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# New acetylene line list near 3.8- $\mu \mathrm{m}$ - Part II 

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#### Abstract

The investigation of the $3.8 \mu \mathrm{~m}$ spectral region of acetylene ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ main isotopologue has been completed from spectra recorded with Fourier Transform Spectrometer (FTS) using high optical path length. This work is the second of a series dedicated to the $\Delta P=4$ spectral region. In the first paper of the series (JQSRT 2023;295:108413) 14 bands of ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ were studied in the beginning of the region. In the present work the whole $\Delta P=4$ spectral region was investigated. 52 newly observed vibrational bands have been studied as well as the 5 intense bands present in the HITRAN and GEISA databases. The band centers and the upper level spectroscopic constants were retrieved for all bands. The comparison with the data from HITRAN and GEISA databases revealed important deviations from the measurements due to wrong extrapolations (especially line positions). The effective dipole moment operator parameters describing intensities of all transitions observed in the $\Delta P=4$ spectra region were refined. A complete list of calculated line parameters for 7515 transitions has been generated for 71 bands between $2389 \mathrm{~cm}^{-1}$ and $2890 \mathrm{~cm}^{-1}$.


## 1. Introduction

This paper is the second of the series dedicated to the investigation of the spectral region near $3.8-\mu \mathrm{m}$ under large experimental absorption paths conditions. In the first work [1] of the series 14 bands of ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ were studied in the beginning of the $\Delta P=4$ spectral region whereas the whole region could not be analyzed due to the edge of the optical filter used in Ref. [1]. $P$ is the polyad number defined as $P=5 V_{1}+3 V_{2}+5 V_{3}+V_{4}+V_{5}$, where $V_{i}$ are the vibrational normal mode principal quantum numbers, with $i=1-5$. In the present work no optical filter was used allowing to investigate 57 other bands including the 5 intense bands present in databases.

The $\Delta P=4$ spectral region was previously studied in Ref. [2]. In result of that investigation 421 lines of the 5 bands were posted in spectroscopic databases. In Ref. [3] the set of 8 effective dipole moment parameters for this region was reported. In our previous work [1] the ASD-1000 database [4] based on the effective operators proposed in Ref. [5] has been used to assign 824 transitions of 14 bands never measured before in the low part of the region. Note that for some of the newly observed bands predicted line positions issued from Ref. [4] appeared shifted from the observations with deviations up to $0.1 \mathrm{~cm}^{-1}$. The new observations [1] allowed retrieving the set of the spectroscopic constants describing upper levels of the corresponding bands. For several bands the comparisons between measured and calculated line positions showed deviations for high rotational quantum number $J$ appearing due to resonance interactions between levels. The line positions in the final line list were calculated using spectroscopic constants. For the line intensities no attempt has been done to use Herman-Wallis factors to reproduce the rotational dependences of the observed transition dipole moments squared since such procedure fails in many cases (see Ref. [1]). On the contrary the predicted using effective dipole moment (EDM) parameters line intensities, where mixing of the states is taken into account, reproduced very well the rotational dependence of the observed transition dipole moments squared. As a consequence only the calculations with refined EDM parameters were used to generate line intensities in the generated line list of Ref. [1].

The present paper is devoted to the analysis of spectra recorded without optical filter in order to compile a full ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ line list giving the best agreement between the simulating spectra and the observations in the whole $\Delta P=4$ spectral region. The experimental setup and conditions are presented in Section 2. A brief description of the measurements is given in Section 3. The band-by-band rotational analysis leading to spectroscopic parameters is presented in Section 4. The measurements are compared to the predictions of the EH and calculations using spectroscopic parameters in the same section. The new set of the EDM parameters is presented
in the Section 5. The details of the final line list construction for ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ in the $\Delta P=4$ spectral region are given in Section 6.

## 2. Experimental procedure

Three Fourier transform spectra were recorded using Bruker IFS-125HR spectrometer connected to the White type cell with the base length of 27.795 m built in the V.E. Zuev Institute of Atmospheric Optics SB RAS. The spectra were recorded with a pressure of pure acetylene equal to 0.997 matm and absorption path lengths of $168.51,613.23$ and 1057.95 m . The temperature of the gas in the cell measured by platinum probe was equal to 301.4-301.6 K depending on spectrum. The spectral resolution was equal to $0.005 \mathrm{~cm}^{-1}$, corresponding to a maximum optical path difference of 180 cm . The instrument was fitted with a tungsten source, a 1.15 mm entrance aperture (diameter) together with a collimator focal length of 418 mm , a KBr beam splitter and an MCT detector (no non-linear correction from MCT detector was performed). The acetylene commercial sample was used without purification $\left(95 \%\right.$ of $\mathrm{C}_{2} \mathrm{H}_{2}$ with traces of $\mathrm{CH}_{4}(\sim 0.1 \%)$ and $\mathrm{PH}_{3}(\sim 0.1 \%), \mathrm{CO}_{2}(\sim 0.04 \%)$ and acetone as impurities) and is different to the one used in Ref. [1]. No artificial optical weighting has been performed (boxcar function was selected). A Mertz procedure was used to correct phase of average interferogram. The $R(64)$ to $R(78)$ transitions of the $v_{3}$ band of carbon dioxide (presents in the cell as impurity) have been used for the wavenumber calibration (via HITRAN wavenumbers as etalons). The RMS deviation of the wavenumber calibration is equal to $0.1 \times 10^{-3} \mathrm{~cm}^{-1}$. Note that an error in the calibration of spectra from Ref. [1] led to systematic deviation of $0.8 \times 10^{-3}$ $\mathrm{cm}^{-1}$ in the positions retrieved in Ref. [1]. This mistake has been fixed in the present work so that line positions measured in the whole $\Delta P=4$ spectral regions are consistent with accuracy better than $10^{-3} \mathrm{~cm}^{-1}$.

## 3. Line parameters measurements

As in our previous work the ASD-1000 line list [4] allowed assigning the majority of the transitions observed in our spectra. However, systematical deviations were observed so the predictions were rescaled in order to be used as initial guess. The multispectrum fitting procedure [6] has then been applied to the three experimental spectra recorded in the present work in order to retrieve line positions and intensities fixing the self-widths to the values of the HITRAN database [7]. The Voigt profile has been used together with the calculated instrument line shape (ILS) describing the effects of the limited optical path difference and of the size of the beam inside the interferometer (see Ref. [8]). The assignment allowed performing the
conversion of the intensities to the standard temperature 296K using lower state energies from ASD-1000 line list [4] and partition function from Ref. [9]. An example of the multispectrum fitting performed in the present work is given in Fig. 1 between 2688.446 and $2688.632 \mathrm{~cm}^{-1}$.


Fig. 1. Observed (black) and calculated (red) spectra (together with residuals obs-calc) between 2688.446 and $2688.632 \mathrm{~cm}^{-1}$. The fitted line noted with a star is a ${ }^{12} \mathrm{C}^{13} \mathrm{H}_{2}$ transition, all others transitions are from ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ and are studied for the first time.

The present work includes measurements for 71 bands, 52 among them were studied for the first time. For the 5 bands studied in Ref. [2] and present in HITRAN [7] or GEISA [10] databases the new measurements allowed to reach higher $J$ values. Note that in Ref. [2] and in HITRAN and GEISA databases, the upper state of the $\left(v_{2}+\left(v_{4}+v_{5}\right)^{0}-v_{4}{ }^{1}\right)$ band is wrongly written with $\ell_{4}=\ell_{5}=0$ instead of $\ell_{4}=-\ell_{5}=1$ (namely $0101100 \_0001010$ instead of 0101 11-1_000 1010 ). Moreover, the upper states of the $\left(v_{3}-v_{4}{ }^{1}\right)$ and $\left(v_{2}+\left(v_{4}+v_{5}\right)^{0}-v_{4}{ }^{1}\right)$ bands have similar contributions of the base functions making thus the vibrational assignment ambiguous. In the present work, we used the vibrational notation adopted in ASD-1000 [4] where the notation for these two bands is reversed comparing to the notation given in the HITRAN and GEISA databases and in Ref. [2]. The 14 bands observed in Ref. [1] have been reinvestigated only in term of line positions in order to improve the rotational analysis of the energy levels. The accuracy of measurements is estimated to be better than $0.001 \mathrm{~cm}^{-1}$ for line positions and between 5 and $10 \%$ for most of the line intensities. As explained in Ref. [1], for some bands the largest contributions of the harmonic oscillators basis states to the predicted upper or lower states, considering as function of $J$, intersect, making ambiguous the vibrational assignment after crossings. In such cases we use the same vibrational labeling for a series of transitions, keeping the regularity of the rotational transitions inside the bands (see section 5 of

Ref. [11] for the details). The whole set of measurements performed in this work is given as Supplementary Material I, containing 5092 line positions and 2674 line intensities (note that for the 14 bands studied in Ref. [1] only line positions have been reinvestigated in the present work). For blended, saturated or very weak transitions the line intensity measurements are not accurate and have been ignored whereas the line positions have been conserved. Note that the accuracy of line positions for the saturated or non saturated transitions is similar since a profile is fitted.

## 4. Line positions: band-by-band rotational analysis

In order to accurately reproduce and interpolate measurements the measured line positions were fitted using the following equation for the energies of the levels written up to eighth order of perturbation theory:

$$
\begin{equation*}
T(v, J, e / f)=G_{e / f}+B_{e l f} J(J+1)-D_{e f f}[J(J+1)]^{2}+H_{e f f}[J(J+1)]^{3}+L_{e f f}[J(J+1)]^{4}+M_{e f f}[J(J+1)]^{5} . \tag{1}
\end{equation*}
$$

Although the energy of an unperturbed state is usually described with a fewer amount of spectroscopic parameters, in order to reach satisfactory residuals for the perturbed state it is required more parameters. The spectroscopic constants of the lower vibrational levels have been fixed to the values given in Refs. [12,13] (except for the $V_{2}=1$ level fitted from Ref. [14], see Table 1). The different sets of the spectroscopic constants were fitted for $e$ and $f$ sublevels assuming different perturbing mechanism for them. The defined spectroscopic constants allowed reproduce the most of the observed line positions with RMS within $0.001-0.002 \mathrm{~cm}^{-1}$ depending on the band. For some bands the oscillations in obs-calc residuals are observed. The description of such perturbed bands by spectroscopic constants is then valid only up to a certain $J$ value starting from which the deviations dramatically increase. Therefore some line positions measured for high $J$ values were excluded from the fit. The spectroscopic constants retrieved in this work are given in the Table 1.

