642 input MC-SESRs data of the training samples are noise-free synthetic data, and output data are the 643 dwt and the permeability of layers 1-4 (k1, k2, k3, k4) (Figure 2c). First, to accurately extract and 644 map features of the input data, we need to set the number of mapping groups (Q) and feature nodes 645 (P) of each group and their corresponding enhancement nodes (M) based on the BL architecture 646 (Figure 2) introduced in Section 2.3. After that, the BL network is fixed. We tested different 647

configurations of the BL neural network to present the root-mean-squared errors (RMSEs) of
 training models (water table depth and permeability):

$$RMSE^{j} = \sqrt{\frac{\sum_{1}^{n} (\text{Output}_{Y_{i}^{j}} - \text{True}_{Y_{i}^{j}})^{2}}{n}},$$
(30)

where *i* denotes the corresponding numbers of different parameters (i = 1 for dwt, and i = 2 - 5 for 650 k1-4 respectively). *n* is the number of samples for training the network, which is 5000 in this case. 651 Output Y_i^j and True Y_i^j are the reconstructed and true output of the *j*th parameter of the *i*th 652 sample. Here, we separately present the RMSEs of different parameters since the output dataset 653 indicate different properties and in different scales. The ranges of P, Q and M are [10:5:100], 654 [10:5:100], and [10:10:500], respectively. The regularization coefficient is set to 10^{-8} (see Chen 655 & Liu, 2017). The optimum sets of parameters for training models are given in Table 2. The 656 RMSEs of water table depth can be limited to 0.034 m. The RMSEs of permeability of layer 1 are 657 much higher than layers 2-4. In contrast with deep layers, the permeability of the top layer is easier 658 to be directly investigated in situ. k2 and k3 reach their optimum under P=15, Q=10 and M=500, 659 and correspondingly, the RMSEs for estimating the dwt and k4 are satisfactory with the same 660 setting. 661

- 662 **Table 2**
- 663 *RMSEs of training data set with different configurations of the BL model (bold numbers denote* 664 *the corresponding minimum RMSEs)*

Param	eters of	BL model		RMSE o	f training mo	odels	
Р	Q	М	dwt (m)	k1 (D)	k2 (D)	k3 (D)	k4 (D)
100	100	500	0.0210	2.4174	0.1462	0.1899	0.1526
80	40	500	0.0271	2.4090	0.1713	0.2005	0.1644
15	10	500	0.0339	2.4274	0.1415	0.1603	0.1616
10	10	500	0.0336	2.4239	0.1473	0.1628	0.1500

As the parameters' estimation accuracy is the highest when the number of enhancement nodes (*M*) reaches the maximum in the search range, we expanded this range to search for an appropriate neural network. The neural network gets more complex structures with a large number of groups, mapping feature nodes, and enhancement nodes, which may empower the BL model to describe the approximate mapping relationship between the input and output data from the training

data set. As shown in Figure 2b, M directly reflects the complexity of the connected matrix for 670 linking the integration of the feature mapping layer and the enhancement layer with the output 671 layer. To examine whether the RMSEs would be reduced by keeping increasing the enhancement 672 nodes and fixing P = 15 and Q = 10, we display the RMSEs varying with the number of 673 enhancement nodes (Figure 10). In addition, we utilized 500 untrained samples from the validation 674 dataset to test the inverted performance with increasing M. Further, the measured data in practice 675 ineluctably contain some noise. With the improvement of pre-and post-processing techniques on 676 near-surface SE applications, the signal-to-noise ratio (SNR) can be achieved to 20-45 dB (Butler 677 & Russel, 2003; Butler et al., 2007). Thereby, to account for the possible interferences from self-678 noise and background noise, we add 5% random noise of the mean amplitude of synthetic SESRs 679 at each trace (SNR ≈ 26 dB) to the initial validation and testing datasets without noise 680 681 contamination. Similar to the treatment of the training dataset, the RMSEs of the validation dataset are calculated by replacing the number of samples in Equation 30 to 500 and updating the 682 corresponding output dataset. Slightly though, the RMSE set keeps decreasing with M increasing 683 (Figures 10a, 10c, 10e, and 10g), which indicates the neural network has been adapted to the 684 685 training data set. However, there are different trends shown in untrained samples (Figures 10b, 10d, 10f, and 10h). 686

The parameter estimation using untrained noisy data as input performs better when M is 687 lower than 300 (Figures 10b, 10d, 10f, and 10h). The number of enhancement nodes of each 688 parameter reaching a minimum RMSE is given in Table 3. To show the influence of chosen M on 689 the inversion accuracy, we contrast the true and reconstructed models by inputting noisy MC-690 SESRs of the validation dataset under the BL neural networks trained by M = 50, 200, 500, and691 1000, respectively. Taking the water table depth as an example to display (Figure 11), the majority 692 of reconstructed models are visually closer to the true models with increasing M, but the RMSE 693 increases when $M \ge 200$ (Figures 11c-d). The reconstructed permeability also presents a similar 694 trend (see Figures S1-S3 of Supporting Information). It can be attributed to the large departure of 695 a few estimations from the true models. Finally, to detect the dynamic water table, we choose M =696 697 240 as the number of enhancement nodes to train the BL model.





Figure 10. RMSEs of output data (a-b: water table depth, c-d: permeability of layer 1, e-f: permeability of layer 2, and g-h: permeability of layers 3-4) vary with the number of enhancement nodes (P=15, Q=10). Panels in the left column (a, c, e, g) represent the training data set and panels in the right column (b, d, f, h) represent the validation noisy dataset.

- 703 **Table 3**
- *RMSEs of validation data set with the optimum number of enhancement nodes (bold numbers denote the corresponding minimum RMSEs)*

Enhancement node	RMSE of validation models				
М	dwt (m)	k1 (D)	k2 (D)	k3 (D)	k4 (D)
240	0.0895	2.7884	0.8879	0.5321	0.4339
20	0.1839	2.6092	0.4798	0.6212	0.5654
300	0.1945	4.5221	0.3084	0.9505	0.8540
220	0.1196	2.7551	0.6383	0.4510	0.4140
200	0.1117	2.8753	0.5839	0.4730	0.4101

706



707

Figure 11. Comparisons of the true and reconstructed depth of water table (dwt) of the validation dataset with (a) M = 50, (b) M = 200, (c) M = 500, and (d) M = 1000

710 **4.2. Comparisons of reconstructed and true models**

After the 500 validation samples validated the BL model obtained by the 5000 training 711 712 samples, we took the third step to attain MC-SESRs inversion. We applied this BL neural network configured by P=15, Q=10, and M=240 to invert the water table depth and permeability of 1000 713 testing samples with the same amount of noise contamination as the original testing MC-SESRs 714 dataset. The testing dataset is independent of the training or validation datasets. The RMSEs of the 715 716 testing dataset are calculated similarly to the validation dataset (Equation 30). The reconstructed depth of the water table has great consistency with corresponding true values (Figure 12a), whose 717 RMSE is 0.09 m. The inversion results can nicely reconstruct the permeability of layer 2 (Figure 718 12c), whose RMSE is 0.46 D. the reconstructed permeability of layers 3 and 4 deviates more from 719 true values than layer 2 (Figure 12d), while their RMSEs are acceptable (0.56 D and 0.43 D, 720 respectively). Nevertheless, the permeability of the partially saturated layer 1 cannot be 721

- reconstructed, which concentrates around 5 D. It reflects that the SESRs data did not constrain the
- permeability of the unsaturated layer well since the low saturation makes a very low effective
- permeability to obtain a small SE coupling coefficient (Equation 11).



