

## Supplementary information

### Sensitivity to runaway albedo feedback

5 Pluto's and Triton's N<sub>2</sub> atmospheres are in global solid-gas equilibrium with their surface N<sub>2</sub> ice. For a high-enough surface pressure, the pressure at a reference altitude will be nearly the same across the globe, and the surface pressures and N<sub>2</sub> ice temperatures will follow vapor-pressure equilibrium. This global balance is maintained through N<sub>2</sub> sublimation and condensation processes, with sublimation winds transporting atmospheric mass and latent heat  
10 from areas of sublimation to areas of condensation. Local energy balance determines where N<sub>2</sub> sublimates or condenses. In general, sublimation tends to occur from areas of high insolation, while condensation tends to occur onto areas of low insolation, with the transition near the terminator. Locally, changes in N<sub>2</sub> ice albedo can impact the energy balance and modify the condensation-sublimation rates. A local decrease (resp. increase) in N<sub>2</sub> ice albedo can even  
15 invert the surface energy balance and trigger sublimation (resp. condensation) instead of condensation (resp. sublimation). Such an inversion of the surface energy balance is more likely to happen at places where condensation-sublimation rates are the lowest, i.e. near the terminator or more generally in the diurnal zone, where day/night cycles occur.

20 For instance, we can roughly estimate the diurnal mean sublimation rate of N<sub>2</sub> on Pluto by neglecting the internal heat flux and the sensible heat flux from the atmosphere and write the daytime surface energy balance as follows:

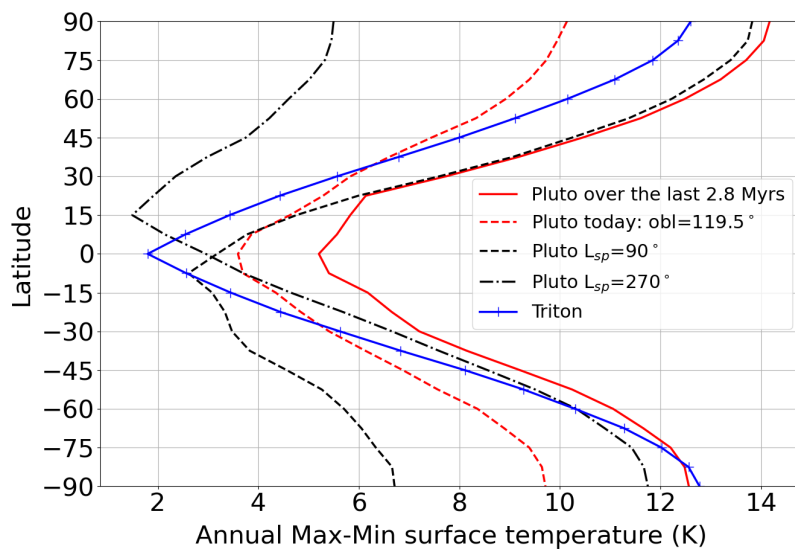
$$\epsilon\sigma T^4 = (1 - A)F - L \, dM/dt$$

25 where F is the diurnal mean incoming solar flux (W m<sup>-2</sup>), A is the N<sub>2</sub> ice surface albedo (e.g., 0.8), T is the diurnal mean N<sub>2</sub> ice surface temperature (here assumed to be ~37 K for a surface pressure of ~1 Pa),  $\epsilon$  is the N<sub>2</sub> ice emissivity (here assumed to be ~0.8), and  $\sigma$  is the Stefan-Boltzmann constant, L is the N<sub>2</sub> latent heat of sublimation (~2.5x10<sup>5</sup> J kg<sup>-1</sup>), and dM/dt is the  
30 N<sub>2</sub> ice sublimation rate (kg s<sup>-1</sup>). In these conditions, the term  $\epsilon\sigma T^4$  is equal to 0.085 W m<sup>-2</sup>. At the north pole, F varies from ~1 W m<sup>-2</sup> (summer solstice) to 0 W m<sup>-2</sup> (polar night) over an annual cycle, and therefore dM/dt varies from large positive to large negative values, i.e., the poles are dominated by intense sublimation (0.25 mm/Pluto day) followed by intense condensation (0.19 mm/Pluto day) over an annual cycle. A local change in N<sub>2</sub> ice surface albedo  
35 does not significantly change this trend. By contrast, in the diurnal zone (30°S-30°N), F remains in the range 0.2-0.4 W m<sup>-2</sup> over an annual cycle, and both sublimation and condensation can be maintained throughout the year depending on whether the N<sub>2</sub> ice surface albedo is low (<0.58) or high (>0.78). Albedo positive feedbacks occurring at the seasonal timescale are therefore easier to occur in the diurnal zone than at the poles.

40 The sensitivity of a N<sub>2</sub> ice surface to albedo positive feedbacks can be qualitatively represented by its ability to maintain sublimation or condensation throughout an annual cycle, which is best obtained when the annual contrasts in diurnal mean surface temperature are small (or diurnal mean insolation, but using surface temperatures seem to be a better proxy, because it includes  
45 the effects of subsurface thermal inertia).