Table 1. Spectroscopic parameters (in $\mathrm{cm}^{-1}$ ) of the rovibrational bands of acetylene assigned in the FTS spectra in the $\Delta P=4$ region. The bands are listed according to the increasing values of the upper state energy.

| $V_{1} V_{2} V_{3} V_{4} V_{5} \ell_{4} \ell_{5} \varepsilon^{a}$ | $G_{e / f}$ | $B_{e / f}$ | $D_{e / f} \times 10^{6}$ | $H_{\text {eff }} \times 10^{9}$ | $L_{\text {elf }} \times 10^{11}$ | $M_{\text {eff }} \times 10^{14}$ | $n_{\text {fit }} / N_{\text {tot }}{ }^{\text {b }}$ | $\Delta G^{c}$ | Bands ${ }^{\text {d }}$ | $R m s{ }^{e}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Lower vib | ational levels | 12,13] |  |  |  |  |  |  |  |  |
| 0000000 e | 0.0 | 1.1766462 | 1.6270 | 0.0016 |  |  |  |  |  |  |
| 000101 Of | 611.693755 | 1.18055377 | 1.67973 | 0.00187 |  |  |  |  |  |  |
| 0001010 e | 611.693759 | 1.17532307 | 1.6405 | 0.00177 |  |  |  |  |  |  |
| 000010 1e | 729.15410 | 1.1764413 | 1.6326 | 0.0017 |  |  |  |  |  |  |
| 000010 1f | 729.15410 | 1.1811398 | 1.6714 | 0.0018 |  |  |  |  |  |  |
| 00011 1-1e | 1328.0722 | 1.180508 | 3.595 | 0.276 |  |  |  |  |  |  |
| 000202 Of | 1228.7997 | 1.179109 | 1.692 |  |  |  |  |  |  |  |
| 0002020 e | 1228.8011 | 1.17908 | 19.0 | 2.45 |  |  |  |  |  |  |
| 0002000 e | 1230.3894 | 1.17937 | -15.8 | -2.46 |  |  |  |  |  |  |
| 00011 1-1f | 1340.5507 | 1.1800836 | 1.715 |  |  |  |  |  |  |  |
| 0001111 f | 1342.8023 | 1.179838 | 1.647 |  |  |  |  |  |  |  |
| 0001111 e | 1342.8034 | 1.179804 | -0.226 | -0.278 |  |  |  |  |  |  |
| 0000200 e | 1449.1107 | 1.181234 | 4.415 | 0.652 |  |  |  |  |  |  |
| 0000202 f | 1458.2936 | 1.180757 | 1.669 |  |  |  |  |  |  |  |
| 000020 2e | 1458.2944 | 1.180714 | -1.052 | -0.643 |  |  |  |  |  |  |
| 000303 0e | 1851.3699 | 1.180358 | 10.15 |  |  |  |  |  |  |  |
| 000303 Of | 1851.3749 | 1.18006 | 6.33 | 3.9 |  |  |  |  |  |  |
| 000301 Of | 1854.5970 | 1.18583 | -3.8 | -6.1 |  |  |  |  |  |  |
| 0003010 e | 1854.5978 | 1.17533 | -6.2 |  |  |  |  |  |  |  |
| 00021 2-1f | 1939.9987 | 1.185710 | 3.065 |  |  |  |  |  |  |  |
| 00021 2-1e | 1939.9999 | 1.177984 | 2.867 | 0.165 |  |  |  |  |  |  |
| 000210 1e | 1959.6916 | 1.182691 | 3.22 |  |  |  |  |  |  |  |
| 0002101 f | 1959.6921 | 1.179939 | 3.23 | 0.6 |  |  |  |  |  |  |
| 0002121 f | 1961.9321 | 1.180731 | -1.03 | -0.515 |  |  |  |  |  |  |
| 0002121 e | 1961.9332 | 1.18069 | -1.31 | -1 |  |  |  |  |  |  |
| $0100000 \mathrm{e}^{\text {f }}$ | 1974.31610(2) | 1.1704678(2) | 1.6321(6) | 0.0033(4) |  |  |  |  |  |  |
| 0001212 e | 2074.1790 | 1.181561 | 1.056 |  |  |  |  |  |  |  |
| 0001212 f | 2074.1807 | 1.181533 | 0.95 | 0.17 |  |  |  |  |  |  |
| 000121 Of | 2047.8761 | 1.187537 | 2.592 | -0.148 |  |  |  |  |  |  |
| 0001210 e | 2047.8766 | 1.177928 | 2.457 | 0.113 |  |  |  |  |  |  |
| 00012-1 2f | 2065.7923 | 1.184239 | 1.672 |  |  |  |  |  |  |  |
| 00012-1 2e | 2065.7929 | 1.180042 | 1.618 |  |  |  |  |  |  |  |
| 000030 1f | 2169.1559 | 1.188211 | 2.782 | -0.189 |  |  |  |  |  |  |
| 000030 1e | 2169.1575 | 1.178631 | 2.550 | 0.165 |  |  |  |  |  |  |
| 0000303 e | 2187.4505 | 1.182540 | 0.86 |  |  |  |  |  |  |  |
| 0000303 f | 2187.4521 | 1.182494 | 0.56 |  |  |  |  |  |  |  |

## Upper vibrational levels (this work)

 $P=4$| $000313-1$ |
| ---: |
| $000311-$ |
| 000311 |
| 01001 |
| 01001 |
| 00013 |

0102020
000
00041 2-1e
00032 3-2f
00032 3-2e
000323 of
000323 0e
00032-1 2
00032-1 2 f
0010000 e
01011 1-1e
01011 1-1f
0101111
0101111
1000000
0100200 e
010020 2f
010020 2e

| $2556.7939(7)$ | $1.18318(1)$ | $18.34(8)$ |  |
| :---: | :---: | :---: | :---: |
|  | $2560.5946(4)$ | $1.183264(9)$ | $-12.66(5)$ |
| $1.056 .046(4)$ | $1.18166(3)$ | $5.16(7)$ |  |
| 1 e | 2585 |  |  |
| 1 e | $2701.9098(2)$ | $1.1702027(7)$ | $1.6306(4)$ |
| 01 f | $2701.9109(9)$ | $1.174895(2)$ | $1.667(1)$ |
| $1-1 \mathrm{e}$ | $2757.7974(6)$ | $1.18532(1)$ | $9.06(8)$ |


|  | 20.1 |
| :--- | :--- |
|  | -19.1 |
|  | $2.16(7)$ |
| $.06(8)$ | 2.3 |

$-1.32(2) \quad 0.347(7)$
0.347(7) 46/49
$46 / 49$
$61 / 61$
$8 / 8$
$77 / 77$
$27 / 2$
$26 / 26$
$2556.7939(7)$
$2560.5946(4)$
$2585.046(4)$
$2701.9098(2)$
$2701.9109(9)$
$2757.7974(6)$
$\left(3 v_{4}+v_{5}\right)^{2}$ II
$\left(3 v_{4}+v_{5}\right)^{0}$
00031 30003111 010010 1e 010010 If $P=5$