725

Figure 12. Comparisons of the true and reconstructed (a) depth of water table, (b) permeability of layer 1, (c) permeability of layer 2 and (d) permeability of layers 3-4 using noisy MC-SESRs data (SNR \approx 26 dB).

Based on the settings of the basic test model, we used the SESRs data introduced in Section 729 730 3.3 to characterize variations in the water table depth. As the data uncertainty not only can originate from the noise but also possibly contains the errors of the model parameters, here, we assumed 731 five-percent errors of dwt, permeability, and porosity included in the basic test model. Still, the 732 data are assumed to be contaminated by five-percent random noise in the following tests. 733 734 Meanwhile, as the sensitivity analysis of SESRs to the dwt in Section 3.3 shows, the short-offset SESRs are more sensitive than the long-offset SESRs to the variations of dwt, we test to apply the 735 different number of channels to reconstruct the dynamic dwt. All 101 channels' or 26 short-offset 736 channels' SESRs data used to invert the dwt can obtain comparable accuracy under five-percent 737 errors in model parameters (Figure 13). This test indicates that we can reconstruct dynamic shallow 738

dwt by using less short-offset MC-SESRs data. Since higher errors may occur in realistic measurements, we compare the inversion accuracy under five-percent, ten-percent, and twentypercent errors in the pre-defined model using 26 short-offset channels' SESRs in Figure 14. The inverted water table depths are more deviated from the true values by enhancing errors. However, the overall inverted values are consistent with the true values with twenty-percent errors in the known model parameters, except for the result in September (Figure 14c).



Figure 13. Detection of the water table depth using noisy MC-SESRs data collected from (a) 101 traces (5 - 105 m) and (b) 26 traces (5 - 30 m). The blue diamonds represent the inverted value without the model errors; The red diamonds represent the true values with 5%-misspecified errors in pre-defined model parameters; The circles represent the inverted values, whose misspecified levels are indicated by the shaded areas and error bars.

745



751

Figure 14. Detection of the water table depth using the noisy 26-channel SESRs data with misspecified errors of (a) 5%, (b) 10%, and (c) 20% in pre-defined model parameters. Diamonds represent the true values; The circles represent the inverted values, whose misspecified levels are indicated by the shaded areas and error bars.

As the absolute pressure head in the vadose zone is assumed to be the distance between its 756 elevation and the water table level, the effective permeability and water saturation are calculated 757 by the MVG model. We show that the true and the inverted permeabilities vary with time in Figure 758 15. The permeability can still be reconstructed in the time-lapse profiles (Figure 15a). The 759 predicted accuracy is also reduced when errors added to the model are enhanced (Figures 15b and 760 15c). Particularly, the inverted errors of permeability increase in layer 4 due to the increasingly 761 762 attenuated seismic and SE signals strength. The model parameters may be misspecified by larger errors, which causes lower inverted accuracy in deep layers due to the fragile signals. 763





Figure 15. Comparison of true (black lines) and inverted (pink) permeability with the changing
water table depth by accounting for errors of (a) 5%, (b) 10% and (c) 20% in pre-defined model
parameters.

768 **5. Discussion**

To test the capability of this neural network in the presence of noise, we decrease the SNR 769 to 20 dB, 16 dB, and 14 dB by considering different random noise levels (10%, 15%, and 20%) 770 into synthetic MC-SESRs data. Based on the assumptions in Section 4.3, we attempt to use the 771 SESRs data at different noise levels to detect the changing water table levels. As shown in Figure 772 16, the inverted accuracy is reduced when the noise is enhanced from 5% to 10% and more. In this 773 case, the water table detection can be achieved at a 10% noise level when 26-channel SESR data 774 (5 - 30 m) have been involved in the inversion (Figure 16a). This scenario can be improved by 775 increasing the data by using more traces. The RMSE reaches 0.1671 m at a 20%-noise level when 776 the used channels increase to 101. Correspondingly, the source-receiver offset ranges from 5 to 777 105 m (Figures 16b, 16d, and 16f). The inverse modeling may be able to perform well for stronger 778 noise levels when the used MC-SESR data are sufficient. Note that the monitoring test in Section 779

4.2 discussed the influence of different levels of errors in model parameters (Figures 13-15). Ideally, although the water table and permeability changed with time and contained model perturbations, the well-trained network (Figure 2) can recover their true values for a specific site. Therefore, the inverted values are still close to the true values using 26-channel data with mixing the noise level of 5% (Figure 13). However, the porosity of each layer is also assumed to be misspecified. Thus, the increased errors in the pre-defined model decrease the inverted accuracy of the water table depth and permeability.



787

Figure 16. Comparison of true (blue) and predicted (purple) water table depth by adding (a-b) 10%, (c-d) 15% and (e-f) 20% random noise into data. The left panels (a, c, and e) use 26-channel SESRs data and the right panels (b, d, and f) use 101-channel SESRs data. The shaded areas indicate the misspecified levels.

As aforementioned sensitivity of permeability and water table depth in Sections 3.2-3.3, 792 the SESRs at different source-receiver offsets respond to the variations of different layers. The 793 number and locations of sensors used for inversion may affect the inverted results. We test the 794 inverted RMSEs using MC-SESRs with different offsets by 1000 untrained random models. The 795 796 interval distance of adjacent sensors is kept at 1 m. It starts from offset = 10 m, which means that MC-SESRs data obtained by 6 traces in the range of 5 - 10 m are used for inversion (see Section 797 2.3 X: SESR_{5000×36×6}). Figure 17 shows that the RMSEs dropped considerably when the used 798 799 offsets increased to 30 m, but they continued reducing to a lesser extent. Generally, more SESRs data used for inversion should obtain higher inverted accuracy. 800