On Supplementary Figure 1, we compare the sensitivity of Pluto's and Triton's latitudes to runaway albedo feedback for the annual and astronomical timescales. This sensitivity is qualitatively estimated by the difference between the maximum and minimum diurnal mean

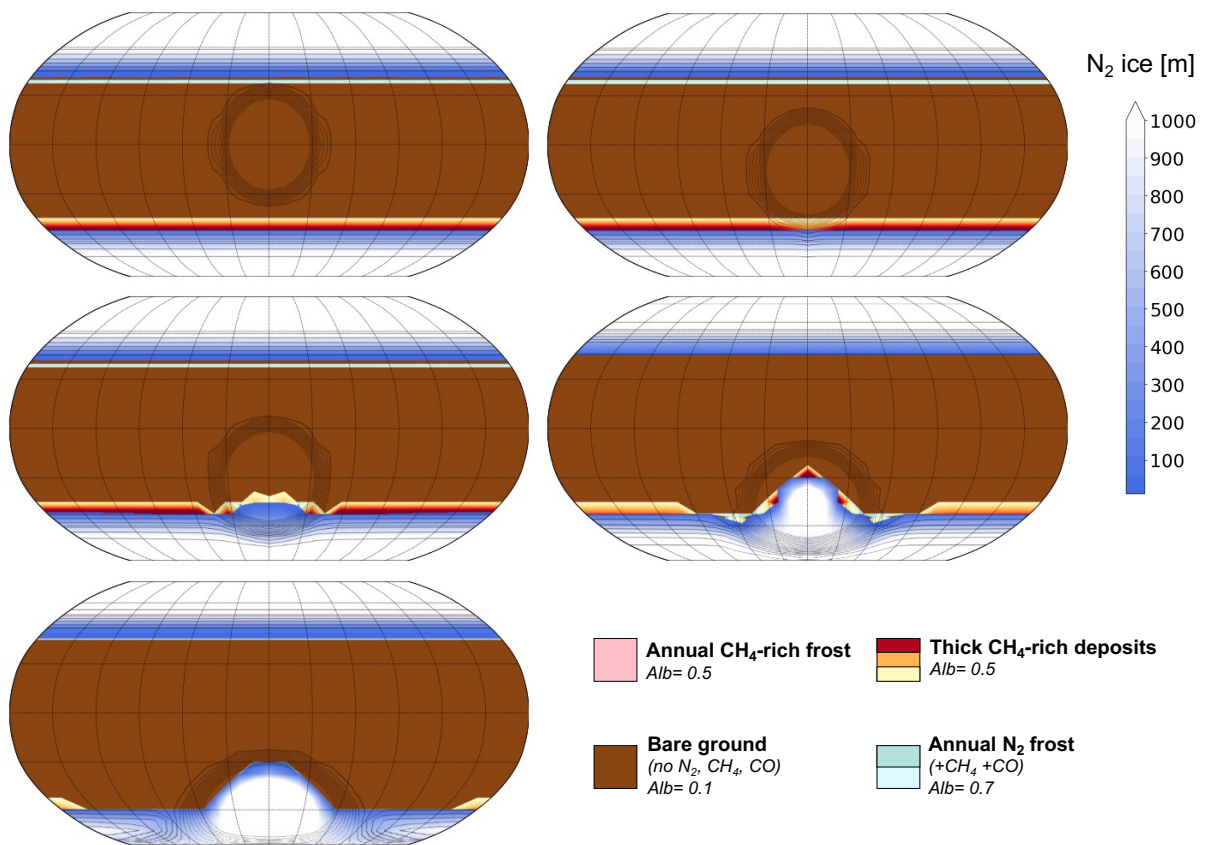
50 surface temperatures reached over the considered timescale, with low values likely to create  
 conditions for runaway albedo variations. We find that on both Pluto and Triton, the  
 temperature difference is minimal in the equatorial regions over annual and astronomical  
 timescales, because these regions correspond to the diurnal zone with a day/night cycle, and  
 maximal at the poles, because these regions experience long polar winter and summer. On  
 55 Pluto, the lowest values are obtained during the periods corresponding to a solar longitude of  
 perihelion of  $90^\circ$  and  $270^\circ$ , i.e., when one hemisphere is much warmer or much colder  
 than the opposite hemisphere on annual average. Note that the equatorial temperature  
 difference is even smaller for Triton than on Pluto, thus suggesting that Triton's equatorial  
 regions are even more sensitive to runaway albedo variations than Pluto's equatorial  
 60 regions. This could explain the diversity of terrains and colors observed in Triton's  
 equatorial regions, at the edge of the southern bright cap.



65 *Supplementary Figure 1. Latitude versus the variation between the minimum and maximum  
 diurnal mean surface temperature at that latitude over Pluto and Triton. For Pluto we consider  
 the timescale of the last obliquity cycle (i.e. the minimum and maximum are calculated over the  
 last 2.8 Myr, solid red line), the annual timescale at the current epoch (dashed red line), and  
 the epochs with solar longitude of perihelion of  $90^\circ$  and  $270^\circ$  (black lines). For Triton, both  
 annual and astronomical timescales give the same results (blue solid line). Minimal variations  
 70 are obtained in the equatorial regions on both objects, suggesting that these regions are the  
 most sensitive to albedo runaway forcings.*

Alternative simulations of Triton

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Supplementary Figure 2. Volatile ice distribution obtained after a 20-Myr simulation performed with the LMD volatile transport model for Triton with a 8-km deep (Sputnik-like) crater centered at the equator, 15°S, 30°S, 45°S, and 60°S. Black contours show the bedrock's topography.

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