0102020
of

|  | 00042 2-2e | 3883.0585(6) | 1.18754(1) | -10.44(9) | -10.9(1) | 26/28 | 2554.9863(6) | $\left(4 v_{4}+2 v_{5}\right)^{0} \mathrm{II}-\left(v_{4}+v_{5}\right)^{0}$ | 1.5 | P |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 001101 of | 3897.1612(2) | 1.176382(1) | 2.505(1) |  | 13/27 | 2666.7719(2) | $v_{3}+v_{4}{ }^{1}-2 v_{4}{ }^{0}$ | 1.0 | P |
|  |  |  |  |  |  | 70/78 | 2668.3601(2) | $v_{3}+v_{4}{ }^{1}-2 v_{4}{ }^{2}$ | 1.1 | P |
|  | 001101 0e | 3897.1632(2) | 1.170674(2) | 2.466(4) |  | 29/41 | 2666.7739(2) | $v_{3}+v_{4}{ }^{1}-2 v_{4}{ }^{0}$ | 1.0 | P |
|  |  |  |  |  |  | 49/94 | 2668.3621(2) | $v_{3}+v_{4}{ }^{1}-2 v_{4}{ }^{2}$ | 1.1 | P |
|  | 00042 2-2f | 3906.2098(9) | 1.18477(3) | 5.3(1) |  | 4/14 | 2565.6591(9) | $\left(4 v_{4}+2 v_{5}\right)^{0}$ II - $\left(v_{4}+v_{5}\right)^{0}$ | 4.2 | P |
| N | 010210 1f | 3908.1358(8) | 1.17381(2) | 3.41(6) |  | 12/22 | 2677.7465(8) | $v_{2}+\left(2 v_{4}+v_{5}\right)^{1} \mathrm{I}-2 v_{4}{ }^{0}$ | 1.2 | P |
| N | 010210 1e | 3908.1363(5) | 1.17602(1) | 3.25(4) |  | 23/29 | 2677.7470(5) | $v_{2}+\left(2 v_{4}+v_{5}\right)^{1} \mathrm{I}-2 v_{4}{ }^{0}$ | 0.6 | P |
| N | 010212 1f | 3910.1846(8) | 1.17435(2) | -1.43(6) |  | 2/14 | 2679.7953(8) | $v_{2}+\left(2 v_{4}+v_{5}\right)^{3}-2 v_{4}{ }^{0}$ | 0.4 | P |
|  |  |  |  |  |  | 15/15 | 2681.3834(8) | $v_{2}+\left(2 v_{4}+v_{5}\right)^{3}-2 v_{4}{ }^{2}$ | 0.5 |  |
| N | 0102121 e | 3910.1861(8) | 1.17430(2) | -1.92(7) | -1.7(1) | 5/8 | 2679.7968(8) | $v_{2}+\left(2 v_{4}+v_{5}\right)^{3}-2 v_{4}{ }^{0}$ | 0.5 | P |
|  |  |  |  |  |  | 17/17 | 2681.3849(8) | $v_{2}+\left(2 v_{4}+v_{5}\right)^{3}-2 v_{4}{ }^{2}$ | 0.7 |  |
|  | 1001010 e | 3968.8832(2) | 1.1686998(8) | 1.6387(8) |  | 77/83 | 2626.0797(2) | $v_{1}+v_{4}^{1}-\left(v_{4}+v_{5}\right)^{2}$ | 0.6 |  |
|  |  |  |  |  |  | 84/90 | $2640.8110(2)$ | $v_{1}+v_{4}{ }^{1}-\left(v_{4}+v_{5}\right)^{0}$ | 1.0 |  |
|  | 100101 of | 3968.8836(2) | 1.1740327(8) | 1.6891(8) |  | 87/90 | 2626.0801(2) | $v_{1}+v_{4}{ }^{1}-\left(v_{4}+v_{5}\right)^{2}$ | 0.9 |  |
|  |  |  |  |  |  | 76/80 | 2628.3329(2) | $v_{1}+v_{4}{ }^{1}-\left(v_{4}+v_{5}\right)^{0}$ | 0.9 |  |
|  | 010121 of | 4001.2594(2) | 1.178727(3) | 2.741(7) | 0.125(5) | 44/44 | 2658.4559(2) | $v_{2}+\left(v_{4}+2 v_{5}\right)^{1}$ II $-\left(v_{4}+v_{5}\right)^{2}$ | 1.0 |  |
|  |  |  |  |  |  | 58/58 | 2660.7087(2) | $v_{2}+\left(v_{4}+2 v_{5}\right)^{1}$ II $-\left(v_{4}+v_{5}\right)^{0}$ | 0.8 |  |
|  | 010121 0e | 4001.2600(3) | 1.171278(3) | $2.096(8)$ | 0.067(5) | 37/37 | 2658.4565(3) | $v_{2}+\left(v_{4}+2 v_{5}\right)^{1}$ II $-\left(v_{4}+v_{5}\right)^{2}$ | 0.8 |  |
|  |  |  |  |  |  | 32/32 | 2673.1878(3) | $v_{2}+\left(v_{4}+2 v_{5}\right)^{1}$ II $-\left(v_{4}+v_{5}\right)^{0}$ | 0.4 |  |
|  | 001010 1e | 4015.5364(2) | 1.170794(3) | 2.066(7) | 0.089(5) | 66/66 | 2672.7330(2) | $v_{3}+v_{5}^{1}-\left(v_{4}+v_{5}\right)^{2}$ | 0.6 |  |
|  |  |  |  |  |  | 77/77 | 2687.4642(2) | $v_{3}+v_{5}{ }^{1}-\left(v_{4}+v_{5}\right)^{0}$ | 0.6 |  |
|  | 001010 1f | 4015.5365(2) | 1.177594(2) | 1.493(6) | -0.326(4) | 72/72 | 2672.7331(2) | $v_{3}+v_{5}{ }^{1}-\left(v_{4}+v_{5}\right)^{2}$ | 0.6 |  |
|  |  |  |  |  |  | 70/70 | 2674.9858(2) | $v_{3}+v_{5}{ }^{1}-\left(v_{4}+v_{5}\right)^{0}$ | 0.6 |  |
| N | 01012-1 2e | 4024.3843(3) | 1.177802(3) | 1.649 (4) |  | 37/37 | 2696.3121(3) | $v_{2}+\left(v_{4}+2 v_{5}\right)^{1} \mathrm{I}-\left(v_{4}+v_{5}\right)^{0}$ | 0.5 |  |
| N | 01012-1 2 f | 4024.3848(3) | $1.173597(2)$ | 1.639(3) |  | 52/52 | $2696.3126(3)$ | $v_{2}+\left(v_{4}+2 v_{5}\right)^{1} I-\left(v_{4}+v_{5}\right)^{0}$ | 0.6 |  |
| N | 01012 1 2f | 4032.7087(6) | 1.175152(8) | 0.87(3) | 0.17(3) | 40/40 | 2689.9053(6) | $v_{2}+\left(v_{4}+2 v_{5}\right)^{3}-\left(v_{4}+v_{5}\right)^{2}$ | 0.7 |  |
| N | 010121 2e | 4032.7089(6) | 1.175152(8) | 0.88(2) | -0.17(2) | 38/38 | 2689.9055(6) | $v_{2}+\left(v_{4}+2 v_{5}\right)^{3}-\left(v_{4}+v_{5}\right)^{2}$ | 0.5 |  |
|  | 100010 1e | 4091.1720(2) | 1.169604(1) | 1.621(1) |  | 21/21 | 2862.3708(2) | $v_{1}+v_{5}^{1}-2 v_{4}{ }^{2}$ | 1.0 |  |
|  |  |  |  |  |  | 35/35 | 2642.0612(2) | $v_{1}+v_{5}{ }^{1}-2 v_{5}{ }^{0}$ | 0.6 |  |
|  |  |  |  |  |  | 68/71 | 2632.8776(2) | $v_{1}+v_{5}{ }^{1}-2 v_{5}{ }^{2}$ | 0.9 |  |
|  | 100010 1f | 4091.1722(2) | 1.174396(1) | 1.669(1) |  | 20/20 | 2862.3710(2) | $v_{1}+v_{5}{ }^{1}-2 v_{4}{ }^{2}$ | 1.0 |  |
|  |  |  |  |  |  | 25/26 | 2642.0614(2) | $v_{1}+v_{5}{ }^{1}-2 v_{5}{ }^{0}$ | 0.9 |  |
|  |  |  |  |  |  | 78/86 | 2632.8778(2) | $v_{1}+v_{5}{ }^{1}-2 v_{5}{ }^{2}$ | 0.8 |  |
|  | 010030 1e | 4138.8770(3) | 1.172269(4) | 2.60(1) | 0.21(1) | 39/39 | 2689.7663(3) | $v_{2}+3 v_{5}^{1}-2 v_{5}{ }^{0}$ | 0.6 |  |
|  |  |  |  |  |  | 43/43 | $2680.5826(3)$ | $v_{2}+3 v_{5}{ }^{1}-2 v_{5}{ }^{2}$ | 0.8 |  |
|  | 010030 1f | 4138.8772(4) | $1.181742(5)$ | 2.69(2) | -0.27(2) | 12/12 | $2689.7665(4)$ | $v_{2}+3 v_{5}{ }^{1}-2 v_{5}{ }^{0}$ | 0.6 |  |
|  |  |  |  |  |  | 47/47 | 2680.5828(4) | $v_{2}+3 v_{5}{ }^{1}-2 v_{5}{ }^{2}$ | 0.8 |  |
| N | 0100303 e | 4156.8634(5) | 1.176154(6) | 0.76(2) | -0.20(2) | 42/42 | 2698.5690(5) | $v_{2}+3 v_{5}^{3}-2 v_{5}{ }^{2}$ | 0.7 |  |
| N | 0100303 f | 4156.8638(6) | $1.176148(7)$ | 0.74(2) | 0.27(2) | 38/39 | 2698.5694(6) | $v_{2}+3 v_{5}{ }^{3}-2 v_{5}{ }^{2}$ | 0.4 |  |

$P=7$


| $11 / 23$ | $2631.5191(4)$ |
| :---: | :---: |
| $35 / 39$ | $2634.7469(4)$ |
| $11 / 24$ | $2631.5214(8)$ |
| $20 / 39$ | $2634.7492(8)$ |
| $35 / 55$ | $2634.2406(5)$ |
| $22 / 25$ | $2649.9387(6)$ |
| $28 / 49$ | $2653.1666(6)$ |
| $21 / 29$ | $2649.9411(5)$ |
| $32 / 45$ | $2653.1632(5)$ |
| $28 / 53$ | $2653.4145(5)$ |
| $24 / 39$ | $2609.7742(5)$ |
| $30 / 47$ | $2629.4660(5)$ |
| $3 / 7$ | $2611.0008(5)$ |
| $23 / 38$ | $2608.7593(5)$ |
| $18 / 25$ | $2630.6926(5)$ |
| $6 / 7$ | $2611.0037(3)$ |
| $41 / 41$ | $2608.7622(3)$ |
| $40 / 40$ | $2630.6955(3)$ |
| $6 / 11$ | $2630.3893(8)$ |
| $13 / 37$ | $2640.0817(7)$ |
| $6 / 10$ | $2643.5386(6)$ |
| $2 / 4$ | $2641.2982(6)$ |
| $4 / 13$ | $2643.599(2)$ |
| $2 / 4$ | $2641.358(2)$ |
| $39 / 39$ | $2669.3394(5)$ |
| $36 / 36$ | $2658.2337(3)$ |
| $26 / 26$ | $2677.9271(3)$ |
| $26 / 26$ | $2660.3628(4)$ |
| $22 / 22$ | $2658.1213(4)$ |
| $26 / 26$ | $2660.3641(5)$ |
| $24 / 24$ | $2658.1226(5)$ |
| $3 / 3$ | $2685.472(1)$ |
| $3 / 3$ | $2685.478(2)$ |
| $55 / 60$ | $2625.7542(3)$ |
| $24 / 25$ | $2639.4852(3)$ |
| $7 / 7$ | $2621.5678(3)$ |
| $40 / 47$ | $2613.1826(3)$ |
| $24 / 24$ | $2639.4865(2)$ |
|  |  |
| 26 |  |


| $\mathrm{v}_{2}+\left(3 v_{4}+v_{5}\right)^{2} \mathrm{II}-3 \mathrm{v}_{4}{ }^{1}$ | 1.3 |
| :---: | :---: |
| $v_{2}+\left(3 v_{4}+v_{5}\right)^{2} \mathrm{II}-3 v_{4}{ }^{3}$ | 1.2 |
| $v_{2}+\left(3 v_{4}+v_{5}\right)^{2} \mathrm{II}-3 v_{4}{ }^{1}$ | 1.6 |
| $v_{2}+\left(3 v_{4}+v_{5}\right)^{2} \mathrm{II}-3 v_{4}{ }^{3}$ | 1.2 |
| $v_{2}+\left(3 v_{4}+v_{5}\right)^{0}-3 v_{4}{ }^{1}$ | 1.3 |
| $v_{3}+2 v_{4}{ }^{2}-3 v_{4}{ }^{1}$ | 1.1 |
| $v_{3}+2 v_{4}{ }^{2}-3 v_{4}{ }^{3}$ | 0.9 |
| $v_{3}+2 v_{4}{ }^{2}-3 v_{4}{ }^{1}$ | 1.0 |
| $v_{3}+2 v_{4}{ }^{2}-3 v_{4}{ }^{3}$ | 0.8 |
| $v_{3}+2 v_{4}{ }^{0}-3 v_{4}{ }^{1}$ | 0.9 |
| $v_{1}+2 v_{4}{ }^{0}-\left(2 v_{4}+v_{5}\right)^{1} \mathrm{I}$ | 2.0 |
| $v_{1}+2 v_{4}{ }^{0}-\left(2 v_{4}+v_{5}\right)^{1}$ II | 2.0 |
| $v_{1}+2 v_{4}{ }^{2}-\left(2 v_{4}+v_{5}\right)^{1} \mathrm{I}$ | 4.0 |
| $v_{1}+2 v_{4}^{2}-\left(2 v_{4}+v_{5}\right)^{3}$ | 1.0 |
| $v_{1}+2 v_{4}{ }^{2}-\left(2 v_{4}+v_{5}\right)^{1}$ II | 1.8 |
| $v_{1}+2 v_{4}{ }^{2}-\left(2 v_{4}+v_{5}\right)^{1} \mathrm{I}$ | 1.4 |
| $v_{1}+2 v_{4}^{2}-\left(2 v_{4}+v_{5}\right)^{3}$ | 0.7 |
| $v_{1}+2 v_{4}{ }^{2}-\left(2 v_{4}+v_{5}\right)^{1}$ II | 1.0 |
| $v_{2}+\left(2 v_{4}+2 v_{5}\right)^{0} \mathrm{II}-\left(2 v_{4}+v_{5}\right)^{1} \mathrm{I}$ | 2.2 |
| $v_{2}+\left(2 v_{4}+2 v_{5}\right)^{0} \mathrm{II}-\left(2 v_{4}+v_{5}\right)^{1} \mathrm{I}$ | 2.0 |
| $v_{2}+\left(2 v_{4}+2 v_{5}\right)^{2} \mathrm{II}-\left(2 v_{4}+v_{5}\right)^{1} \mathrm{I}$ | 2.3 |
| $v_{2}+\left(2 v_{4}+2 v_{5}\right)^{2}$ II $-\left(2 v_{4}+v_{5}\right)^{3}$ | 0.5 |
| $v_{2}+\left(2 v_{4}+2 v_{5}\right)^{2} \mathrm{II}-\left(2 v_{4}+v_{5}\right)^{1} \mathrm{I}$ | 0.7 |
| $v_{2}+\left(2 v_{4}+2 v_{5}\right)^{2}$ II $-\left(2 v_{4}+v_{5}\right)^{3}$ | 0.9 |
| $v_{3}+\left(v_{4}+v_{5}\right)^{0}-\left(2 v_{4}+v_{5}\right)^{1}$ II | 1.2 |
| $v_{3}+\left(v_{4}+v_{5}\right)^{0}-\left(2 v_{4}+v_{5}\right)^{1} \mathrm{I}$ | 1.1 |
| $v_{3}+\left(v_{4}+v_{5}\right)^{0}-\left(2 v_{4}+v_{5}\right)^{1}$ II | 1.7 |
| $v_{3}+\left(v_{4}+v_{5}\right)^{2}-\left(2 v_{4}+v_{5}\right)^{1} \mathrm{I}$ | 1.6 |
| $v_{3}+\left(v_{4}+v_{5}\right)^{2}-\left(2 v_{4}+v_{5}\right)^{3}$ | 0.9 |
| $v_{3}+\left(v_{4}+v_{5}\right)^{2}-\left(2 v_{4}+v_{5}\right)^{1} I$ | 1.6 |
| $v_{3}+\left(v_{4}+v_{5}\right)^{2}-\left(2 v_{4}+v_{5}\right)^{3}$ | 0.9 |
| $2 v_{2}+v_{5}{ }^{1}-v_{2}$ | 1.6 |
| $2 v_{2}+v_{5}{ }^{1}-v_{2}$ | 2.0 |
| $v_{1}+\left(v_{4}+v_{5}\right)^{0}-\left(v_{4}+2 v_{5}\right)^{1}$ II | 0.8 |
| $v_{1}+\left(v_{4}+v_{5}\right)^{2}-\left(v_{4}+2 v_{5}\right)^{1} \mathrm{II}$ | 1.5 |
| $v_{1}+\left(v_{4}+v_{5}\right)^{2}-\left(v_{4}+2 v_{5}\right)^{1} I$ | 1.6 |
| $v_{1}+\left(v_{4}+v_{5}\right)^{2}-\left(v_{4}+2 v_{5}\right)^{3}$ | 1.0 |
| $v_{1}+\left(v_{4}+v_{5}\right)^{2}-\left(v_{4}+2 v_{5}\right)^{1}$ II | 0.9 |