801 Picking a model to contrast the true with reconstructed parameters, the predicted permeability can reconstruct the effective permeability above the capillary fringe based on the 802 water table estimation. However, the predicted saturated permeability of layer 1 deviates from its 803 true value (Figure 18a). The inverted saturated permeability of the top layer poorly fits the true 804 value embodied in the whole test set (Figure 12b). As the effective permeability drops considerably 805 at low water saturations, the SE coupling coefficient is rather small. Thus, the information of the 806 saturated permeability in layer 1 cannot be extracted by the mapping feature layer of input MC-807 SESRs data. The water table depth and permeability of layers 2-4 of the model are well estimated. 808 Although the noisy MC-SESRs data for inversion are affected by disturbances (Figure 18c), the 809 MC-SESRs data calculated by the predicted model (Figure 18d) well fit the synthetic MC-SESRs 810 data (Figure 18b). The fitting errors concentrate in 10-25 m and low frequencies (~3 Hz) (Figure 811 18e). The inversion accuracy for this case is satisfactory by using data from 26 channels (~30 m) 812 to train and invert the water table depth and permeability. One estimation with lower accuracy is 813 presented in the Figure S4 of Supporting Information, whose modeling result from the inverted 814 parameters can recover the overall shape and trend of the original data, but the maximum absolute 815 difference is one order of magnitude larger than Figure 18e. 816



817

Figure 17. RMSEs between inverted and true models vary with the offset (SNR \approx 26 dB). (a) water table depth, (b) permeability of layers 1-2 and (c) permeability of layers 3-4





Figure 18. Comparisons of the true model and the reconstructed model using 26-channel SESR data. (a) The blue (solid) and cyan (dashed) lines represent the true and predicted water table depth, respectively. The black (solid) and pink (dashed) lines represent the true and reconstructed permeability, respectively. (b-d) display the 26-channel synthetic and noisy SESR data modeling by (b-c) the true model and (d) the inverted model. (e) shows SESRs difference between the data modeling by the true model and the inverted model.

827 6. Conclusions

In this paper, we propose using MC-SESRs to process multi-channel SE signals and 828 seismic signals recorded at the ground surface. By analyzing the sensitivity of MC-SESRs to the 829 water table depth and permeability, the results indicate that MC-SESRs data obtained by different 830 offsets respond to the variations of different water table depths and permeability. Moreover, we 831 introduce a simple and efficient BL approach to interpret MC-SESRs data to quantitatively infer 832 the water table depth and permeability of layered-porous materials. As a type of non-invasive 833 measurement, MC-SESRs obtained by surface observations can supplement traditional piezometer 834 installations. It can be applied to rapidly and accurately detect the water table for a specific 835 investigated field even though pre-defined model parameters are misspecified by 20%. This feature 836 of monitoring the water table has potential applications for assessing groundwater storage and 837 studying frost thawing and volcanic eruption. Nevertheless, as aforementioned, the dynamic 838

effective excess charge density using the scaling factors by volumetric average and relaxation time

suffers several limits as predictions, particularly at the pore scale. We suggest considering explicit

frequency- and saturation-dependence in the future (Jougnot & Solazzi, 2021; Solazzi et al., 2022;

- 842 Thanh et al., 2022).
- 843

844 Appendix A

Tables A1 and A2 list the acronyms as well as the notation and description of symbols used in the manuscript, respectively. The formulations of frequency-dependent (dynamic) and saturation-dependent parameters are summarized in Table A3.

Acronyms	Meaning	
SE	SeismoElectric	
SESR	SeismoElectric Spectral Ratio	
MC-SESR	Multi-Channel SeismoElectric Spectral Ratio	
EDL	Electrical Double Layer	
AVO	Amplitude variation Versus Offset	
BL	Broad Learning	
RVFLNN	Random Vector Functional Link Neural Network	
EM	ElectroMagnetic	
MVG	Mualem-van Genuchten	
VG	van Genuchten	
LAC GRTM	Luco-Apsel-Chen Generalized Reflection and Transmission Method	
dwt	Water table depth	

848 **Table A1**. Acronyms and meaning

Description **Symbol** Unit rad/s Angular frequency ω Hz Frequency f Angular transition frequency Hz ωt The critical angle of evanescent rad/s $\theta_{\rm c}$ electromagnetic waves S_{w} Water saturation - $S_{\rm wr}$ Residual water saturation -Effective water saturation $S_{\rm e}$ σ^{*} S/m Complex electrical conductivity Electrical conductivity of pore water S/m $\sigma_{\rm w}$ Static bulk electrical conductivity S/m σ_0 Electric field V/m Ε A/m^2 Total current density J A/m^2 Streaming cross-coupling coefficient L^* Streaming cross-coupling coefficient at $L_0^{\rm sat}$ A/m^2 the saturated condition in low frequency Saturated effective excess charge density $\hat{Q}_{\rm v.0}^{\rm sat}$ C/m^3 in low frequency Effective excess charge density in low $\hat{Q}_{\rm v.0}$ C/m^3 frequency \hat{Q}_{v}^{*} C/m^3 Complex effective excess charge density Cation exchange capacity CEC C/kg Mobility of the counterions in the diffuse m^2/sV β_+ layer Mobility of the counterions in the Stern β_{+}^{sur} m^2/sV layer $f_{\rm Q}$ Fraction of counterions in the Stern layer C_0^{sat} V/m Streaming voltage coupling coefficient Salinity of pore water mol/L $C_{\rm w}$ Electrical formation factor F -Cementation exponent of Archie's law mSaturation exponent of Archie's law _ п Pore-fluid pressure Ра $p_{\rm f}$ kg/m^3 Mass density of fluid $\rho_{\rm f}$ Mass density of solid kg/m^3 $\rho_{\rm s}$ $ho_{ m b}^{ m sat}$ Saturated bulk mass density kg/m³ Averaging solid displacement m/s us Averaging pore-fluid displacement m/s $\mathbf{u}_{\mathbf{f}}$ Averaging filtration displacement w m/s k^* m² Frequency-dependent permeability Effective permeability in low frequency k_0 -

Table A2. Nomenclature of the Material Properties

$k_0^{\rm sat}$	m ²	Saturated permeability in low frequency
ϕ	m^3/m^3	Porosity
$\alpha_{\rm VG}$	m ⁻¹	Parameters of van Genuchten model
n _{VG}	-	Parameters of van Genuchten model
$ au_{ m w}$	-	Tortuosity
$\eta_{ m w}$	Pa·s	Dynamic viscosity of pore-water
α	-	Biot coefficient
α^{sat}	-	Saturated Biot coefficient
Т	°C or K	Temperature
ε_0	F/m	Vacuum permittivity
κ _w	-	Dielectric constant of water
ĸa	-	Dielectric constant of air
Ks	-	Dielectric constant of solid phase
Ks	Pa	Bulk modulus of solid phase
G	Pa	Frame shear modulus
K _{fr}	Pa	Frame bulk modulus
Kw	Pa	Bulk modulus of water
Ka	Pa	Bulk modulus of air
K _G	Pa	Undrained bulk modulus
Ĉ	Pa	Biot modulus
М	Pa	Biot modulus