|  |  |  |  |  | 1.02(7) | 7/7 | 2621.5691(3) | $v_{1}+\left(v_{4}+v_{5}\right)^{2}-\left(v_{4}+2 v_{5}\right)^{1} \mathrm{I}$ | 1.6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 50/52 |  |  | 2613.1839(2) | $v_{1}+\left(v_{4}+v_{5}\right)^{2}-\left(v_{4}+2 v_{5}\right)^{3}$ | 1.2 |
|  | 10011 1-1f |  | 4688.8394(3) | 1.173380(2) |  | 1.627(3) | 54/55 | 2623.0456(3) | $v_{1}+\left(v_{4}+v_{5}\right)^{0}-\left(v_{4}+2 v_{5}\right)^{1} \mathrm{I}$ | 1.1 |
|  | 01013 1-1e | 4710.735(1) | 1.17764(2) | 6.59(5) |  | 6/6 | 2644.942(1) | $v_{2}+\left(v_{4}+3 v_{5}\right)^{0}-\left(v_{4}+2 v_{5}\right)^{1} \mathrm{I}$ | 0.5 |
|  | 001020 0e | 4727.0684(6) | 1.17627(1) | 5.44(6) |  | 18/20 | 2679.1918(6) | $v_{3}+2 v_{5}{ }^{0}-\left(v_{4}+2 v_{5}\right)^{1}$ II | 0.9 |
|  |  |  |  |  |  | 16/16 | 2661.2767(6) | $v_{3}+2 v_{5}{ }^{0}-\left(v_{4}+2 v_{5}\right)^{1} \mathrm{I}$ | 1.1 |
|  | 001020 2e | 4736.3131(4) | $1.176002(6)$ | -2.04(2) |  | 9/9 | 2688.4374(4) | $v_{3}+2 v_{5}{ }^{2}-\left(v_{4}+2 v_{5}\right)^{1}$ II | 1.6 |
|  |  |  |  |  |  | 9/9 | 2662.1341(4) | $v_{3}+2 v_{5}^{2}-\left(v_{4}+2 v_{5}\right)^{3}$ | 1.8 |
|  |  |  |  |  |  | 9/9 | 2670.5215(4) | $v_{3}+2 v_{5}^{2}-\left(v_{4}+2 v_{5}\right)^{1} \mathrm{I}$ | 1.4 |
|  | 0010202 f | 4736.3141(6) | $1.17598(1)$ | 1.89(5) |  | 9/9 | 2688.4384(6) | $v_{3}+2 v_{5}^{2}-\left(v_{4}+2 v_{5}\right)^{1}$ II | 1.4 |
|  |  |  |  |  |  | 7/7 | 2662.1351(6) | $v_{3}+2 v_{5}^{2}-\left(v_{4}+2 v_{5}\right)^{3}$ | 1.8 |
|  |  |  |  |  |  | $7 / 7$ | 2670.5225(6) | $v_{3}+2 v_{5}{ }^{2}-\left(v_{4}+2 v_{5}\right)^{1} \mathrm{I}$ | 1.8 |
| N |  |  |  |  |  | 2/3 | 2674.418(1) | $v_{2}+\left(v_{4}+3 v_{5}\right)^{0}-\left(v_{4}+2 v_{5}\right)^{1} \mathrm{I}$ | 0.0 |
|  | 1000200 e | 4800.1351(4) | $1.174525(7)$ | 4.46 (3) | 0.64(3) | 51/51 | 2630.9776(4) | $v_{1}+2 v_{5}{ }^{0}-3 v_{5}{ }^{1}$ | 0.9 |
|  | 1000202 f | 4809.5098(5) | 1.174023(7) | 1.77(3) | 0.15(3) | 13/13 | 2640.3523(5) | $v_{1}+2 v_{5}{ }^{2}-3 v_{5}{ }^{1}$ | 1.2 |
|  |  |  |  |  |  | 30/30 | 2622.0592(5) | $v_{1}+2 v_{5}{ }^{2}-3 v_{5}{ }^{3}$ | 0.8 |
|  | 1000202e | 4809.5104(5) | 1.173977(8) | -1.06(4) | -0.61(5) | $18 / 19$ $32 / 32$ | $2640.3529(5)$ $2622.0598(5)$ | $\begin{aligned} & v_{1}+2 v_{5}{ }^{2}-3 v_{5}{ }^{1} \\ & v_{1}+2 v_{5}^{2}-3 v_{5}{ }^{3} \end{aligned}$ | 1.4 0.9 |

## Notes

The confidence interval ( 1 SD ) is given in parenthesis in the unit of the last quoted digit. The parameters of the lower vibrational levels of ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ were constrained to the values given in Refs. [12,13].
${ }^{a}$ Normal mode labeling: $V_{i=1-5}$ are the vibrational quantum numbers, $\ell_{4,5}$ are the vibrational angular momentum quantum numbers associated to the degenerate bending modes and $\varepsilon=e$ or $f$ is the symmetry type relative to the Wang transformation. The labeling was obtained according to the maximum value of the modulus squared of the expansion coefficients of the vibrational eigenfunction in the normal mode basis (for low $J$ values). " N " marks upper states newly observed-
${ }^{b} N_{\text {tot }}$ is the total number of the observed transitions reaching a given vibrational state and $n_{f i t}$ is the number of positions included in the fit of the parameters.
${ }^{c}$ Band center: $\Delta G_{c}=G_{c}{ }^{\prime}-G_{c}{ }^{\prime}$
${ }^{d}$ Observed band in Plíva notation [15].
${ }^{e}$ Root mean square deviation in $10^{-3} \mathrm{~cm}^{-1}$ unit. " P " marks perturbed states.
${ }^{f}$ The spectroscopic constants of the $v_{2}$ state have been obtained fitting the $v_{2}-v_{5}$ band from Ref. [14].

In Ref. [1] the recommended line list was constructed as a mix of measurements and calculations and no interpolations was performed where large deviations were observed. In the present work we found a more accurate way to generate line positions using a mix of calculations from spectroscopic constants and predictions (most of the time rescaled) from the effective Hamiltonian (ASD-1000). The rescaling of the EH predictions allows, in most cases, better agreement with the measurements than the calculations using spectroscopic constants. The main advantage of the EH predictions is that most of the interactions are taken into account so that, contrary to the calculation with spectroscopic constants, no drastic deviation from measurements is observed in cases of perturbation.


Fig.2. Residuals in $\mathrm{cm}^{-1}$ obtained for the $v_{2}+\left(v_{4}+v_{5}\right)^{0}-v_{4}{ }^{1}$ band present in HITRAN and GEISA databases. Cross symbols are used for the $P_{e e}$ and $R_{e e}$ branches and open circles for the $Q_{e f}$ branch. See text for details.

A first example is given in Fig. 2 for the $P_{e e}, Q_{e f}$ and $R_{e e}$ sub-branches of the $v_{2}+\left(v_{4}+v_{5}\right)^{0}-v_{4}{ }^{1}$ band included in the HITRAN and GEISA databases. Note that the $v_{2}+\left(v_{4}+v_{5}\right)^{0}-v_{4}{ }^{1}$ band contains also the weaker $P_{f f}, Q_{f e}$ and $R_{f f}$ sub-branches that have been measured for the first time in the present work. In Fig. 2, first panel presents residuals in $\mathrm{cm}^{-1}$ between predictions with effective Hamiltonian and measurements
(cross symbols for $P_{e e}$ and $R_{e e}$ sub-branches and open circles for $Q_{e f}$ sub-branch for all panels of Fig. 2). As it can be observed the residuals smoothly increase from $-2 \times 10^{-3}$ $\mathrm{cm}^{-1}$ for lowest $m$ values up to $5 \times 10^{-3} \mathrm{~cm}^{-1}$ for highest $m$ values in the $P$ branch, and up to $7 \times 10^{-3}$ and $9 \times 10^{-3} \mathrm{~cm}^{-1}$ for highest $m$ values in the $R$ and $Q$ branches respectively ( $m$ is $-J, J$ and $J+1$ in $P, Q$ and $R$ branches, respectively). These smooth residuals can be easily modeled using polynomial expressions of the order 2-4 depending on branches (dashed-green line in the upper panel of Fig. 2). The subtraction of the fitted polynomial values from the EH predictions allows rich satisfactory modelling of the line positions. Note that polynomial modelling of the residuals in the $Q$ branch differs from that for $P$ and $R$ branches. In the second panel of Fig. 2 the residuals obtained with the rescaled EH predictions (green symbols) are plotted together with the residuals obtained using spectroscopic constants of the Table 1(red symbols). As it can be observed in the second panel, the oscillations in red residuals are much larger comparing to the green ones, implying the use for this band of the rescaled EH predictions instead of spectroscopic constants calculations. In the last two panels the residuals between HITRAN and measured line positions are given (blue symbols). In the last panel the vertical scale is reduced to $+/-0.002 \mathrm{~cm}^{-1}$. It can be clearly observed that the residuals are very good in the range of measurements of Ref. [2] but increase quickly from $J=25$ pointing out the limitations of the extrapolate calculations based on spectroscopic constants as it was performed in Ref. [2]. The deviation between databases and measurements in the cases of such extrapolations can reach several $\mathrm{cm}^{-1}$ as for the $Q$-branch of the $v_{3}-v_{4}{ }^{1}$ band presented in Fig. 3 (see third panel). Once again, the rescaled predictions (green symbols) give better agreement with the measurements then the spectroscopic constants (red symbols). Note that the same symbols have been used in Figs. 2-6.