850 **Table A3.** Frequency- and saturation-dependent parameters and corresponding formulations

Parameter	Unit	Expression	References
Angular transition frequency $\omega_t(S_w)$	Hz	$\frac{\eta_{\rm w}\phi S_{\rm w}}{\rho_{\rm w}k_0(S_{\rm w})\tau_{\rm w}(S_{\rm w})}$	Revil & Mahardika, 2013; Solazzi et al., 2020
Tortuosity $ au_{w}(S_{w})$	-	ϕFS_{w}^{1-n}	Revil & Jougnot, 2008; Jougnot et al., 2018
Dynamic permeability k [*] (ω, S _w)	-	$\frac{k_0(S_w)}{1 - \frac{i\omega}{2\omega_t}}$	Revil & Mahardika, 2013
Effective water saturation $S_e(S_w)$	-	$\frac{S_{\rm w} - S_{\rm wr}}{1 - S_{\rm wr}}$	

Quasi-static		$1 \left[\left(1 \right)^{m_{\text{VG}}} \right]^2$		
effective	-	$k_0^{\text{sat}}S_e^{\frac{1}{2}} \left[1 - \left(1 - S_e^{\overline{m_{VG}}} \right) \right]$	Mualem, 1976; van	
permeability		$m_{\rm He} = 1 - n_{\rm He}^{-1}$	Genuchten, 1980	
$k_0(S_w)$		$m_{\rm VG} = 1 - m_{\rm VG}$		
Specific		$1 (1)^{m_{VG}}$	Richards 1931 van	
moisture	m ⁻¹	$\alpha_{\rm VG} m_{\rm VG} \phi (1 - S_{\rm wr}) S_{\rm e}^{\overline{m_{\rm VG}}} \left(1 - S_{\rm e}^{\overline{m_{\rm VG}}} \right)$	Genuchten 1980	
capacity $C_{\rm m}(S_{\rm w})$		$1 - m_{VG}$	Gendenten, 1980	
Frequency-				
dependent				
effective excess	-	$\hat{Q}_{v,0}(S_w) \left 1 - \frac{i\omega}{\omega} \right $	Revil & Mahardika,	
charge density		$\sqrt{\omega_{t}}$	2013	
$\hat{Q}_{v}^{*}(\omega, S_{w})$				
Complex				
electrical	S /m	$S_{w}^{n}\sigma_{w}$	Paril et al. 2015	
conductivity	5/11	$\frac{1}{F} + \sigma_{\rm sur}(S_{\rm w}) + \iota[\sigma_{\rm quad}(S_{\rm w}) - \omega\varepsilon_0\kappa(S_{\rm w})]$	Revii et al., 2015	
$\sigma^*(\omega, S_{\mathrm{w}})$				
Effective surface			Revil 2013: Revil &	
conductivity	S/m	S/m	$\frac{2}{3}m\frac{(F-1)}{F}S_{w}^{n-1}\beta_{+}(1-f_{Q})\rho_{s}CEC$	Mahardika 2013
$\sigma_{\rm sur}(S_{\rm w})$		5 1	Wanaruka, 2015	
Effective				
quadrature	S/m	$2_{m}(F-1)_{C} \stackrel{n-1}{\to} e^{-1}e^{$	Revil, 2013; Revil &	
conductivity	5/11	$-\frac{1}{3}m \frac{1}{F} S_{W} + \beta_{+} M f_{Q} \rho_{s} CEC$	Mahardika, 2013	
$\sigma_{\text{quad}}(S_{\text{w}})$				
Dielectric	_	$(F-1)\kappa_{\rm s} + S_{\rm w}{}^n\kappa_{\rm w} + (1-S_{\rm w}{}^n)\kappa_{\rm a}$	Linde et al. 2006	
constant $\kappa(S_w)$	_	F	Linde et al., 2000	
Biot coefficient		$S_{\rm w} - S_{\rm wr}$ asat	Revil & Mahardika,	
$\alpha(S_{\mathrm{w}})$	-	$\frac{1-S_{\rm wr}}{1-S_{\rm wr}}$	2013	
Mass density of	kg/m ³	$S_{11} a_{11} + (1 - S_{1}) a_{11}$		
fluid $\rho_{\rm f}(S_{\rm w})$	K6/ III	$S_W p_W + (1 - S_W) p_a$		
Bulk modulus of	Pa	$\frac{1}{S - 1 - S}$		
fluid K _f	10	$\frac{S_{W}}{K_{W}} + \frac{1}{K_{a}} \frac{S_{W}}{K_{a}}$		

852 Acknowledgments

Kaiyan Hu thanks the financial support of the National Natural Science Foundation of 853 China (Grant No. 42104069), and the special fund for the scientific and technological development 854 of Shenzhen guided by the central government of China (Grant No. 2021Szvup003). Hengxin Ren 855 thanks the support from the National Natural Science Foundation of China (Grant No. 42022027), 856 the Guangdong Provincial Key Laboratory of Geophysical High-resolution Imaging Technology 857 (Grant No. 2022B1212010002), and the Shenzhen Science and Technology Program (Grant No. 858 859 KQTD20170810111725321). The authors acknowledge the contributors and releasers of Broad 860 Learning System codes (Chen & Liu, 2017) and the data set used in this work (Hu et al., 2022) for making their resources publicly available. We wish to thank editor Douglas Schmitt, associate 861 editor Joel Sarout, and two anonymous reviewers for their constructive comments and suggestions, 862 which greatly helped us to improve our manuscript. 863

864 **Open Research**

The data set and the main codes for inversion related to this manuscript can be found in the Hydrogeophysics Community of Zenodo (https://doi.org/10.5281/zenodo.7820571). The subroutines of the broad learning system can be found at https://broadlearning.ai/ (Chen & Liu, 2017). The used code of the peak-trough averaging algorithm is located at https://datadryad.org/stash/share/xXcw75yKN0M_C_MMcqYVKQxb-qAvGjf7ICPnahRBH4Y (Zheng et al., 2021).

871 **References**

- Archie, G. E. (1942). The electrical resistivity log as an aid in determining some reservoir
- 873 characteristics. Transactions of the American Institute of Mining, Metallurgical and Petroleum
- 874 Engineers, 146, 54–62. https://doi.org/10.2118/942054-G
- Biot, M. A. (1956). Theory of propagation of elastic waves in a fluid saturated porous solid: I. low
- frequency range. The Journal of the Acoustical Society of America, 28(2), 168–178.
- 877 https://doi.org/10.1121/1.1908241
- Biot, M. A. (1962a). Mechanics of deformation and acoustic propagation in porous media. *Journal*
- of Applied Physic, 33, 1482-1498. https://doi.org/10.1063/1.1728759
- Biot, M. A. (1962b). Generalized theory of acoustic propagation in porous dissipative media. *The*
- *Journal of the Acoustical Society of America*, *34*, 1254-1264. https://doi.org/10.1121/1.1918315

- 882 Bordes, C., Sénéchal, P., Barrière, J., Brito, D., Normandin, E., & Jougnot, D. (2015). Impact of
- 883 water saturation on seismoelectric transfer functions: a laboratory study of coseismic
- phenomenon. *Geophysical Journal International*, 200(3), 1317-1335.
- 885 https://doi.org/10.1093/gji/ggu464
- 886 Butler, K. E., Russell, R. D., Kepic, A. W., & Maxwell, M. (1996). Measurement of the
- seismoelectric response from a shallow boundary. *Geophysics*, 61, 1769–1778.
 https://doi.org/10.1190/1.1444093
- Butler, K. E., Fleming, S. W., & Russell, R. D. (1999). Field test for linearity of seismoelectric
 conversions. *Canadian Journal of Exploration Geophysics*, *35*, 20-23.
- Butler, K. E., & Russell, R. D. (2003). Cancellation of multiple harmonic noise series in
 geophysical records, *Geophysics*, 68, 1083-1090. https://doi.org/10.1190/1.1581080
- Butler, K. E., Dupuis, J. C., & Kepic, A. W. (2007). Improvements in signal-to-noise in
 seismoelectric acquisition. In Proceedings of exploration 07, Fifth Decennial International
- 895 Conference on Mineral Exploration (pp. 1137–1141), Toronto.
- 896 Butler, K. E., Kulessa, B., & Pugin, A. J. (2018). Multimode seismoelectric phenomena generated
- using explosive and vibroseis sources. *Geophysical Journal International*, 213(2), 836-850.
 https://doi.org/10.1093/gji/ggy017
- Carsel, R. F., & Parrish, R. S. (1988). Developing joint probability distributions of soil water
 retention characteristics. *Water Resources Research*, 24(5), 755-769.
 https://doi.org/10.1029/WR024i005p00755
- 902 Chen, C. P., & Liu, Z. (2017). Broad learning system: An effective and efficient incremental
- 903 learning system without the need for deep architecture. *IEEE Transactions on Neural Networks*
- *and Learning Systems*, 29(1), 10-24. https://doi.org/10.1109/TNNLS.2017.2716952
- Dahlquist, G., & Björck, Å. (1974). *Numerical Methods*. Englewood Cliffs N. J., Prentice-Hall.
- Devi, M. S., Garambois, S., Brito, D., Dietrich, M., Poydenot, V., & Bordes, C. (2018). A novel
- 907 approach for seismoelectric measurements using multielectrode arrangements: II-Laboratory
- measurements. *Geophysical Journal International*, 214(3), 1783–1799.
 https://doi.org/10.1093/gji/ggy251
- 910 Du, J., Vong, C. M., & Chen, C. P. (2020). Novel efficient RNN and LSTM-like architectures:
- 911 Recurrent and gated broad learning systems and their applications for text classification. *IEEE*
- 912 Transactions on Cybernetics, 51(3), 1586-1597. https://doi.org/10.1109/TCYB.2020.2969705

- 913 Dukhin, S. S., & Derjaguin, B. V. (1974). Electrokinetic phenomena. In Surface and Colloid
- 914 Science, (ed. E. Matijevic), 7, 322. Wiley.
- 915 Dupuis, J. C., & Butler, K. E. (2006). Vertical seismoelectric profiling in a borehole penetrating
- 916 glaciofluvial sediments. *Geophysical Research Letters*, 33(16).
- 917 https://doi.org/10.1029/2006GL026385
- Dupuis, J. C., Butler, K. E., & Kepic, A. W. (2007). Seismoelectric imaging of the vadose zone of
- a sand aquifer. *Geophysics*, 72, A81–A85. https://doi.org/10.1190/1.2773780
- 920 Dzieran, L., Thorwart, M., Rabbel, W., & Ritter, O. (2019). Quantifying interface responses with
- 921 seismoelectric spectral ratios. Geophysical Journal International, 217(1), 108-121.
- 922 https://doi.org/10.1093/gji/ggz010
- Dzieran, L., Thorwart, M., & Rabbel, W. (2020). Seismoelectric monitoring of aquifers using local
- 924 seismicity—a feasibility study. Geophysical Journal International, 222(2), 874-892.
- 925 https://doi.org/10.1093/gji/ggaa206
- 926 Feng, S., Ren, W., Han, M., & Chen, Y. W. (2019). Robust manifold broad learning system for
- 927 large-scale noisy chaotic time series prediction: A perturbation perspective. Neural Networks, 117,
- 928 179-190. https://doi.org/10.1016/j.neunet.2019.05.009
- 929 Fitterman, D. V. (2015). Tools and techniques: Active-source electromagnetic methods. Treatise
- 930 on Geophysics (Second Edition), 11, 295-333. https://doi.org/10.1016/B978-0-444-53802931 4.00193-7
- Garambois. S., & Dietrich, M. (2001). Seismoelectric wave conversions in porous media: Field
 measurements and transfer function analysis. *Geophysics*, 66(5), 1417–1430.
 https://doi.org/10.1190/1.1487087
- Garambois, S., & Dietrich, M. (2002). Full waveform numerical simulations of
 seismoelectromagnetic wave conversions in fluid-saturated stratified porous media. *Journal of*
- 937 *Geophysical Research: Solid Earth*, 107(B7), 1–19. https://doi.org/10.1029/2001JB000316
- Ghanbarian, B., Hunt, A. G., Ewing, R. P., & Sahimi, M. (2013). Tortuosity in porous media: a
- 939 critical review. Soil Science Society of America Journal, 77(5), 1461-1477.
- 940 https://doi.org/10.2136/sssaj2012.0435
- Glover, P. W. J., & Jackson, M. D. (2010). Borehole electrokinetics. The Leading Edge, 29(6),
- 942 724–728. https://doi.org/10.1190/1.3447786