Fig.3. Residuals in $\mathrm{cm}^{-1}$ obtained for the $v_{3}-v_{4}{ }^{1}$ band present in HITRAN and GEISA databases. Cross symbols are used for the $P_{e e}$ and $R_{e e}$ branches and open circles for the $Q_{e f}$ branch. See text for details.

Fig. 4 shows the residuals obtained for the $v_{2}+\left(v_{4}+v_{5}\right)^{0}-v_{4}{ }^{1}$ sub-band absent in HITRAN and GEISA databases. The residuals for $P_{f f}$ and $R_{f f}$ branches are given by plus symbols and those for $Q_{f e}$ branch by dot symbols. As it can be seen the both residuals (with spectroscopic constants calculations or with rescaled EH predictions) are similar and within $+/-0.0005 \mathrm{~cm}^{-1}$. In such case the calculations with spectroscopic constants from Table 1 have been used for final recommended line list.


Fig.4. Residuals in $\mathrm{cm}^{-1}$ obtained for the $v_{2}+\left(v_{4}+v_{5}\right)^{0}-v_{4}{ }^{1} f f$ and $f e$ sub-band observed for the first time. For the $P_{f f}$ and $R_{f f}$ branches the symbol plus is used while the point is used for $Q_{f e}$ branch. See text for details.

In Fig. 5, the residuals are plotted for the $v_{2}+2 v_{5}{ }^{0}-v_{5}{ }^{1}$ band demonstrating the improvement of the residuals using rescaled predictions (green symbols) comparing to the spectroscopic constants calculations (red symbols). In Fig. 6 the calculations with spectroscopic constants show drastic increases of the residuals for high $m$ values (red symbols) while the rescaled predictions (green symbols) accurately describes the line positions of the $v_{3}+2 v_{4}{ }^{0}-3 v_{4}{ }^{1}$ band.


Fig.5. Residuals in $\mathrm{cm}^{-1}$ obtained for the $v_{2}+2 \nu_{5}{ }^{0}-v_{5}{ }^{1}$ band observed for the first time. Cross symbols are used for the $P_{e e}$ and $R_{e e}$ branches and open circles for the $Q_{e f}$ branch. See text for details.


Fig.6. Residuals in $\mathrm{cm}^{-1}$ obtained for the $v_{3}+2 v_{4}{ }^{0}-3 v_{4}{ }^{1}$ band observed for the first time. Cross symbols are used for the $P_{e e}$ and $R_{e e}$ branches and open circles for the $Q_{e f}$ branch. See text for details.

## 5. Effective dipole moment fitting and comparisons with measurements

The effective dipole moment parameters reported in Ref. [3] were obtained by the fitting of the line intensities of five vibrational bands [2] with the maximum $J$ values around $20-25$. In the present work measurements for these five bands were greatly extended up to $J=39-43$ depending on the band while the measurements for low $J$ values were not performed. The new measurements allowed refine the set of EDM parameters. The definition of the parameters and the calculation formulas can be found in Refs. [3,5,16]. The line intensity fit including all available measurements (this work and Ref. [1,2]) for 71 bands was performed. The statistical information on the result of the fit is collected in Table 2. The result of fit of the bands measured in Ref. [1] and in this work is slightly worse with RMS about 3-5\% comparing to $1-2 \%$ for the strongest bands measured in Ref. [2]. The larger deviations can be explained by the weakness of the measured lines but also by the fact that many transitions are overlapped due to long optical absorption paths used in Ref. [1] and present work.

Table 2. Band statistics of the EDM parameters fit in the $3.8-\mu \mathrm{m}$ spectral region.

$$
\begin{array}{cccc}
V_{1} V_{2} V_{3} V_{4} V_{5} \ell_{4} \ell_{5} \\
\text { Upper level - Lower level } & \text { Region }\left(\mathrm{cm}^{-1}\right) & J_{\max } N & \operatorname{MR}(\%) \mathrm{RMS}(\%)
\end{array}
$$

Bands present in the 2020 edition of the HITRAN and GEISA databases.
Statistics are presented twice for each band, first corresponding to the EDM fit using measurements from Ref. [2], and then using measurements of this work.

| 0 | 1 | 0 | 0 | 1 | 01 | - | 0 | 0 | 0 | 0 | 0 |  |  | 0 | 2649.8-2752.4 | 25 | 60 | 0.77 | 1.40 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 2601.0-2792.1 | 43 | 42 | -2.60 | 3.95 |
| 0 | 0 | 0 | 3 | 1 | 1-1 | - | 0 | 0 | 0 | 0 | 0 |  |  | 0 | 2515.5-2609.0 | 21 | 33 | 1.16 | 2.11 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 2491.3-2647.1 | 35 | 26 | -1.12 | 3.53 |
| 1 | 0 | 0 | 0 | 0 | 00 | - | 0 | 0 | 0 | 0 | 1 |  |  | 1 | 2583.7-2694.1 | 24 | 55 | -0.18 | 0.86 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 2534.0-2728.3 | 42 | 34 | 0.72 | 1.95 |
| 0 | 1 | 0 | 1 | 1 | 1-1 | - | 0 | 0 | 0 | 1 | 0 |  |  | 0 | 2627.3-2737.2 | 24 | 57 | 0.39 | 0.85 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 2585.2-2769.3 | 39 | 94 | 0.65 | 2.71 |
| 0 | 0 | 1 | 0 | 0 | 00 | - | 0 | 0 | 0 | 1 |  |  |  | 0 | 2614.6-2713.7 | 23 | 39 | -0.36 | 1.95 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 2573.5-2757.7 | 39 | 45 | 0.49 | 3.16 |

Bands measured for the first time in the present work

| 0 | 0 | 0 | 1 | 3 | $1-1$ | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $2728.4-2807.3$ | 19 | 23 | 0.15 | 3.11 |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0 | 0 | 0 | 3 | 1 | 1 | 1 | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $2541.7-2623.8$ | 19 | 3 | -2.24 | 6.14 |
| 0 | 0 | 0 | 4 | 1 | $4-1$ | - | 0 | 0 | 0 | 1 | 0 | 1 | 0 | $2501.8-2635.5$ | 29 | 25 | 1.57 | 4.46 |  |
| 0 | 0 | 0 | 5 | 1 | $1-1$ | - | 0 | 0 | 0 | 2 | 0 | 0 | 0 | $2539.1-2634.0$ | 23 | 23 | -0.79 | 4.06 |  |
| 0 | 0 | 0 | 5 | 1 | $3-1$ | - | 0 | 0 | 0 | 2 | 0 | 2 | 0 | $2533.9-2639.3$ | 24 | 44 | -0.28 | 3.60 |  |
| 0 | 0 | 1 | 0 | 2 | 0 | 0 | - | 0 | 0 | 0 | 1 | 2 | 1 | 0 | $2638.5-2720.7$ | 17 | 1 | 5.83 | 5.83 |
| 0 | 0 | 1 | 0 | 2 | 0 | 0 | - | 0 | 0 | 0 | 1 | $2-1$ | 2 | $2634.3-2661.1$ | 11 | 3 | -5.48 | 5.80 |  |
| 0 | 0 | 1 | 0 | 2 | 0 | 2 | - | 0 | 0 | 0 | 1 | 2 | 1 | 0 | $2688.1-2716.5$ | 13 | 6 | -2.19 | 4.62 |
| 0 | 0 | 1 | 0 | 2 | 0 | 2 | - | 0 | 0 | 0 | 1 | 2 | 1 | 2 | $2635.6-2655.0$ | 5 | 2 | 0.94 | 7.08 |
| 0 | 0 | 1 | 0 | 2 | 0 | 2 | - | 0 | 0 | 0 | 1 | $2-1$ | 2 | $2668.5-2697.7$ | 15 | 5 | 1.99 | 6.14 |  |
| 0 | 0 | 1 | 1 | 1 | 1 | 1 | - | 0 | 0 | 0 | 2 | 1 | 0 | 1 | $2609.1-2714.3$ | 23 | 12 | -2.92 | 4.51 |
| 0 | 0 | 1 | 1 | 1 | 1 | 1 | - | 0 | 0 | 0 | 2 | 1 | 2 | 1 | $2621.4-2696.6$ | 22 | 20 | 0.33 | 4.60 |



## Bands previously measured in Ref. [1]

| 0 | 0 | 0 | 3 | 1 | $3-1$ | - | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $2469.6-2636.4$ | 37 | 41 | 1.60 | 3.11 |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0 | 0 | 0 | 3 | 2 | 3 | 0 | - | 0 | 0 | 0 | 0 | 1 | 0 | 1 | $2493.1-2603.9$ | 25 | 25 | -1.34 | 4.83 |
| 0 | 0 | 0 | 3 | 2 | $3-2$ | - | 0 | 0 | 0 | 0 | 1 | 0 | 1 | $2458.1-2596.5$ | 27 | 61 | -0.21 | 3.79 |  |
| 0 | 0 | 0 | 3 | $2-1$ | $2-$ | -0 | 0 | 0 | 0 | 1 | 0 | 1 | $2490.5-2606.1$ | 28 | 66 | -1.52 | 3.36 |  |  |
| 0 | 0 | 0 | 4 | 1 | $2-1$ | - | 0 | 0 | 0 | 1 | 0 | 1 | 0 | $2507.5-2652.5$ | 32 | 71 | 0.48 | 2.43 |  |
| 0 | 0 | 0 | 4 | 2 | $2-2$ | - | 0 | 0 | 0 | 1 | 1 | $1-1$ | $2511.8-2587.2$ | 20 | 18 | 1.28 | 3.89 |  |  |
| 0 | 1 | 0 | 2 | 0 | 0 | 0 | - | 0 | 0 | 0 | 0 | 1 | 0 | 1 | $2399.8-2498.4$ | 29 | 47 | 1.18 | 4.00 |
| 0 | 1 | 0 | 2 | 0 | 2 | 0 | - | 0 | 0 | 0 | 0 | 1 | 0 | 1 | $2389.1-2514.5$ | 30 | 39 | -0.99 | 5.29 |
| 1 | 0 | 0 | 0 | 1 | 0 | 1 | - | 0 | 0 | 0 | 0 | 2 | 0 | 0 | $2557.5-2705.5$ | 32 | 33 | 0.19 | 3.18 |
| 1 | 0 | 0 | 0 | 1 | 0 | 1 | - | 0 | 0 | 0 | 0 | 2 | 0 | 2 | $2545.7-2691.7$ | 34 | 70 | 1.85 | 3.64 |
| 1 | 0 | 0 | 1 | 0 | 1 | 0 | - | 0 | 0 | 0 | 1 | 1 | 1 | 1 | $2547.7-2695.2$ | 32 | 71 | 1.99 | 4.00 |
| 1 | 0 | 0 | 1 | 0 | 1 | 0 | - | 0 | 0 | 0 | 1 | 1 | $1-1$ | $2549.8-2707.1$ | 34 | 77 | -1.32 | 4.13 |  |
| 1 | 0 | 0 | 1 | 1 | 1 | 1 | - | 0 | 0 | 0 | 1 | 2 | 1 | 2 | $2560.4-2612.7$ | 21 | 24 | 1.76 | 4.77 |
| 1 | 0 | 0 | 1 | 1 | $1-1$ | - | 0 | 0 | 0 | 1 | 2 | 1 | 0 | $2564.2-2670.9$ | 25 | 13 | -0.30 | 3.56 |  |