- 943 Gong, X., Zhang, T., Chen, C. P., & Liu, Z. (2022). Research review for broad learning system:
- algorithms, theory, and applications. IEEE Transactions on Cybernetics, 52(9), 8922-8950.
- 945 https://doi.org/10.1109/TCYB.2021.3061094
- 946 Grobbe, N., & Slob, E. (2016). Seismo-electromagnetic thin-bed responses: Natural signal
- 947 enhancements? Journal of Geophysical Research: Solid Earth, 121(4), 2460-
- 948 2479. https://doi.org/10.1002/2015JB012381
- Grobbe, N., Revil, A., Zhu, Z., & Slob, E. (Eds.). (2020). Seismoelectric exploration: Theory, *experiments, and applications* (Vol. 252). John Wiley & Sons.
- Guarracino, L., & Jougnot, D. (2018). A physically based analytical model to describe effective
- 952 excess charge for streaming potential generation in water saturated porous media. Journal of
- 953 *Geophysical Research: Solid Earth*, *123*(1), 52-65. https://doi.org/10.1002/2017JB014873
- Haartsen, M. W., & Pride, S. R. (1997). Electroseismic waves from point sources in layered media.
- 955 Journal of Geophysical Research: Solid Earth, 102(B11), 24745–24769.
 956 https://doi.org/10.1029/97JB02936
- Haines, S. S., & Pride, S. R. (2006). Seismoelectric numerical modeling on a
 grid. *Geophysics*, 71(6), N57-N65. https://doi.org/10.1190/1.2357789
- Hu, H., & Gao, Y. (2011). Electromagnetic field generated by a finite fault due to electrokinetic
 effect. *Journal of Geophysical Research: Solid Earth*, *116*(B8), 1–14.
 https://doi.org/10.1029/2010JB007958
- Hu, K., Jougnot, D., Huang, Q., Looms, M. C., & Linde, N. (2020). Advancing quantitative
 understanding of self- potential signatures in the critical zone through long-term monitoring. *Journal of Hydrology*, 585, 124771. https://doi.org/10.1016/j.jhydrol.2020.124771
- Hu, K., Ren, H., Huang, Q., Zeng, L., Butler, K. E., Jougnot, D., Linde, N., & Holliger, K. (2022).
- Dataset for "Water Table and Permeability Estimation from Multi-Channel Seismoelectric
 Spectral Ratios" [Data set]. Zenodo. https://doi.org/10.5281/zenodo.7820571
- Hu, K., Huang, Q., Han, P., Han, Z., Yang, Z., Luo, Q., et al. (2023). A hydrochemical study of
- 969 groundwater salinization in Qinzhou Bay, Guangxi, Southern China. *Earth and Space Science*, 10,
- 970 e2022EA002565. https://doi. org/10.1029/2022EA002565
- Huang, Q. (2002). One possible generation mechanism of co-seismic electric signals, *Proceeding*
- of the Japan Academy, Series B, 78(7), 173–178. https://doi.org/10.2183/pjab.78.173

- Hunter, R. J. (1981). Zeta Potential in Colloid Science: Principles and Applications. Academic
 Press.
- Jackson, M. D. (2010). Multiphase electrokinetic coupling: Insights into the impact of fluid and
- charge distribution at the pore scale from a bundle of capillary tubes model. *Journal of Geophysical Research: Solid Earth*, *115*(B7), 1-17. https://doi.org/10.1029/2009JB007092
- Jardani, A., Revil, A., Boleve, A., Crespy, A., Dupont, J. P., Barrash, W., & Malama, B. (2007).
- 979 Tomography of the Darcy velocity from self-potential measurements. *Geophysical Research*
- 980 Letters, 34(24), 1-6. https://doi.org/10.1029/2007GL031907
- Jardani, A., Revil, A., Slob, E., & Söllner, W. (2010). Stochastic joint inversion of 2D seismic and
- 982 seismoelectric signals in linear poroelastic materials: A numerical investigation. *Geophysics*,
- 983 75(1), N19–N31. https://doi.org/10.1190/1.3279833
- Jougnot, D., Linde, N., Revil, A., & Doussan, C. (2012). Derivation of soil-specific streaming
- potential electrical parameters from hydrodynamic characteristics of partially saturated soils. *Vadose Zone Journal*, *11*(1). https://doi.org/10.2136/vzj2011.0086
- Jougnot, D., Rubino, J. G., Carbajal, M. R., Linde, N., & Holliger, K. (2013). Seismoelectric
- effects due to mesoscopic heterogeneities. *Geophysical Research Letters*, 40(10), 2033-2037.
- 989 https://doi.org/10.1002/grl.50472
- Jougnot, D., Jiménez-Martínez, J., Legendre, R., Le Borgne, T., Méheust, Y., & Linde, N. (2018).
- ⁹⁹¹ Impact of small-scale saline tracer heterogeneity on electrical resistivity monitoring in fully and
- 992 partially saturated porous media: Insights from geoelectrical milli-fluidic experiments. Advances
- *in Water Resources*, *113*, 295-309. https://doi.org/10.1016/j.advwatres.2018.01.014
- Jougnot, D., Roubinet, D., Guarracino, L., & Maineult, A. (2020). Modeling streaming potential
- in porous and fractured media, description and benefits of the effective excess charge density
- approach. In Advances in modeling and interpretation in near surface geophysics (pp. 61-96).
 Springer, Cham.
- Jougnot, D., & Solazzi, S. G. (2021). Predicting the frequency-dependent effective excess charge
- 999 density: A new upscaling approach for seismoelectric modeling. *Geophysics*, 86(5), WB77-
- 1000 WB86. https://doi.org/10.1190/geo2020-0524.1
- 1001 Jouniaux, L., & Zyserman, F. (2016). A review on electrokinetically induced seismo-electrics,
- 1002 electro-seismics, and seismo-magnetics for earth sciences. Solid Earth, 7(1), 249-284.
- 1003 https://doi.org/10.5194/se-7-249-2016

- 1004 Knight, R. J., & Endres, A. L. (2005). An introduction to rock physics principles for near-surface
- 1005 geophysics. In: Butler D. K. (Ed.), Near Surface Geophysics, Part 1: Concepts and Fundamentals.
- 1006 Society of Exploration Geophysicists, 13, p. 31-70.
- 1007 Linde, N., Binley, A., Tryggvason, A., Pedersen, L. B., & Revil, A. (2006). Improved
- 1008 hydrogeophysical characterization using joint inversion of cross-hole electrical resistance and
- 1009 ground-penetrating radar traveltime data. Water Resources Research, 42(11), W12404.
- 1010 https://doi.org/10.1029/2006WR005131
- 1011 Linde, N., Jougnot, D., Revil, A., Matthai, S. K., Arora, T., Renard, D., & Doussan, C. (2007a).
- 1012 Streaming current generation in two-phase flow conditions. *Geophysical Research Letter*, 34(3),
- 1013 L03306. https://doi.org/10.1029/2006GL028878
- 1014 Linde, N., Revil, A., Bolève, A., Dagès, C., Castermant, J., Suski, B., & Voltz, M. (2007b).
- 1015 Estimation of the water table throughout a catchment using self-potential and piezometric data in
- 1016 a Bayesian framework. *Journal of Hydrology*, *334*, 89–99. https://doi.org/10.
 1017 1016/j.jhydrol.2006.09.027
- 1018 Mao, S., Lecointre, A., van der Hilst, R. D., & Campillo, M. (2022). Space-time monitoring of
- groundwater fluctuations with passive seismic interferometry. *Nature Communications*, *13*, 4643.
 https://doi.org/10.1038/s41467-022-32194-3
- 1021 Mikhailov, O. V., Haartsen, M. W., & Toksöz, M. N. (1997). Electroseismic investigation of the 1022 shallow subsurface: Field measurements and numerical modeling. *Geophysics*, 62, 97–105.
- 1023 https://doi.org/10.1190/1.1444150
- 1024 Monachesi, L. B., Zyserman, F. I., & Jouniaux, L. (2018). An analytical solution to assess the SH
- seismoelectric response of the vadose zone. *Geophysical Journal International*, 213(3), 1999–
- 1026 2019. https://doi.org/10.1093/gji/ggy101
- Mualem, Y. (1976). A new model for predicting the hydraulic conductivity of unsaturated porous
 media, *Water Resources Research*, *12*(3), 513–522. https://doi.org/10.1029/WR012i003p00513
- 1029 Niu, Q., & Zhang, C. (2019). Permeability prediction in rocksexperiencing mineral precipitation
- anddissolution: A numerical study. *Water Resources Research*, 55(4), 3107–3121.
 https://doi.org/10.1029/2018WR024174
- 1032 Pao, Y. H., Park, G. H. & Sobajic, D. J. (1994). Learning and generalization characteristics of the
- random vector functional-link net, *Neurocomputing*, 6(2), 163–180. https://doi.org/10.1016/0925-
- 1034 2312(94)90053-1

- 1035 Pride, S. (1994). Governing equations for the coupled electromagnetics and acoustics of porous
- 1036 media. *Physical Review B*, 50(21), 15678. https://doi.org/10.1103/PhysRevB.50.15678
- Pride, S. R., & Haartsen, M. W. (1996). Electroseismic wave properties. *The Journal of the Acoustical Society of America*, *100*, 1301–1315. https://doi.org/10.1121/1.416018
- Pride, S. R., & Garambois, S. (2002). The role of Biot slow waves in electroseismic wave
 phenomena. *The Journal of the Acoustical Society of America*, *111*, 697–
 706. https://doi.org/10.1121/1.1436066
- 1042 Ren, H., Huang, Q., & Chen, X. (2007). Numerical simulation of seismoelectromagnetic waves in
- 1043 layered porous media. In Paper Presented at Proceeding of the 8th China International Geo-
- 1044 Electromagnetic Workshop.
- 1045 Rabbel, W., Iwanowski Strahser, K., Strahser, M., Dzieran, L., & Thorwart, M. (2020).
- 1046 Seismoelectric field measurements in unconsolidated sediments in comparison with other methods
- 1047 of near surface prospecting. In: Grobbe, N., Revil, A., Zhu, Z., & Slob, E. (Eds.), Seismoelectric
- 1048 exploration: Theory, experiments, and applications, American Geophysical Union Monograph
- 1049 Vol. 252, John Wiley & Sons, p. 347-363.
- 1050 Ren, H., Huang, Q. & Chen, X. (2010). A new numerical technique for simulating the coupled
- seismic and electromagnetic waves in layered porous media, *Earthquake Science*, 23(2), 167–176.
- 1052 https://doi.org/10.1007/s11589-009-0071-9
- 1053 Ren, H., Huang, Q., & Chen, X. (2016a). Existence of evanescent electromagnetic waves resulting
- 1054 from seismoelectric conversion at a solid–porous interface. *Geophysical Journal* 1055 *International*, 204(1), 147-166. https://doi.org/10.1093/gji/ggv400
- 1056 Ren, H., Huang, Q., & Chen, X. (2016b). Numerical simulation of seismo-electromagnetic fields
- associated with a fault in a porous medium. *Geophysical Journal International*, 206, 205–220.
- 1058 https://doi.org/10.1093/gji/ggw144
- 1059 Ren, H., Huang, Q., & Chen, X. (2018). Quantitative understanding on the amplitude decay
- 1060 characteristic of the evanescent electromagnetic waves generated by seismoelectric
- 1061 conversion. Pure and Applied Geophysics, 175(8), 2853-2879. https://doi.org/10.1007/s00024-
- 1062 018-1823-z
- 1063 Revil, A., & Cerepi, A. (2004). Streaming potentials in two-phase flow conditions. *Geophysical*
- 1064 *Research Letters*, *31*(11). https://doi.org/10.1029/2004GL020140

- Revil, A., & Linde, N. (2006). Chemico-electromechanical coupling in microporous
 media. *Journal of Colloid and Interface Science*, 302(2), 682-694.
 https://doi.org/10.1016/j.jcis.2006.06.051
- 1068 Revil, A., Linde, N., Cerepi, A., Jougnot, D., Matthäi, S., & Finsterle, S. (2007). Electrokinetic
- 1069 coupling in unsaturated porous media. Journal of Colloid & Interface Science, 313(1), 315-327.
- 1070 https://doi.org/10.1016/j.jcis.2007.03.037
- Revil A., & Jougnot D. (2008). Diffusion of ions in unsaturated porous materials. *Journal of Colloid & Interface Science*, *319*(1), 226-235. https://doi.org/10.1016/j.jcis.2007.10.041
- 1073 Revil, A., Karaoulis, M., Johnson, T., & Kemna, A. (2012). Some low-frequency electrical
- 1074 methods for subsurface characterization and monitoring in hydrogeology. *Hydrogeology Journal*,
- 1075 20(4), 617–658. https://doi.org/10.1007/s10040-011-0819-x
- 1076 Revil, A. (2013). Effective conductivity and permittivity of unsaturated porous materials in the
 1077 frequency range 1 mHz–1GHz. *Water Resources Research*, 49(1), 306-327.
 1078 https://doi.org/10.1029/2012WR012700
- 1079 Revil, A., & Jardani, A. (2013). *The self-potential method: Theory and applications in*1080 *environmental geosciences*. Cambridge University Press.
- 1081 Revil, A., & Mahardika, H. (2013). Coupled hydromechanical and electromagnetic disturbances
 1082 in unsaturated porous materials. *Water Resources Research*, 49(2), 744-766.
 1083 https://doi.org/10.1002/wrcr.20092
- Revil, A., Jardani, A., Sava, P., & Haas, A. (2015). *The Seismoelectric Method: Theory and Applications*. John Wiley & Sons.
- Richards, L. A. (1931). Capillary conduction of liquids through porous media, *Physics*, *1*, 318 –
 333. https://doi.org/10.1063/1.1745010
- 1088 Rosas-Carbajal, M., Jougnot, D., Rubino, J. G, Monachesi, L., Linde, N., & Holliger, K. (2020).
- 1089 Seismoelectric signals produced by mesoscopic heterogeneities: spectroscopic analysis of
- 1090 fractured media. In: Grobbe, N., Revil, A., Zhu, Z., & Slob, E. (Eds.), Seismoelectric exploration:
- 1091 Theory, experiments, and applications, American Geophysical Union Monograph Vol. 252, John
- 1092 Wiley & Sons, p. 269-287.
- 1093 Rutherford, S. R., & Williams, R. H. (1989). Amplitude-versus-offset variations in gas 1094 sands. *Geophysics*, 54(6), 680-688. https://doi.org/10.1190/1.1442696