Note: for a given band, $J_{\max }$ is the maximum observed value of the rotational quantum number of the lower state, $N$ is the number of the measured line intensities included in the fit. $M R$ and $R M S$ are the mean value and the root mean square of the residuals, respectively. Its definition can be found for example in Ref. [3].

The effective dipole moment parameters obtained by the fitting of the present line intensities together with those from Refs. [1,2] (using formulas of Ref. [5,16]) are collected in the Table 3. The parameters obtained in Refs. [1,3] are also presented. In the Ref. [1] the satisfactory description of the line intensities of all 19 bands was achieved by adding only three small parameters to the set of Ref. [3]. In this work an accurate description of all 71 bands was obtained by adding 9 supplemental parameters to the set of Ref. [1].

Table 3. The set of the effective dipole moment parameters describing the line intensities of acetylene in the $3.8-\mu \mathrm{m}$ spectral region

| Parameter $^{\mathrm{a}}$ | $\Delta V_{1}$ | $\Delta V_{2}$ | $\Delta V_{3}$ | $\Delta V_{4}$ | $\Delta V_{5}$ | $\Delta \ell_{4}$ | $\Delta \ell_{5}$ | $\mathrm{PW}^{\mathrm{b}}$ | $[1]^{\mathrm{b}}$ | $[3]^{\mathrm{b}}$ | Order |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $M$ | 0 | 1 | 0 | 0 | 1 | 0 | 1 | $0.2359(3)$ | $0.2401(4)$ | $0.2377(2)$ | $10^{-2}$ |
| $k_{4}$ | 0 | 1 | 0 | 0 | 1 | 0 | 1 | $-0.089(1)$ | $-0.183(7)$ | $-0.191(4)$ |  |
| $b_{J}$ | 0 | 1 | 0 | 0 | 1 | 0 | 1 | $0.589(5)$ | $0.55(1)$ | $0.557(8)$ | $10^{-2}$ |
| $k_{5}$ | 0 | 1 | 0 | 0 | 1 | 0 | 1 | $-0.080(1)$ |  |  |  |
| $a_{5}$ | 0 | 1 | 0 | 0 | 1 | 0 | 1 | $0.0132(5)$ |  |  |  |
| $M$ | 1 | 0 | 0 | 0 | -1 | 0 | 1 | $1.1642(8)$ | $-1.168(1)$ | $1.121(1)$ | $10^{-2}$ |
| $b_{J}$ | 1 | 0 | 0 | 0 | -1 | 0 | 1 | $-0.364(5)$ | $-0.353(6)$ | $-0.398(8)$ | $10^{-2}$ |
| $M$ | 0 | 0 | 1 | -1 | 0 | 1 | 0 | $1.063(2)$ | $1.047(1)$ | $1.0360(7)$ | $10^{-2}$ |
| $b_{J}$ | 0 | 0 | 1 | -1 | 0 | 1 | 0 | $-0.357(4)$ | $-0.36(1)$ | $-0.361(6)$ | $10^{-2}$ |
| $k_{4}$ | 0 | 0 | 1 | -1 | 0 | 1 | 0 | $-1.56(8)$ |  |  | $10^{-2}$ |
| $k_{5}$ | 0 | 0 | 1 | -1 | 0 | 1 | 0 | $-2.2(1)$ |  |  | $10^{-2}$ |
| $M$ | 0 | 0 | 0 | 1 | 3 | 1 | -1 | $3.094(9)$ |  |  | $10^{-5}$ |
| $b_{J}$ | 0 | 0 | 0 | 1 | 3 | 1 | -1 | $-1.14(2)$ |  |  | $10^{-2}$ |
| $M$ | 0 | 0 | 0 | 3 | 1 | 1 | -1 | $1.609(2)$ | $1.631(2)$ | $1.621(2)$ | $10^{-4}$ |
| $k_{4}$ | 0 | 0 | 0 | 3 | 1 | 1 | -1 | $-0.032(1)$ | $-0.027(2)$ |  |  |
| $M$ | 0 | 1 | 0 | 2 | -1 | 0 | 1 | $1.597(6)$ | $1.630(7)$ |  | $10^{-4}$ |
| $M$ | 0 | 1 | 0 | 2 | -1 | 2 | -1 | $0.959(4)$ | $0.934(4)$ |  | $10^{-4}$ |
| $M$ | 1 | 0 | 0 | -2 | 1 | 2 | -1 | $-0.61(3)$ |  |  | $10^{-4}$ |
| $M$ | 0 | 1 | 0 | 0 | 1 | 2 | -1 | $1.38(2)$ |  |  | $10^{-4}$ |
| $M$ | 0 | 0 | 1 | -1 | 0 | -1 | 2 | $-1.08(6)$ |  |  | $10^{-4}$ |

a Parameters $M$ are given in Debye ( $1 \mathrm{D}=3.33546 \times 10^{-30} \mathrm{C} \cdot \mathrm{m}$ ), while the other parameters are dimensionless.
${ }^{\mathrm{b}}$ Confidence intervals ( 1 SD , in unit of the last quoted digit) are given between parenthesis.

The vibration-rotation transition moment squared $|R|^{2}$ calculated using Eq. (2) of Ref. [1] has usually smooth rotational dependence and is useful to analyze the measured intensities. For each band measured and calculated $|R|^{2}$ were plotted versus $m$ ( $m=-J, J$,
$J+1$ for $P, Q$ and $R$ branches respectively). Such plots have been used to check the quality of the intensities calculation. Examples are given in Figs. 7 and 8 respectively for the two bands $v_{3}-v_{4}{ }^{1}$ and $\left(3 v_{4}+v_{5}\right)^{0}$, present in the 2020 edition of the HITRAN and GEISA databases. In these figures we can first observe the good consistency between measurements from this work and those from Ref. [2], with a dispersion of the measurements slightly higher for this work. Note that under present experimental conditions, only transitions with high $J$ values could be measured with sufficient accuracy, transitions with lower $J$ values are saturated in all experimental spectra of this work. In Figs. 7 and 8, one can see that the calculations using EDM parameters from this work (red line) and from previous study [1] (blue line) are very similar since these bands were already included in the fit of EDM parameters in the previous work [3]. It is worth to notice that EDM calculation from Ref. [1] predicts accurately the rotational dependence observed for high $J$ values measured for the first time in this work. The calculation in HITRAN and GEISA databases (using Herman-Wallis factor to fit observed rotational dependences from measurements of Ref. [2]) is also quite close to calculations using EDM parameters. Note that extrapolations of the measurements from the Ref. [2] have been performed for the databases using fixed value of the transition dipole moment squared leading to the singularities in its rotational dependence.


Fig.7. Vibration-rotation transition moments squared $|R|^{2}$ obtained for the $v_{3}-v_{4}{ }^{1}$ band. Cross symbols for $P_{e e}$ and $R_{e e}$ sub-branches and open circles symbols for $Q_{e f}$ sub-branch have been used for measurements from this work (black symbols) and from Ref. [2] (green symbols). Continuous lines correspond to calculations: red and blue lines stand for calculations with EDM parameters from this work and from Ref. [1] respectively, whereas green line stands for the calculation given in the HITRAN and GEISA databases.


Fig.8. Vibration-rotation transition moments squared $|R|^{2}$ obtained for the $\left(3 v_{4}+v_{5}\right)^{0}$ band. See Fig. 7 for legend.

Transition dipole moment squared belonging to the $\left(v_{4}+3 v_{5}\right)^{0}, v_{2}+2 v_{5}{ }^{0}-v_{5}{ }^{1}$ and $v_{3}+v_{4}{ }^{1}-2 v_{4}{ }^{0}$ bands (newly observed) have been plotted in Figs. 9-11 respectively together with calculations using EDM parameters (see Table 3) from Ref. [1] (blue line) and from this work (red line). As it can be observed in Figs. 9-11, except the cold band the rotational dependence of $|R|^{2}$ values predicted by EDM parameters of Ref. [1] is in good agreement with the measurements obtained for the first time in this work. Two additional EDM parameters were required (principal " $M$ " and rotational dependence " $b_{J}$ " parameters, see Table 3) to describe the intensities in the cold $\left(v_{4}+3 v_{5}\right)^{0}$ band presented in Fig. 9. The vibrational transition moment squared of hot bands was slightly corrected by new set of parameters. Since the EDM model takes into account resonance interactions between levels, it allows to reach a good qualitative rotational dependence where intensity modelling using Herman-Wallis factors fails. We believe that using EDM parameters extrapolations of intensities could be performed without risking hazardous extrapolations. This is certainly not the case of model using Herman-Wallis factors.


Fig.9. Vibration-rotation transition moments squared $|R|^{2}$ obtained for the $\left(v_{4}+3 v_{5}\right)^{0}$ band. See Fig. 7 for legend.


Fig.10. Vibration-rotation transition moments squared $|R|^{2}$ obtained for the $v_{2}+2 v_{5}{ }^{0}-v_{5}{ }^{1}$ band. See Fig. 7 for legend.


Fig.11. Vibration-rotation transition moments squared $|R|^{2}$ obtained for the $v_{3}+v_{4}{ }^{1}-2 v_{4}{ }^{0}$ band. See Fig. 7 for legend. Cross symbols for $P_{e e}$ and $R_{e e}$ sub-branches and dot symbols for $Q_{f e}$ sub-branch have been used for measurements.

## 6. Generation of a line list for ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{\mathbf{2}}$ in the $\Delta P=\mathbf{4}$ spectral region

A complete line list in the $\Delta P=4$ spectral region has been generated for the 71 bands studied in this work, including the 5 strongest bands, already present in the 2020 edition of the HITRAN and GEISA databases, and the 14 bands previously studied in Ref. [1]. The line list covers the $2389-2890 \mathrm{~cm}^{-1}$ spectral range and contains 7515 transitions of ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ isotopologue.

One of the difficulties was to decide if extrapolations of measurements could be performed. As for line intensities, as explained in the previous Section, we are confident that the EDM model is able to accurately reproduce interpolated as well as extrapolated line intensities. However for line positions, the spectroscopic constants may lead to an inaccurate extrapolation as demonstrated in Figs. 2 and 3 (last two panels). Moreover, reproducing measurements at high $J$ values using spectroscopic constants in the cases of perturbed bands is also not satisfactory (see Fig. 6 for example). In order to improve residuals between calculated and measured line positions for perturbed bands, we proposed in Section 4 to rescale the prediction of the EH model using polynomial expressions (see Section 4). Such empirical rescaling of the EH predictions may also lead to inaccurate extrapolations of the line positions (as with the spectroscopic constants). If the EH prediction is in good agreement with the measurement without rescaling, its extrapolated position values can be used with confidence. The situation has been evaluated individually for each band. Among the 71 bands presenting in our line list the positions have been generated by EH prediction only for 6 bands. For the other bands rescaled predictions or spectroscopic constants have been used to reproduce measurements with the best precision. The Table 4 summarizes the information on the contents of the recommended acetylene line list from this work. Interpolations were systematically performed. Concerning extrapolations, they have been performed only in a few cases where the upper level of the transition was measured through another subbranch. For example, the calculation from the measurements in the $P_{\text {ee }}$ sub-branch of the $v_{3}+2 v_{5}^{2}-\left(v_{4}+2 v_{5}\right)^{3}$ band has been used to derive the line positions in the $R_{\mathrm{ee}}$ subbranch for which no measurement is present. Extrapolations are indicated in the "subbranch limits" column of the Table 4 by a "/" symbol. No extrapolation was done where the " $"$ " symbol is absent. For example, for the $Q_{\text {ef }}$ sub-branch of the $v_{3}+2 v_{5}{ }^{2}-$ $\left(v_{4}+2 v_{5}\right)^{1} I$ band (denoted $\left.0010202 \_00012-12\right)$ the measurements were obtained only up to $J=6$ whereas the line positions were generated up to $J=15$. In the column "Model" of Table 4, the model used for the line positions calculation is indicated by
"Pred" for prediction using EH model or by "Constants" for the use of spectroscopic constants from Table 1, or by "Pred_Cor" for corrected/rescaled EH model. The line intensities were calculated using EDM model with parameters from Table 3. Note that a line intensity cutoff equal to $10^{-28} \mathrm{~cm} /$ molecule has been applied in the present line list so that some interpolations to the lowest $J$ values (with intensities lower than $10^{-28}$ $\mathrm{cm} / \mathrm{molecule}$ ) were ignored. In the last column of the Table are given uncertainties of calculations using HITRAN codes corresponding to absolute uncertainty ranges. Same codes are chosen for all transitions belonging to a band. From the comparisons between calculated and measured line positions, codes 2, 3 and 4 have been assigned to the line positions, corresponding to uncertainty ranges equal to $0.01-0.1 \mathrm{~cm}^{-1}, 0.001-0.01$ $\mathrm{cm}^{-1}$ and $0.0001-0.001 \mathrm{~cm}^{-1}$, respectively. As for line intensities codes we decided to use RMS from Table 2: RMS values must be inside the uncertainty range defined by the code. For example, for the $\left(v_{4}+3 v_{5}\right)^{0}$ band RMS value is equal to $3.11 \%$ (see Table 2), and are between 2-5\% (code 6 in HITRAN). Codes 5, 4 and 3 for intensities correspond to uncertainty ranges $5-10 \%, 10-20 \%$ and $>20 \%$ respectively. For the bands included in HITRAN2020 (with a code 6 for intensities degraded to a code 5 for extrapolations), two sets of measurements are available. RMS values from Table 2 obtained for the observations of Ref. [2] are systematically smaller than those obtained for this work and could lead to uncertainties between 1 and $2 \%$ (code 7 in HITRAN) which will be an ultimate limit for accuracy due mainly to the knowledge of the concentration of ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ in the sample. We decided for these 5 bands to keep previously used code 6 (2-5\%) that includes RMS values of both sets of measurements (Ref. [2] and this work).

For the broadening and shifting parameters polynomial expressions (functions of $J$ ) or default values (with associated uncertainty codes) described in the HITRAN 2008 edition [17] were used. The recommended line list (in HITRAN format) for the 71 bands of ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ studied in the present work is available as Supplementary Material II and is proposed to replace completely line list from databases in the $\Delta P=4$ spectral region.

Table 4. The details of the line list construction in the $\Delta P=4$ spectral region.

| Band ${ }^{\text {a }}$ |  |  |  |  | -----------Sub-branch limits ${ }^{\text {b }}$--------- ---- |  |  |  |  |  | Spectral range (in $\mathrm{cm}^{-1}$ ) | $N^{c}$ | Model ${ }^{\text {d }}$ | Uncertainty codes ${ }^{\text {e }}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Upper |  | Lower |  | $P_{\text {ee }}$ | $R_{\text {ee }}$ | $Q_{\text {ef }}$ | $P_{\text {ff }}$ | $R_{\text {ff }}$ | $Q_{\text {fe }}$ |  |  |  | Pos | Int |
| Bands present in HITRAN2020 and GEISA2020 databases |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 000 | 31 | 1-1_000 | 000 | 0 | 35 | 33 | NA | NA | NA | -- | 2491-2654 | 69 | Pred | 4 | 6 |
| 001 | 0 | 0 0-000 | 101 | 0 | 41 | 39 | 39 | NA | NA | NA | 2568-2758 | 119 | Pred_Cor | 4 | 6 |
| 010 | 01 | 0 1_000 | 000 |  | 39 | 43 | NA | NA | NA | 43 | 2600-2793 | 125 | Pred_Cor | 4 | 6 |
|  | 11 | 1-1_000 | 101 |  | 39 | 39 | 38 | 30 | 32 | 30 | 2585-2770 | 208 | Pred_Cor (ee+ef)/Constants(ff+fe) | 4 | 6 |
| 100 | 00 | 0 O_000 | 010 |  | 42 | 40 | 41 | NA | NA | NA | 2533-2729 | 123 | Pred_Cor | 4 | 6 |

Bands measured for the first time in the present work

| 000 | 13 | 1-1_000 | 000 | 00 | 21 | 19 | NA | NA | NA | -- | 2710-2808 | 41 | Pred_Cor | 4 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 000 | 31 | $11^{-} 0000$ | 000 | 00 | 19 | 27 | NA | NA | NA | -- | 2541-2654 | 47 | Constants | 4 | 5 |
| 000 | 41 | 4-1-000 | 101 | 10 | 29 | 27 | - | 20 | 20 | -- | 2500-2634 | 86 | Constants | 3 | 6 |
| 000 | 51 | 1-1_000 | 200 | 00 | 23 | 17 | NA | NA | NA | -- | 2540-2635 | 41 | Pred_Cor | 4 | 6 |
| 000 | 51 | 3-1-000 | 202 | 20 | 23 | 21 | 4/20 | 24 | 24 | 5/20 | 2540-2635 | 124 | Pred_Cor (ee)/Constants (ffteftfe) | 3 | 6 |
| 001 | 01 | 0 1_000 | 111 | 11 | 25 | 28 | 31 | 29 | 29 | 32 | 2602-2742 | 168 | Constants | 4 | 6 |
| 001 | 01 | 0 1_-000 | 111 | 1-1 | 29 | 30 | 29 | 31 | 31 | 28 | 2599-2752 | 178 | Pred_Cor | 4 | 6 |
| 001 | 02 | 0 0_000 | 121 | 10 | 17 | 18 | 19 | NA | NA | NA | 2638-2726 | 54 | Const̄ants | 3 | 5 |
| 001 | 02 | 0 0_000 | 1 2-1 | 12 | 15 | 11 | 22 | NA | NA | NA | 2623-2688 | 48 | Pred_Cor | 4 | 5 |
| 001 | 02 | 0 2_000 | 121 | 10 | --/11 | 11 | 20 | --/14 | 14 | 13 | 2684-2722 | 77 | Const̄ants | 3 | 6 |
| 001 | 02 | ( $02^{-} 000$ | 121 | 12 | 11 | --/11 | 16 | 14 | --/14 | 15 | 2635-2697 | 69 | Pred | 3 | 5 |
| 001 | 02 | $02^{-} 000$ | 1 2-1 | 12 | 13 | 15 | 6/15 | --/12 | 12 | 15 | 2638-2707 | 76 | Pred | 3 | 5 |
| 001 | 10 | 1 0_000 | 200 | 00 | 21 | 23 | NA | NA | NA | 33 | 2611-2716 | 77 | Pred_Cor | 4 | 6 |
| 001 | 10 | 1 0_000 | 202 | 20 | 35 | 35 | 36 | 34 | 34 | 23 | 2580-2747 | 191 | Pred_Cor | 4 | 6 |
| 001 | 11 | $11^{-}-000$ | 210 | 01 | 20 | 20 | 13 | 23 | 23 | 14 | 2604-2715 | 107 | Pred | 3 | 6 |
| 001 | 11 | $11^{-} 000$ | 212 | 21 | 12 | 16 | 25 | 19 | 15 | 24 | 2610-2697 | 96 | Constants | 3 | 6 |
| 001 | 11 | 1-1-000 | 210 | 01 | -- | -- | -- | 17 | 19 | 24 | 2617-2703 | 60 | Pred_Cor | 4 | 6 |
| 001 | 11 | 1-1-000 | 212 | 2-1 | 22 | 20 | 25 | 19 | 19 | 20 | 2616-2721 | 125 | Const̄ants | 3 | 6 |
| 001 | 20 | 0 0-000 | 301 | 10 | 25 | 23 | 26 | NA | NA | NA | 2593-2710 | 74 | Pred_Cor | 3 | 6 |
| 001 | 20 | 2 0_000 | 301 | 10 | 15 | 17 | 16 | 10 | 14 | 29 | 2613-2691 | 95 | Pred_Cor (ee+fe)/Constants(fftef) | 3 | 5 |
| 001 | 20 | 2 0_000 | 303 | 30 | 29 | 27 | 26 | 24 | 26 | 19 | 2581-2715 | 136 | Pred_Cor | 3 | 6 |
| 010 | 02 | 0 0_000 | 010 | 01 | 36 | 38 | 33 | NA | NA | NA | 2601-2776 | 107 | Pred_Cor | 4 | 6 |
| 010 | 02 | 0 2_000 | 010 | 01 | 28 | 30 | 35 | 29 | 35 | 34 | 2626-2777 | 185 | Pred_Cor (ee+ef)/Constants (ff+fe) | 4 | 6 |
| 010 | 03 | $31^{-}-000$ | 020 | 00 | 25 | 27 | NA | NA | NA | 23 | 2626-2750 | 75 | Pred_Cor | 4 | 6 |
| 010 | 03 | 3 1_-000 | 020 | 02 | 19 | 21 | 20 | 24 | 26 | 27 | 2624-2745 | 131 | Const̄ants | 3 | 6 |
| 010 | 03 | $33^{-} 000$ | 020 | 02 | 19 | 25 | 28 | 20 | 24 | 27 | 2649-2757 | 131 | Pred_Cor | 4 | 6 |
| 010 | 11 | 1 1_000 | 101 | 10 | 19 | 23 | 38 | 28 | 34 | 31 | 2620-2762 | 167 | Pred_Cor (ee+ef)/Constants (ff+fe) | 4 | 6 |