- 1095 Solazzi, S. G., Rubino, J. G., Jougnot, D., & Holliger, K. (2020). Dynamic permeability functions
- 1096 for partially saturated porous media. Geophysical Journal International, 221(2), 1182-1189.
- 1097 https://doi.org/10.1093/gji/ggaa068
- Sen, P.N., & Goode, P. A. (1992). Influence of temperature on electrical conductivity on shaly 1098 sands. Geophysics, 57, 89-96. https://doi.org/10.1190/1.1443191
- 1099
- Solazzi, S. G., Bodet, L., Holliger, K., & Jougnot, D. (2021). Surface-wave dispersion in partially 1100
- 1101 saturated soils: The role of capillary forces. Journal of Geophysical Research: Solid Earth, 126,
- e2021JB022074. https://doi.org/10.1029/2021JB022074 1102
- Solazzi, S.G., Thanh. L.D., Hu, K., & Jougnot, D. (2022). Modeling the frequency-dependent 1103
- effective excess charge density in partially saturated porous media. Journal of Geophysical 1104
- Research: Solid Earth, 127(11): e2022JB024994. https://doi.org/10.1029/2022JB024994 1105
- Soldi, M., Jougnot, D., & Guarracino, L. (2019). An analytical effective excess charge density 1106
- model to predict the streaming potential generated by unsaturated flow. Geophysical Journal 1107 International, 216(1), 380-394. https://doi.org/10.1093/gji/ggy391 1108
- Soldi, M., Guarracino, L., & Jougnot, D. (2020). An effective excess charge model to describe 1109
- 1110 hysteresis effects on streaming potential. Journal of Hydrology, 588, 124949. https://doi.org/10.1016/j.jhydrol.2020.124949 1111
- 1112 Thanh, L. D., Jougnot, D., Solazzi, S. G., Van Nghia, N., & Van Do, P. (2022). Dynamic streaming
- potential coupling coefficient in porous media with different pore size distributions. *Geophysical* 1113
- 1114 Journal International, 229(1), 720-735, https://doi.org/10.1093/gji/ggab491
- Thompson, A. H., & Gist, G. A. (1993). Geophysical applications of electrokinetic conversion. 1115
- 1116 The Leading Edge, 12, 1169–1173. https://doi.org/10.1190/1.1436931
- van Genuchten, M. T. (1980). A closed-form equation for predicting the hydraulic conductivity of 1117
- 1118 unsaturated soils. Soil Science Society of America Journal, 44(5), 892-898. 1119 https://doi.org/10.2136/sssaj1980.03615995004400050002x
- Wang, J., Zhu, Z., Gao, Y., Morgan, F. D., & Hu, H. (2020). Measurements of the seismoelectric 1120
- responses in a synthetic porous rock. Geophysical Journal International, 222(1), 436-448. 1121
- https://doi.org/10.1093/gji/ggaa174 1122
- 1123 Warden, S., Garambois, S., Jouniaux, L., Brito, D., Sailhac, P., & Bordes, C. (2013). Seismoelectric modelling 1124 wave propagation numerical in partially saturated

- 1125 materials. *Geophysical Journal International*, 194(3), 1498-1513.
- 1126 https://doi.org/10.1093/gji/ggt198
- 1127 Wu, S., Huang, Q., & Zhao, L. (2021). Conventional neural network inversion of airborne transient
- 1128
 electromagnetic
 data.
 Geophysical
 Prospecting,
 69(8-9),
 1761-1772.

 1129
 https://doi.org/10.1111/1365-2478.13136
- 1130 Yang, X. H., Han, P., Yang, Z., Miao, M., Sun, Y. C., & Chen, X. (2022). Broad learning
- 1131 framework for search space design in Rayleigh wave inversion. *IEEE Transactions on Geoscience*
- and Remote Sensing, 60, 1-17. Article no. 4512617. https://doi.org/10.1109/TGRS.2022.3208616
- 1133 Yang, X. H., Han, P., Yang, Z., & Chen, X. (2023). Two-stage broad learning inversion framework
- 1134 for shear-wave velocity estimation. *Geophysics*, 88, WA219-WA237.
 1135 https://doi.org/10.1190/geo2022-0060.1
- 1136 Yuan, S., Ren, H., Huang, Q., Zheng, X.-Z., & Chen, X. (2021). Refining higher modes of
- 1137 Rayleigh waves using seismoelectric signals excited by a weight-drop source: study from 1138 numerical simulation aspect. *Journal of Geophysical Research: Solid Earth, 126*(5),
- 1139 e2020JB021336. https://doi.org/10.1029/2020JB021336
- 1140 Zhang, H.-M., Chen, X.-F., & Chang, S. (2001). Peak-trough averaging method and its
- applications to calculation of synthetic seismograms with shallow focuses. Chinese Journal of

1142 Geophysics, 44(6), 791–799. https://doi.org/10.1002/cjg2.201

- 1143 Zhang, H.-M., Chen, X.-F., & Chang, S. (2003). An efficient numerical method for computing
- synthetic seismograms for a layered half-space with sources and receivers at close or same depths.
- 1145 In Seismic motion, lithospheric structures, earthquake and volcanic sources: The Keiiti Aki
- 1146 volume (pp. 467–486). Springer. https://doi.org/10.1007/PL00012546
- 1147 Zheng, X.-Z., Ren, H., Butler, K. E., Zhang, H., Sun, Y.-C., Zhang, W., et al. (2021).
- 1148 Seismoelectric and electroseismic modeling in stratified porous media with a shallow or ground
- 1149 surface source. Journal of Geophysical Research: Solid Earth, 126(9), e2021JB021950.
- 1150 https://doi.org/10.1029/2021JB021950
- 1151 Zhu, Z., & Toksöz, M. N. (2013). Experimental measurements of the streaming potential and
- 1152 seismoelectric conversion in Berea sandstone. Geophysical Prospecting, 61(3), 688-700.
- 1153 https://doi.org/10.1111/j.1365-2478.2012.01110.x

- 1154 Zyserman, F. I., Monachesi, L. B., & Jouniaux, L. (2017). Dependence of shear wave
- seismoelectrics on soil textures: a numerical study in the vadose zone. Geophysical Journal
- 1156 International, 208(2), 918-935. https://doi.org/10.1093/gji/ggw431