| 010121000001111 | 22 | 20 | 27 | 25 | 21 | 28 | 2598-2710 | 137 | Constants | 3 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $01012180{ }^{-0} 00111-1$ | 22 | --/22 | 33 | 33 | 31 | 20 | 2580-2734 | 161 | Constants | 3 | 6 |
| 010121220001111 | 16 | 22 | 27 | 15 | 23 | 26 | 2650-2743 | 117 | Constants | 4 | 6 |
| 010 1 2-1 2-000 $1111-1$ | 16 | 18 | 27 | 27 | 29 | 20 | 2615-2749 | 137 | Constants | 4 | 6 |
| $0102101-0002000$ | 19 | 21 | NA | NA | NA | 25 | 2630-2726 | 65 | Pred_Cor | 4 | 6 |
| $0102121 \_0002000$ | 17 | 23 | NA | NA | NA | 31 | 2637-2733 | 64 | Pred_Cor | 4 | 6 |
| $0102121 \_0002020$ | --/15 | 15 | 22 | 10 | 14 | 8 | 2657-2719 | 72 | Constants | 4 | 6 |
| $010212-1-0002000$ | 19 | 23 | NA | NA | NA | 33 | 2601-2700 | 75 | Pred_Cor | 4 | 5 |
| $010212-1-0002020$ | 35 | 33 | 34 | 34 | 32 | 23 | 2565-2727 | 185 | Pred Cor (ee+fe)/Constants (fftef) | 4 | 6 |
| 010222000002101 | 14 | 18 | 15 | 17 | 11 | 16 | 2609-2671 | 85 | Constants | 2 | 3 |
| $010222-2-0002101$ | 10 | 10 | 19 | 17 | 17 | 24 | 2599-2682 | 97 | Pred_Cor (ff) +Pred (ee+fe+ef) | 2 | 3 |
| $010311-1 \_0003010$ | 23 | 23 | 28 | -- | -- | -- | 2580-2691 | 74 | Pred_Cor | 3 | 6 |
| $010313-1-0003010$ | 13 | 19 | 9 | 10 | 14 | 27 | 2600-2676 | 86 | Pred-Cor(fe)/Constants (ee+fftef) | 3 | 3 |
| $010313-1 \_0003030$ | 22 | 25 | 22 | 26 | 20 | 15 | 2571-2692 | 118 | Pred_Cor | 3 | 6 |
| $1000101_{-000}^{-1} 020$ | 15 | 11 | 20 | 18 | 10 | 15 | 2818-2890 | 83 | Constants | 3 | 5 |
| 100020000000301 | 26 | 22 | 21 | NA | NA | NA | 2566-2683 | 69 | Pred_Cor | 4 | 6 |
| $1000202-0000301$ | 14 | 14 | 23 | 19 | 13 | 18 | 2590-2675 | 95 | Pred | 3 | 3 |
| $1000202-0000303$ | 22 | 18 | 23 | 21 | 19 | 26 | 2566-2666 | 117 | Pred_Cor | 4 | 5 |
| $10011111_{-00012}^{-1} 0$ | 15 | 13 | 24 | 18 | 20 | 17 | 2592-2680 | 101 | Pred | 3 | 5 |
| $100111-1 \times 0012-12$ | -- | -- | -- | 26 | 22 | 25 | 2557-2674 | 73 | Pred_Cor | 4 | 5 |
| 10020000002101 | 22 | 18 | 27 | NA | NA | NA | 2551-2650 | 67 | Pred_Cor | 3 | 5 |
| $10020000000212-1$ | 26 | 26 | 15 | NA | NA | NA | 2562-2687 | 67 | Pred_Cor | 3 | 5 |
| 100202000002101 | 14 | 16 | -- | -- | -- | 22 | 2576-2650 | 49 | Constants | 2 | 3 |
| 100202000002121 | 24 | 17 | 27 | 21 | 21 | 22 | 2549-2657 | 120 | Pred_Cor (ee+Qef) / Constants (ff+Qfe) | 4 | 5 |
| $10020200000212-1$ | 6 | 8 | 23 | 23 | 23 | 22 | 2570-2681 | 99 | Pred_Cor (ee+Qef)/Constants (ff+Qfe) | 3 | 6 |

## Bands previously measured in Ref. [1]

| 000 |  | $13-1 \_000$ | 00 | 00 | 37 | 33 | NA | NA | NA | NA | 2469-2637 | 68 | Pred_Cor | 4 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 000 | 32 | 2300000 | 01 | 01 | 24 | 23 | -- | 27 | 29 | -- | 2488-2622 | 95 | Constants | 3 | 6 |
| 000 |  | 2 3-2_000 | 01 | 01 | 32 | 27 | 3 | 27 | 21 | 6 | 2458-2599 | 114 | Constants | 3 | 6 |
| 000 | 32 | 2-1 2_000 | 01 | 01 | 30 | 26 | 7 | 27 | 23 | 6 | 2490-2624 | 117 | Pred_Cor | 3 | 6 |
| 000 |  | $12-1-000$ | 10 | 10 | 31 | 29 | 11 | 32 | 32 | 13 | 2507-2659 | 146 | Pred Cor | 4 | 6 |
| 000 |  | 2 2-2-000 | 11 | 1-1 | 20 | 19 | -- | 17 | 15 | -- | 2511-2607 | 73 | Pred_Cor | $4(\mathrm{ee}) / 2$ (ff) | 6 |
| 010 | 20 | 0 0 0_000 | 01 | 01 | 22 | 20 | 29 | NA | NA | NA | 2399-2501 | 71 | Pred_Cor | 4 | 5 |
| 010 |  | 0200000 | 01 | 01 | 24 | 30 | 33 | 15 | 21 | 22 | 2389-2515 | 138 | Pred_Cor (ee+ef)/Constants (ff+fe) | 3 | 6 |
| 100 |  | 10 1-000 | 02 | 00 | 32 | 33 | NA | NA | NA | 31 | 2557-2711 | 96 | Pred_Cor | 4 | 6 |
| 100 | 01 | 10 1_000 | 02 | 02 | 31 | 28 | 34 | 34 | 32 | 35 | 2545-2704 | 188 | Const̄ants | 3 | 6 |
| 100 | 10 | $0180{ }^{-} 000$ | 11 | 11 | 32 | 29 | 33 | 33 | 33 | 36 | 2538-2696 | 190 | Pred_Cor (ee+fe)/Constants (fftef) | 3 | 6 |
| 100 | 10 | 0 1 0-000 | 11 | 1-1 | 34 | 34 | 33 | 31 | 29 | 32 | 2549-2711 | 193 | Pred_Cor (ee+fe)/Constants (fftef) | 3 | 6 |
| 100 | 11 | 1 1 1_000 | 12 | 12 | 23 | 21 | 26 | 22 | 22 | 25 | 2555-2663 | 127 | Pred_Cor (eftfe)/Constants (ff+ee) | 3 | 6 |
| 100 | 11 | 1 1-1_000 | 12 | 10 | 25 | 25 | 26 | -- | -- | -- | 2564-2684 | 76 | Pred_Cor | 4 | 6 |

[^0]${ }^{c} N$ is the number of transitions generated for each band in the recommended line list.
${ }^{\text {a }}$ The model used to generate line positions in the present line list: "Pred" states for prediction using EH model, "Constants" for the use of spectroscopic constants from Table 1, and "Pred Cor" for corrected/rescaled EH model.
${ }^{\mathrm{e}}$ The uncertainty codes according to HITRAN uncertainty ranges

In order to check the quality of the present line list, a synthetic spectrum has been calculated under experimental conditions corresponding to the largest optical absorption path $(1057.95 \mathrm{~m})$. An extract of the comparison between experimental and synthetic spectrum is presented in Fig. 12. As one can see the most of the observed transitions are well reproduced by the present line list except for transitions belonging to ${ }^{12} \mathrm{C}^{13} \mathrm{H}_{2}$ and ${ }^{12} \mathrm{C}_{2} \mathrm{HD}$ isotopologues not studied in the present work. The line positions of these isotopologues reported in Ref. [18] and [19], respectively, were used in the present work for assignments.





Fig.12. Comparison between synthetic (CALC) and observed (OBS) spectra in the $2636-2638 \mathrm{~cm}^{-1}$ spectral domain. The OBS-CALC residuals are given on the first panel. On the second panel the recommended line list is plotted as a stick plot in a $\log$ scale for intensities (in cm/molecule), the transitions included in the 2020 edition of the HITRAN and GEISA databases are shown in red. The two latest panels represent the experimental spectrum (OBS) recorded with absorption path equal to 1057.95 m and corresponding synthetic (CALC) spectrum. In the third panel transitions belonging to the ${ }^{12} \mathrm{C}^{13} \mathrm{H}_{2}$ and ${ }^{12} \mathrm{C}_{2} \mathrm{HD}$ isotopologues are indicated by red and blue crosses respectively.

## 6. Conclusion

The present work is finalizing our study on ${ }^{12} \mathrm{C}_{2} \mathrm{H}_{2}$ transitions in the $\Delta P=4$ spectral region using Fourier transform spectra with long absorption path. Those spectra allowed to identify and analyze 71 bands including the 5 bands given in the 2020 edition of the HITRAN and GEISA databases. The line positions were modeled using either set of spectroscopic constants or global effective Hamiltonian model (most of the time rescaled). The intensity calculations with the effective dipole moment operator demonstrated the good agreement with the observation. Using these calculations a recommended line list, including some interpolations and extrapolations, has been generated and is proposed for updating the whole $\Delta P=4$ spectral region in the HITRAN and GEISA spectroscopic databases.

A forthcoming study, the third and the last of the series, will aim to complete the present work by investigating observed bands of ${ }^{12} \mathrm{C}^{13} \mathrm{CH}_{2}$ and ${ }^{12} \mathrm{C}_{2} \mathrm{HD}$ isotopologues.

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[^0]:    ${ }^{\mathrm{a}}$ Normal mode labeling of the vibrational states: $V_{1} V_{2} V_{3} V_{4} V_{5} \ell_{4} \ell_{5}$
    ${ }^{\mathrm{b}}$ The numbers correspond to maximum $J_{\text {low }}$ values measured for each sub-branch. Notation "NA" refers to non existing sub-branch, whereas the notation "--" corresponds to the cases where no observation is performed for the sub-branch. Extrapolations are indicated by a "/" symbol followed by the maximum extrapolated $J$ values.

